

Exploring quantum matter in the high temperature superconductors



Perimeter Institute, Waterloo
June 23, 2015

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Talk online: sachdev.physics.harvard.edu

Flavors of Quantum Matter

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A. Ordinary quantum matter

Independent electrons, or pairs of electrons



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B. Topological quantum matter

*Long-range quantum entanglement leads
to sensitivity to spatial topology*



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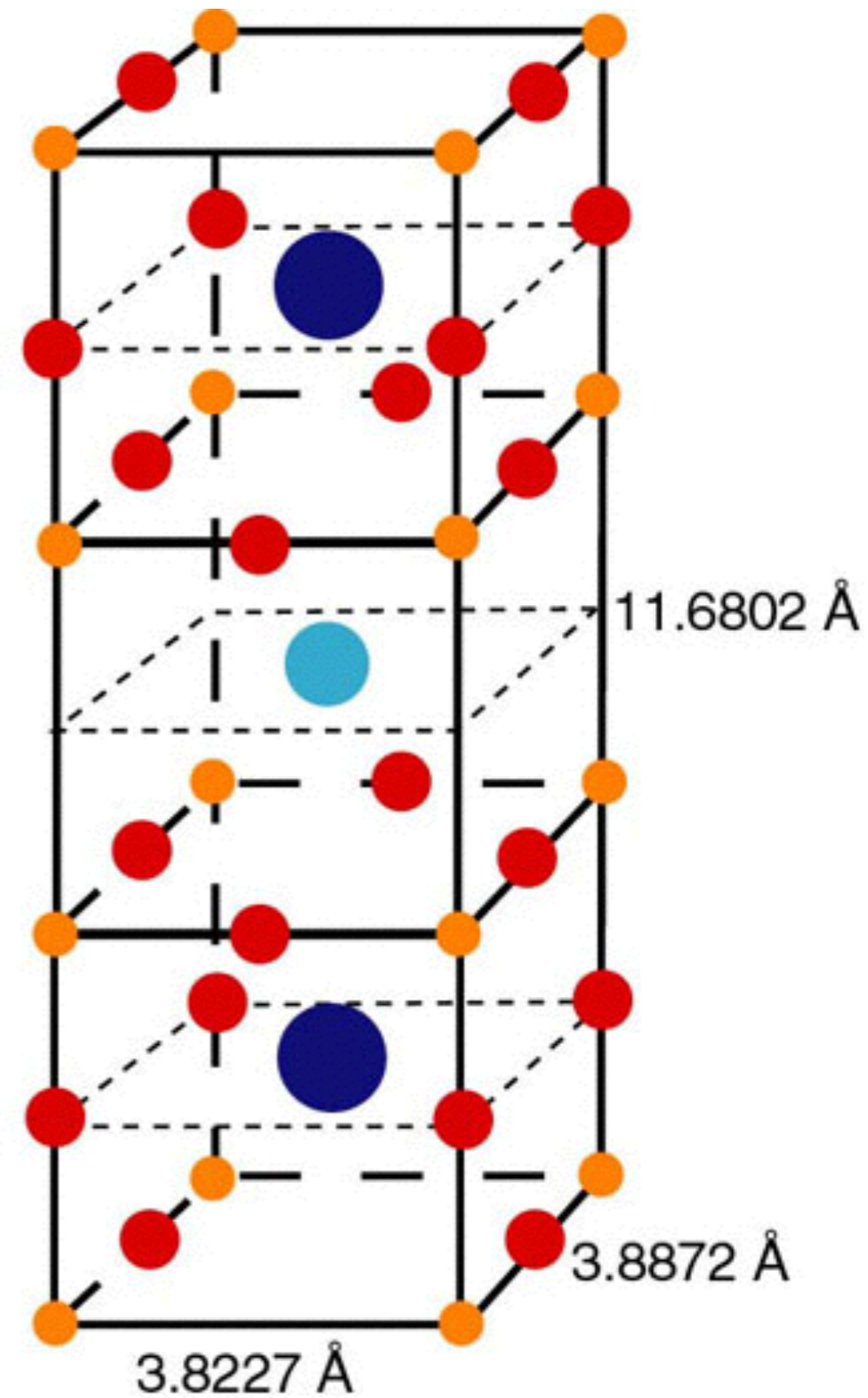
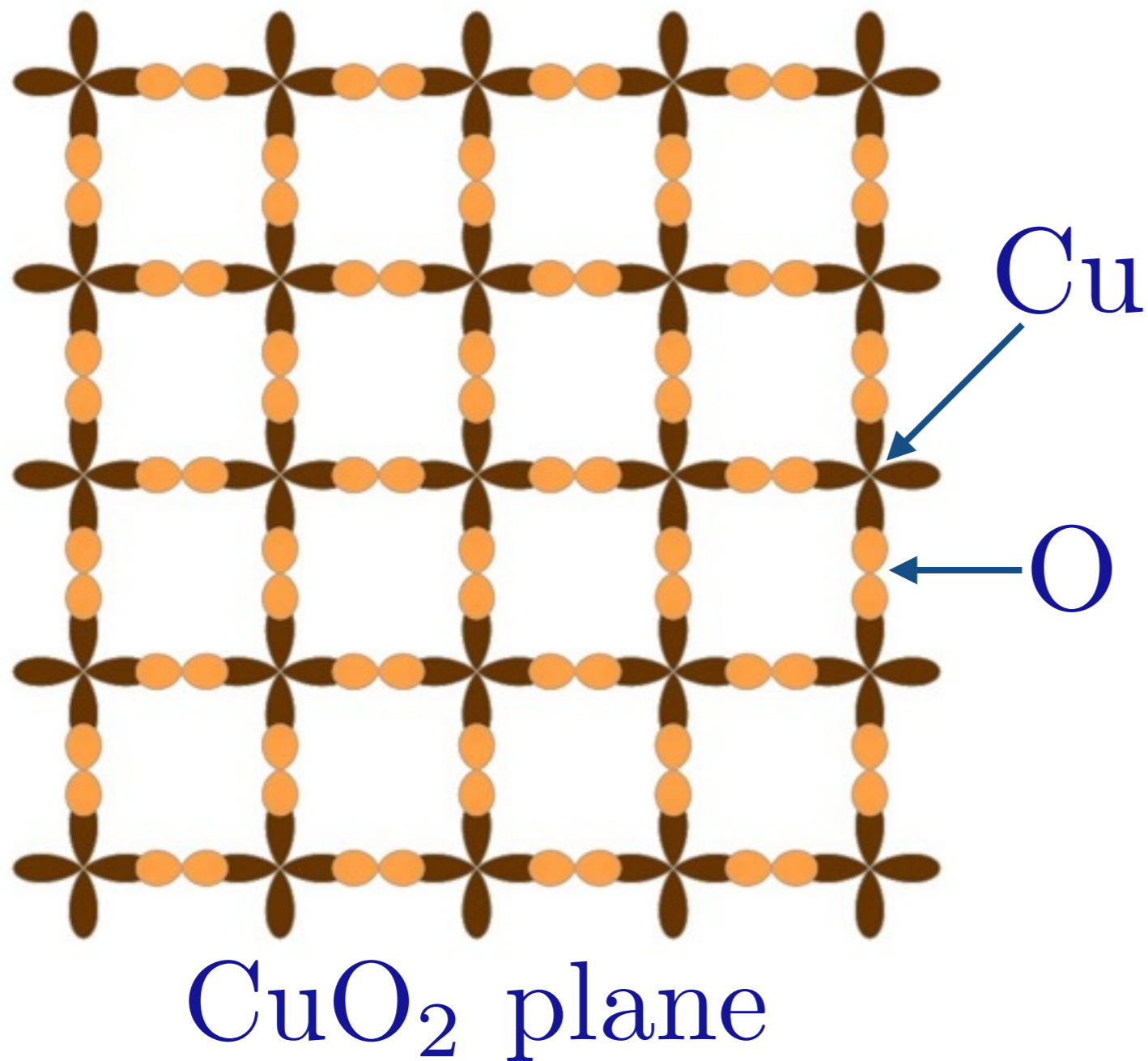


C. Quantum matter without quasiparticles

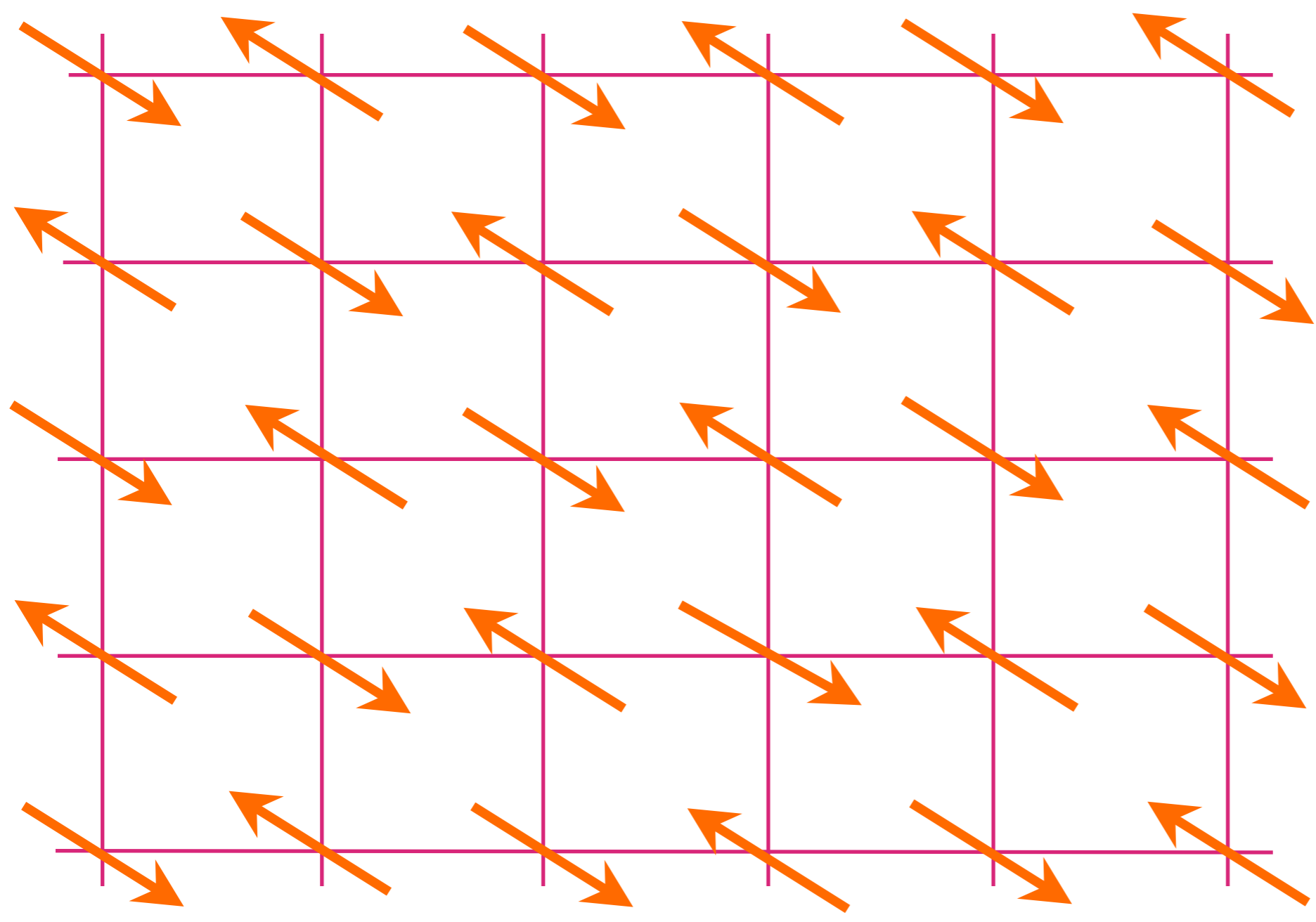
*Strange metals: infinite-range model
maps to extremal charged black holes
and yields Bekenstein-Hawking entropy*

