

Write the electron operator  $c_\alpha$  ( $\alpha = \uparrow, \downarrow$  are spin indices) as

$$\begin{pmatrix} c_\uparrow \\ c_\downarrow \end{pmatrix} = R \begin{pmatrix} \psi_+ \\ \psi_- \end{pmatrix}$$

where  $R$  is a  $SU(2)$  matrix which determines the orientation of the local antiferromagnetic order, and  $\psi_\pm$  are spinless fermions which carry the global electron  $U(1)$  charge.

This parameterization is invariant under a  $SU(2)$  *gauge* transformation

$$\begin{pmatrix} \psi_+ \\ \psi_- \end{pmatrix} \rightarrow U \begin{pmatrix} \psi_+ \\ \psi_- \end{pmatrix} \quad ; \quad R \rightarrow RU^\dagger$$