

# Many-fermion quantum entanglement in the high temperature superconductors and in black holes

Ohio State University  
Columbus

March 10, 2026

Subir Sachdev

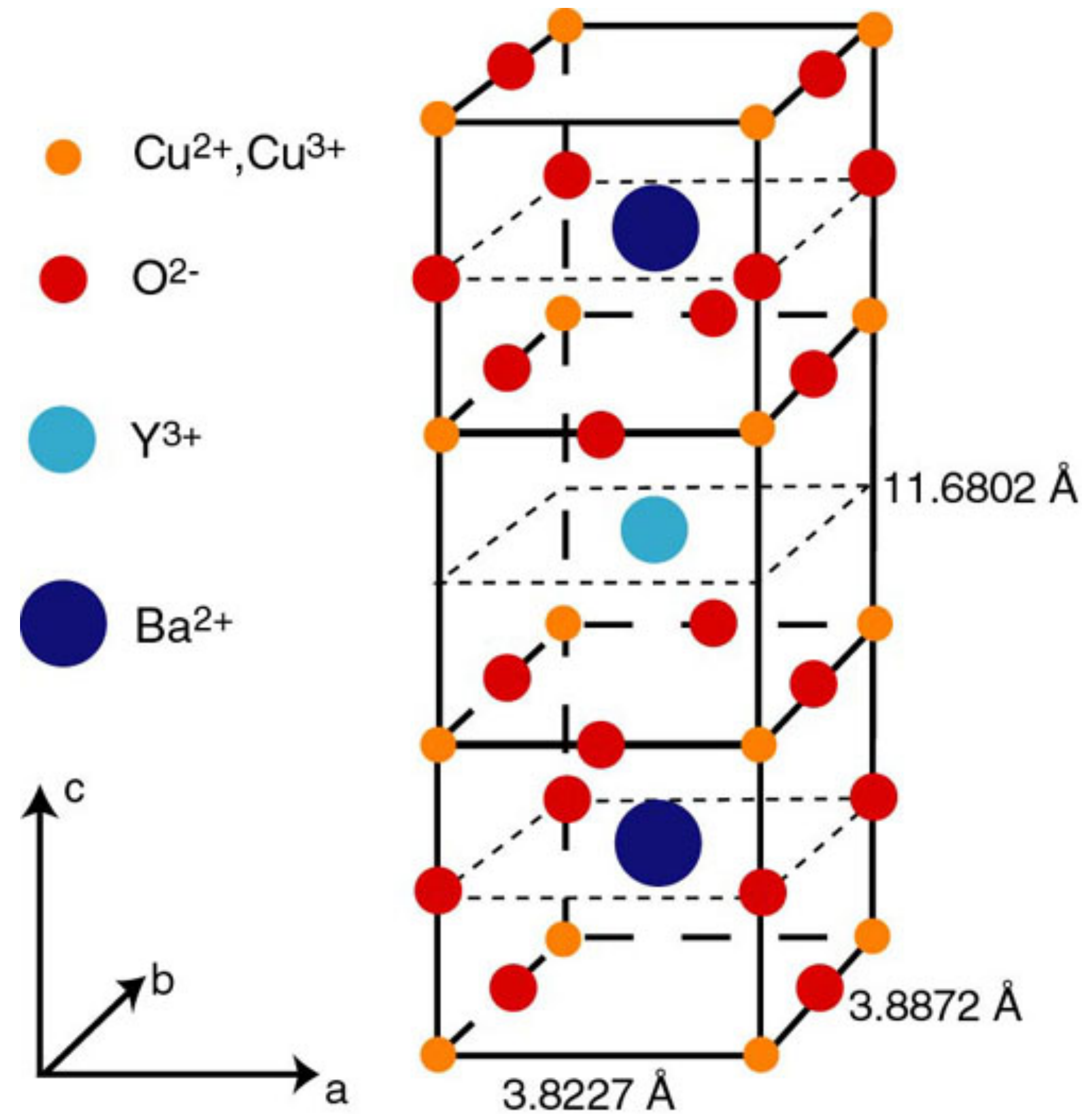