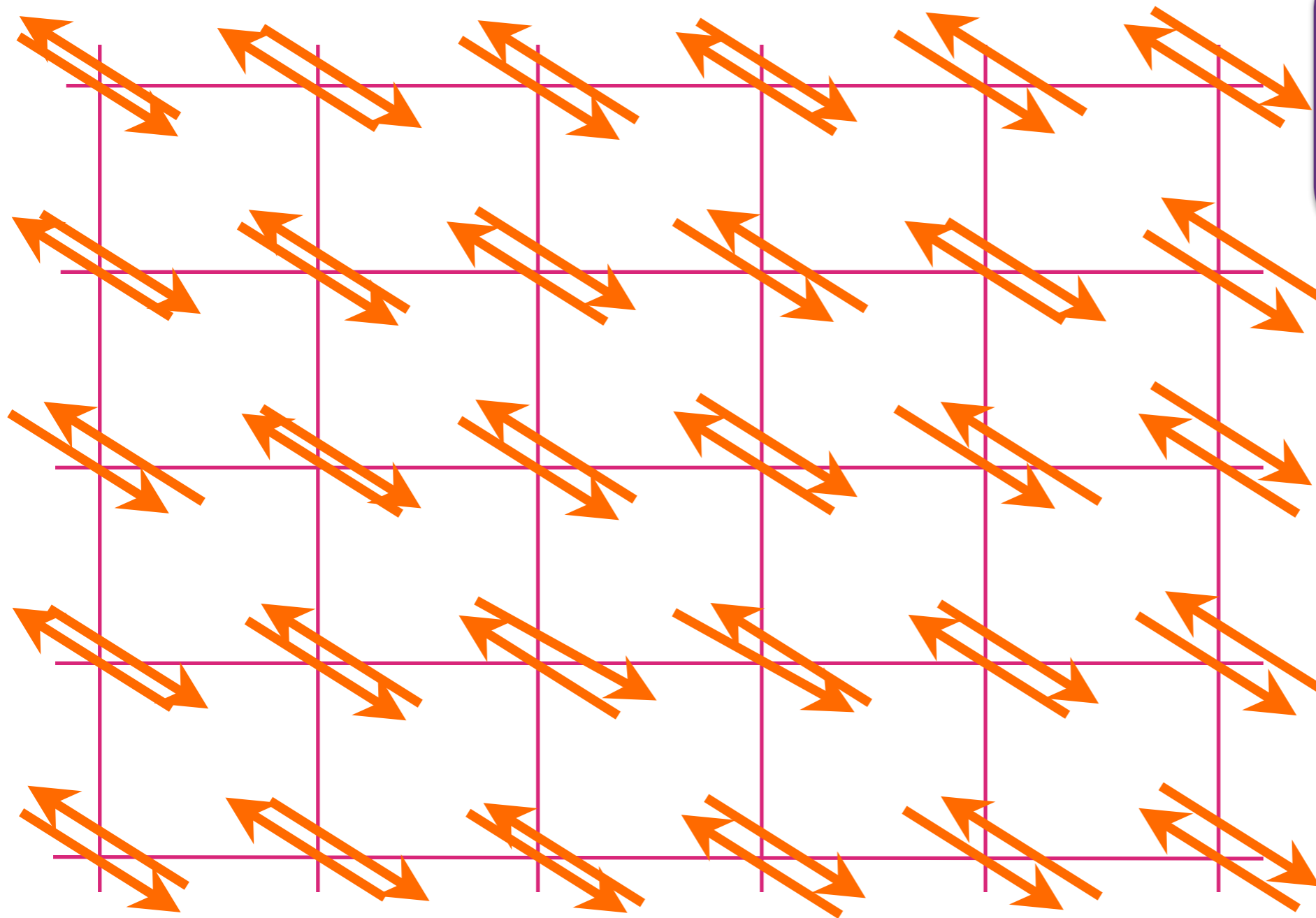


High temperature superconductors



“Undoped”
Anti-
ferromagnet

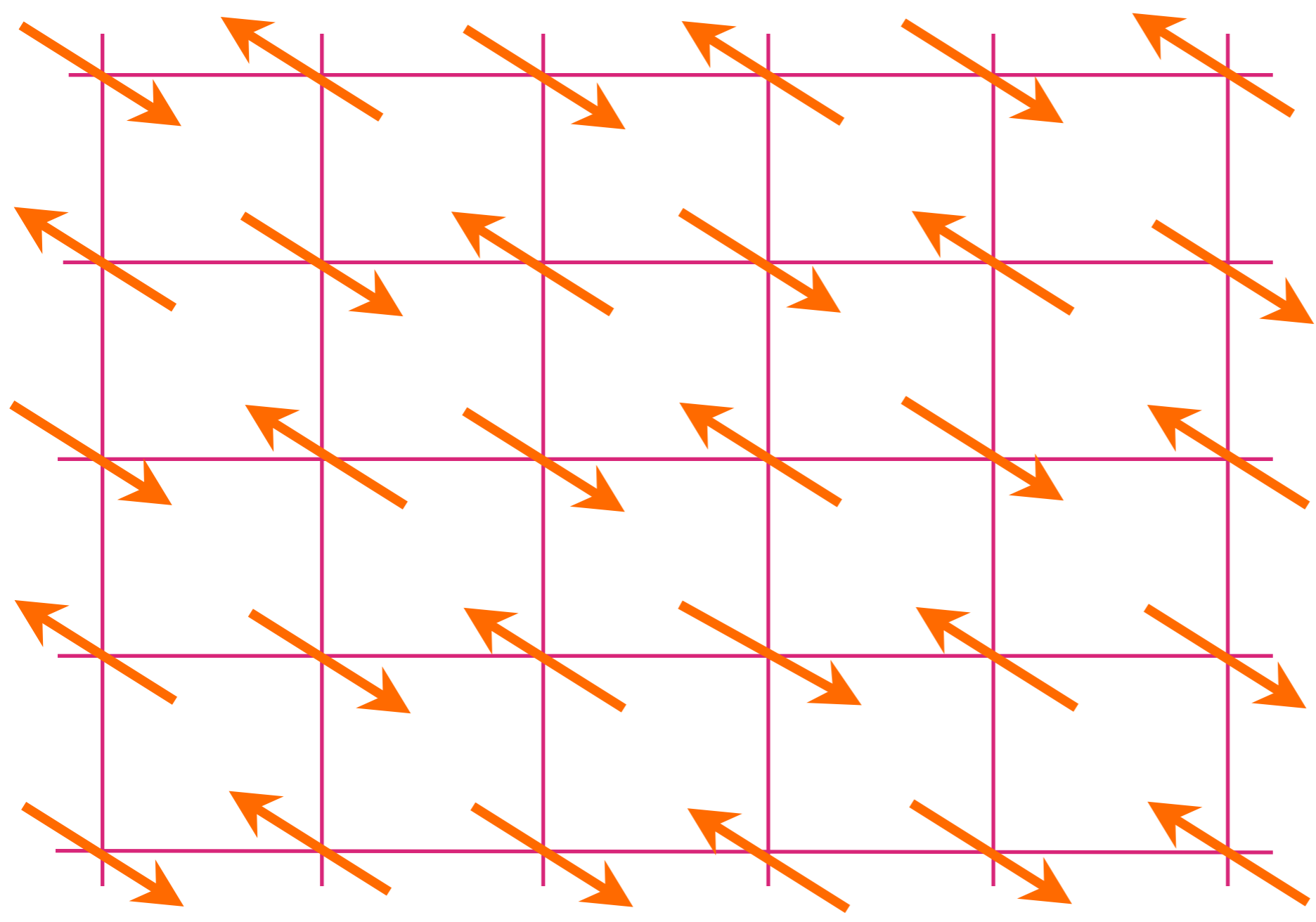


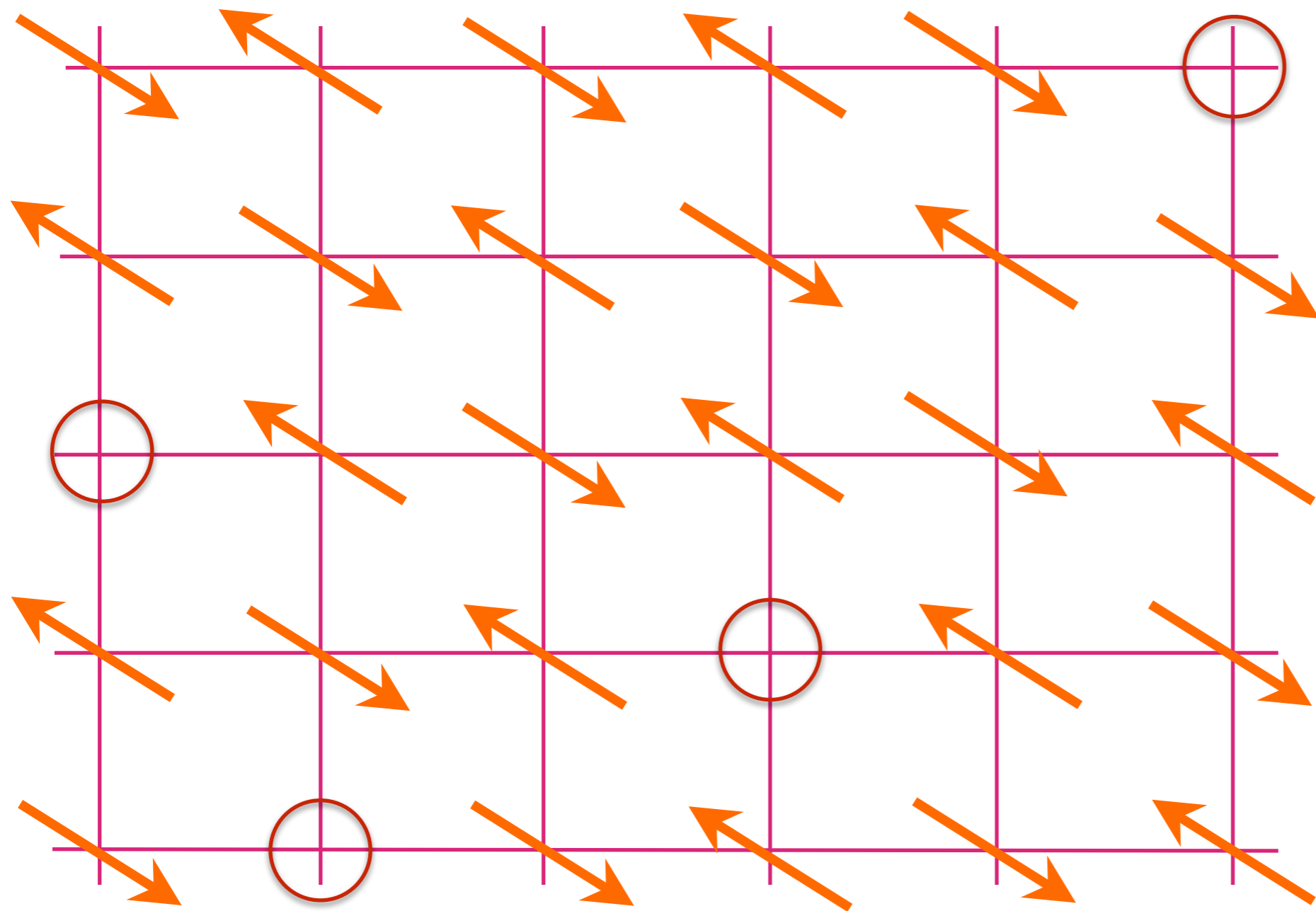


Filled
Band

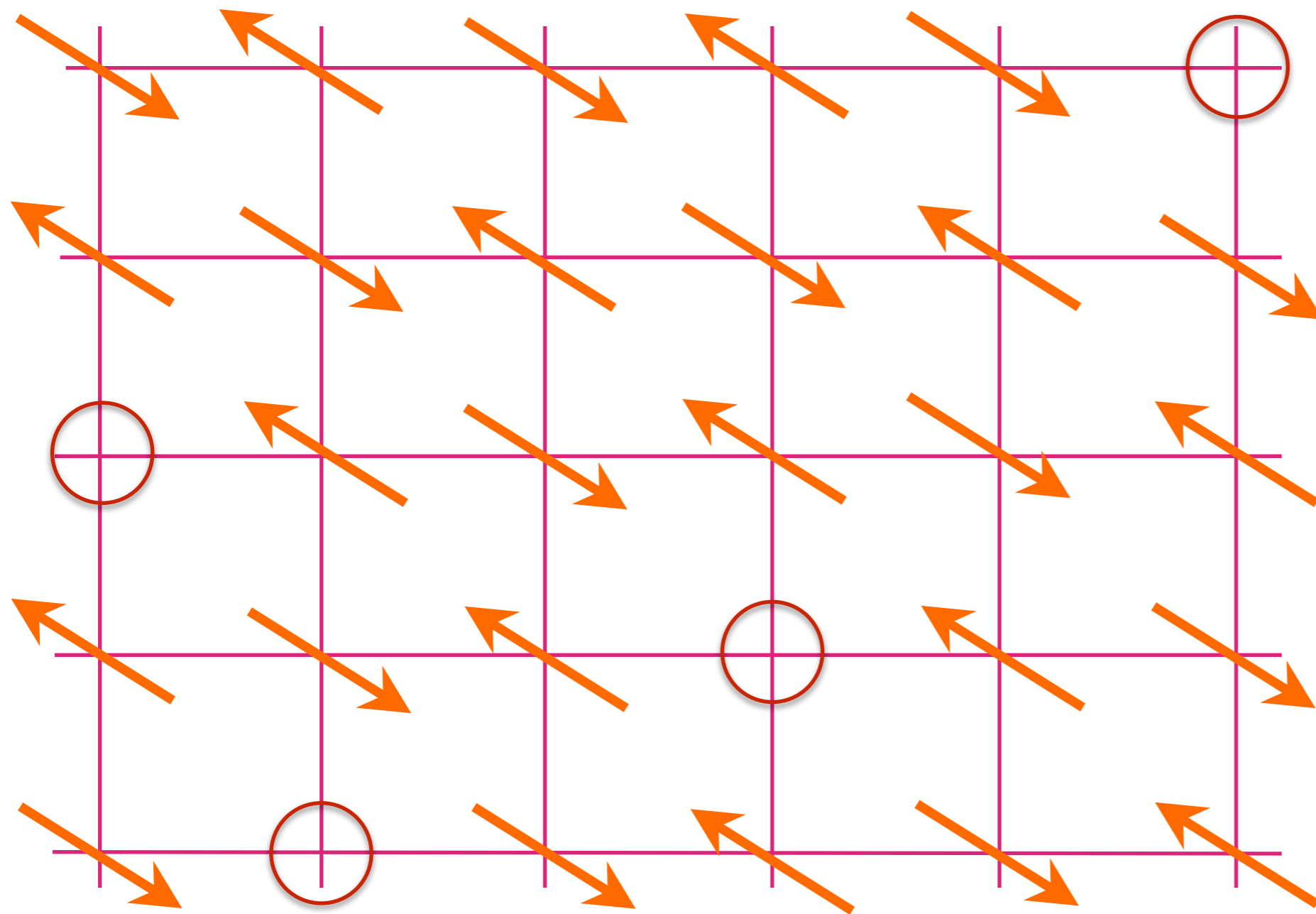


“Undoped”
Anti-
ferromagnet





Anti-ferromagnet
with p holes
per square



Anti-ferromagnet with p holes per square

But relative to the band insulator, there are $1 + p$ holes per square

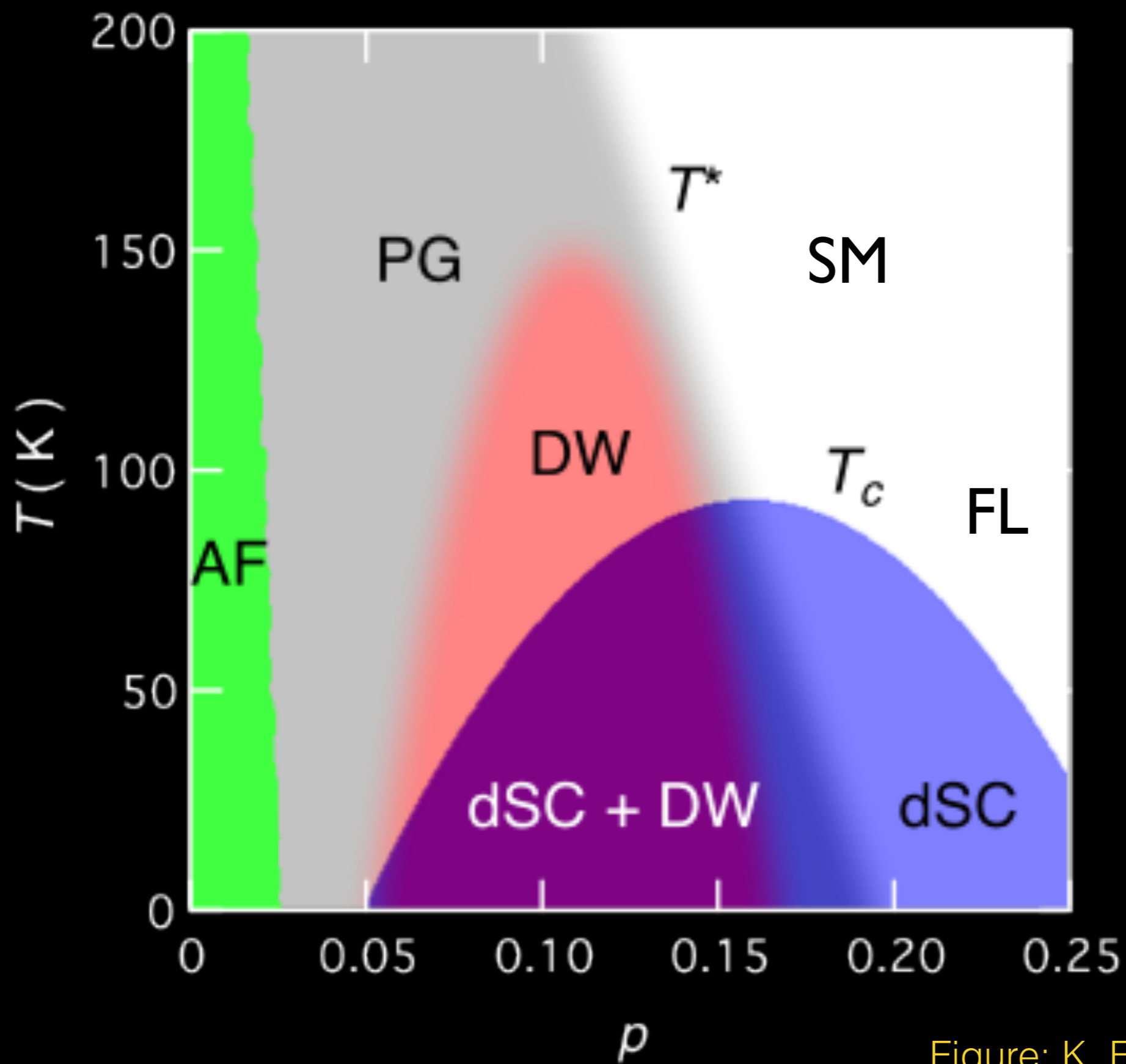


Figure: K. Fujita and J. C. Seamus Davis



Antiferromagnet

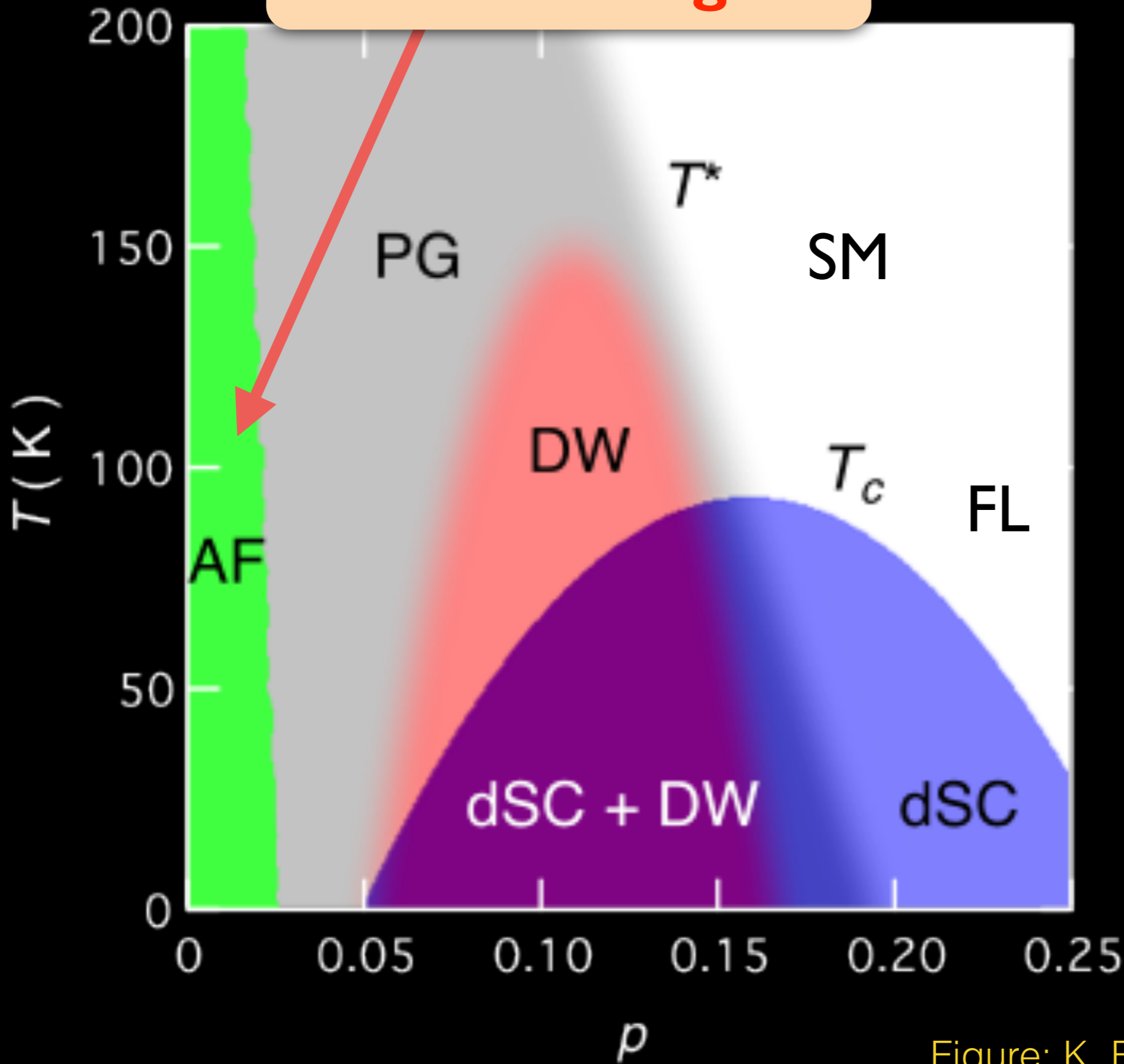


Figure: K. Fujita and J. C. Seamus Davis

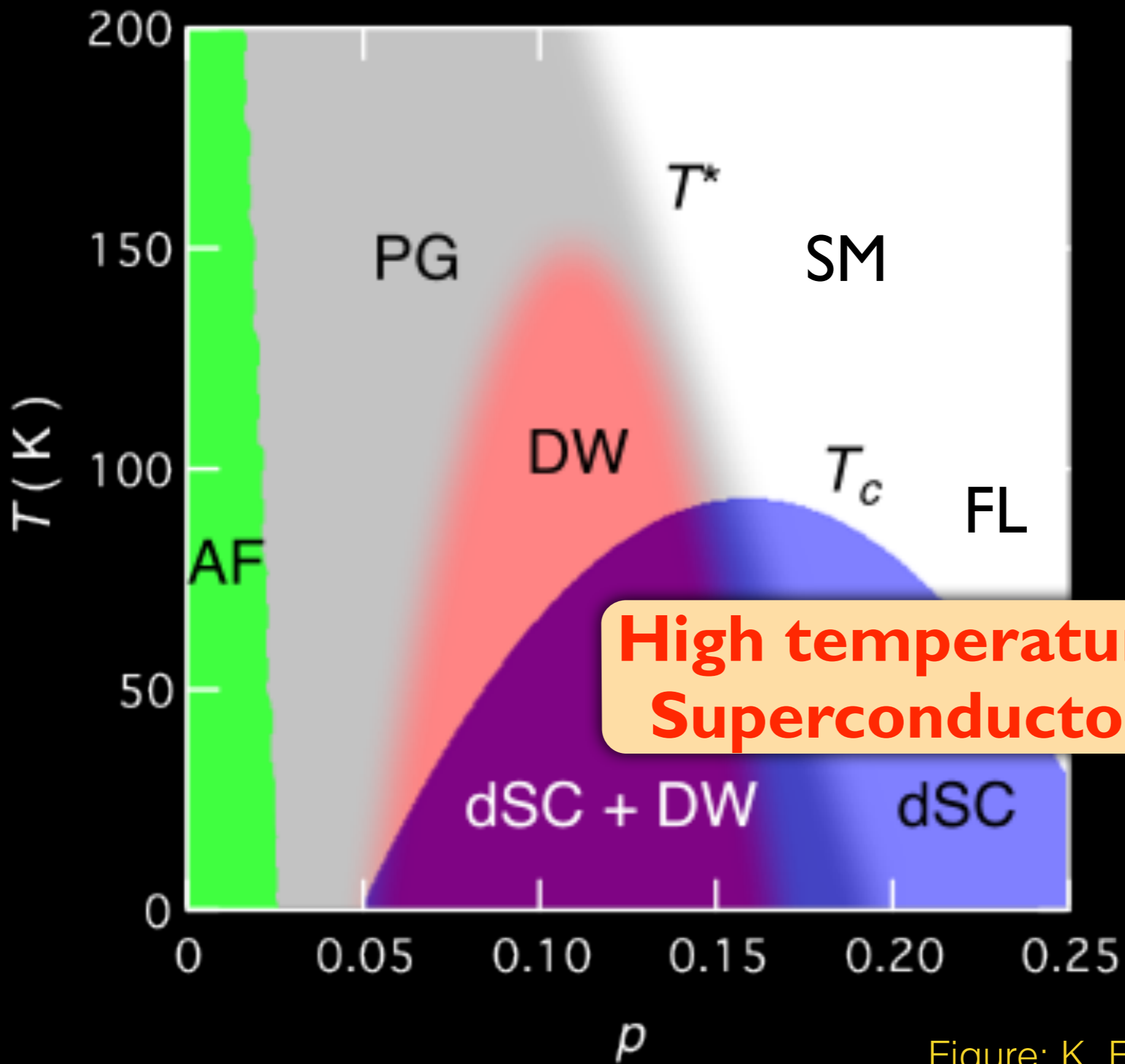
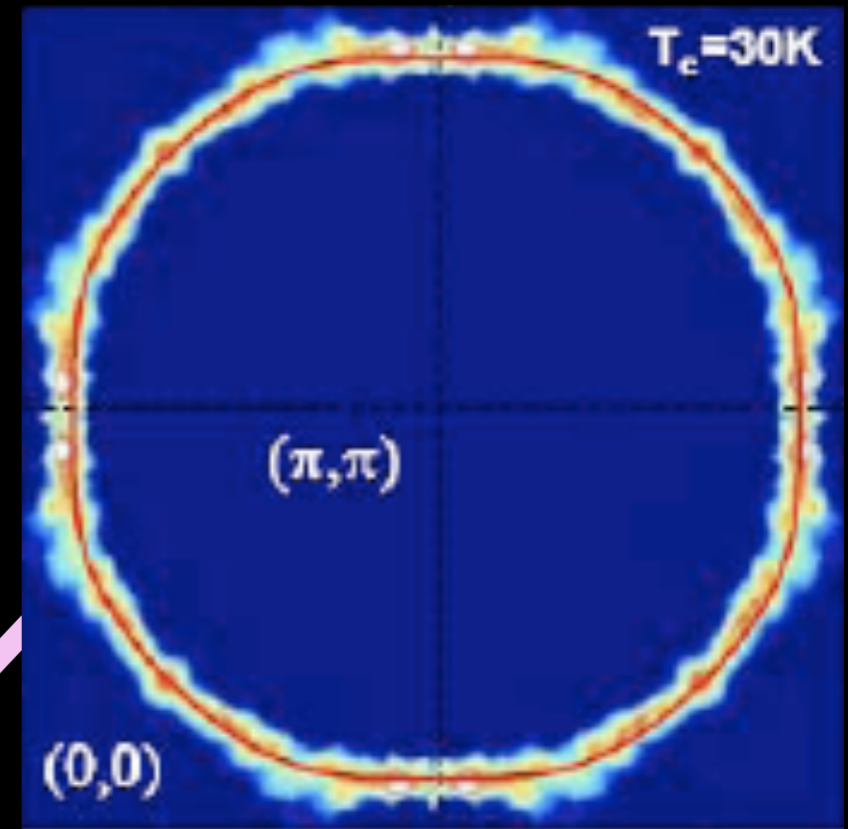
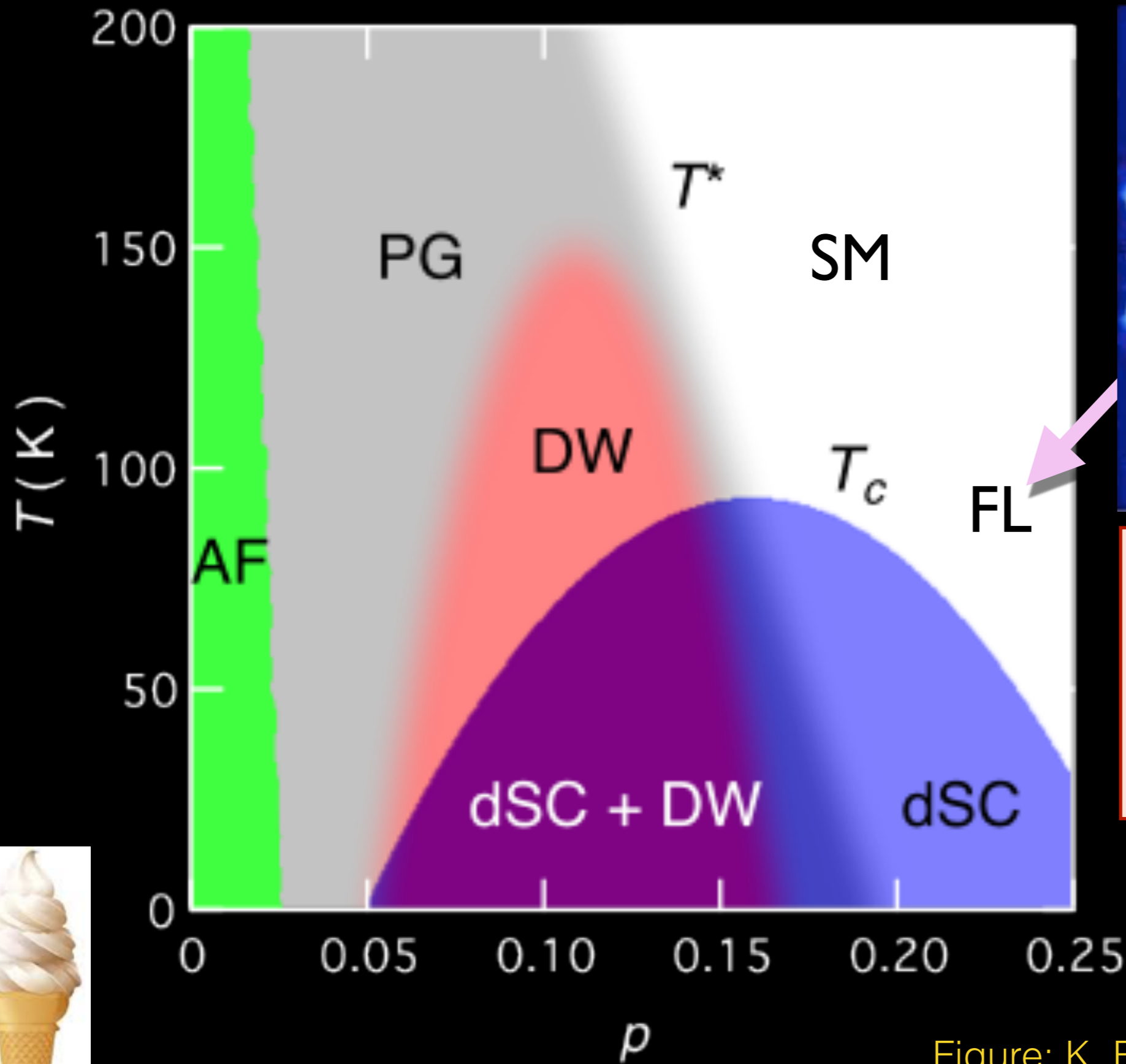


Figure: K. Fujita and J. C. Seamus Davis

M. Platié, J. D. F. Mottershead, I. S. Elfimov, D. C. Peets, Ruixing Liang, D. A. Bonn, W. N. Hardy, S. Chiuzbaian, M. Falub, M. Shi, L. Patthey, and A. Damascelli, Phys. Rev. Lett. **95**, 077001 (2005)



Conventional metal
Area enclosed by Fermi surface = $l + p$

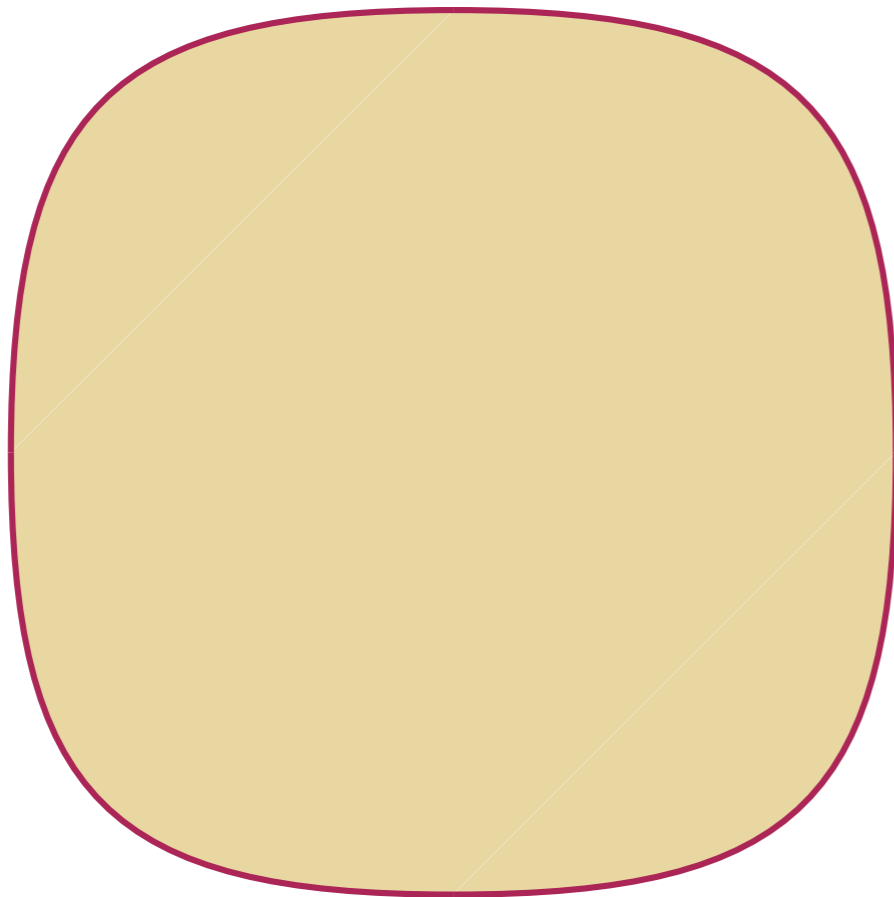


Figure: K. Fujita and J. C. Seamus Davis

Ordinary quantum matter: the Fermi liquid (FL)

- Fermi surface separates empty and occupied states in momentum space.

Fermi surface



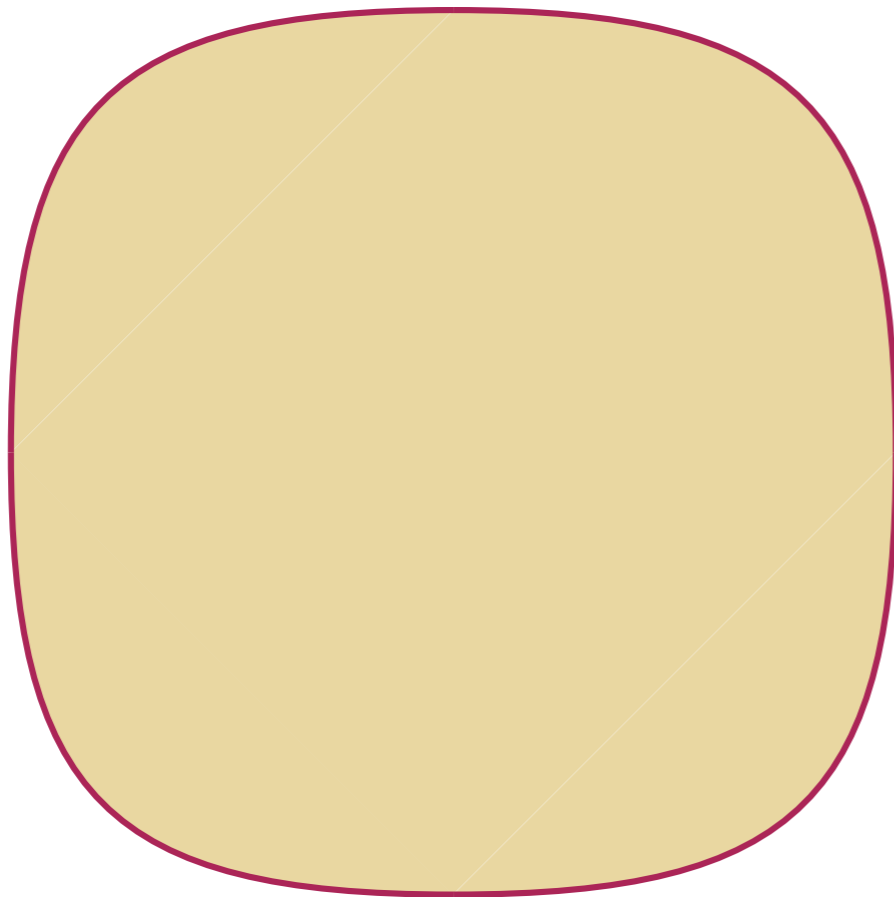
k_y

k_x



Ordinary quantum matter: the Fermi liquid (FL)

Fermi surface

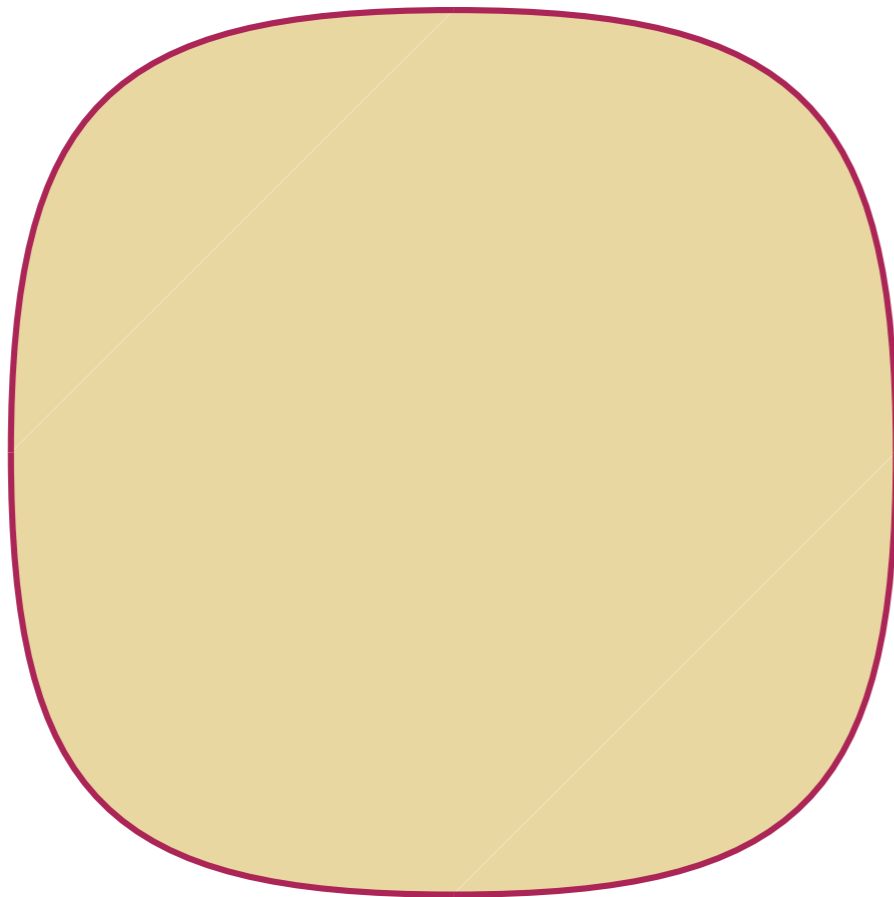


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- Area enclosed by Fermi surface = total density of electrons (mod 2) = $1+p$.



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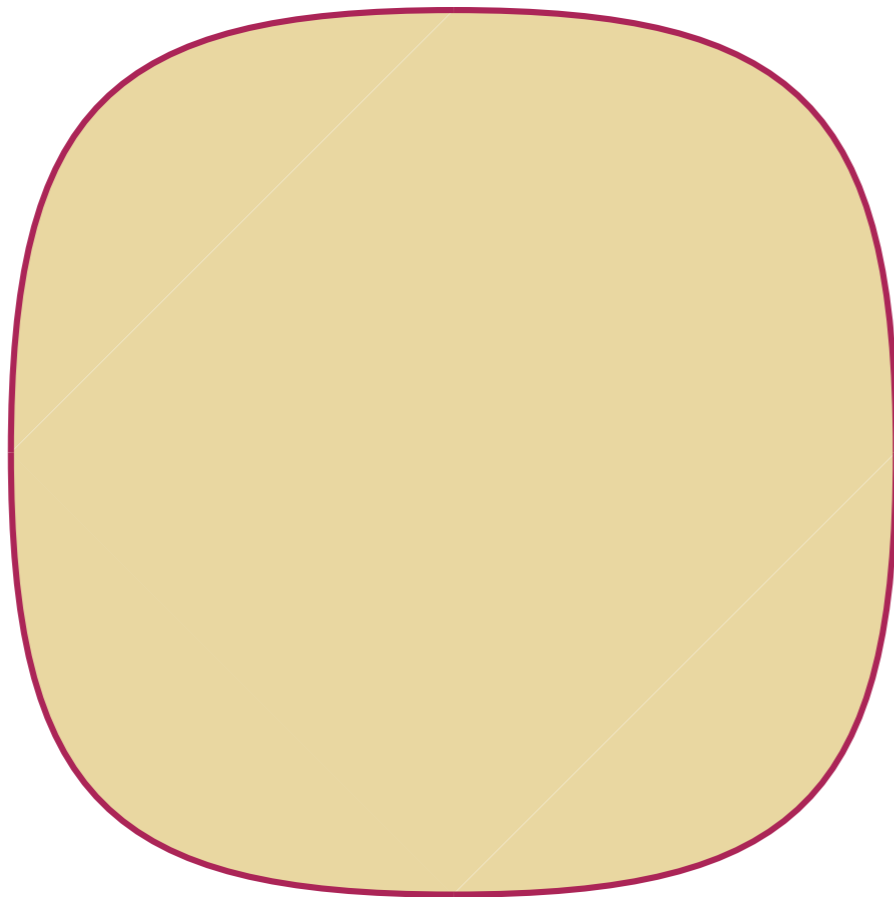


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- Density of electrons can be continuously varied at zero temperature.



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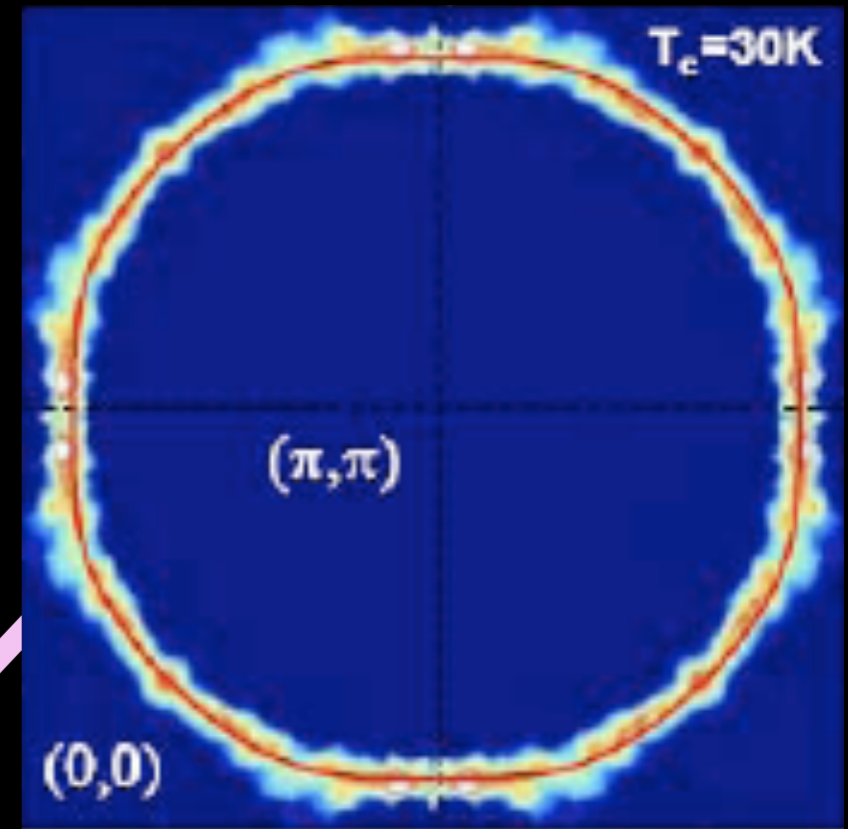
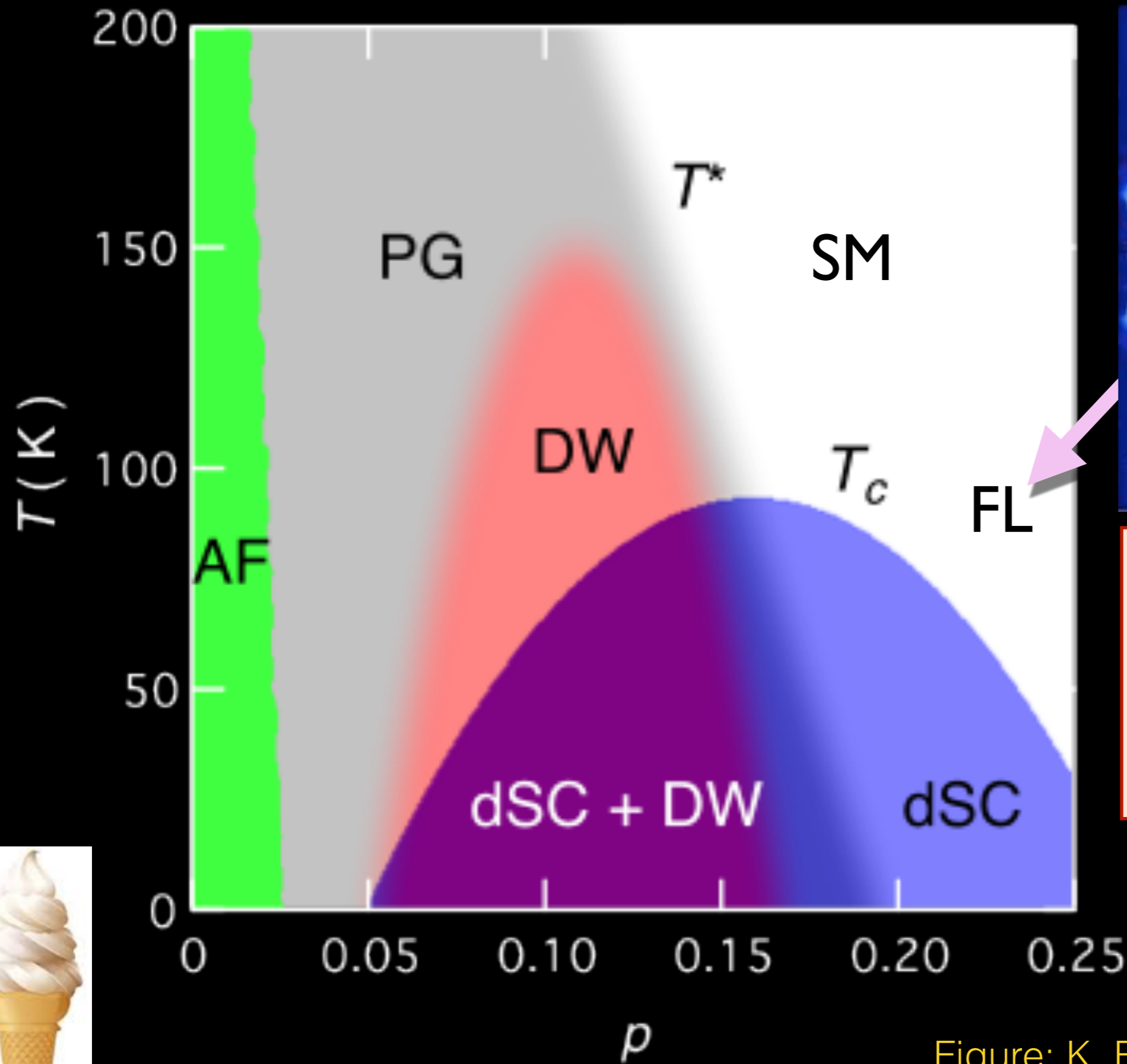
Fermi surface



- Fermi surface separates empty and occupied states in momentum space.
- Area enclosed by Fermi surface = total density of electrons (mod 2) = $1+p$.
- Density of electrons can be continuously varied at zero temperature.
- Long-lived electron-like quasiparticle excitations near the Fermi surface: lifetime of quasiparticles $\sim 1/T^2$.



M. Platié, J. D. F. Mottershead, I. S. Elfimov, D. C. Peets, Ruixing Liang, D. A. Bonn, W. N. Hardy, S. Chiuzbaian, M. Falub, M. Shi, L. Patthey, and A. Damascelli, Phys. Rev. Lett. **95**, 077001 (2005)

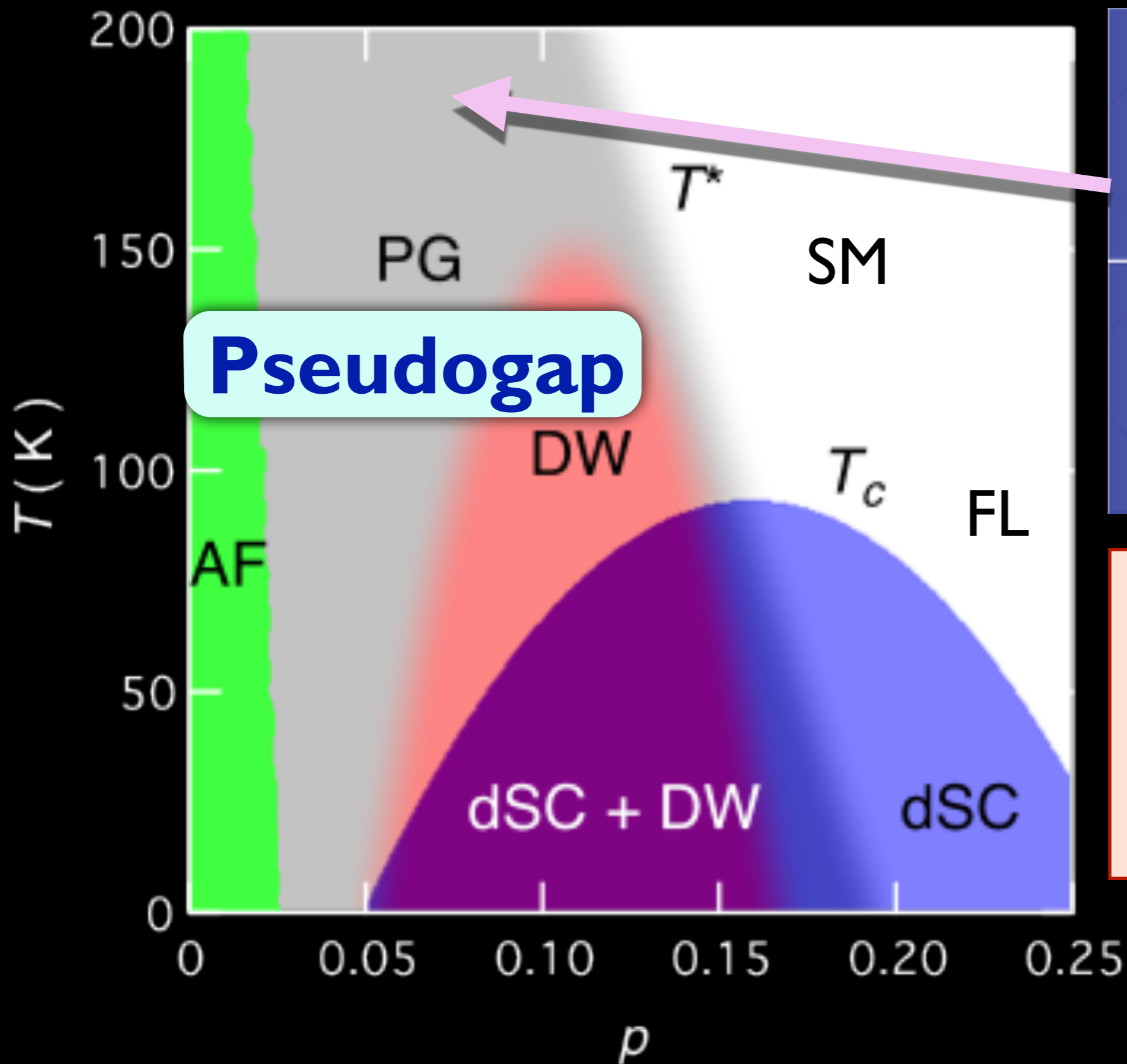


Conventional metal
Area enclosed by Fermi surface = $I + p$

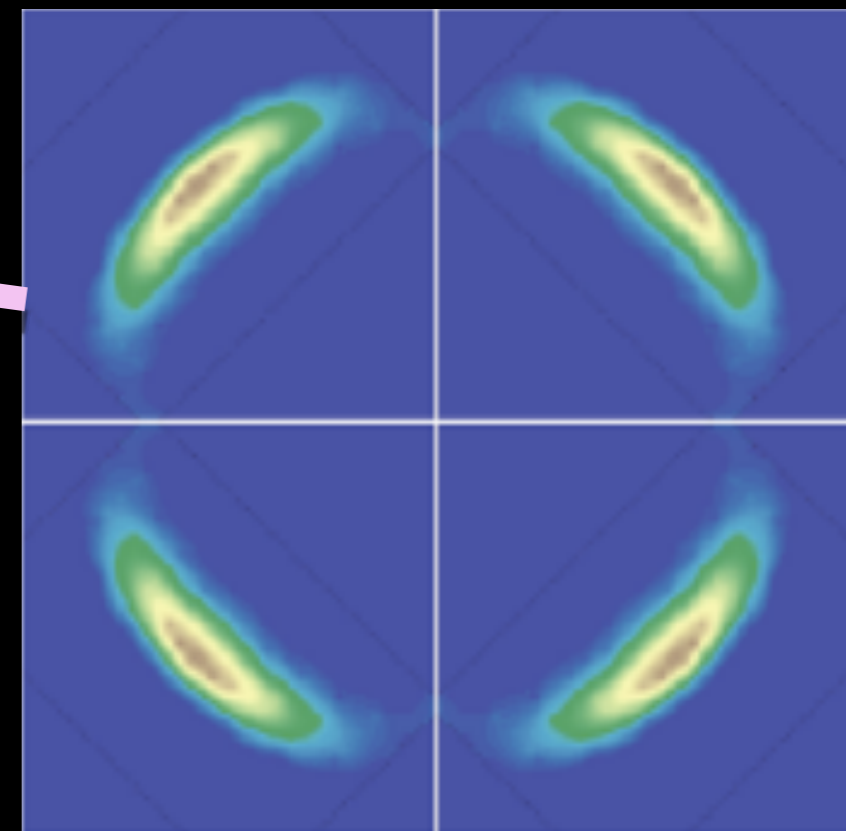


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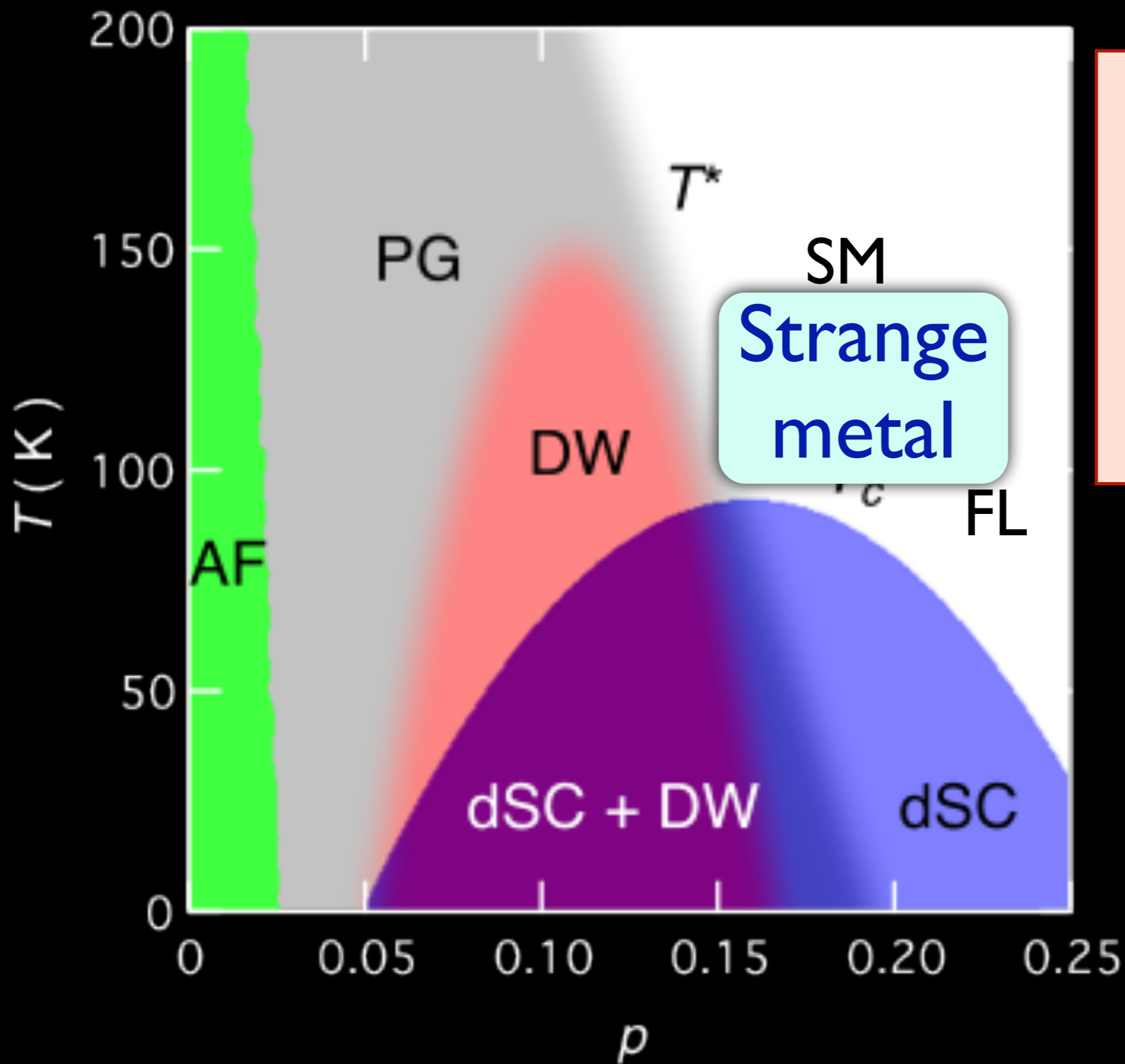
Kyle M. Shen, F. Ronning, D. H. Lu, F. Baumberger, N. J. C. Ingle, W. S. Lee, W. Meevasana, Y. Kohsaka, M. Azuma, M. Takano, H. Takagi, Z.-X. Shen, *Science* **307**, 901 (2005)



Pseudogap



“Fermi arcs”
at
low p



**Metal
without
quasi-
particles**

Outline

1. The pseudogap metal

Fermi liquid co-existing with topological order

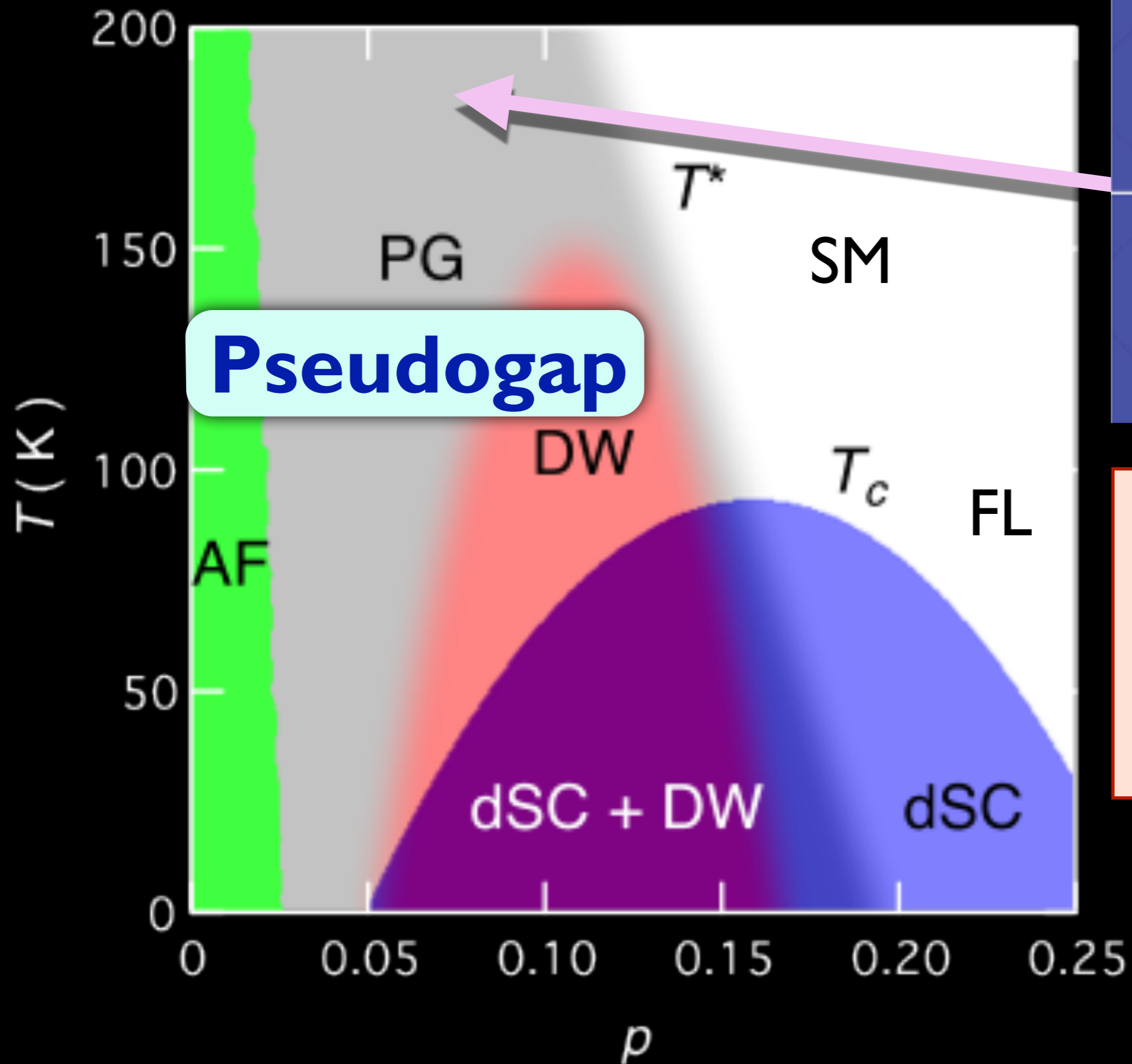
2. The strange metal

Metal without quasiparticles

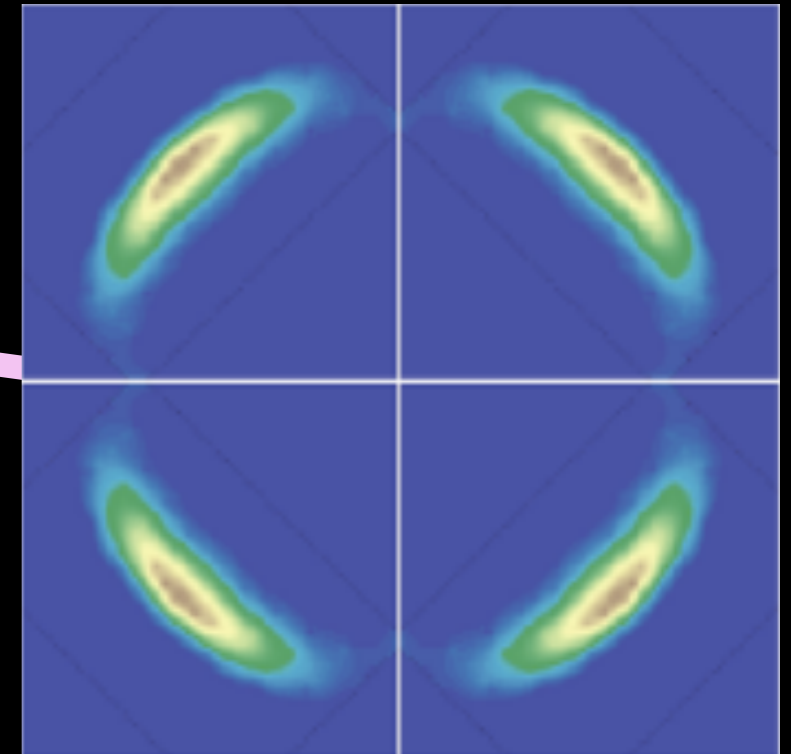
*Infinite-range model: dual to extremal charged
black holes and yields*

Bekenstein-Hawking entropy

Kyle M. Shen, F. Ronning, D. H. Lu, F. Baumberger, N. J. C. Ingle, W. S. Lee, W. Meevasana, Y. Kohsaka, M. Azuma, M. Takano, H. Takagi, Z.-X. Shen, *Science* **307**, 901 (2005)



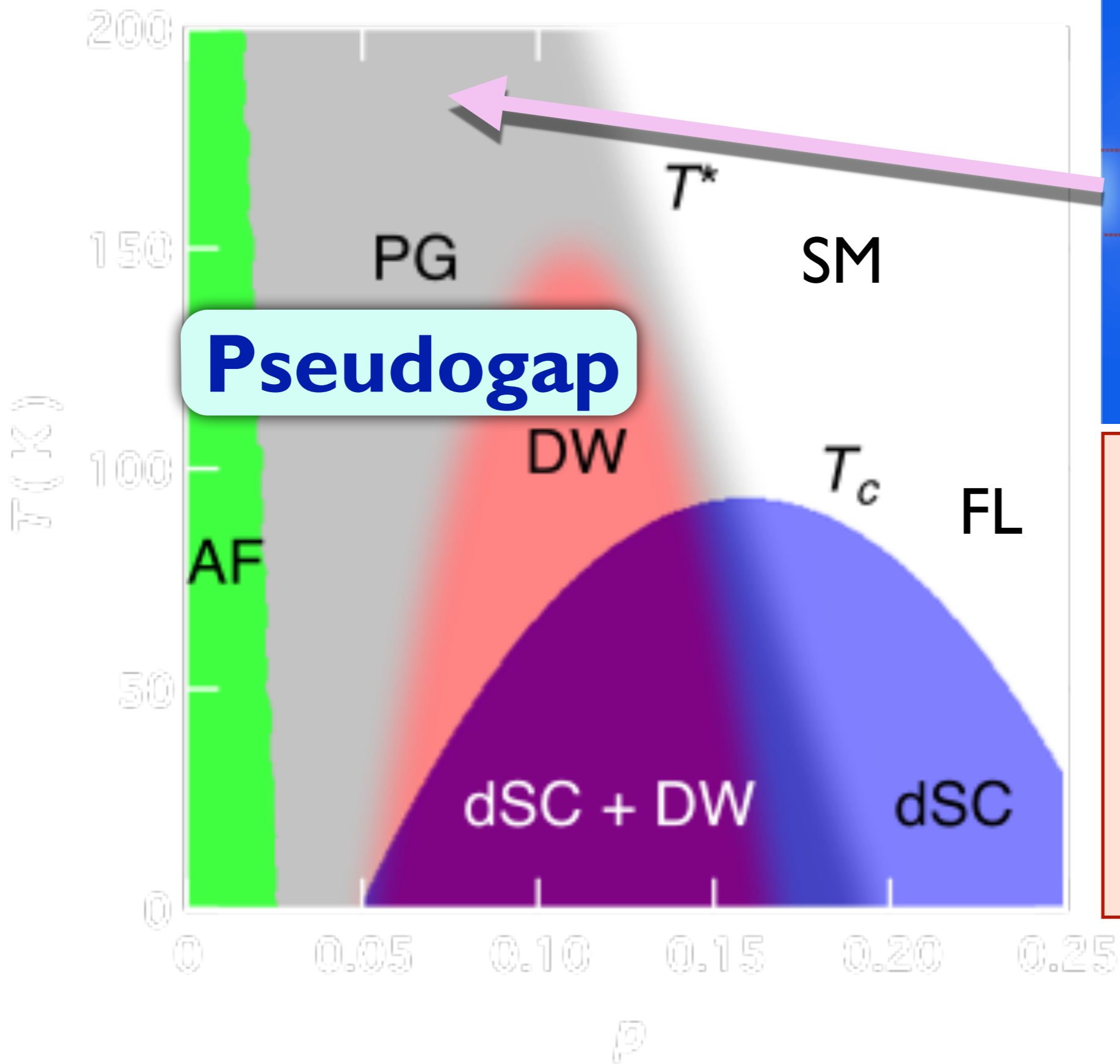
Pseudogap



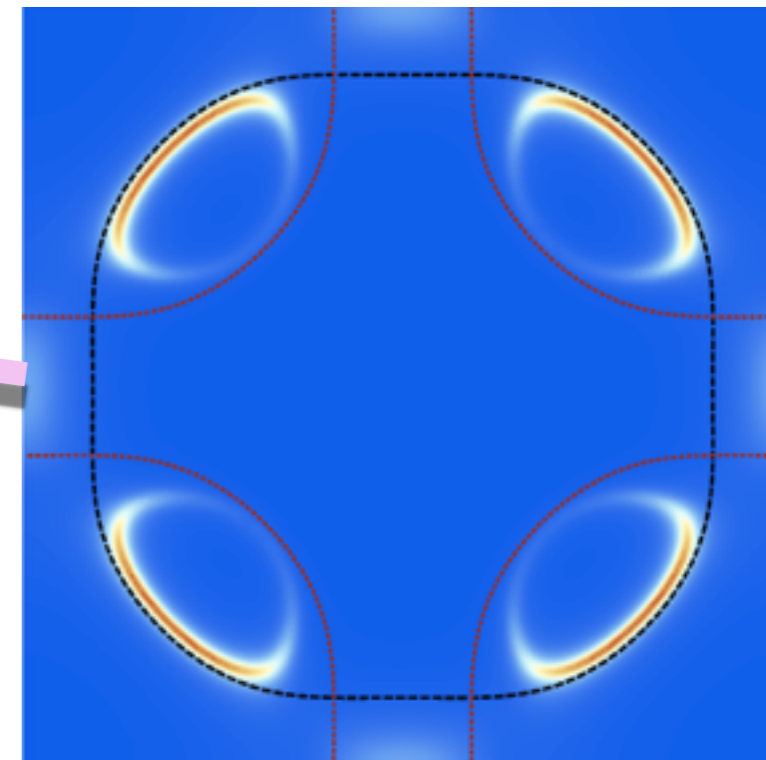
“Fermi arcs”
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Y. Qi and S. Sachdev, Phys. Rev. B **81**, 115129 (2010)

M. Punk, A. Allais, and S. Sachdev, arXiv:1501.00978



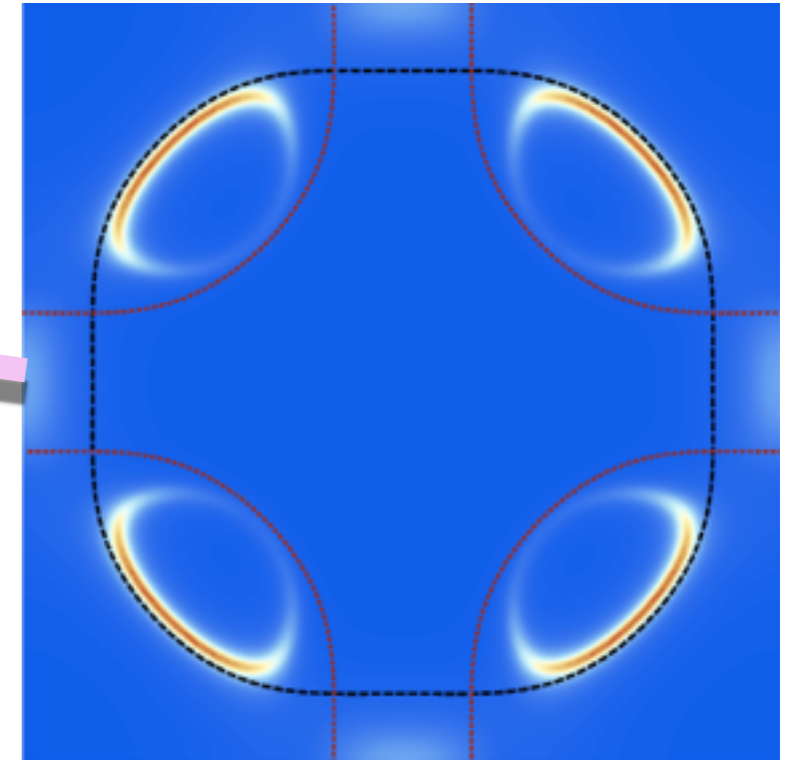
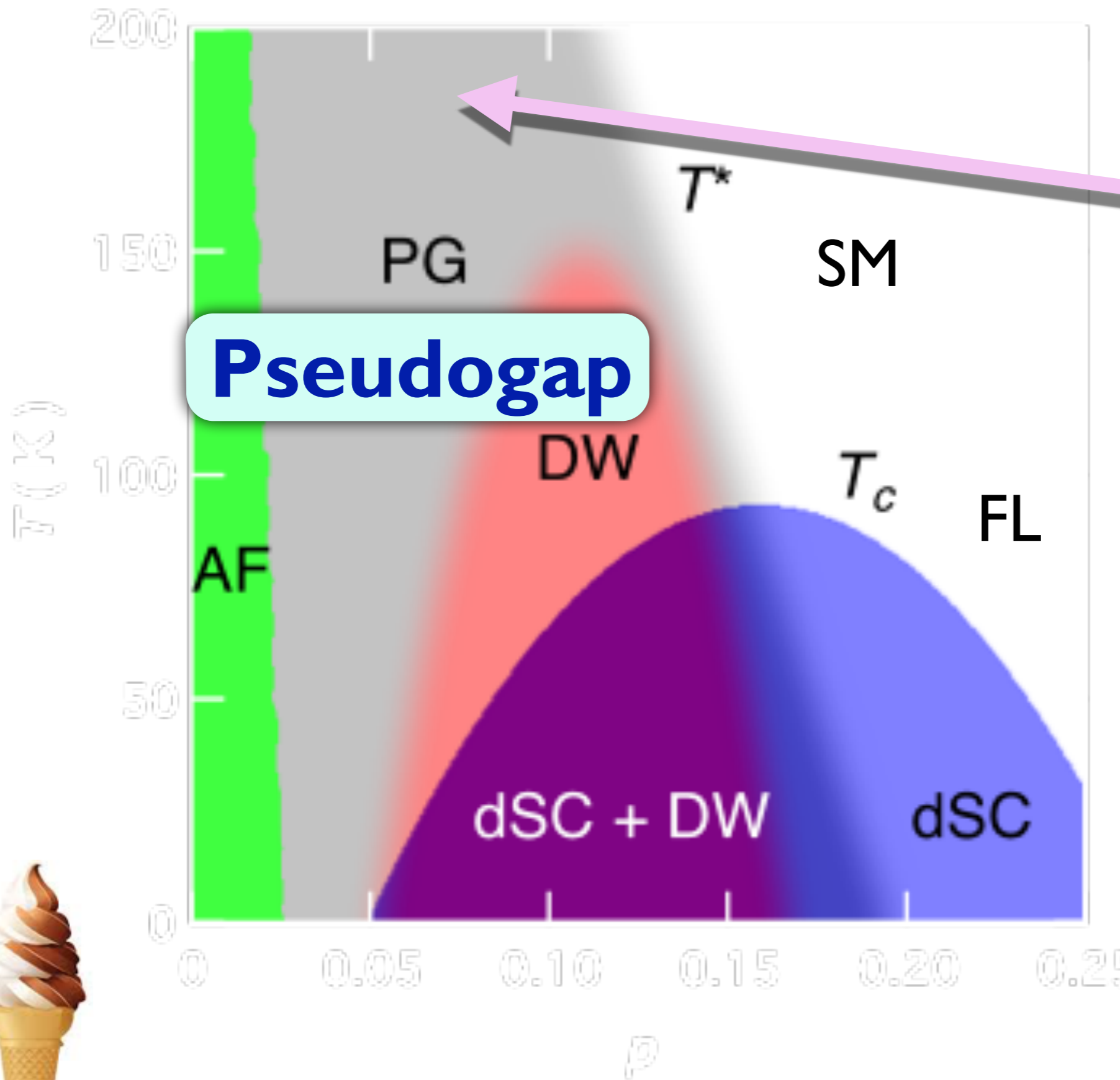
Pseudogap