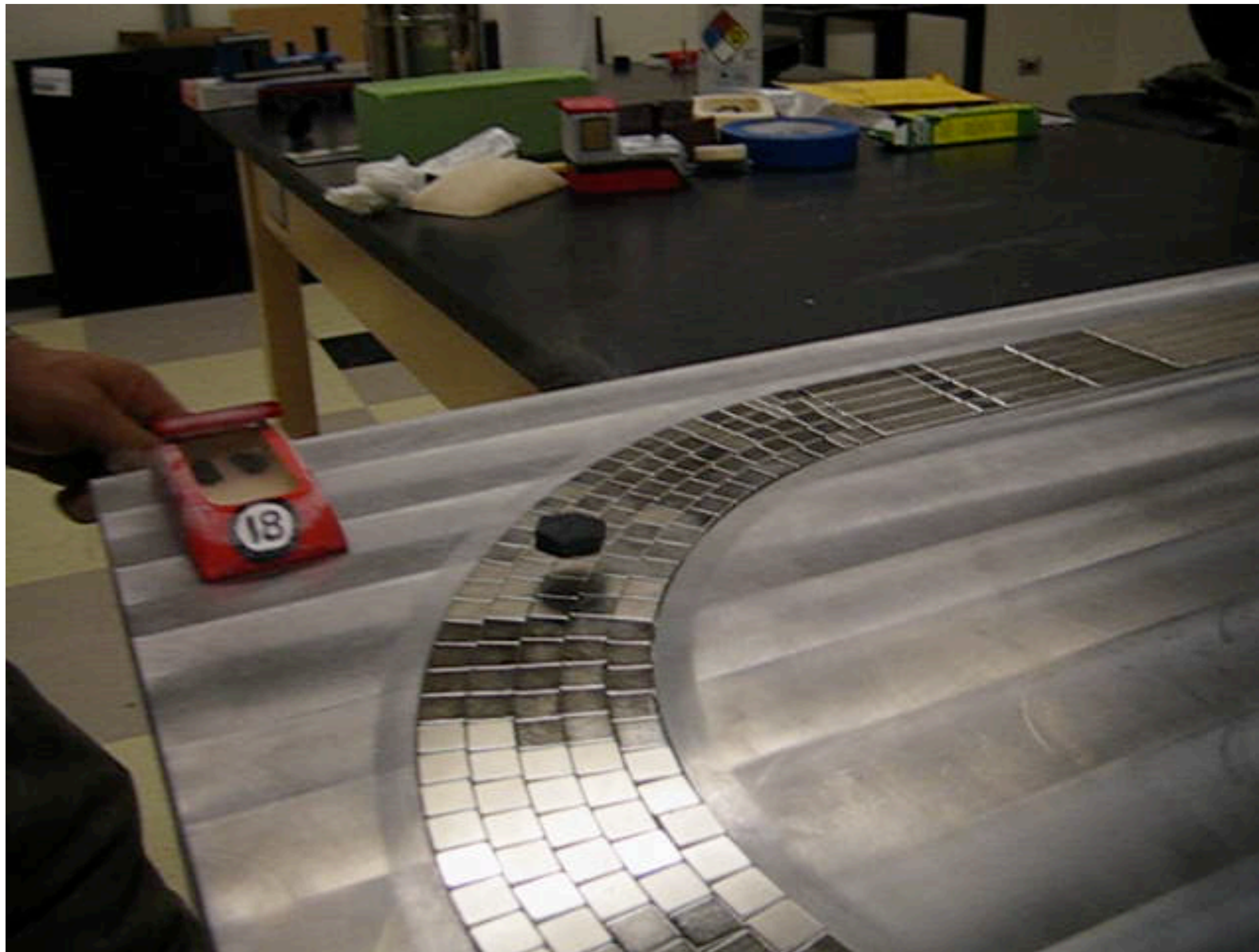
PHYSICS



HARVARD

# Cuprate high temperature superconductors





Nd-Fe-B magnets, YBaCuO superconductor

Julian Hetel and Nandini Trivedi, Ohio State University