A new metal —
a fractionalized
Fermi liquid (FL*)
— with electron-
like quasiparticles
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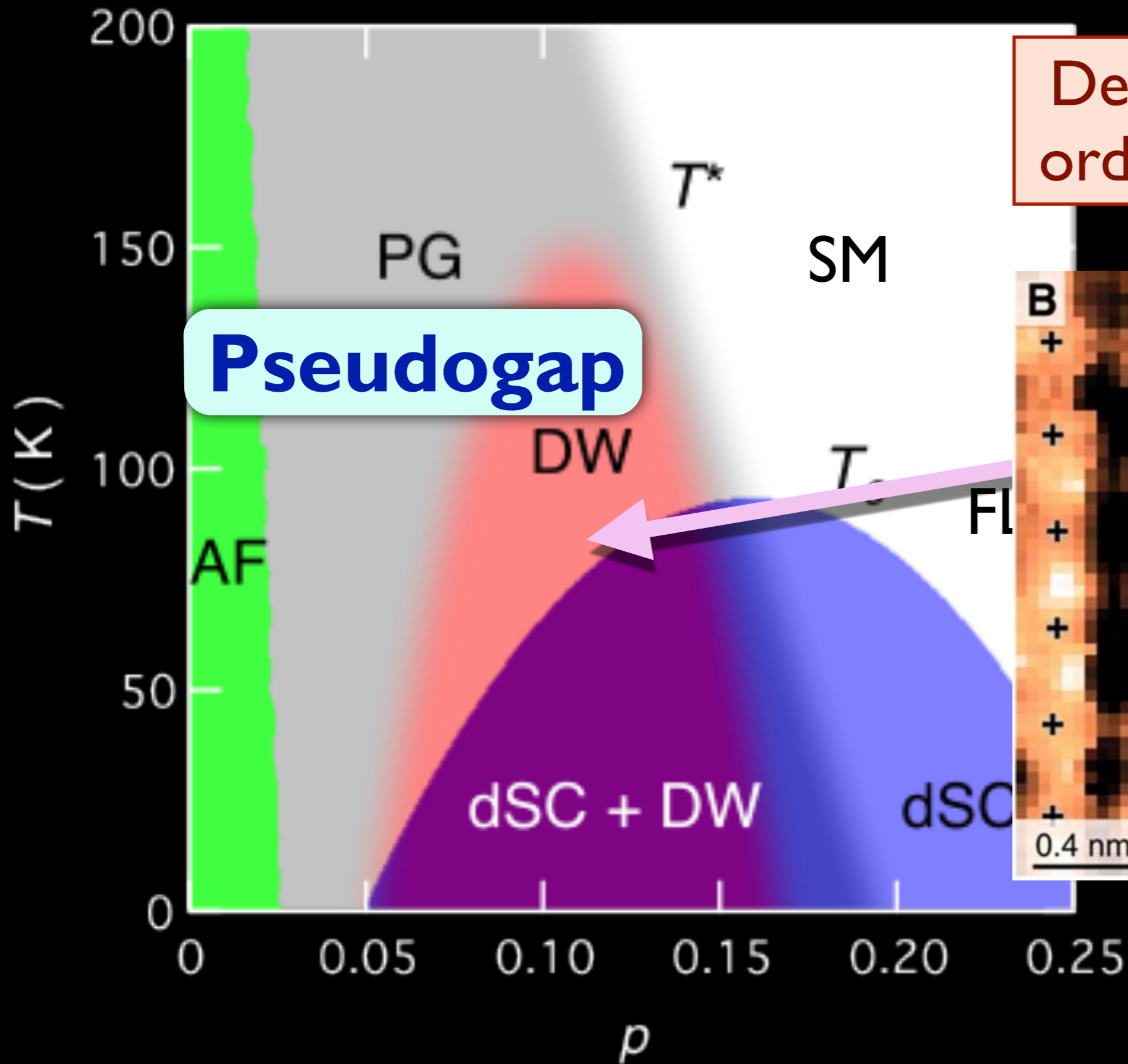
A new metal —
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like quasiparticles
on a Fermi surface
of size p
coexisting with
topological order



Evidence for Fermi surface of long-lived quasiparticles of density ρ

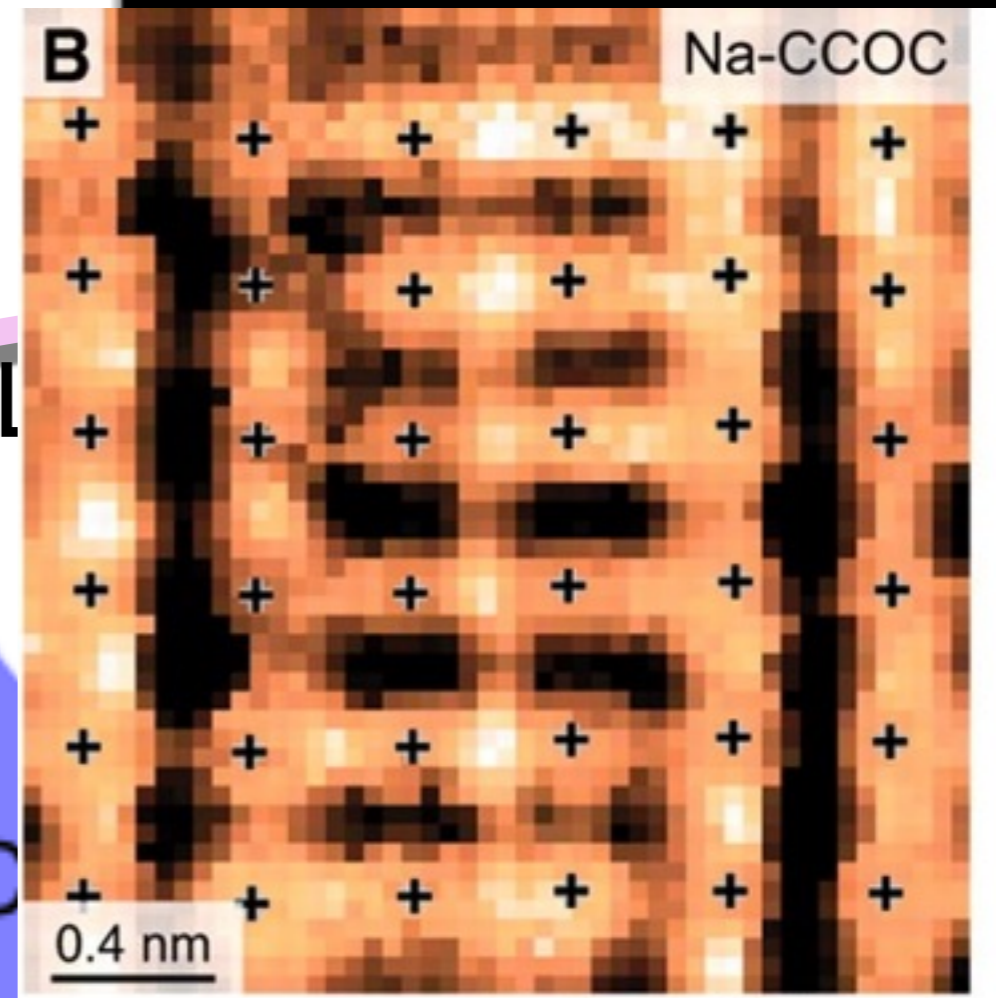
- Hall effect (Ando PRL 2004)
- Optical conductivity (van der Marel PNAS 2013)
- Magnetoresistance (Greven PRL 2014)
- Scanning Tunneling Microscopy (Seamus Davis, PNAS 2014):
d-form factor density wave





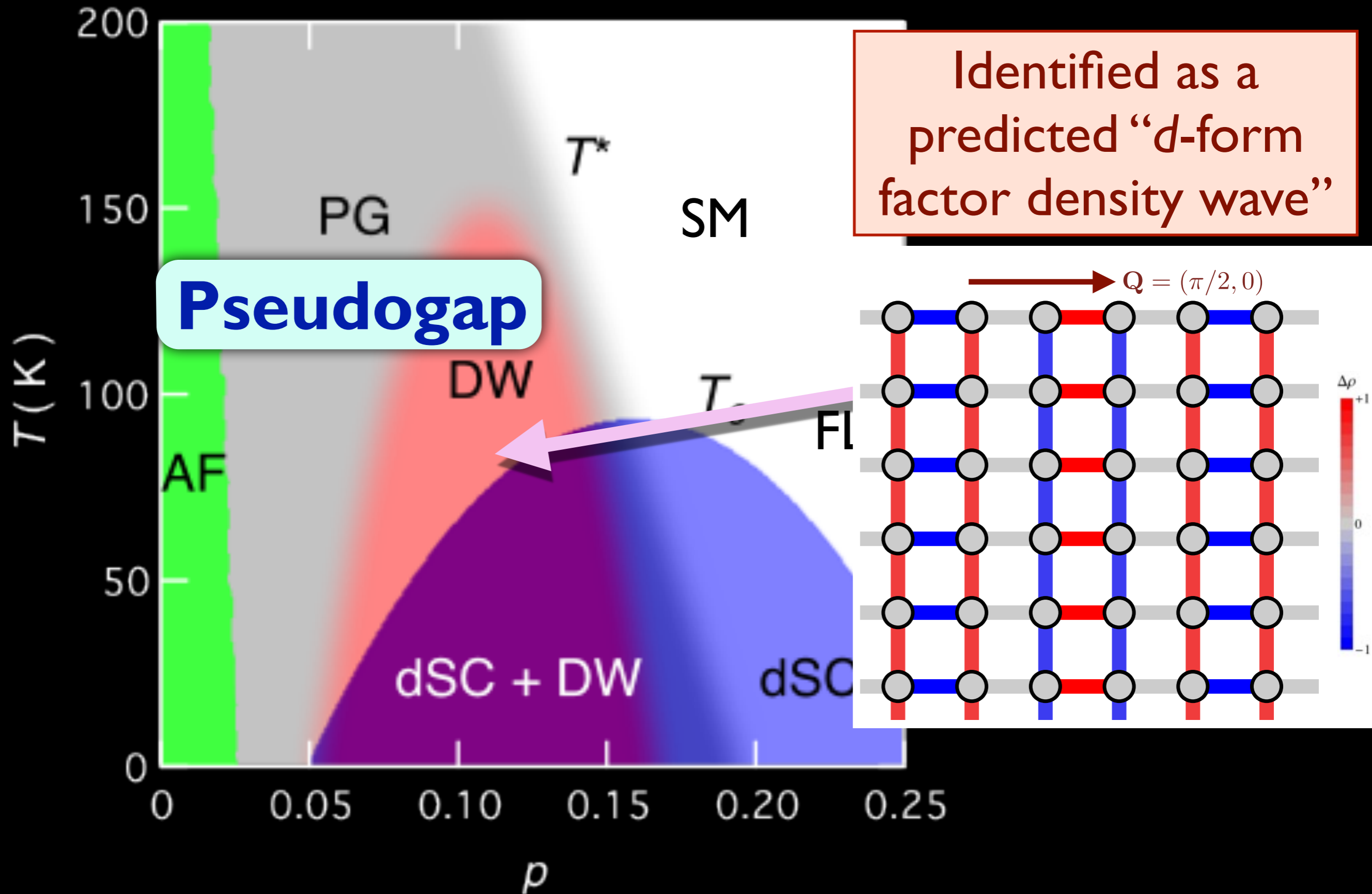
Pseudogap

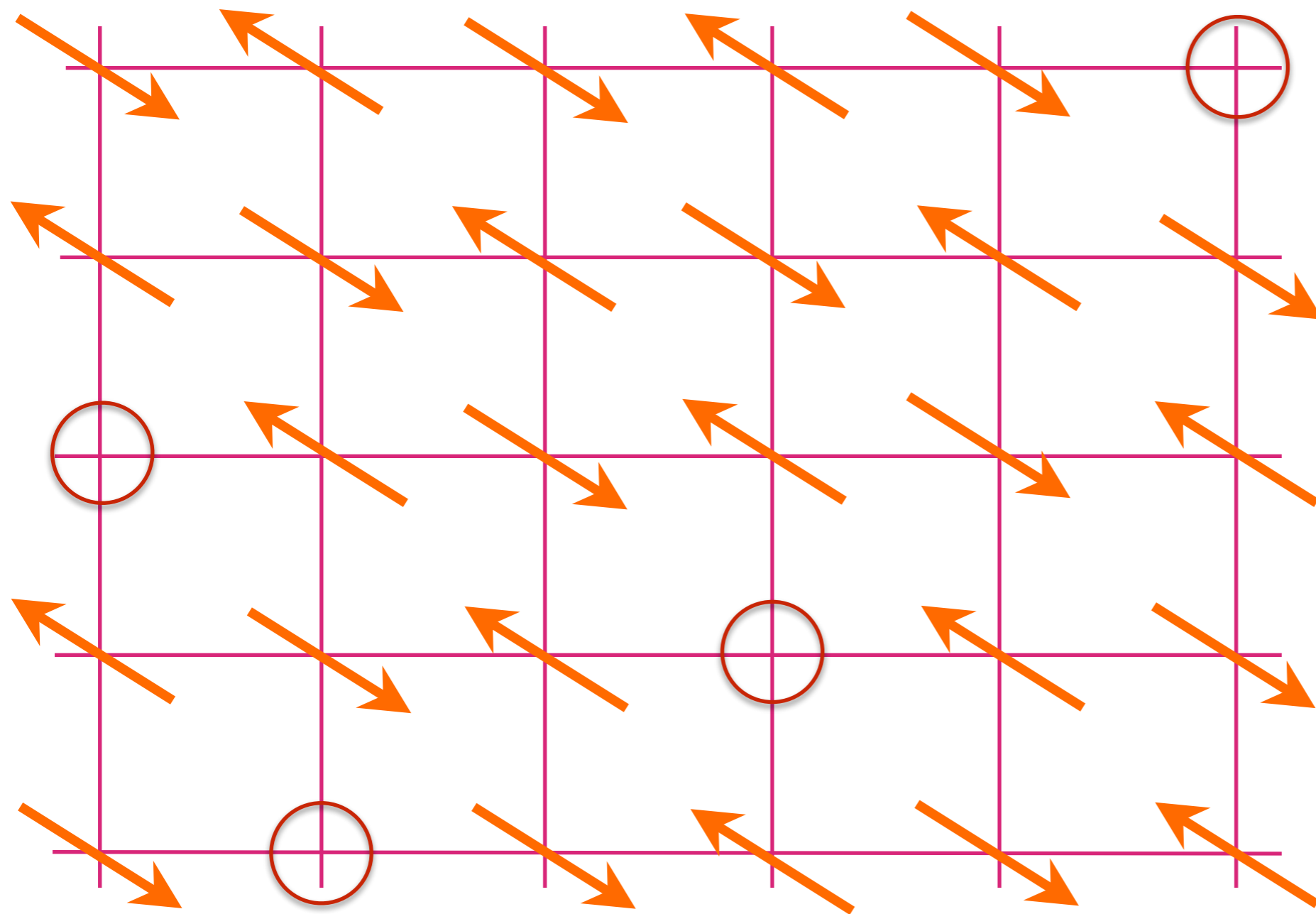
Density wave (DW) order at low T and p



M. A. Metlitski and S. Sachdev, PRB **82**, 075128 (2010). S. Sachdev R. La Placa, PRL **111**, 027202 (2013).

K. Fujita, M. H Hamidian, S. D. Edkins, Chung Koo Kim, Y. Kohsaka, M. Azuma, M. Takano, H. Takagi, H. Eisaki, S. Uchida, A. Allais, M. J. Lawler, E.-A. Kim, S. Sachdev, and J. C. Davis, PNAS **111**, E3026 (2014)




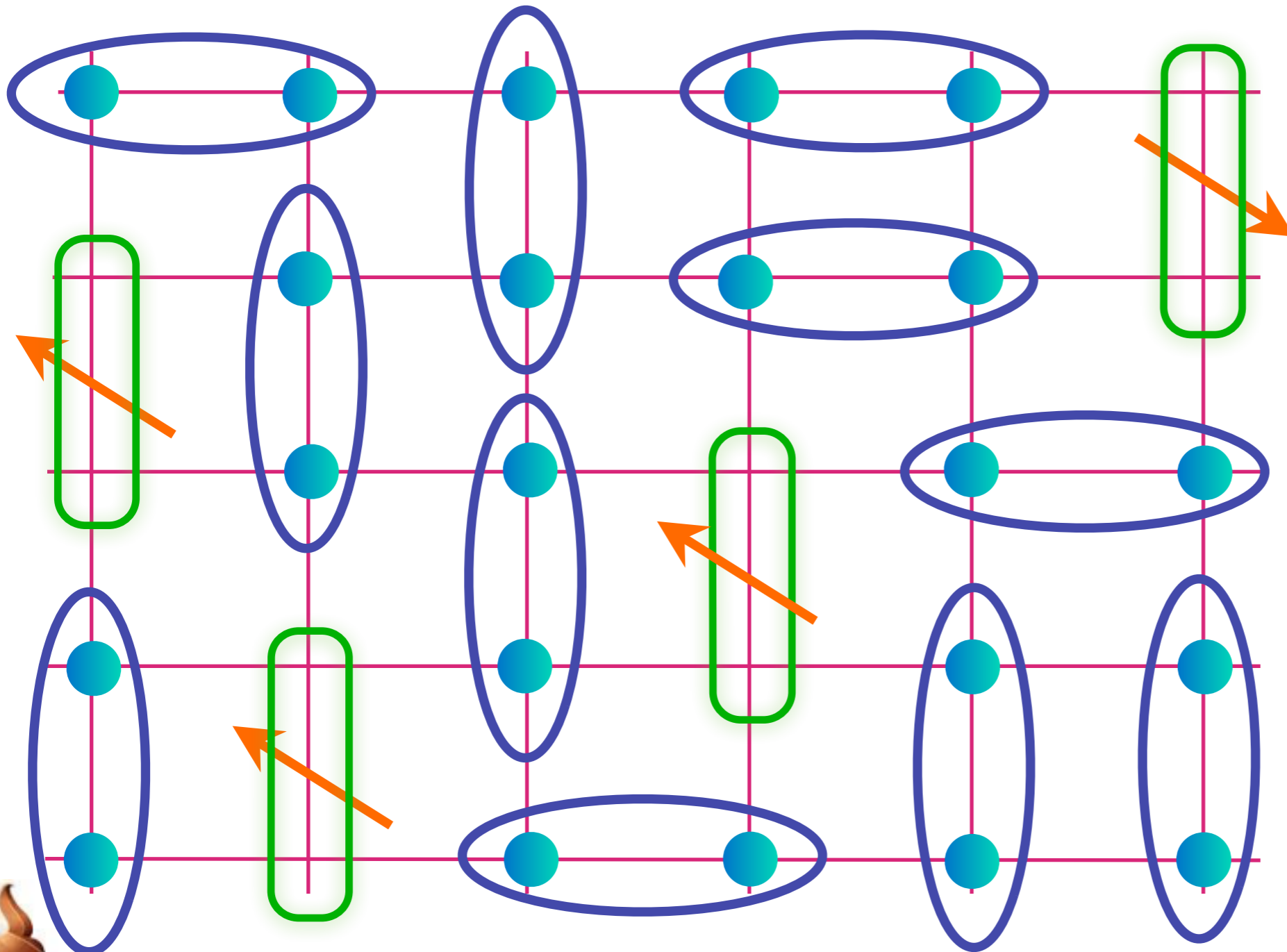


Anti-ferromagnet with p holes per square

Note: relative to the fully-filled band insulator, there are $1+p$ holes per square

Fractionalized Fermi liquid (FL*)


$$= |\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle$$



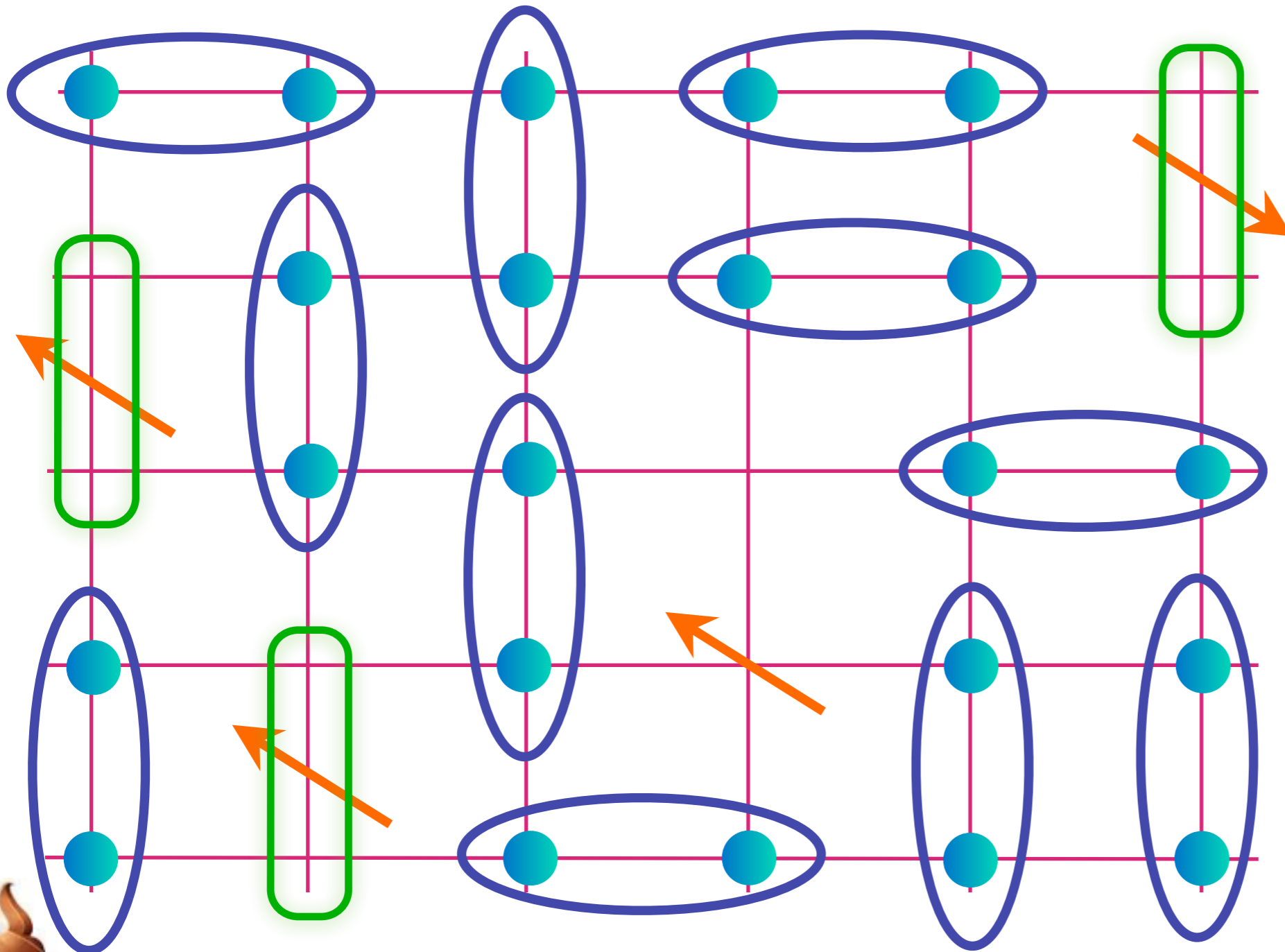
Realizes a metal with a Fermi surface of area p co-existing with “topological order”



Fractionalized Fermi liquid (FL*)



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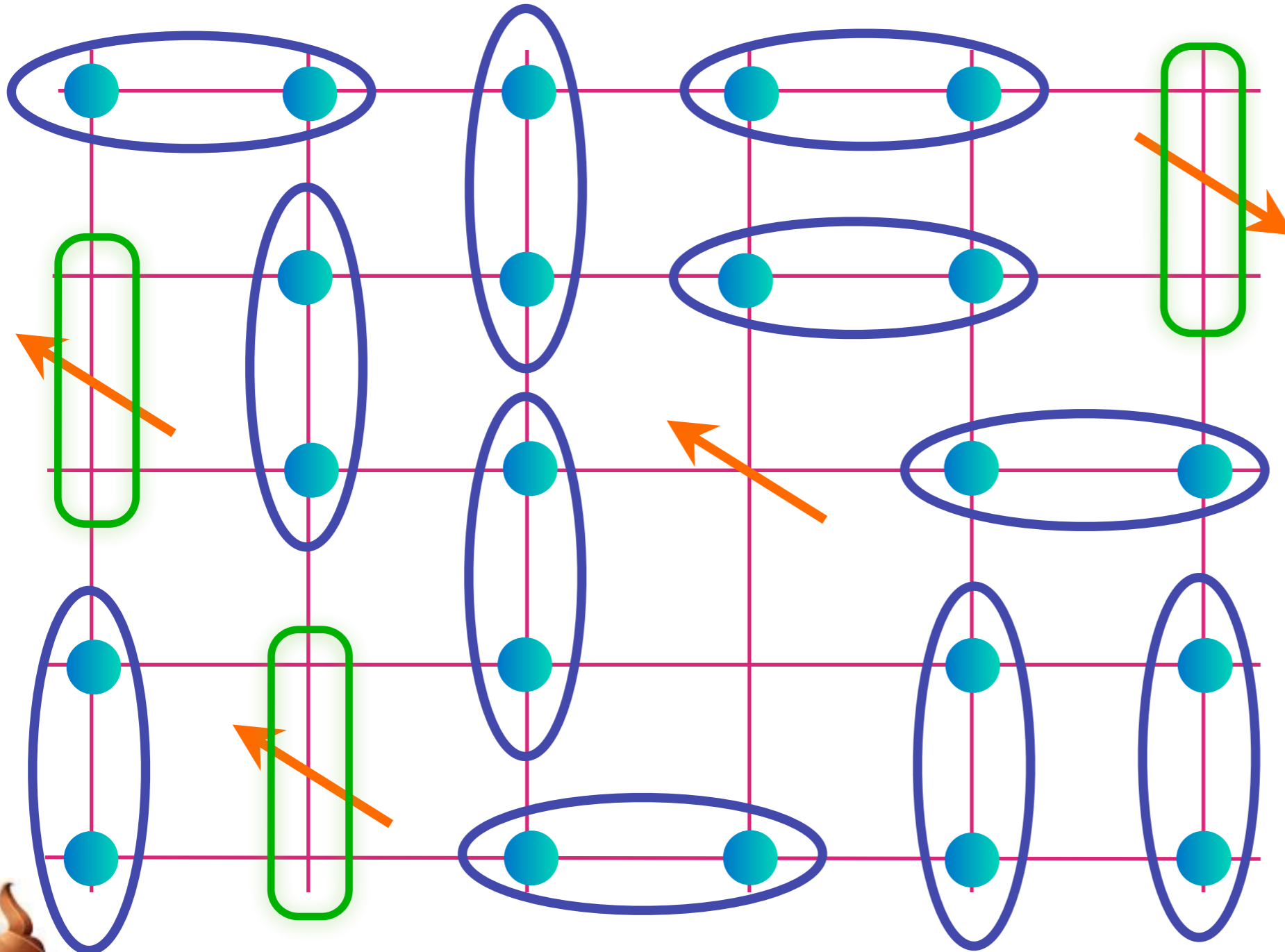


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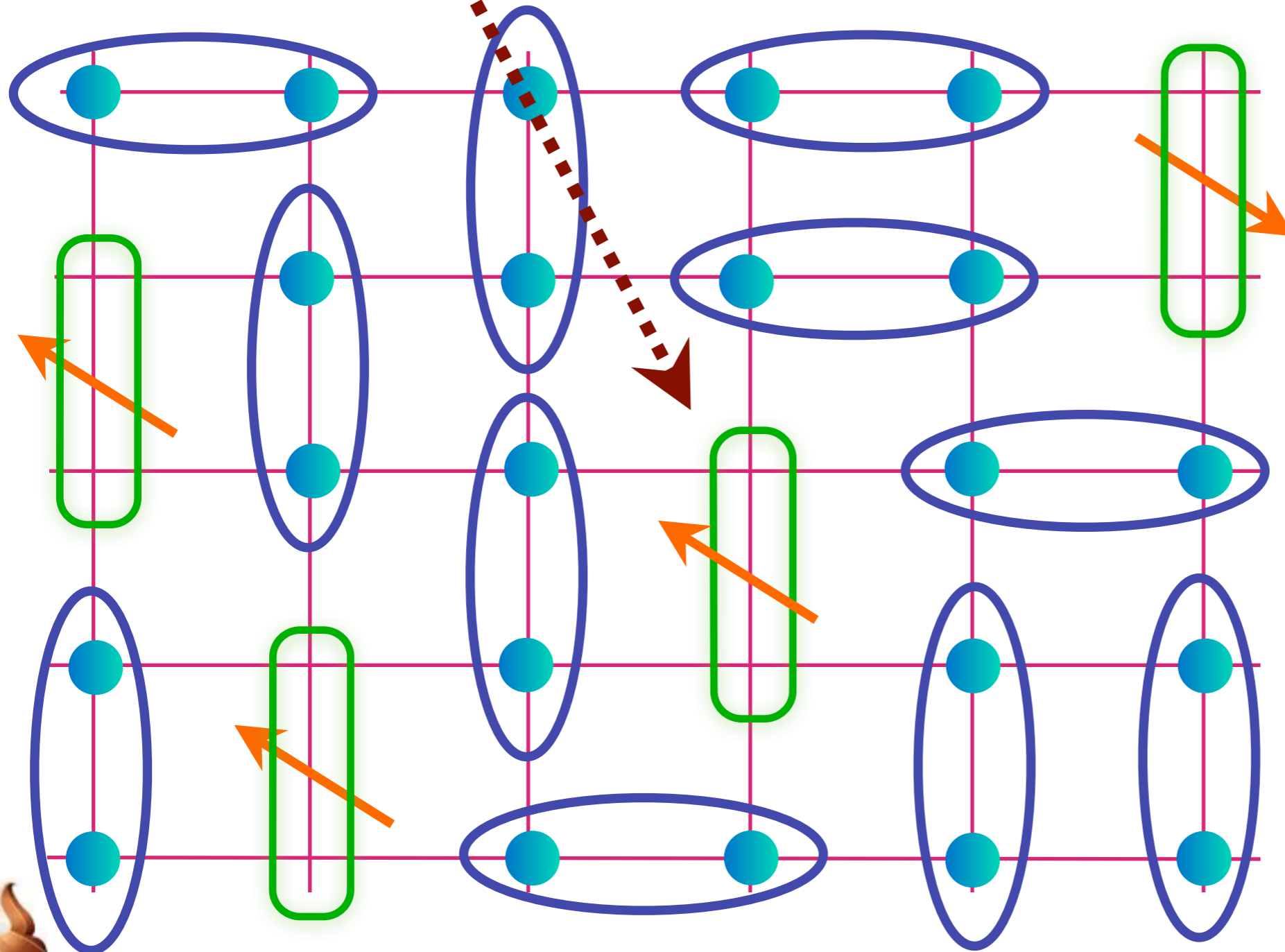

$$= |\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle$$



Realizes a metal with a Fermi surface of area p co-existing with “topological order”




A fermionic “dimer” describing a “bonding” orbital between two sites

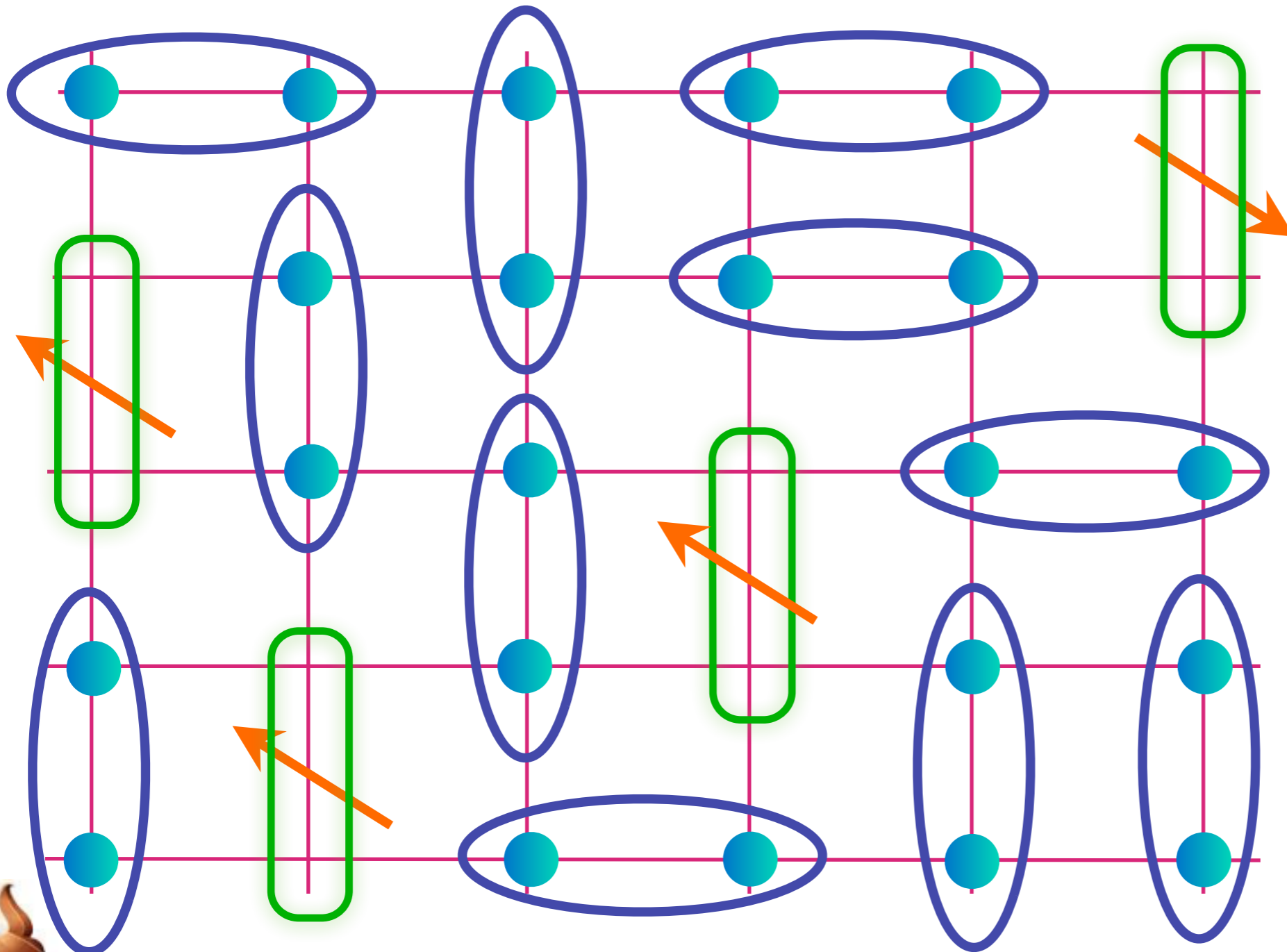


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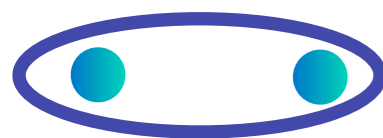

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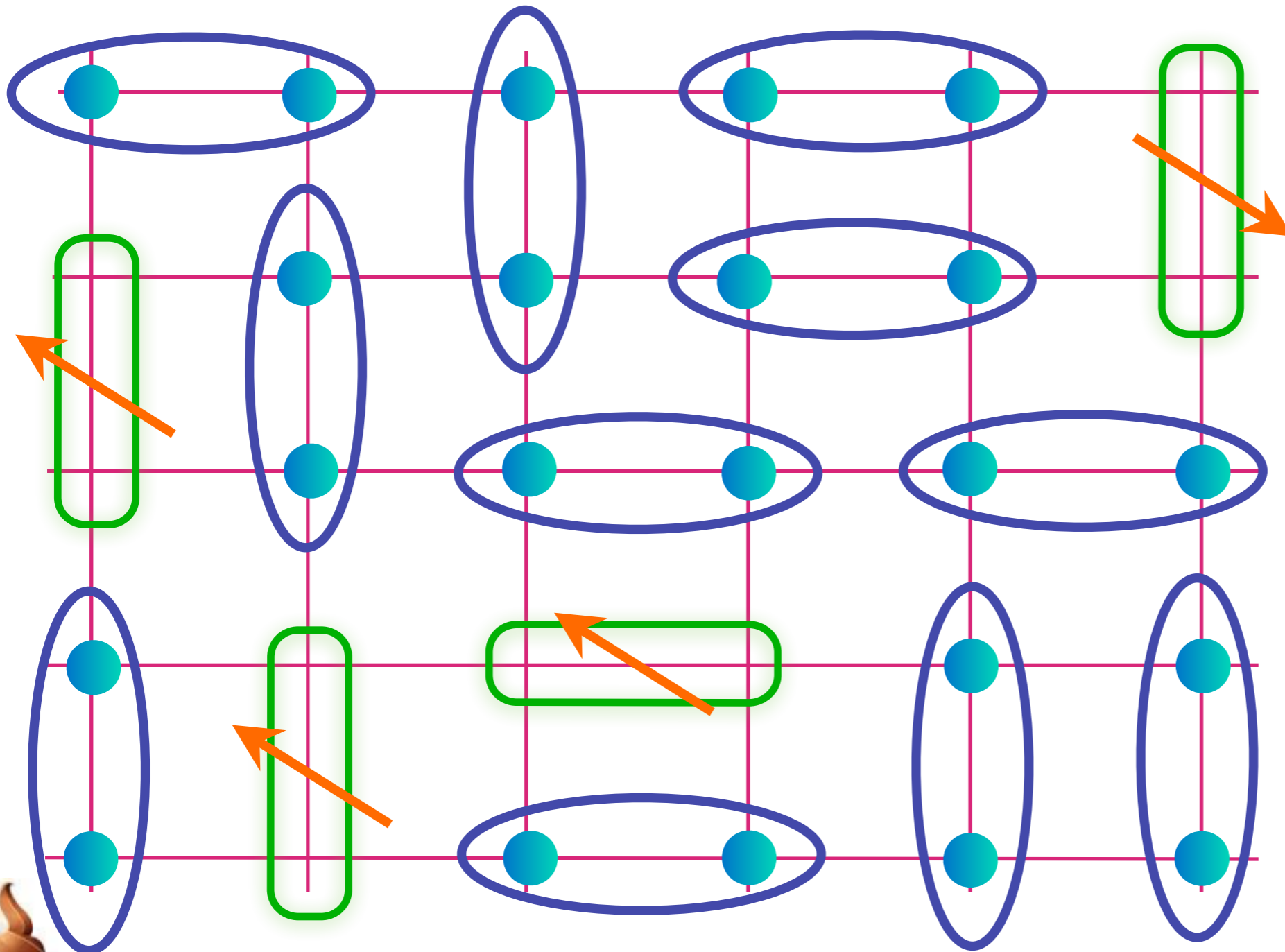


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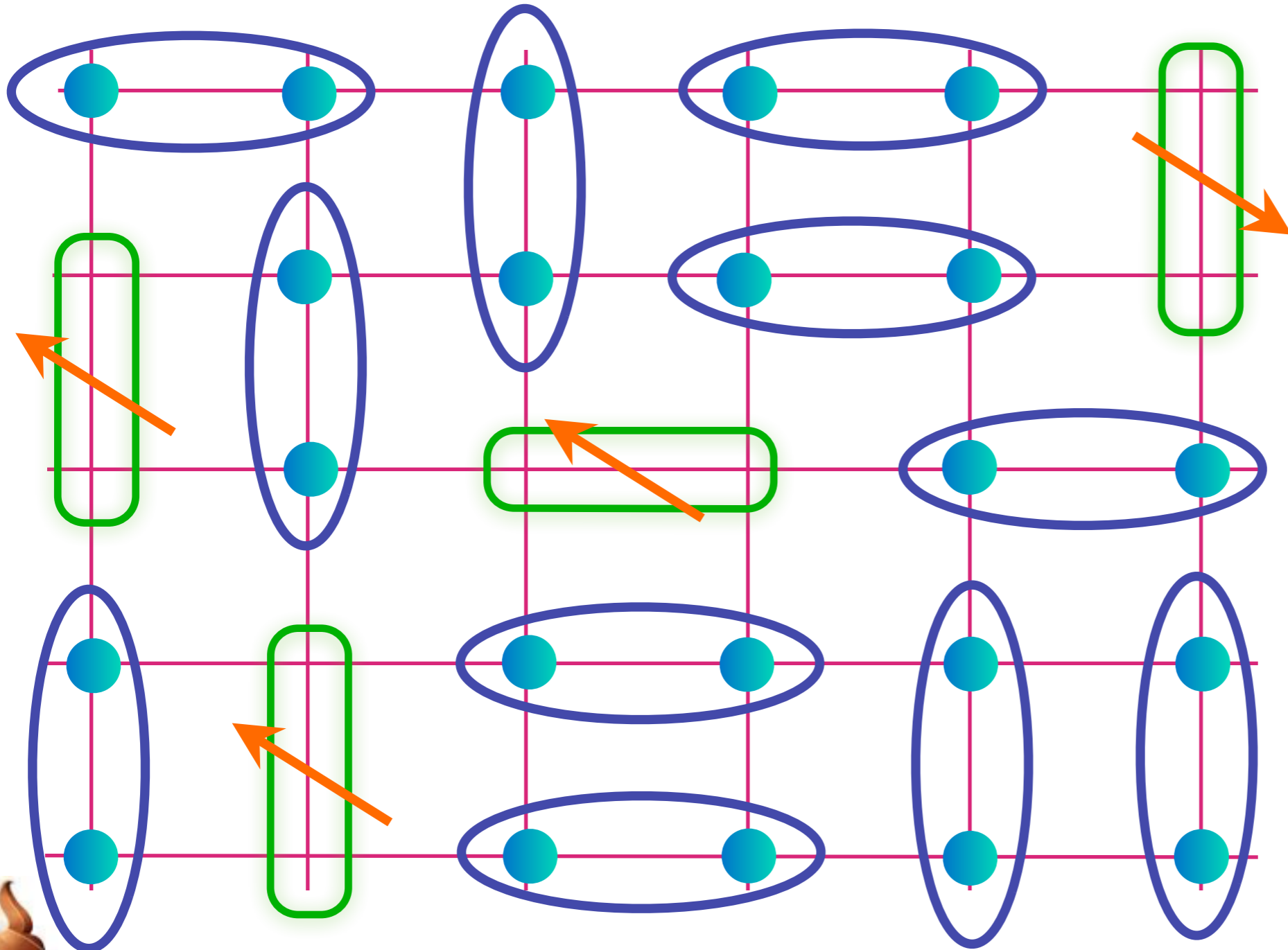
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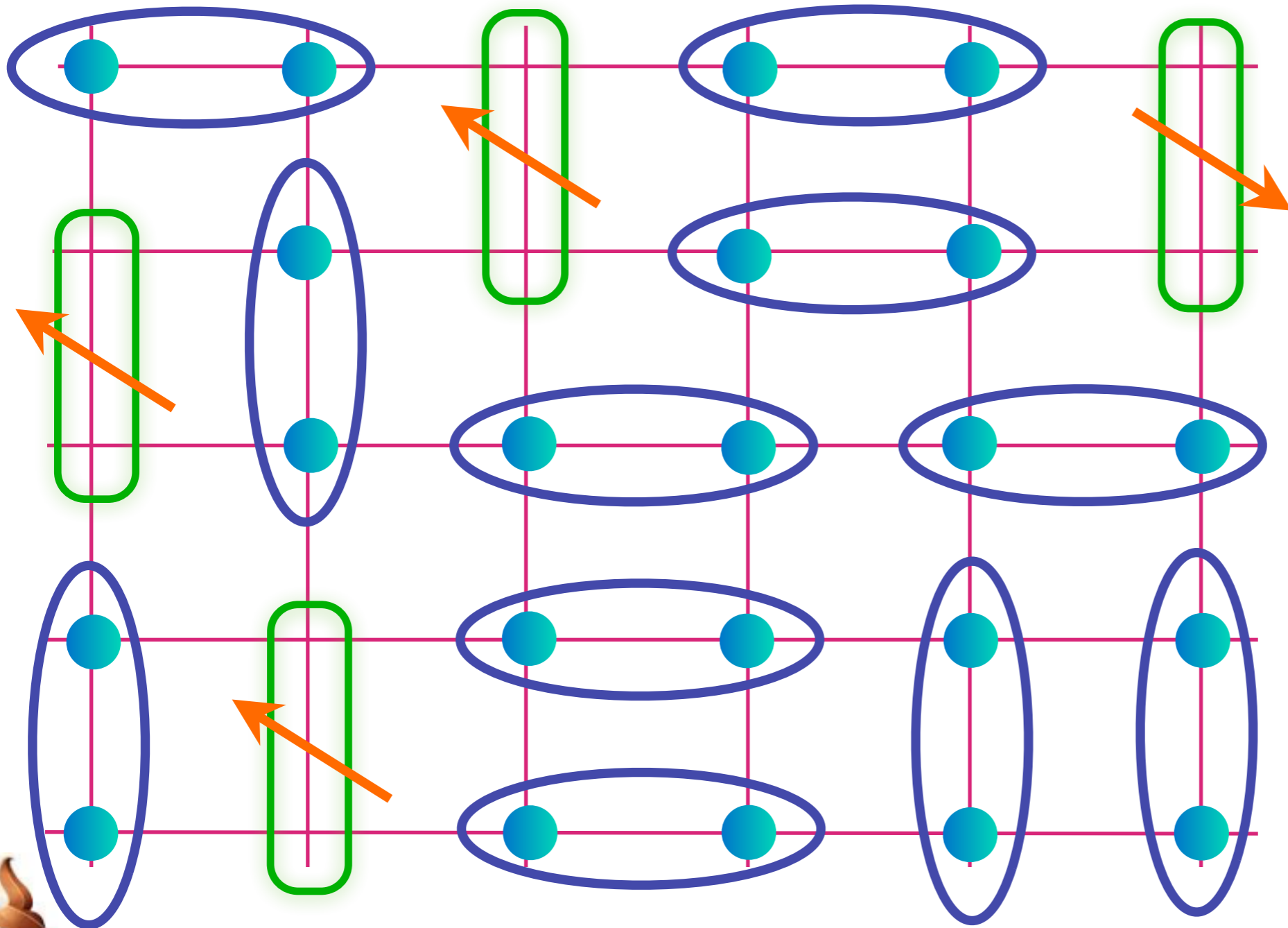


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Fractionalized Fermi liquid (FL*)

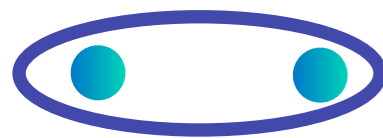
$$\text{blue oval with 2 dots} = |\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle$$

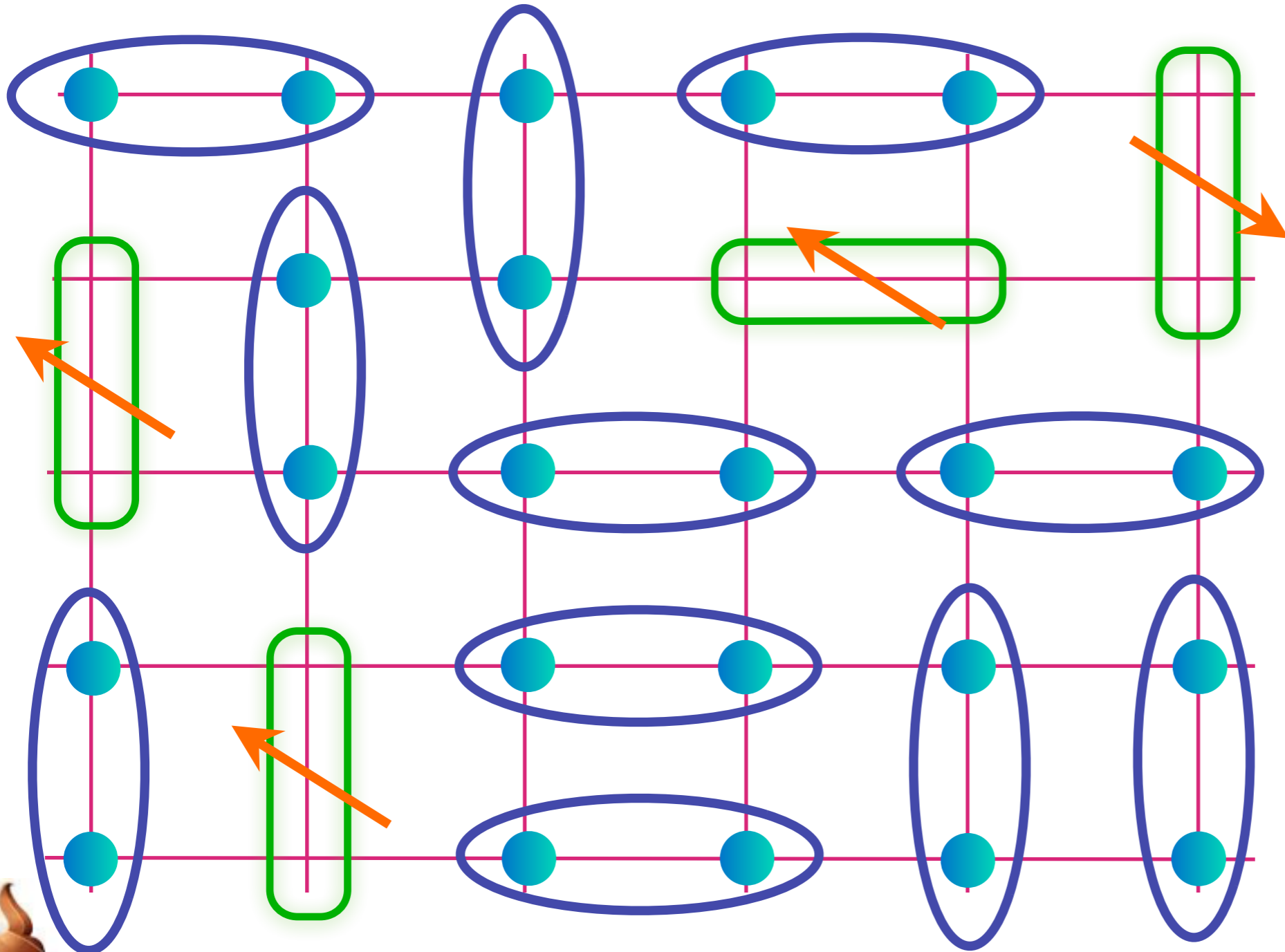


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Fractionalized Fermi liquid (FL*)



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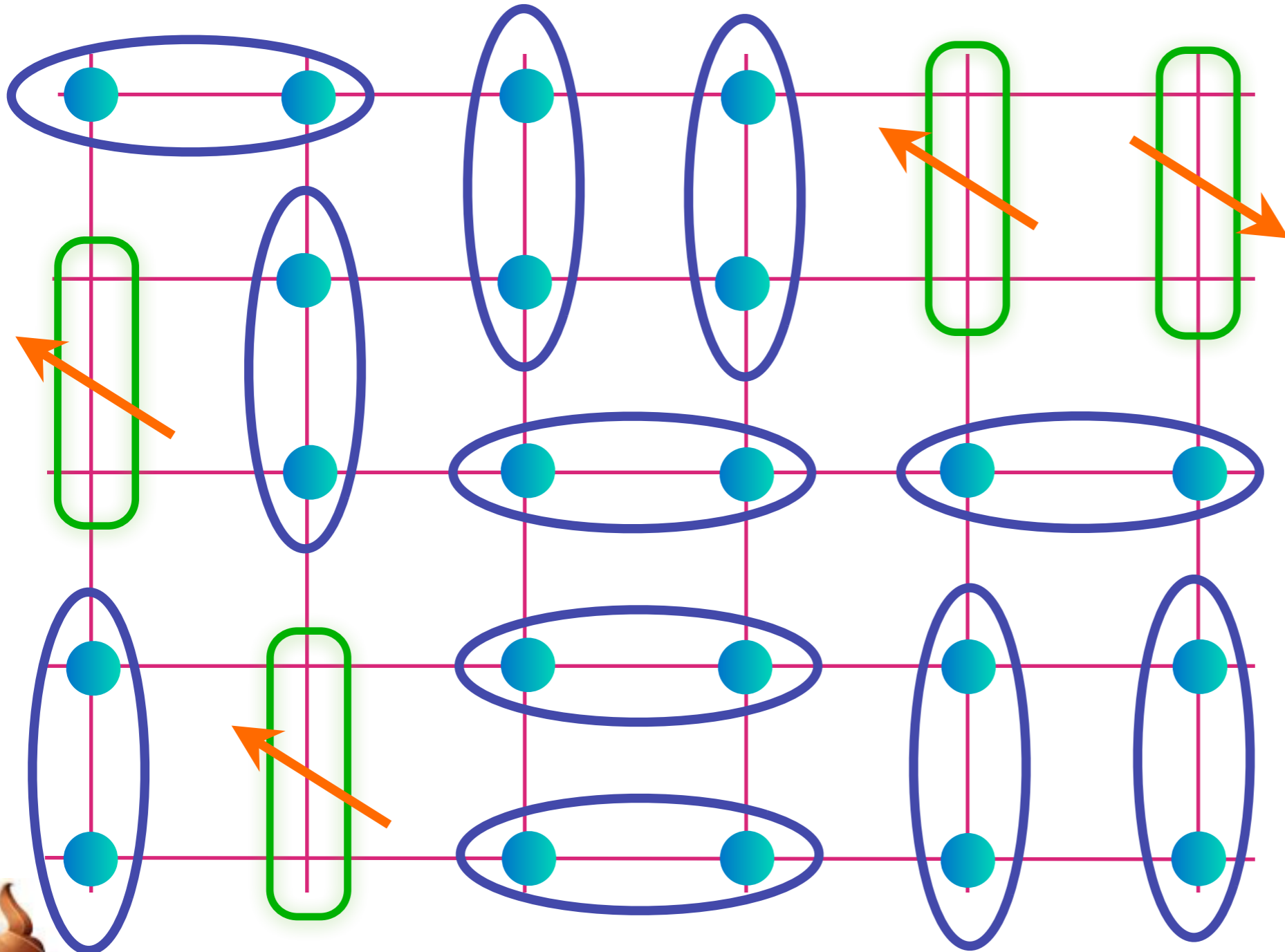


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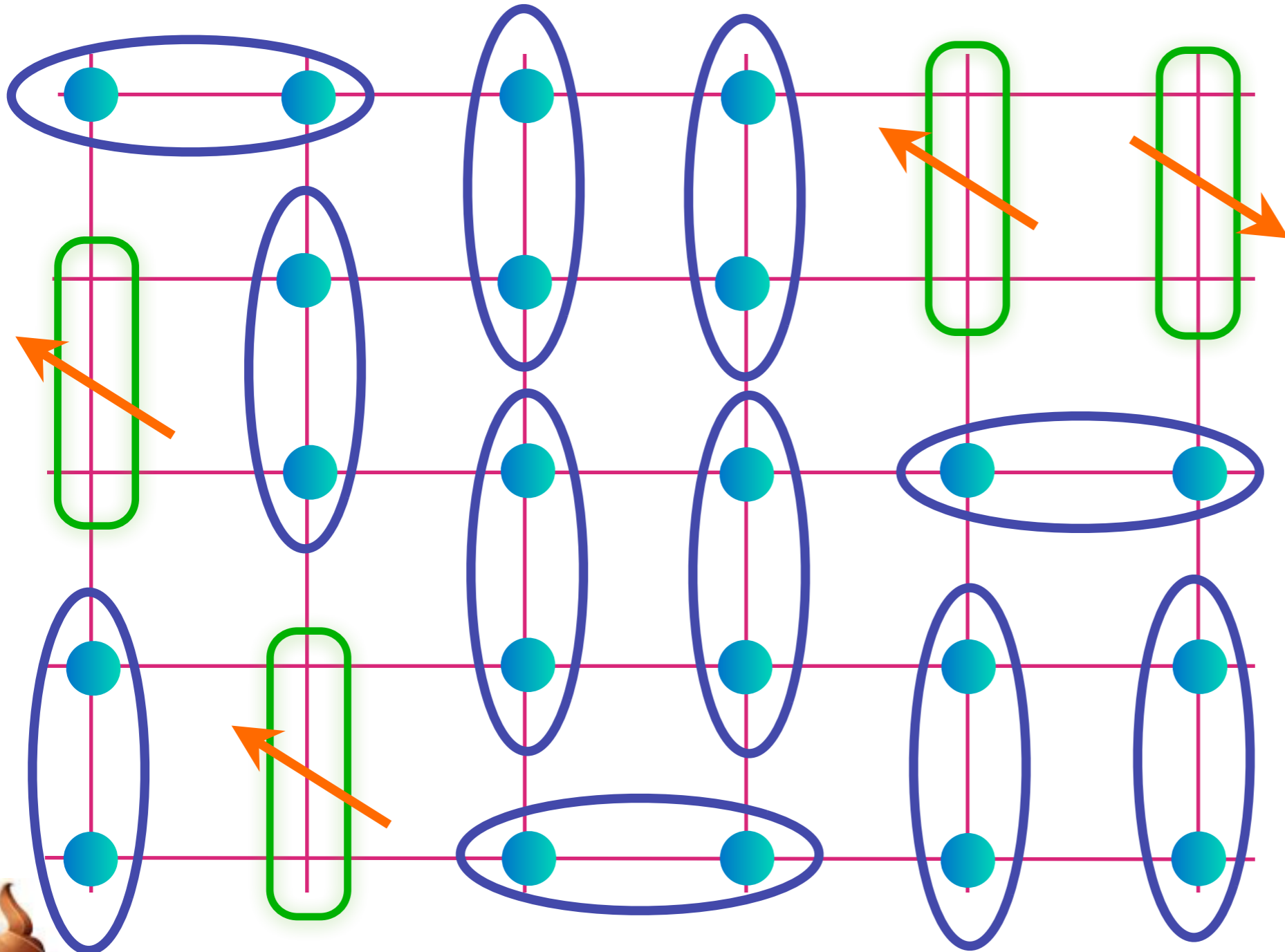