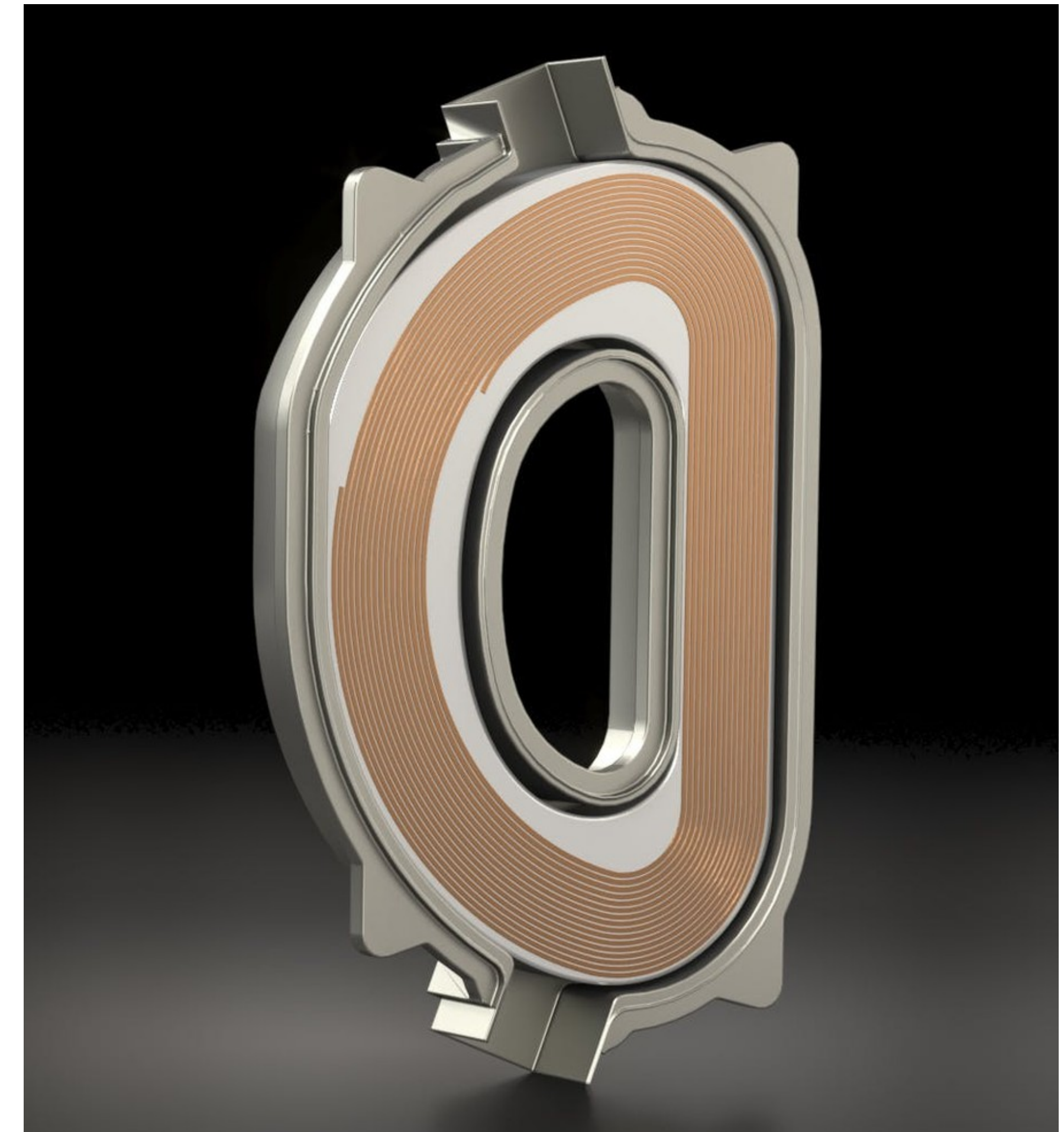
# HTS Magnets: Enabling Technology

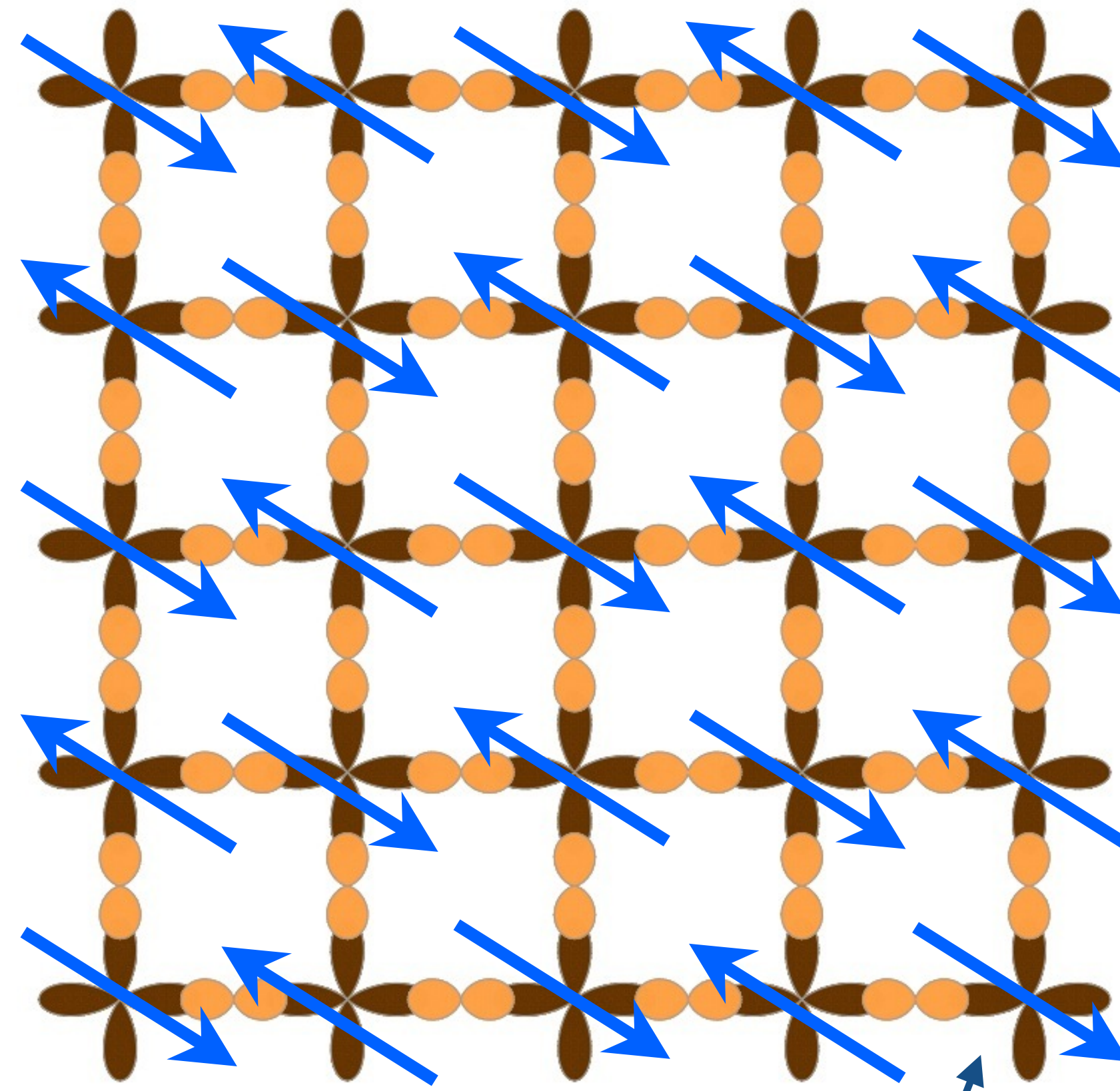
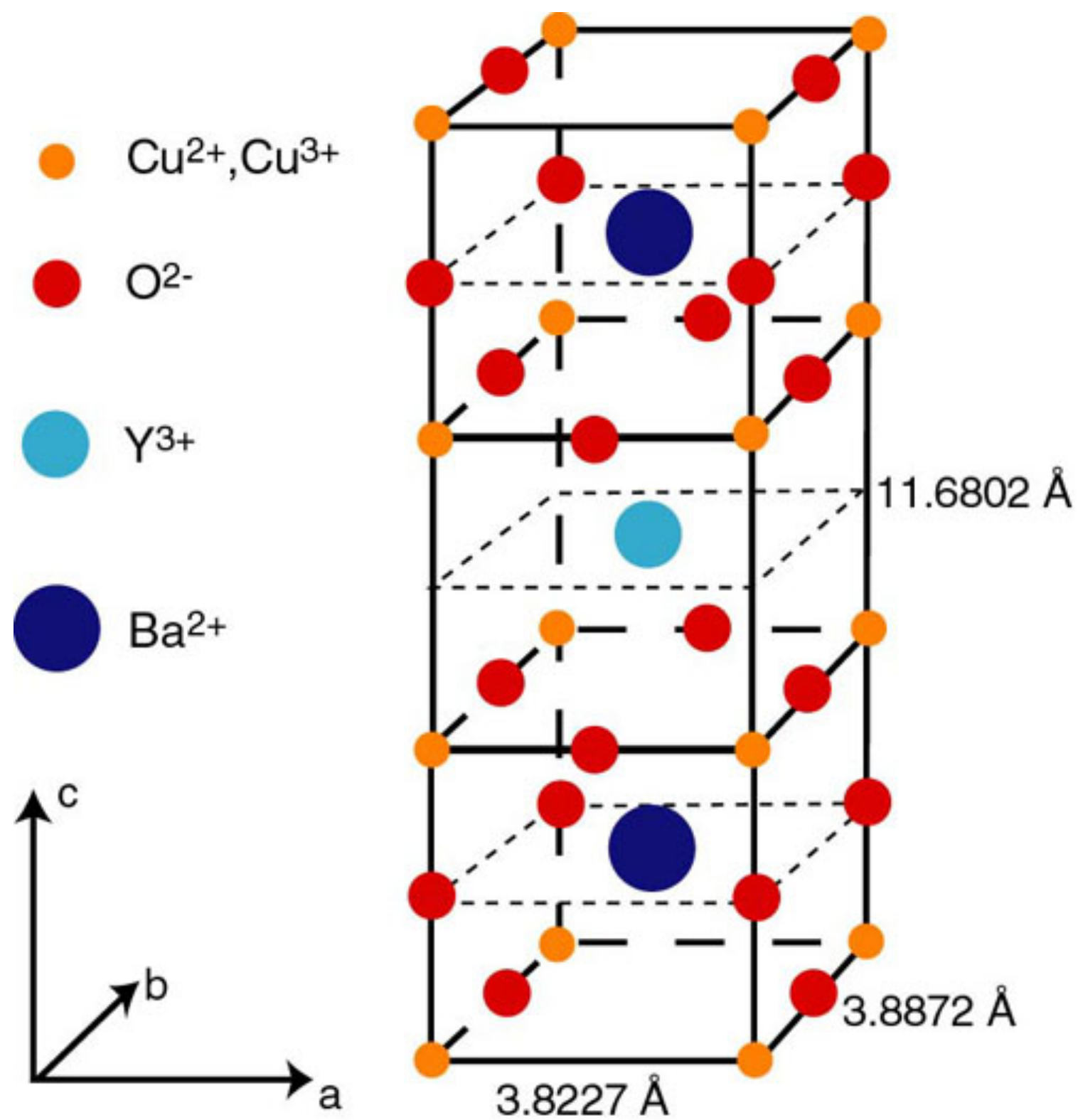
The surest path to limitless,  
clean, fusion energy

YBCO magnets allow for smaller,  
faster, and less expensive  
tokamaks for plasma fusion



Commonwealth  
Fusion Systems





Cu

$$\mathcal{H} = J \sum_{\langle ij \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$$