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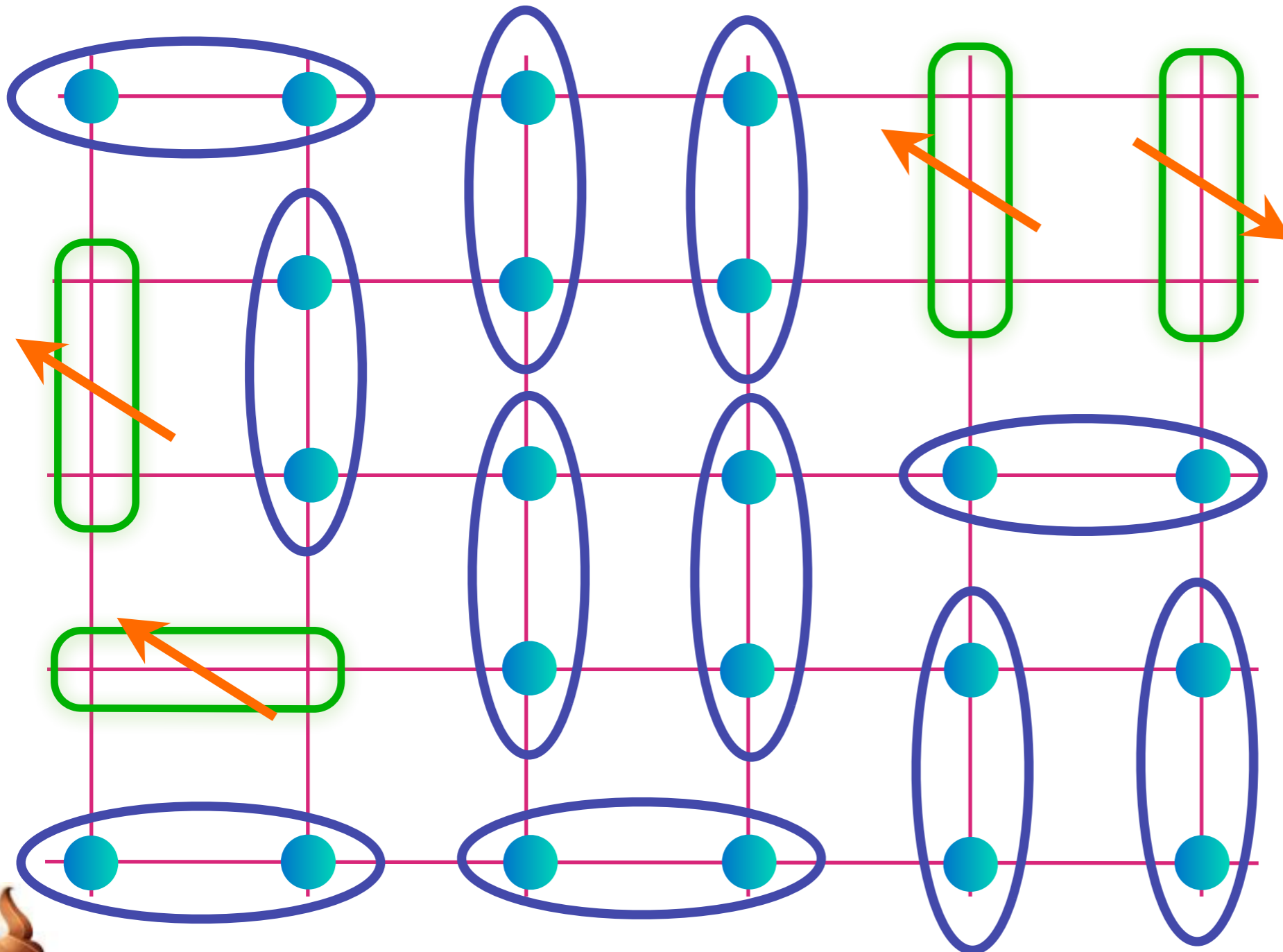


Realizes a metal with a Fermi surface of area p co-existing with “topological order”



Fractionalized Fermi liquid (FL*)


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Realizes a metal with a Fermi surface of area p co-existing with “topological order”

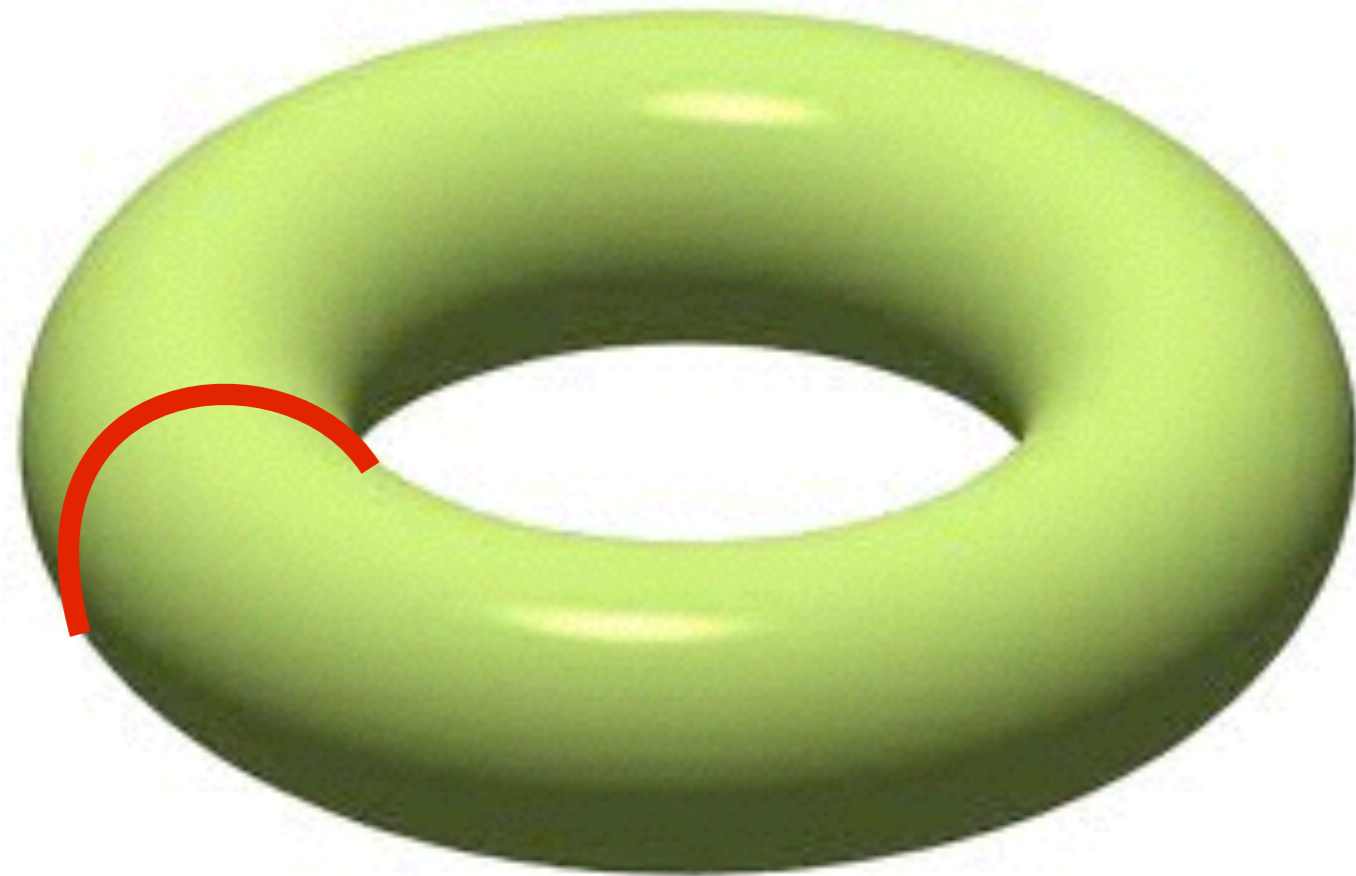


Topological order



Place
pseudogap
metal on a
torus;

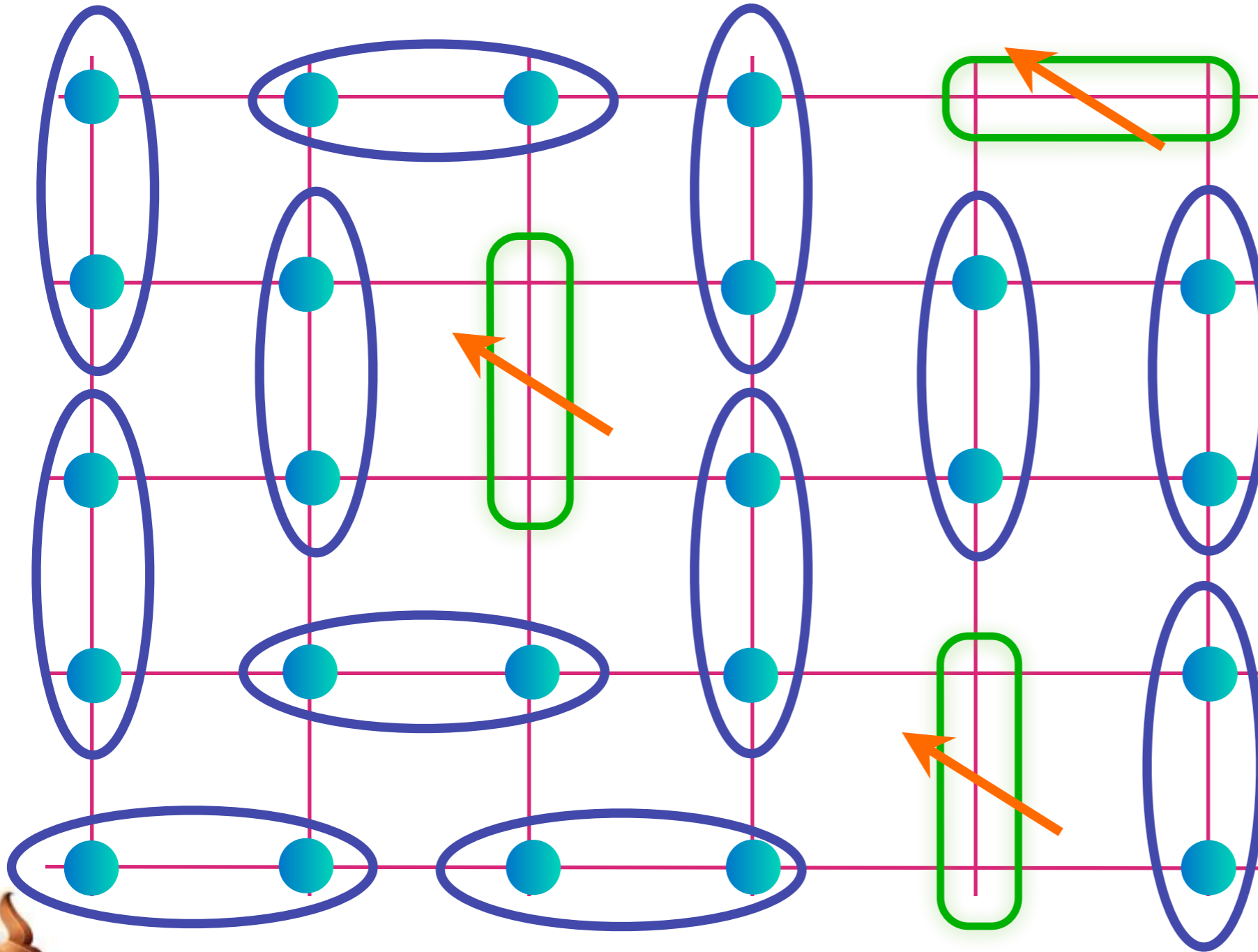
Topological order



Place
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obtain
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with the
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change sign of
every dimer
across red line

Topological order

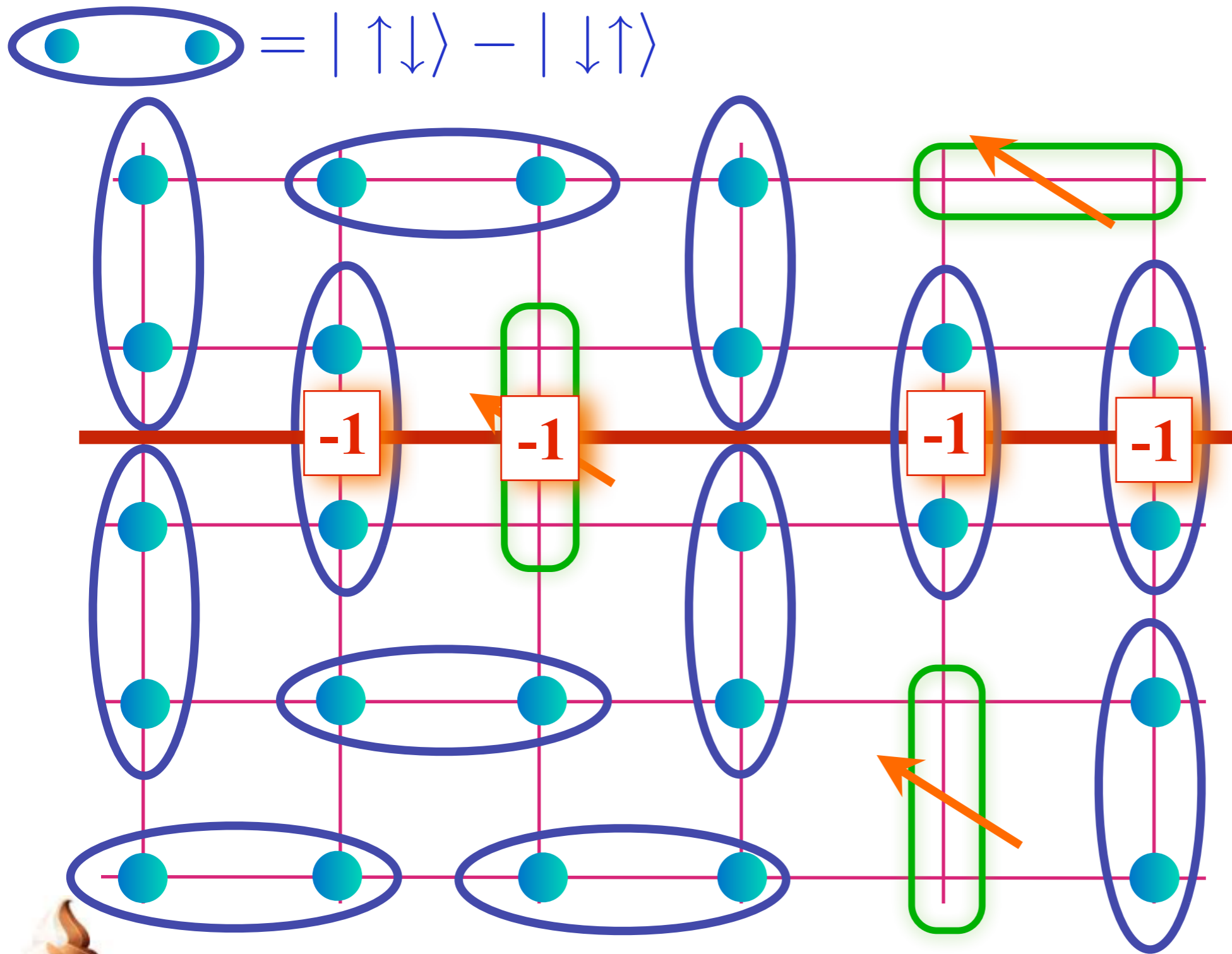

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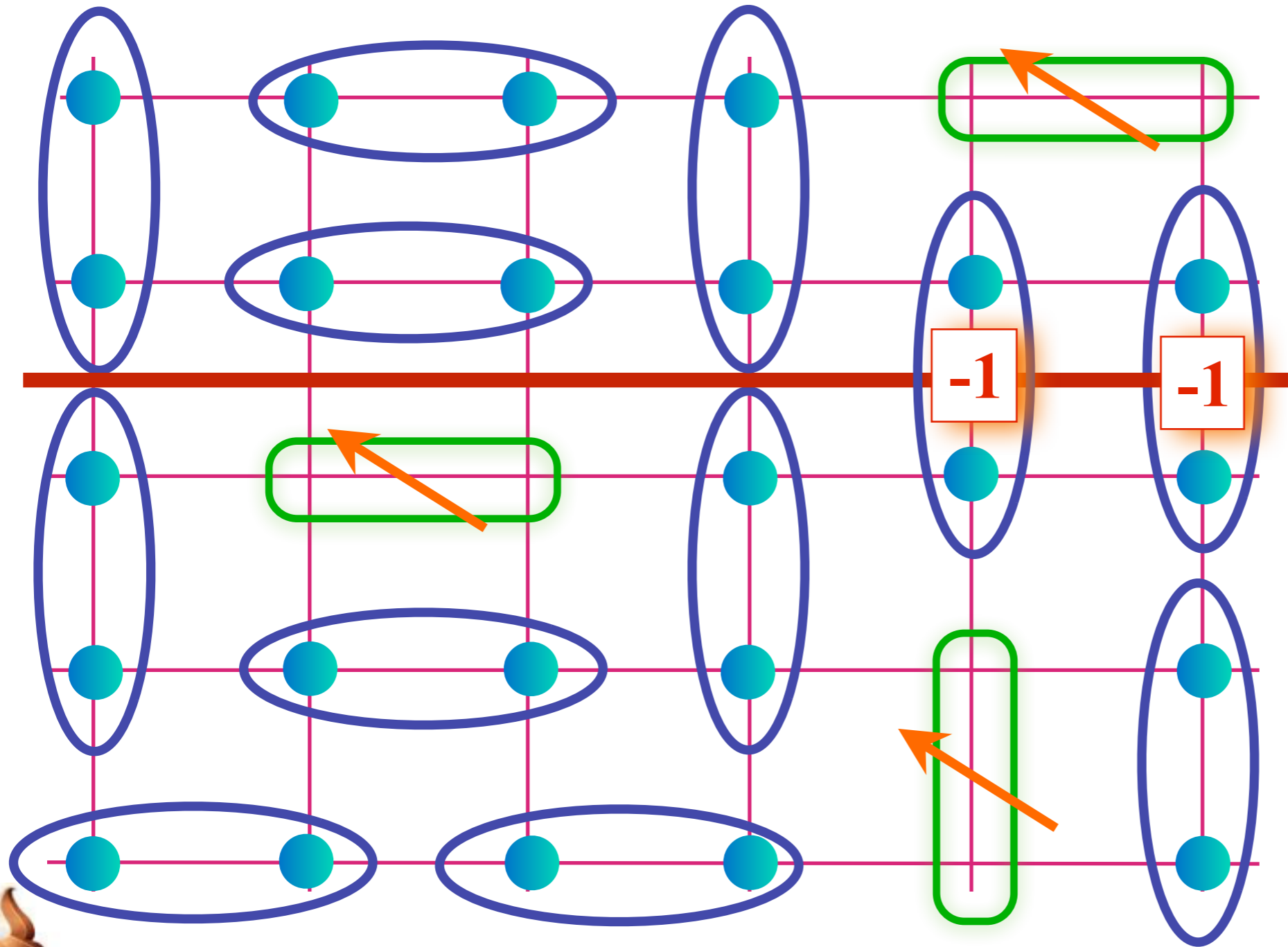


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Topological order

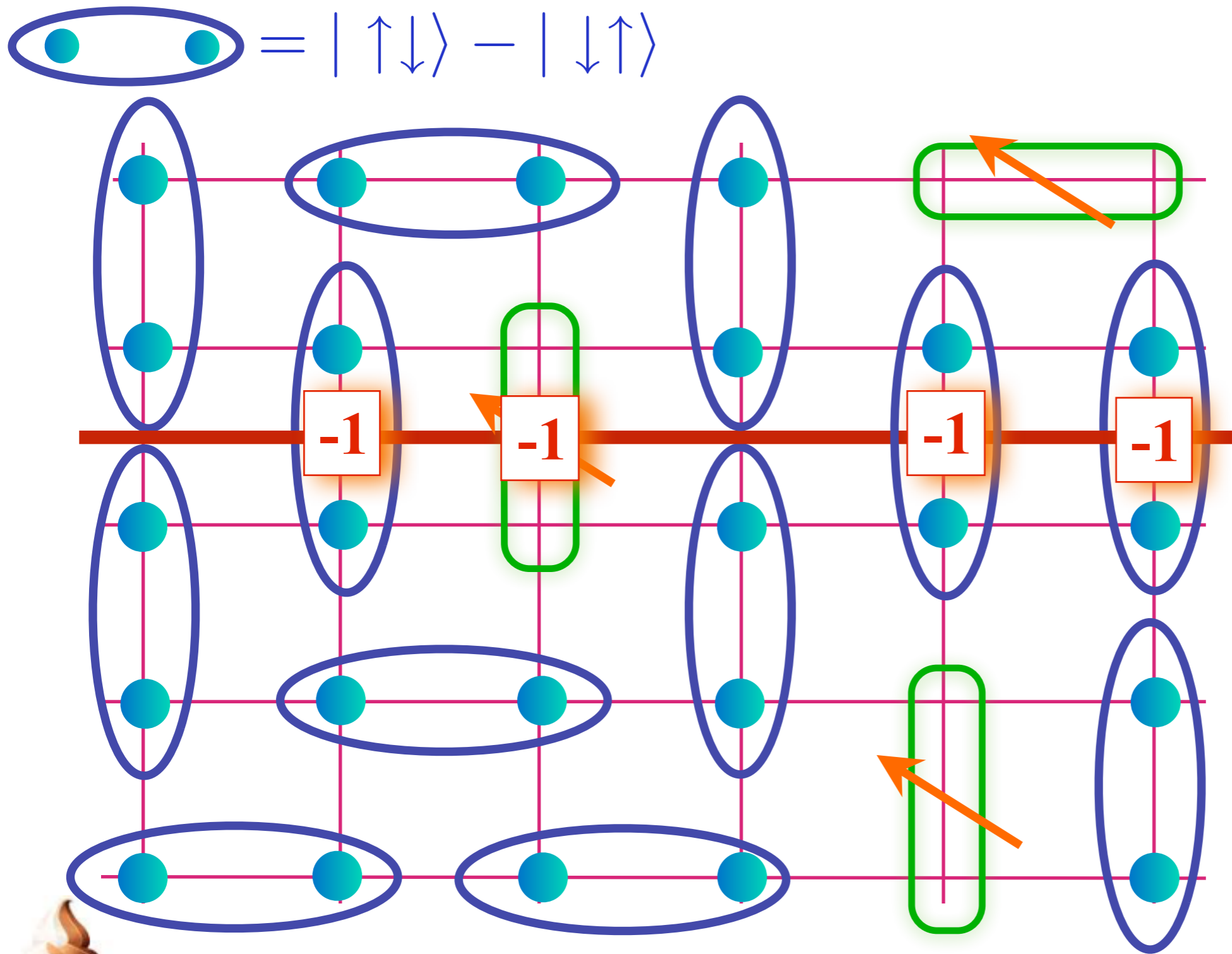
$$\text{[Diagram of two teal dots in a blue oval]} = |\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle$$



Place pseudogap metal on a torus; obtain “topological” states nearly degenerate with the ground state: change sign of every dimer across red line



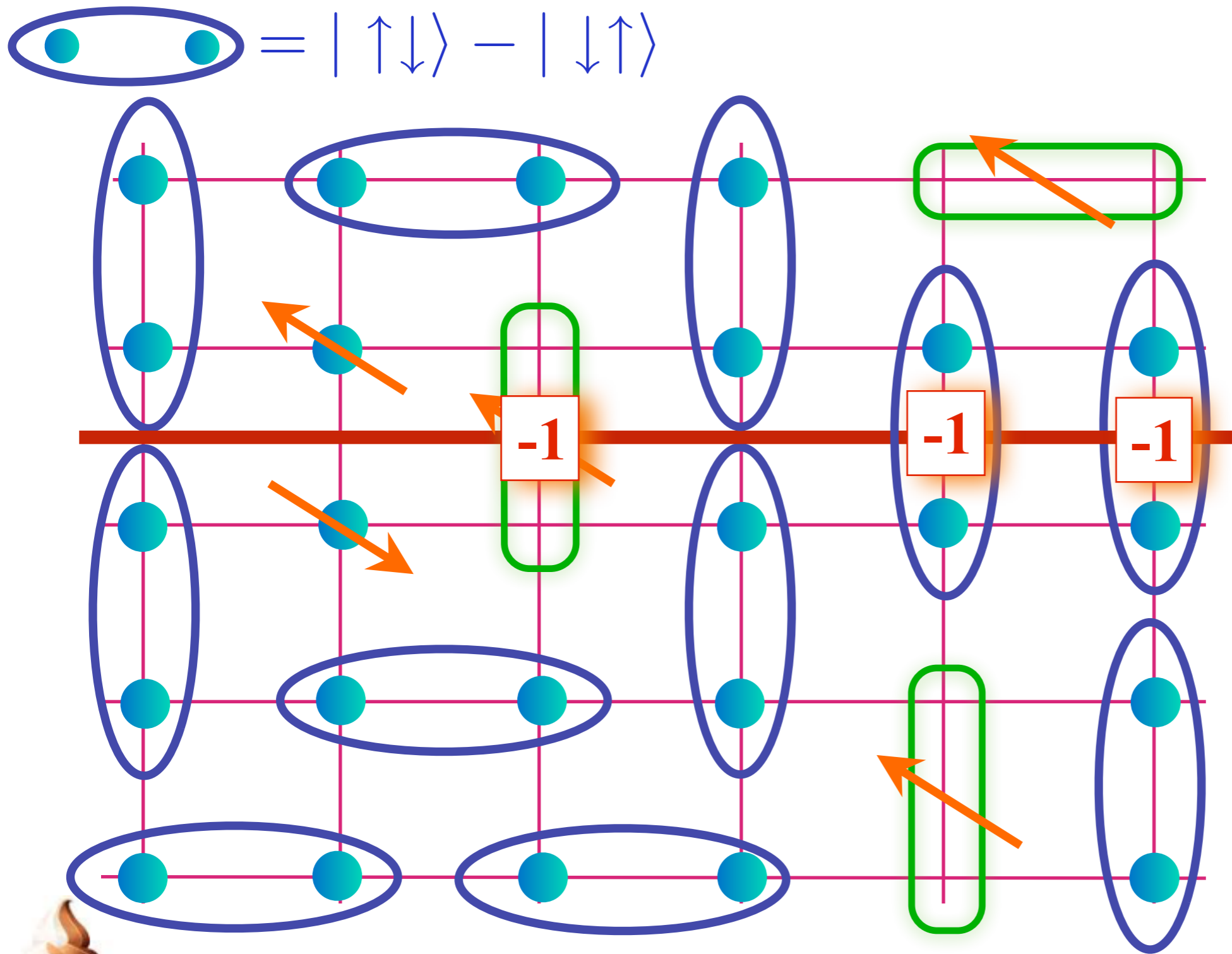
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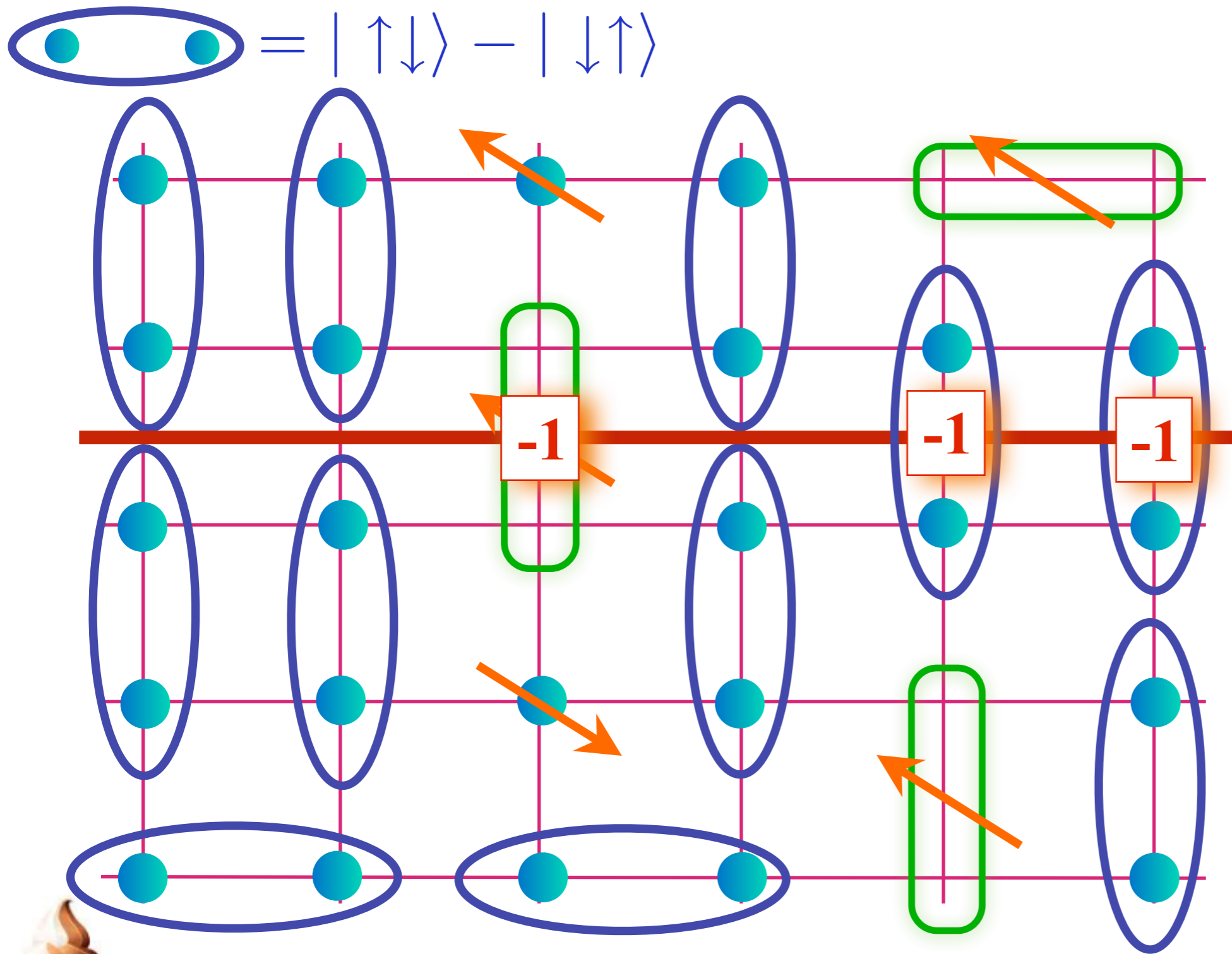
Topological order



Place pseudogap metal on a torus; to change overall sign, a pair of “spinons” have to be moved globally around a circumference of the torus



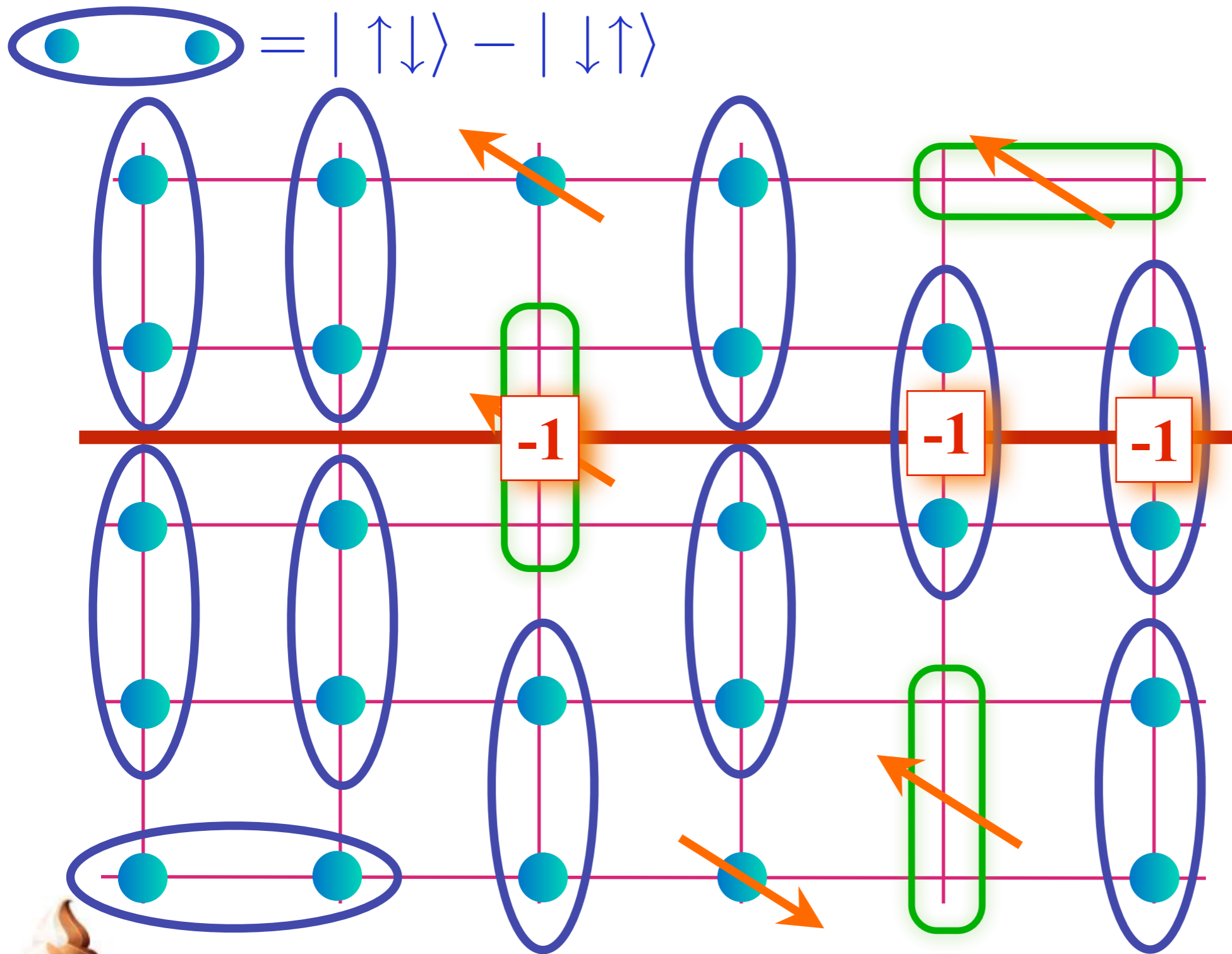
Topological order



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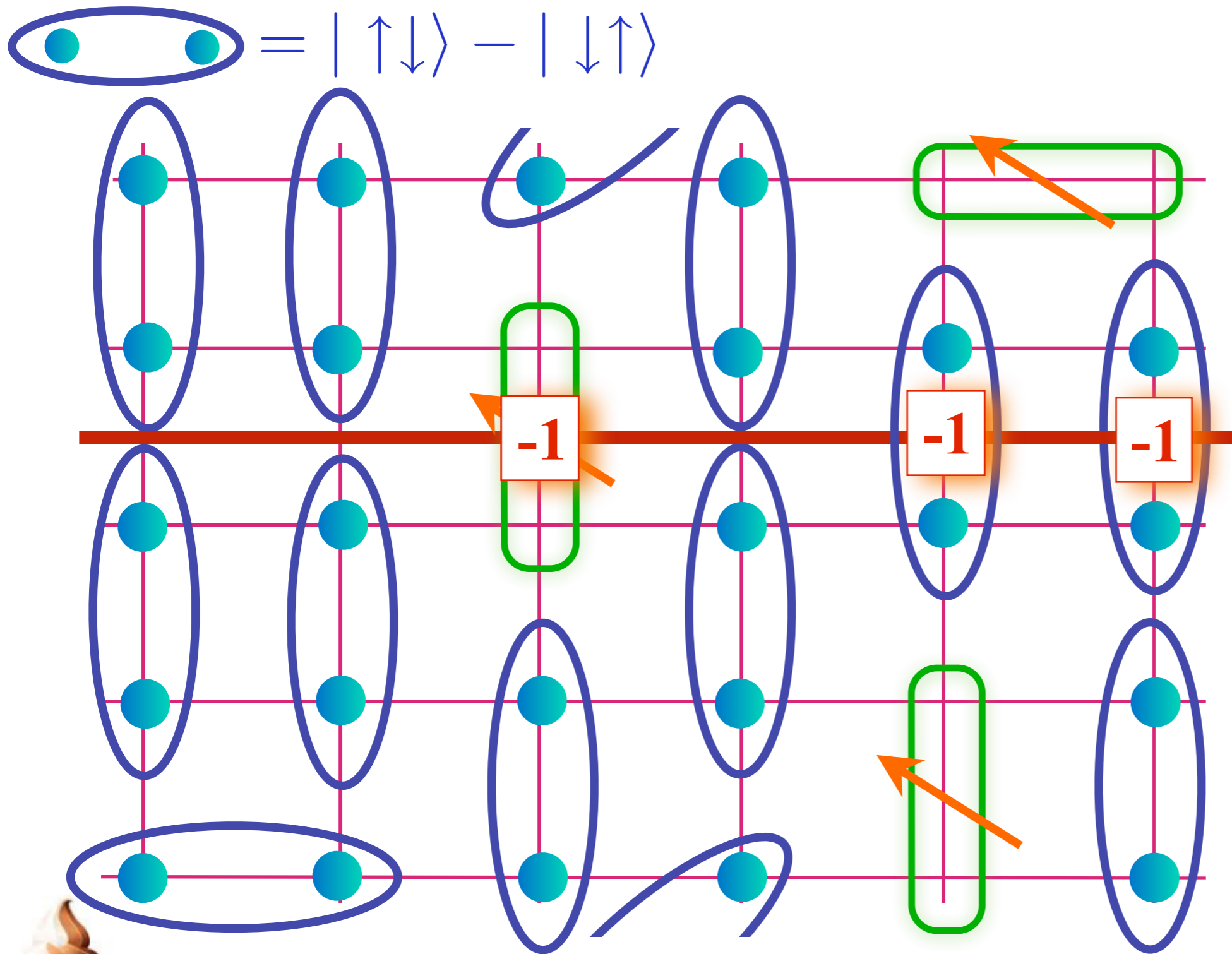
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Topological order



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Outline

1. The pseudogap metal

Fermi liquid co-existing with topological order

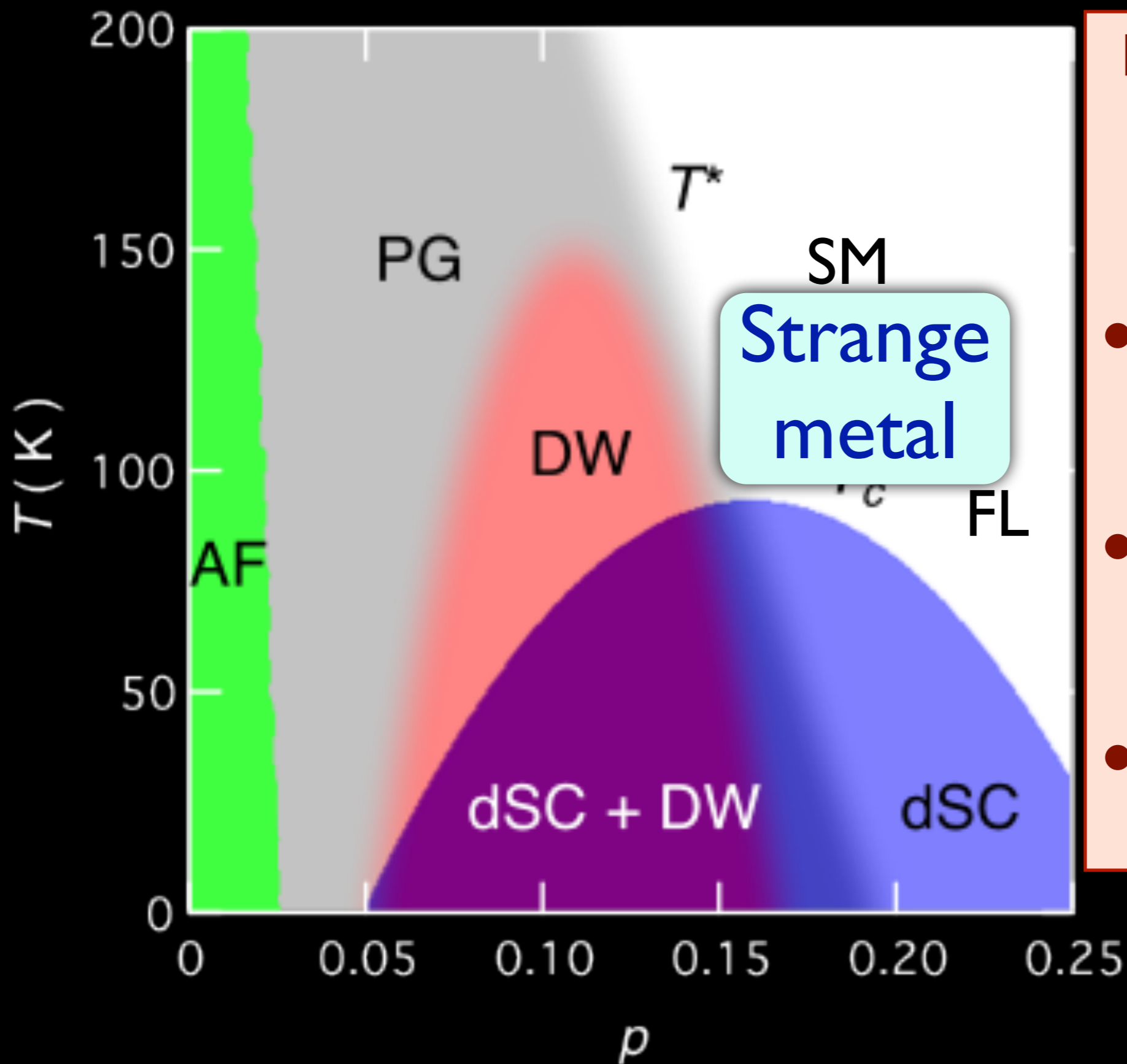
2. The strange metal

Metal without quasiparticles

Infinite-range model: dual to extremal charged

black holes and yields

Bekenstein-Hawking entropy

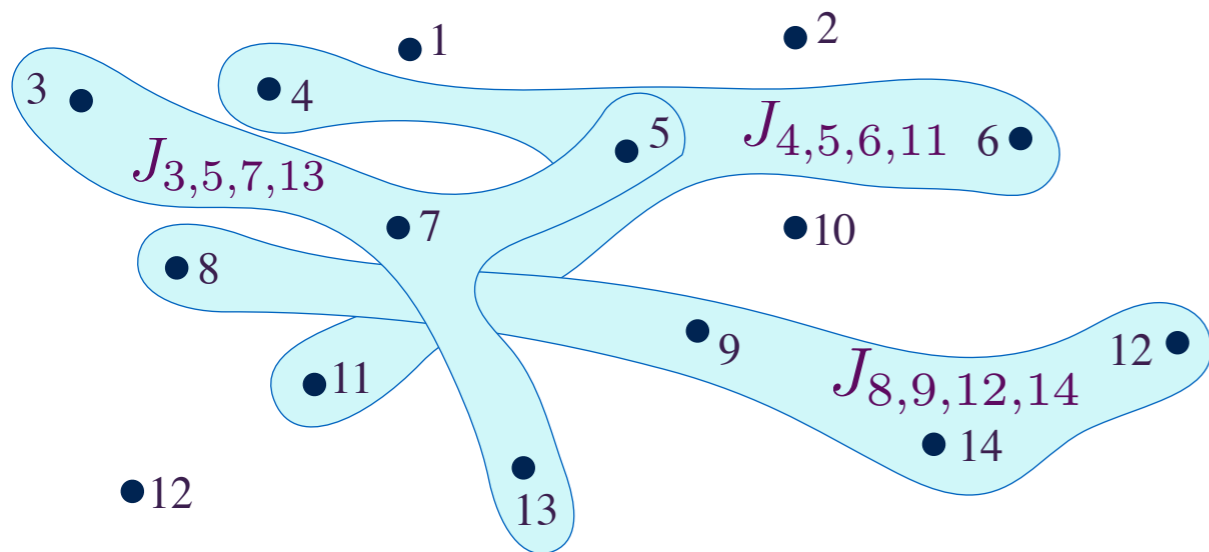


Many experimental indications of a quantum state which has:

- a continuously variable density at zero temperature,
- bulk excitations of arbitrarily low energy,
- and no long-lived quasiparticles.



$$H = \frac{1}{(2N)^{3/2}} \sum_{i,j,k,\ell=1}^N J_{ij;kl} c_i^\dagger c_j^\dagger c_k c_\ell$$



$$Q = \frac{1}{N} \sum_i \langle c_i^\dagger c_i \rangle.$$

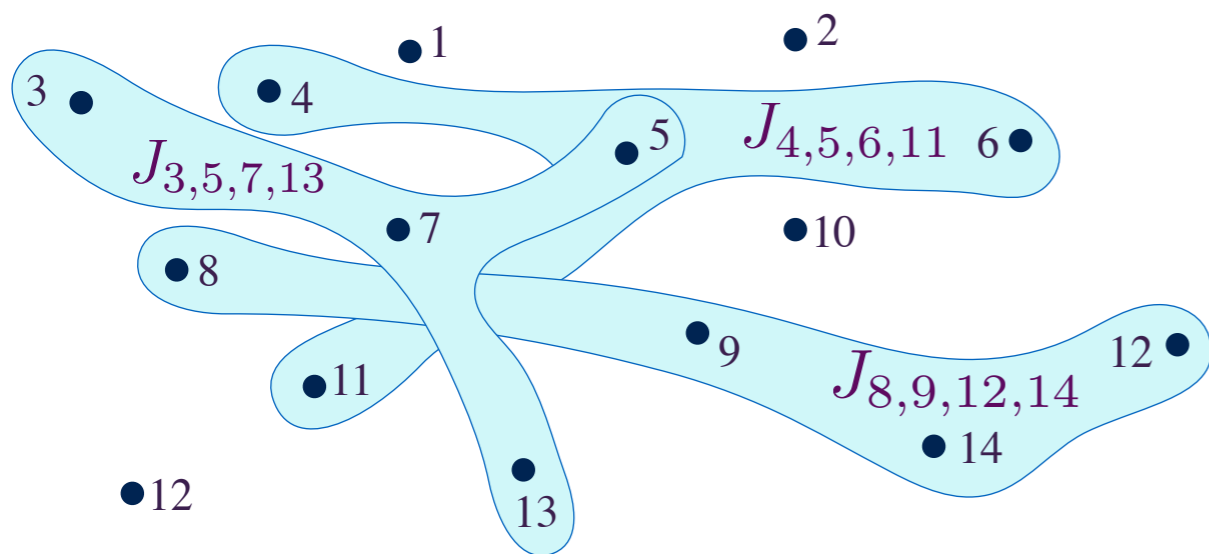
$c_i c_j + c_j c_i = 0$
 $c_i c_j^\dagger + c_j^\dagger c_i = \delta_{ij}$
 $J_{ij;kl}$ independent
 random numbers

An infinite-range model of a strange metal

S. Sachdev and J. Ye, Phys. Rev. Lett. **70**, 3339 (1993)
 A. Kitaev, unpublished
 S. Sachdev, arXiv:1506.05111



$$H = \frac{1}{(2N)^{3/2}} \sum_{i,j,k,\ell=1}^N J_{ij;kl} c_i^\dagger c_j^\dagger c_k c_\ell$$



$$Q = \frac{1}{N} \sum_i \langle c_i^\dagger c_i \rangle.$$

Local fermion density of states

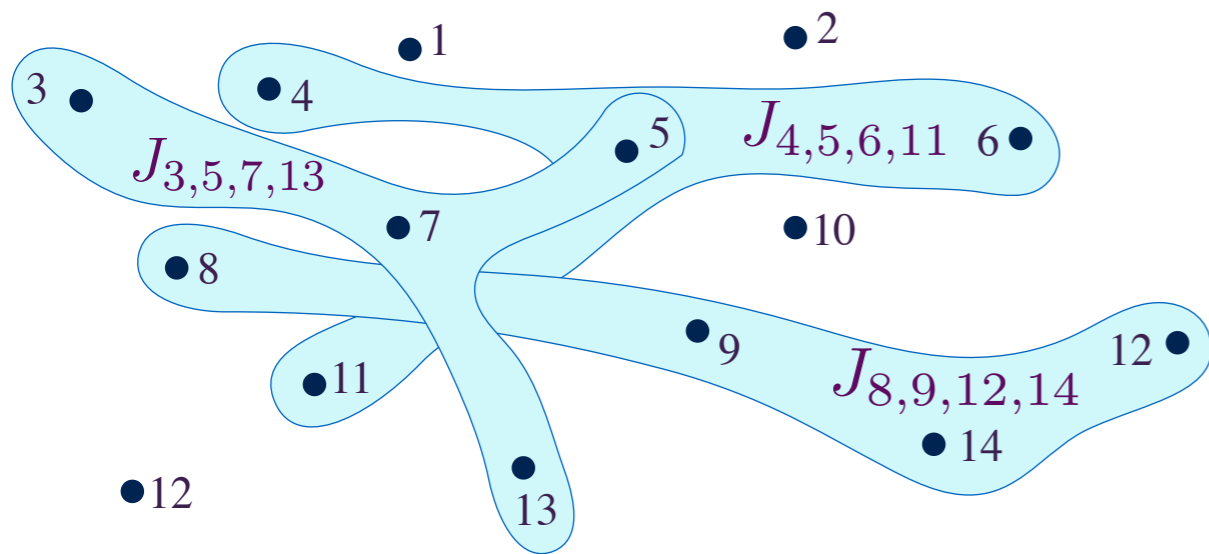
$$\rho(\omega) \sim \begin{cases} \omega^{-1/2}, & \omega > 0 \\ e^{-2\pi\epsilon} |\omega|^{-1/2}, & \omega < 0. \end{cases}$$

S. Sachdev and J. Ye, Phys. Rev. Lett. **70**, 3339 (1993)

$c_i c_j + c_j c_i = 0$
 $c_i c_j^\dagger + c_j^\dagger c_i = \delta_{ij}$
 $J_{ij;kl}$ independent
 random numbers



$$H = \frac{1}{(2N)^{3/2}} \sum_{i,j,k,\ell=1}^N J_{ij;kl} c_i^\dagger c_j^\dagger c_k c_\ell$$



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Known 'equation of state'
determines \mathcal{E} as a function of Q

$$Q = \frac{1}{4} (3 - \tanh(2\pi\mathcal{E})) - \frac{1}{\pi} \tan^{-1} (e^{2\pi\mathcal{E}})$$

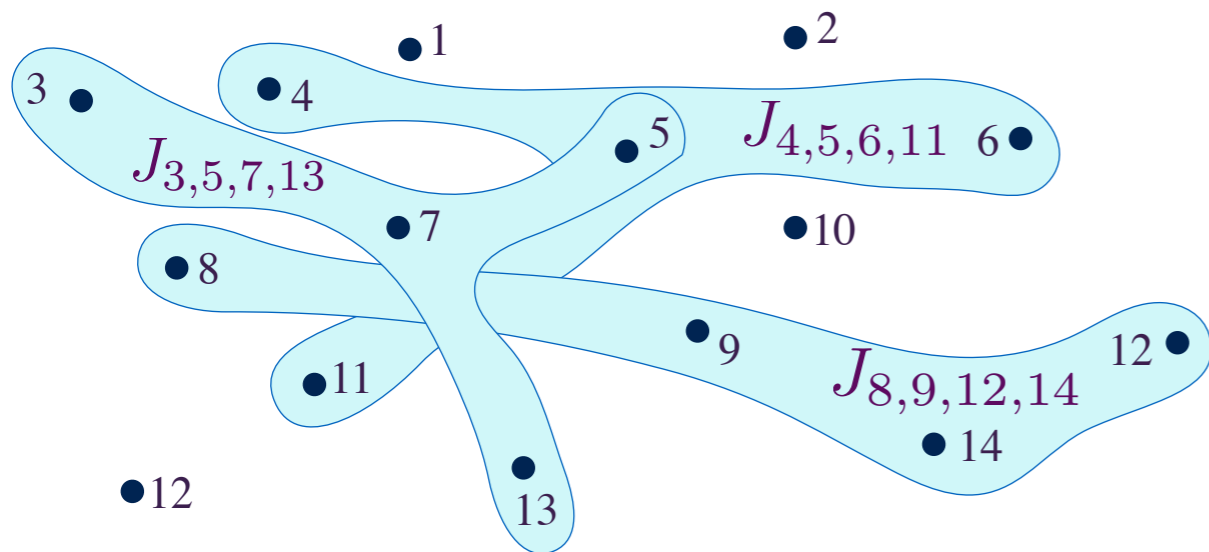
A. Georges, O. Parcollet, and S. Sachdev
Phys. Rev. B **63**, 134406 (2001)

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entropy density, \mathcal{S} , obeys

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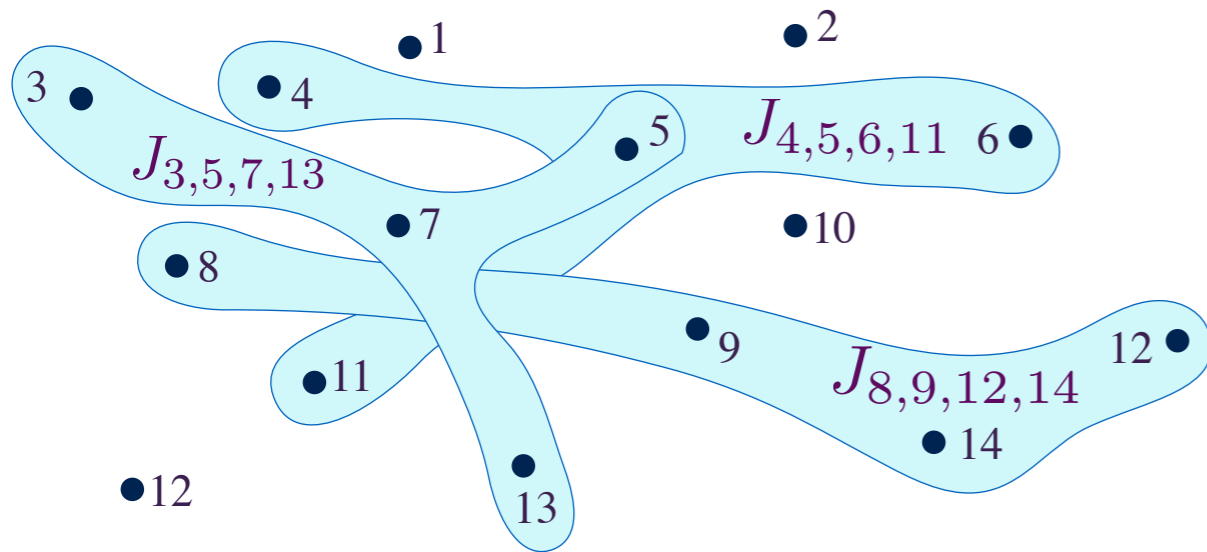
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O. Parcollet, A. Georges, G. Kotliar, and A. Sengupta
Phys. Rev. B **58**, 3794 (1998)