$S = 1/2$  on each site

$|\uparrow\rangle, |\downarrow\rangle$

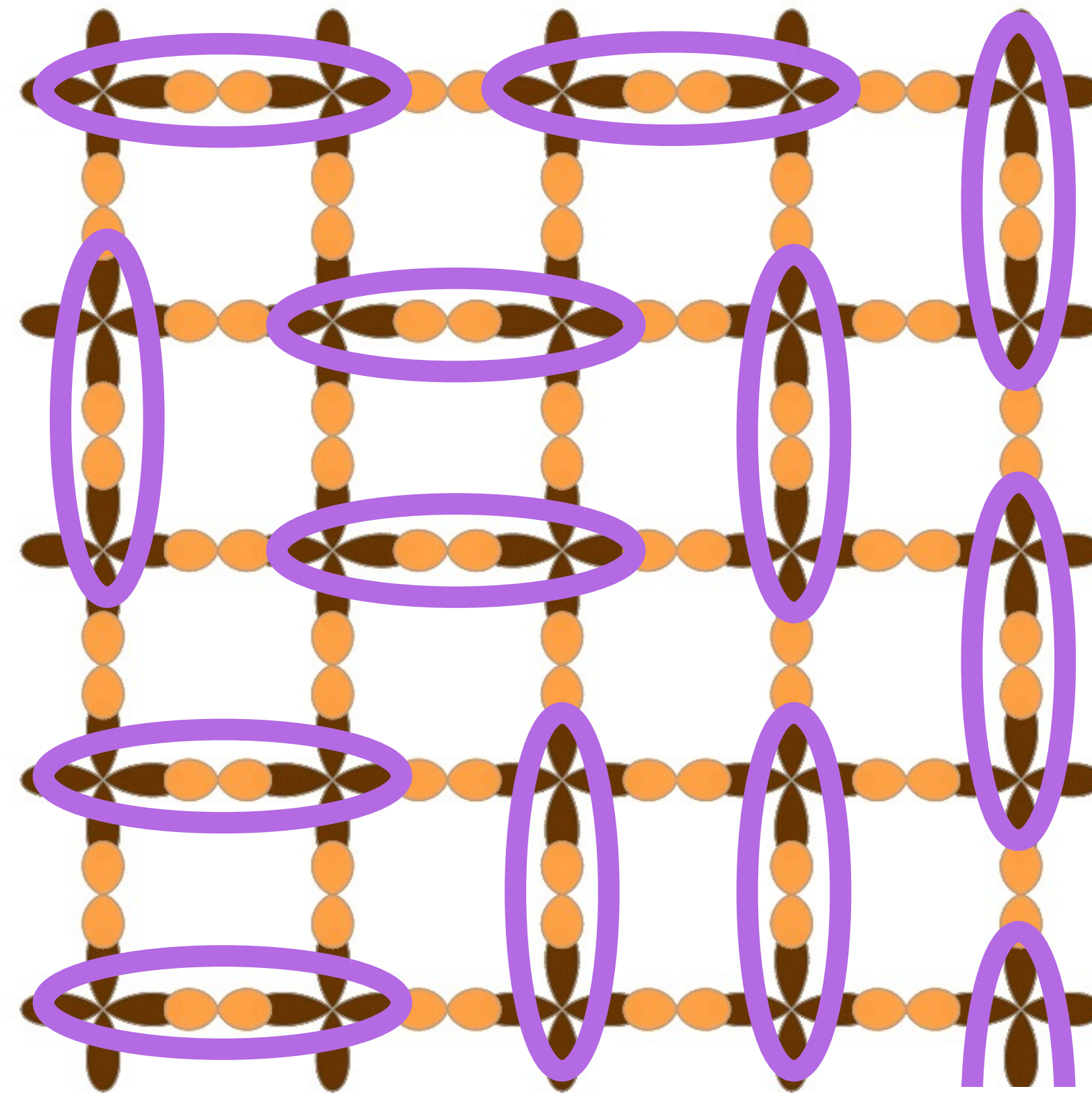
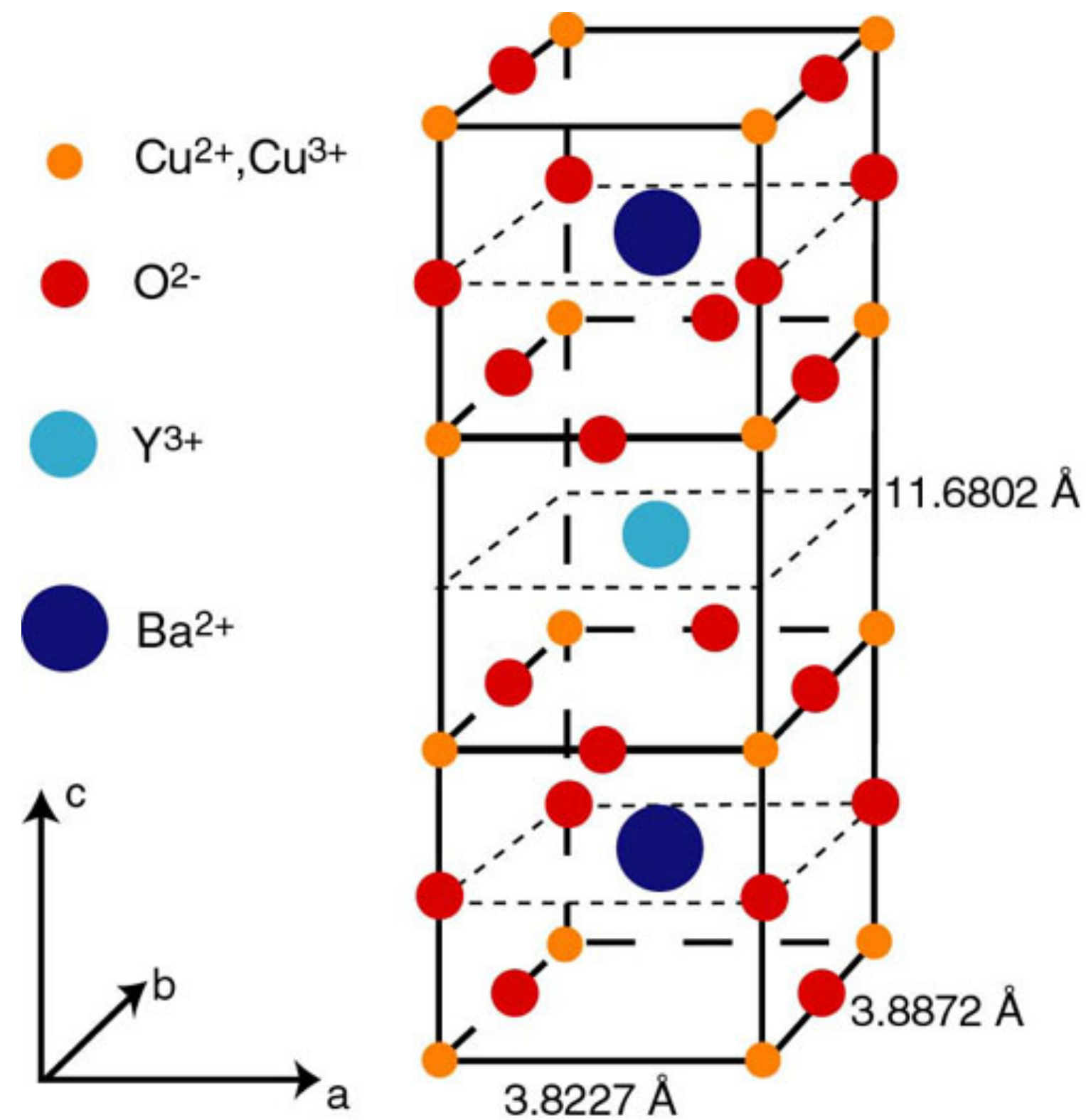
$$S_z |\uparrow\rangle = (1/2) |\uparrow\rangle$$

$$S_z |\downarrow\rangle = -(1/2) |\downarrow\rangle$$

$$(S_x + iS_y) |\downarrow\rangle = |\uparrow\rangle$$

$$(S_x - iS_y) |\uparrow\rangle = |\downarrow\rangle$$

Insulating antiferromagnet with one electron per site



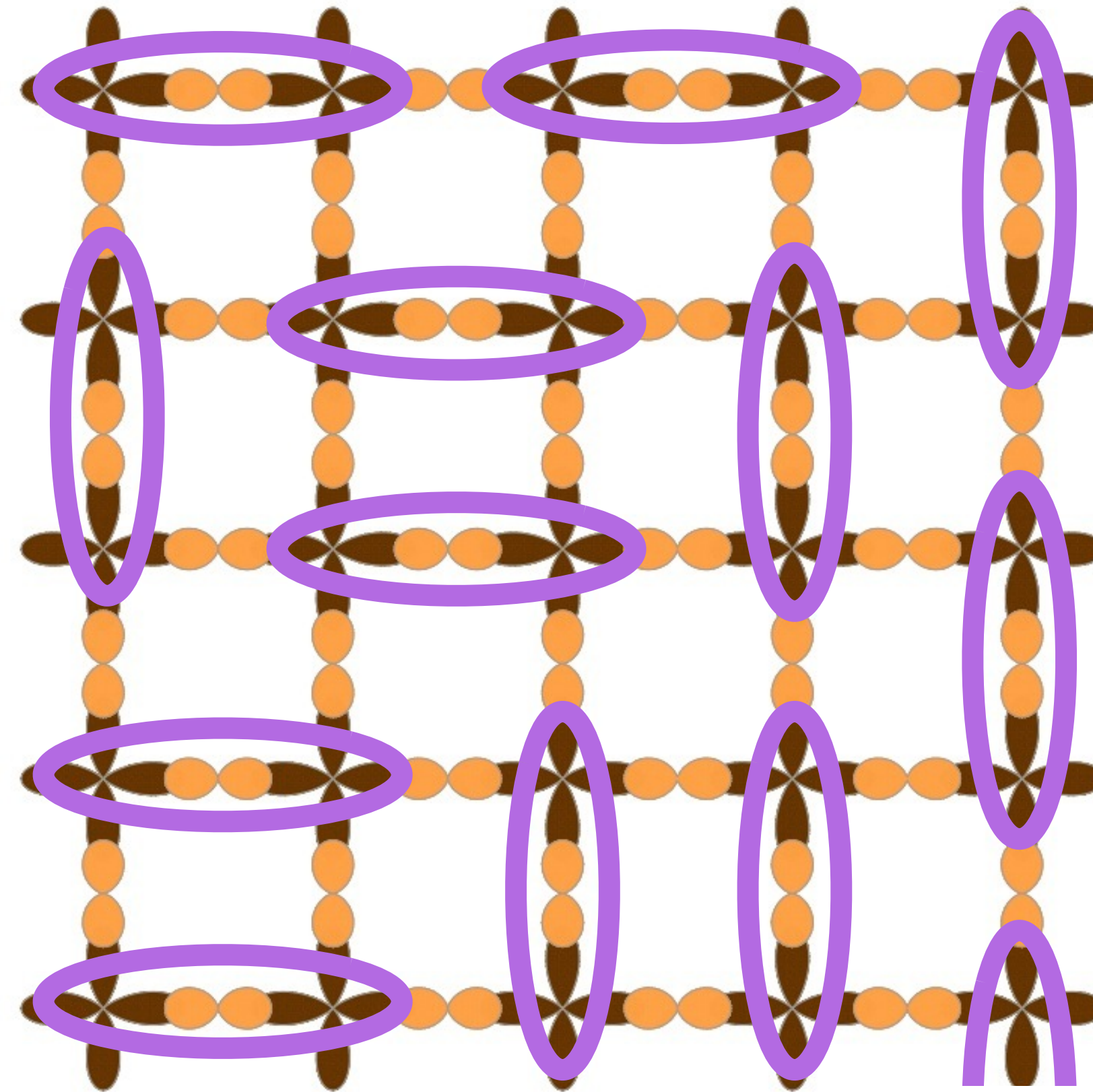
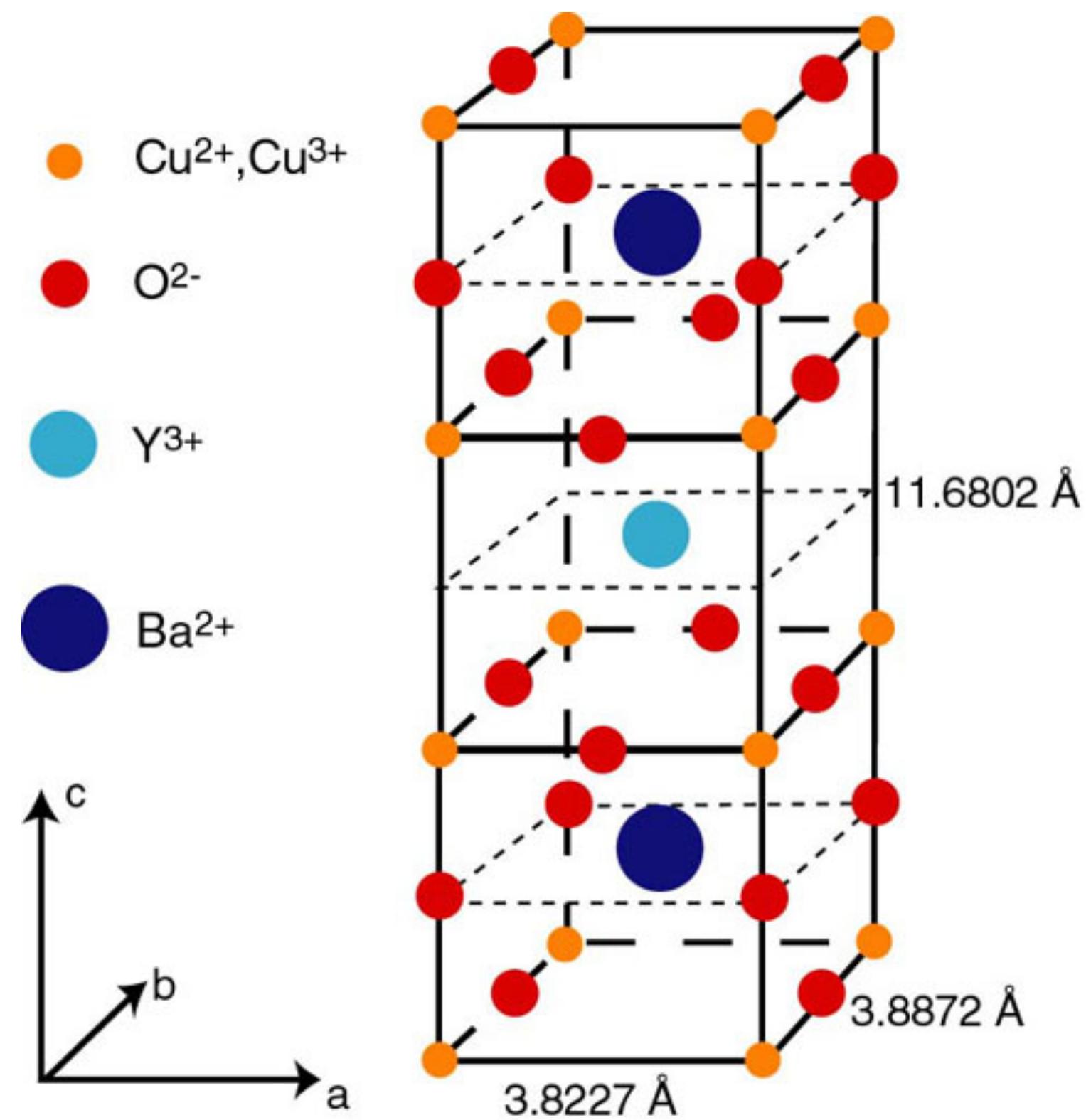
$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$