A. Georges, O. Parcollet, and S. Sachdev
Phys. Rev. B **63**, 134406 (2001)

Einstein-Maxwell theory
+ cosmological constant

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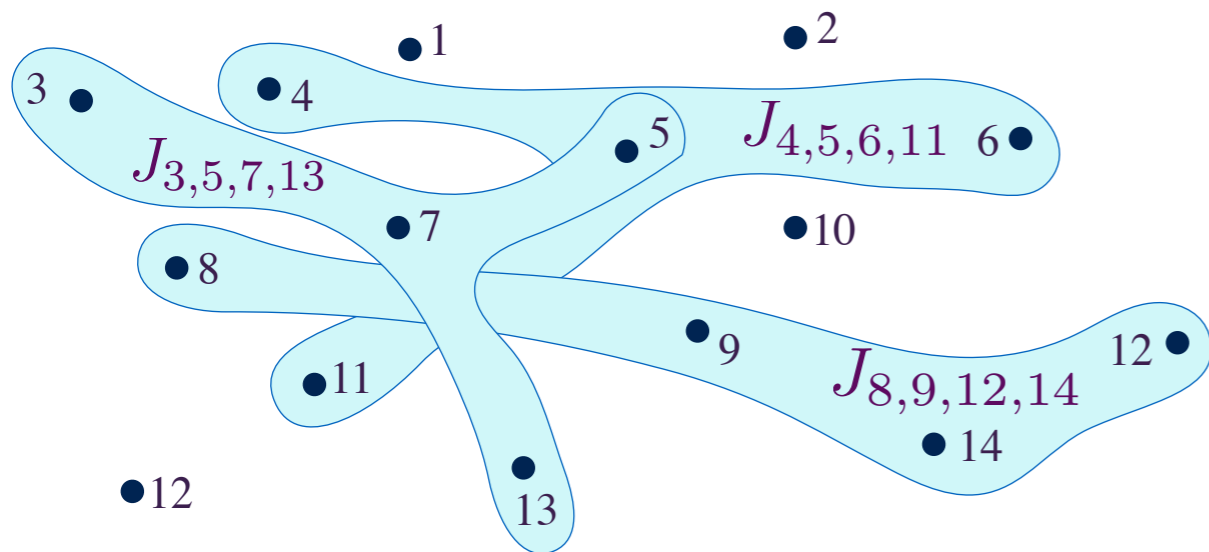
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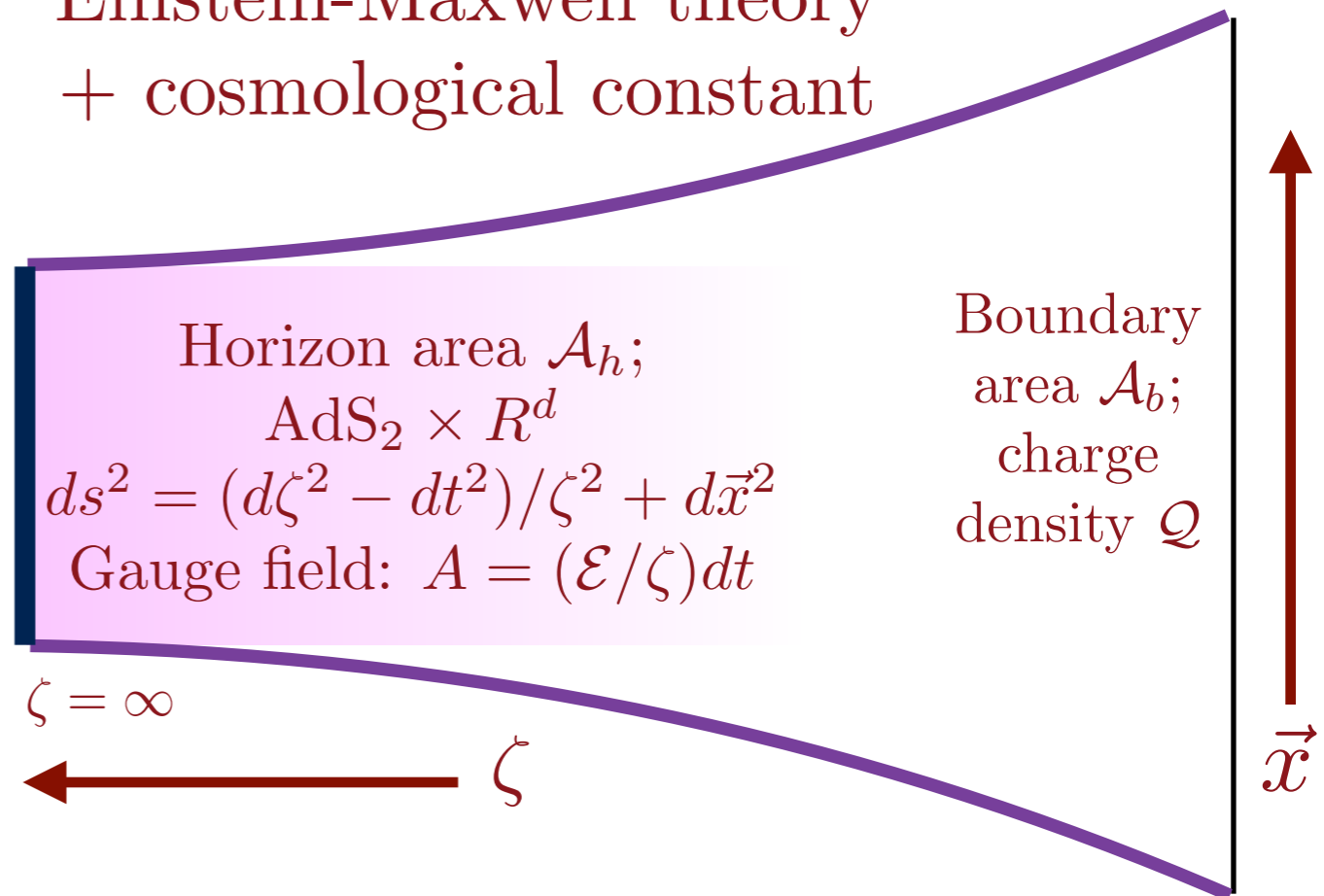
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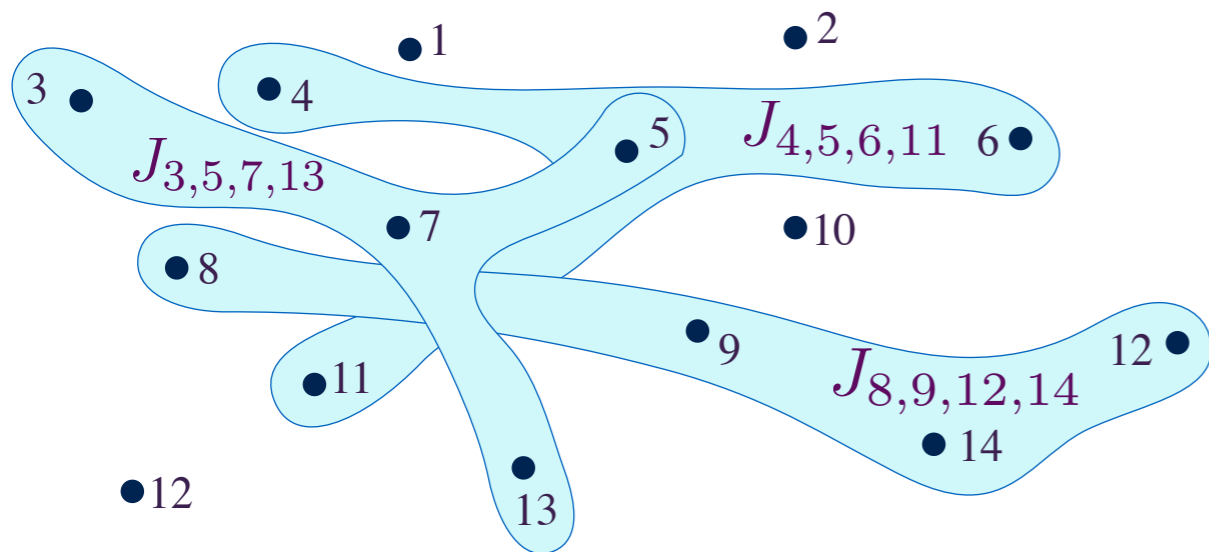
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Einstein-Maxwell theory
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A. Chamblin, R. Emparan, C.V. Johnson, and R.C. Myers
Phys. Rev. D **60**, 064018 (1999)

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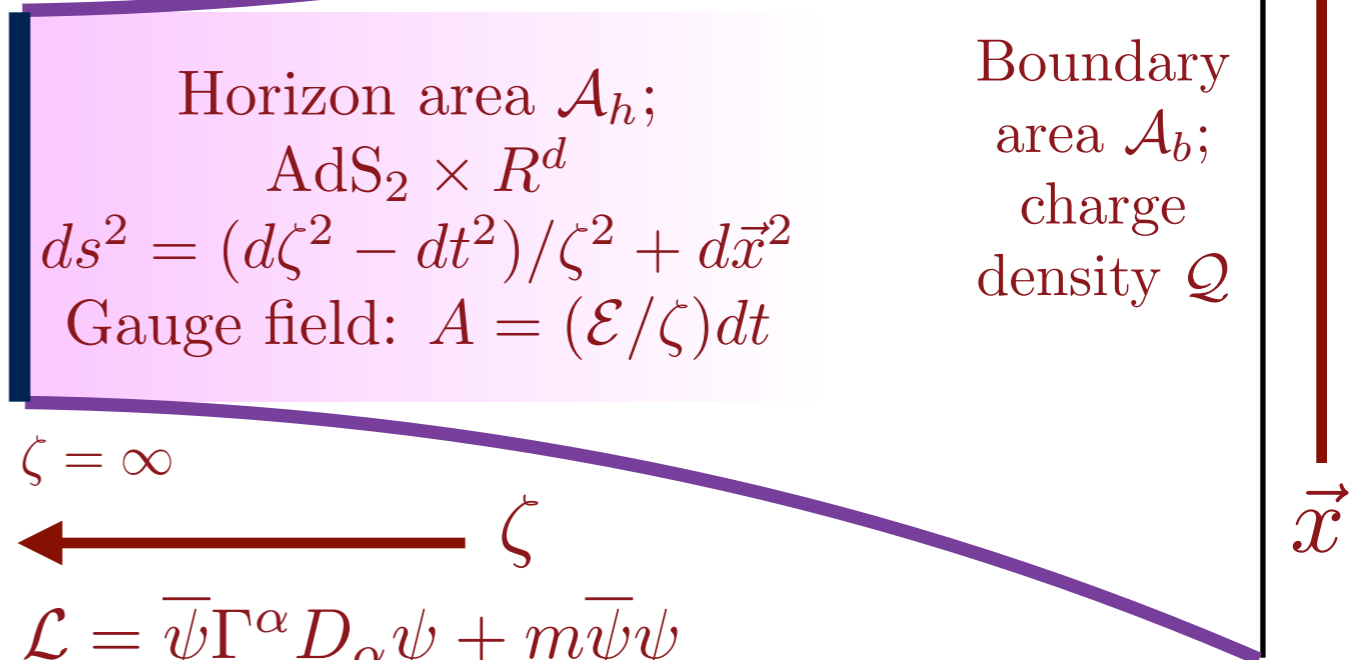
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$$\zeta = \infty$$

$$\leftarrow \zeta$$

$$\mathcal{L} = \bar{\psi} \Gamma^\alpha D_\alpha \psi + m \bar{\psi} \psi$$

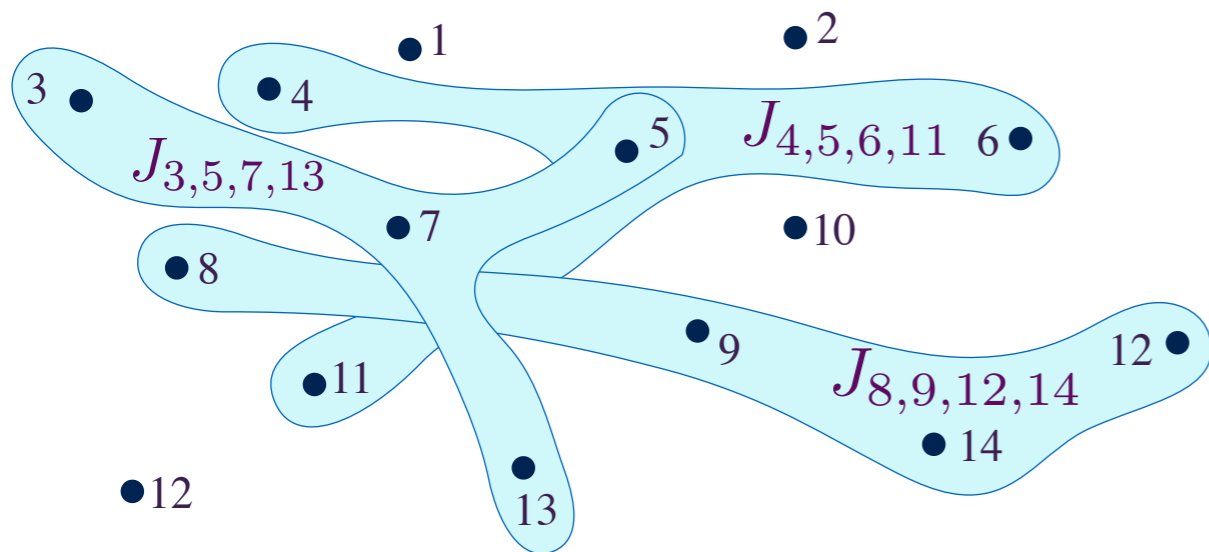
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T. Faulkner, Hong Liu, J. McGreevy, and D. Vegh
Phys. Rev. D 83, 125002 (2011)



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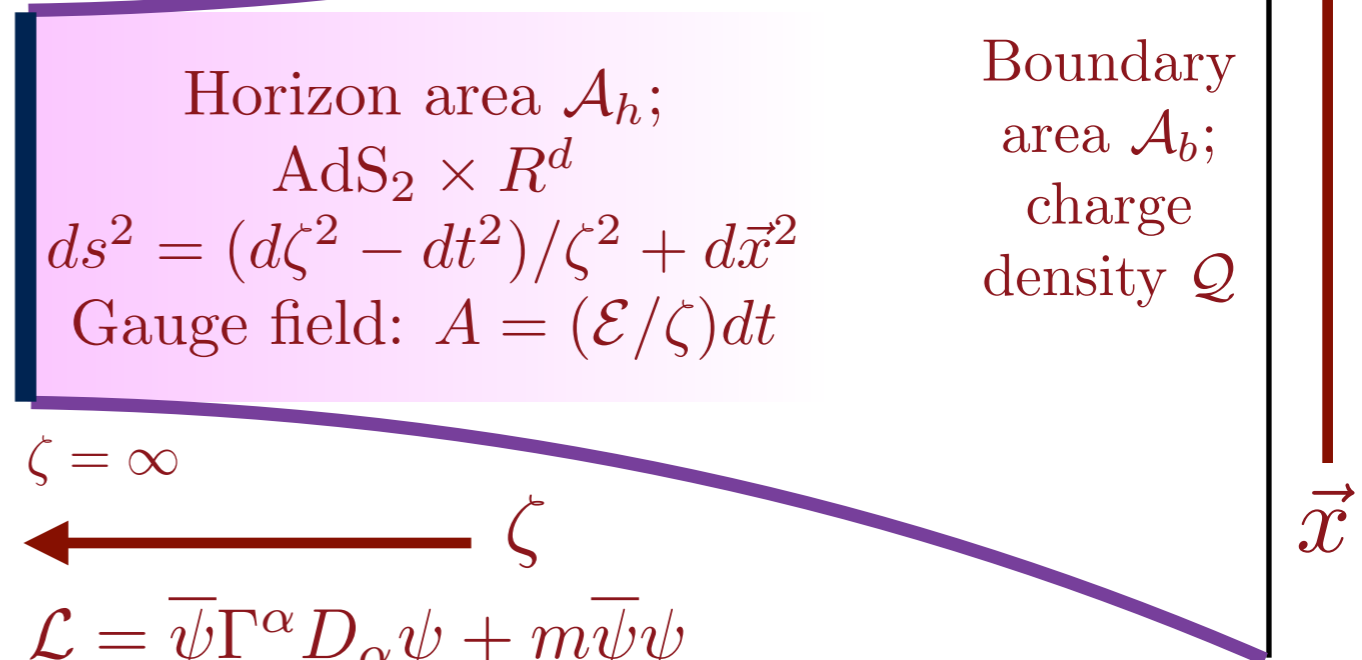
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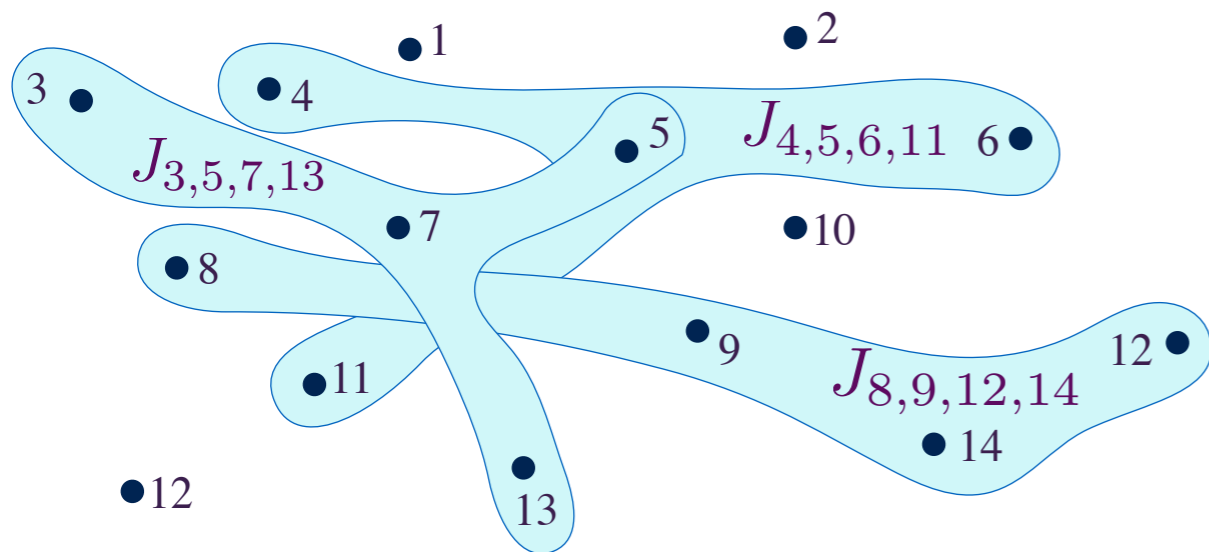
'Equation of state' relating \mathcal{E} and Q depends upon the geometry of spacetime far from the AdS_2

Eliminate r_0 between

$$Q = \frac{r_0^{d-1} \sqrt{2d [(d-1)R^2 + (d+1)r_0^2]}}{\kappa^2 g_F}$$

$$\mathcal{E} = \frac{g_F r_0 \sqrt{2d [(d-1)R^2 + (d+1)r_0^2]}}{2 [(d-1)^2 R^2 + d(d+1)r_0^2]}$$

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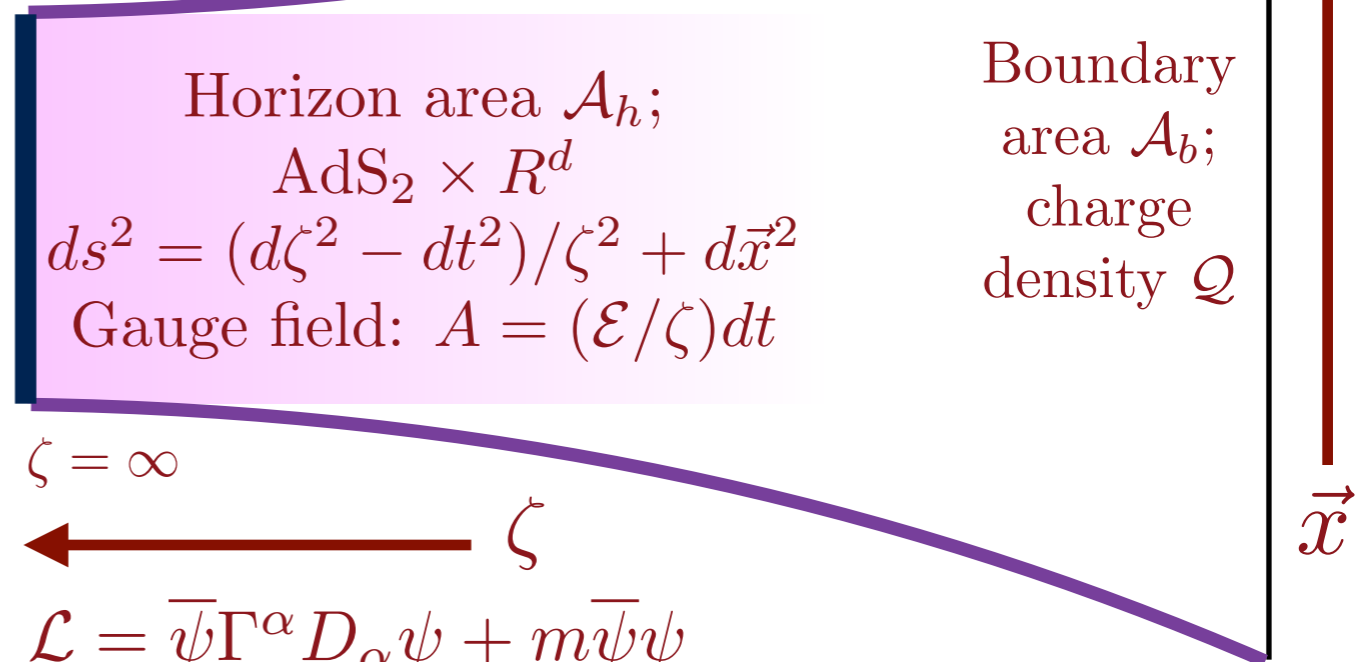
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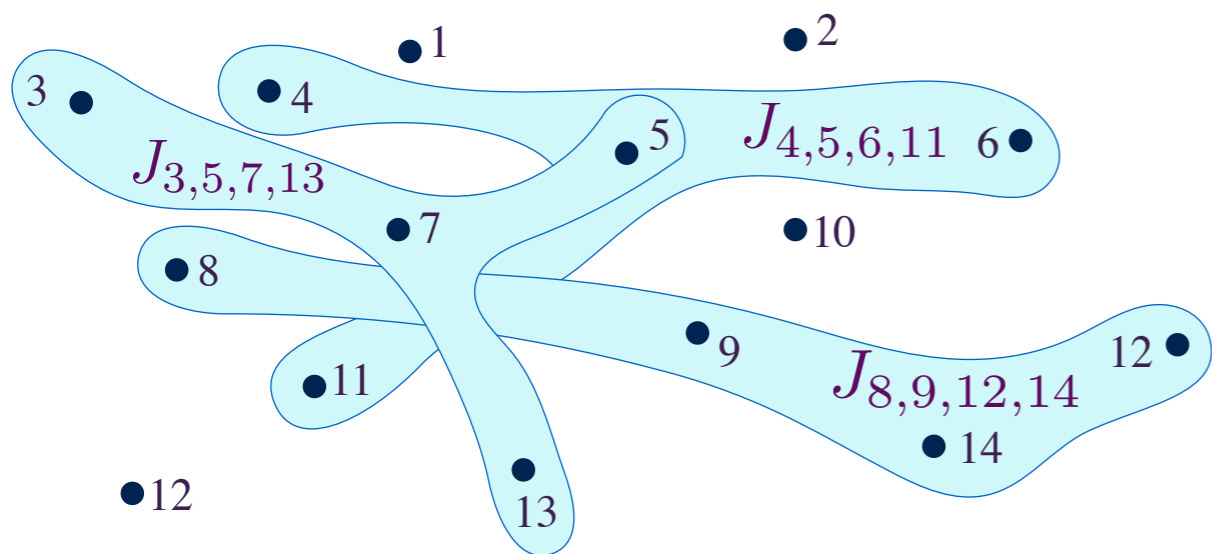
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$$\frac{1}{A_b} \frac{\partial A_h}{\partial Q} = 8\pi G_N \mathcal{E}$$

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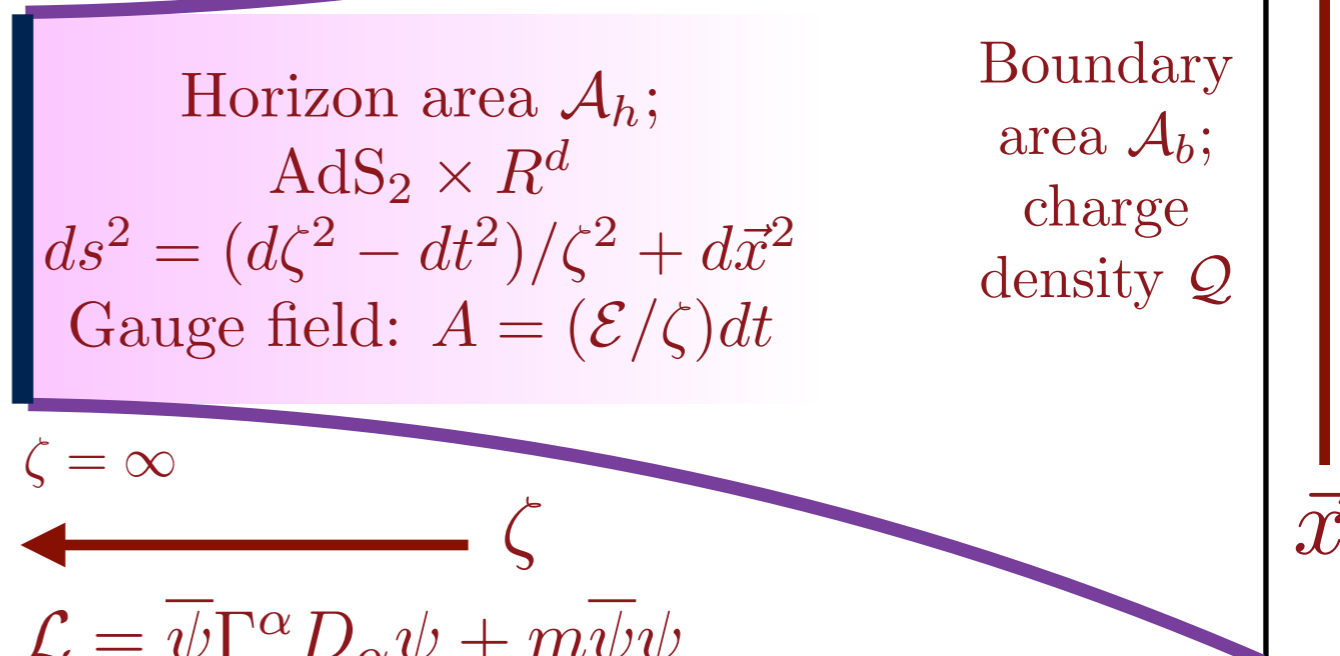
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Combination:

$$\mathcal{S} = \frac{\mathcal{A}_h}{4G_N \mathcal{A}_b}$$

Einstein-Maxwell theory + cosmological constant



Horizon area \mathcal{A}_h ;

$\text{AdS}_2 \times R^d$

$$ds^2 = (d\zeta^2 - dt^2)/\zeta^2 + d\vec{x}^2$$

$$\text{Gauge field: } A = (\mathcal{E}/\zeta)dt$$

Boundary area \mathcal{A}_b ;

charge density Q

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$$\leftarrow \zeta$$

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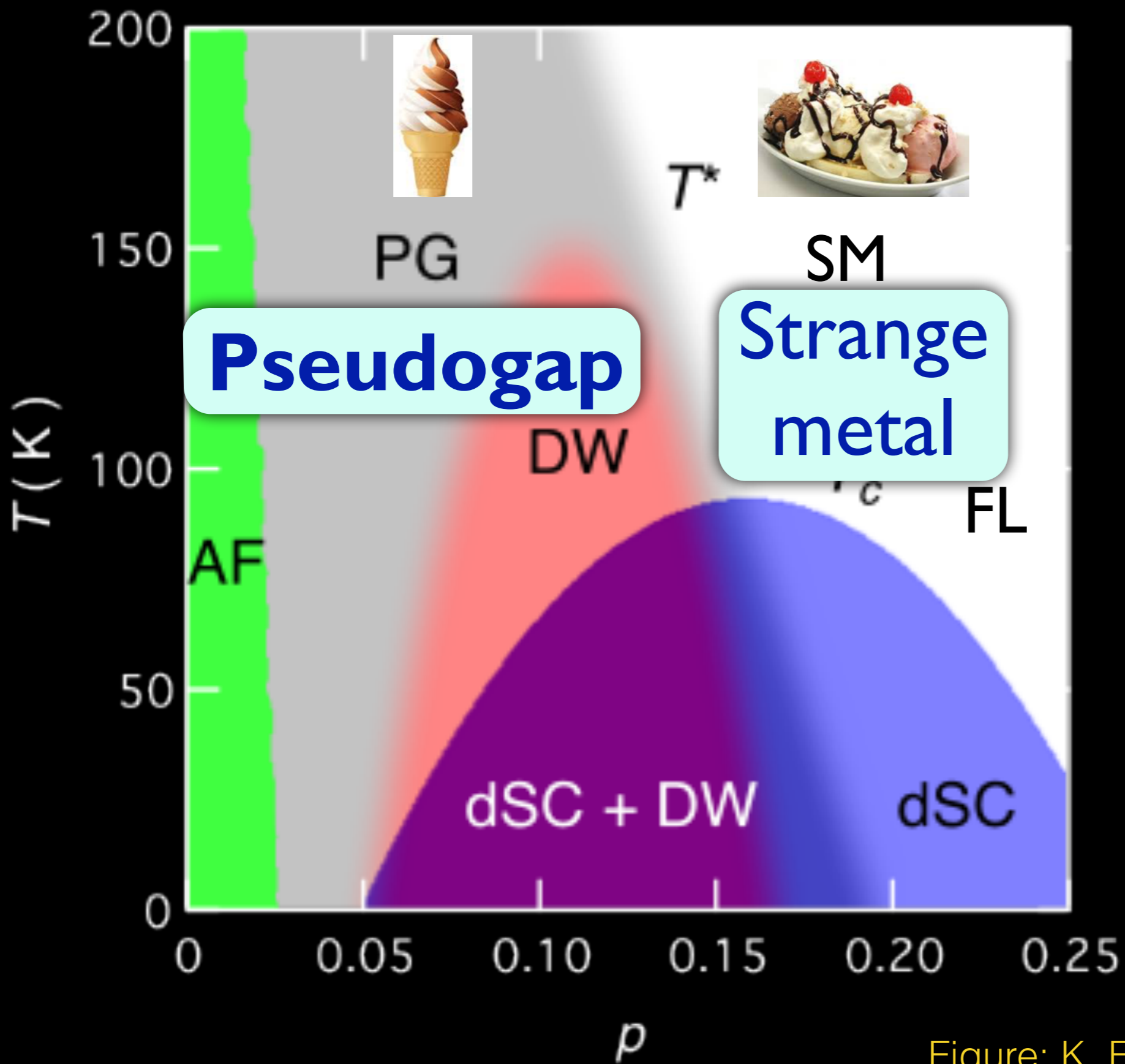


Figure: K. Fujita and J. C. Seamus Davis

1. The pseudogap metal



Fermi liquid co-existing with topological order

2. The strange metal

Metal without quasiparticles

Infinite-range model: dual to extremal charged

black holes and yields

Bekenstein-Hawking entropy