$\mathcal{D} \rightarrow$  dimer covering  
 of lattice



$$\text{Oval} = \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

P.W.Anderson (1987): The key to high temperature superconductivity  
 is the formation of a “resonating valence bond state”.



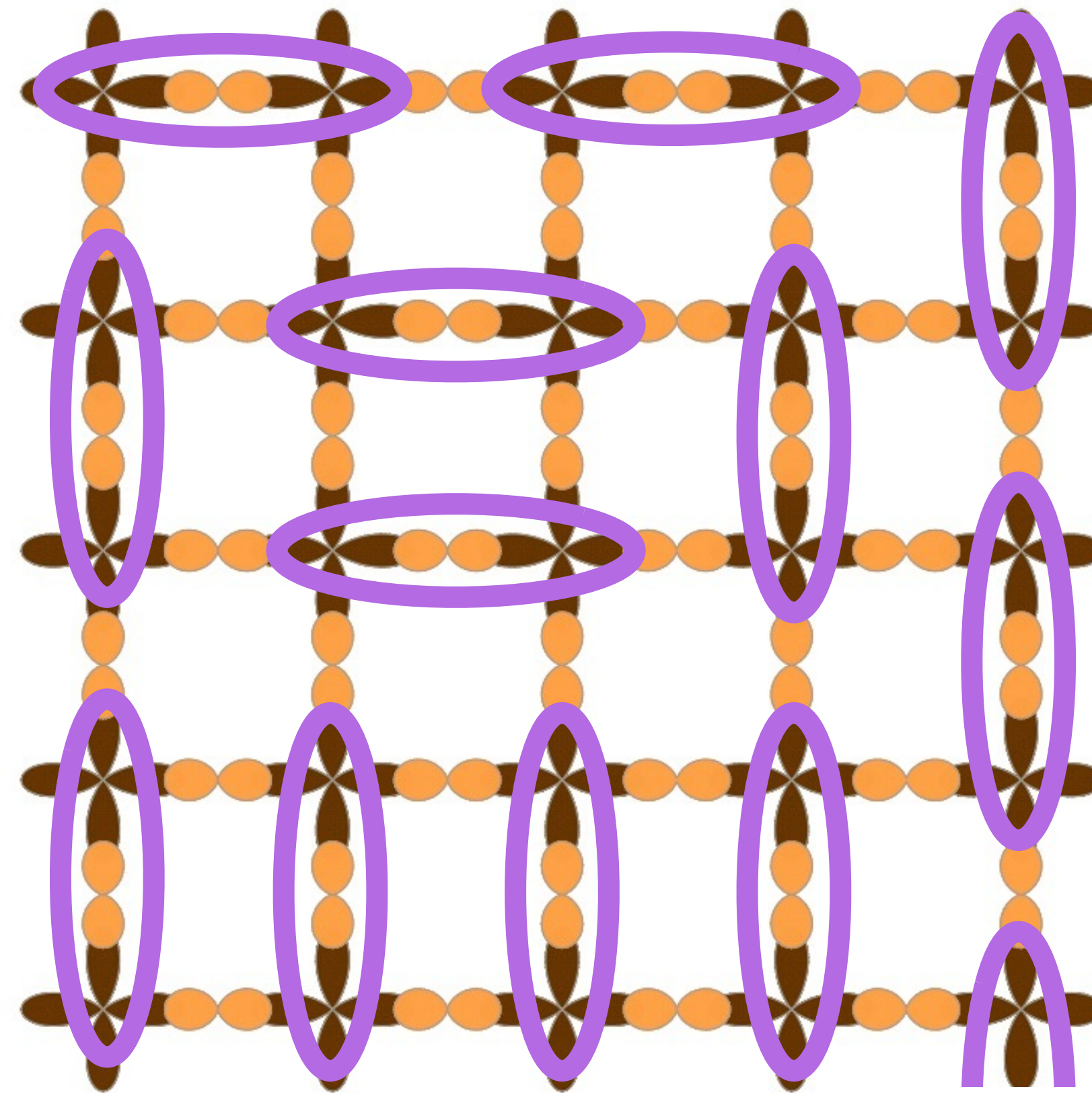
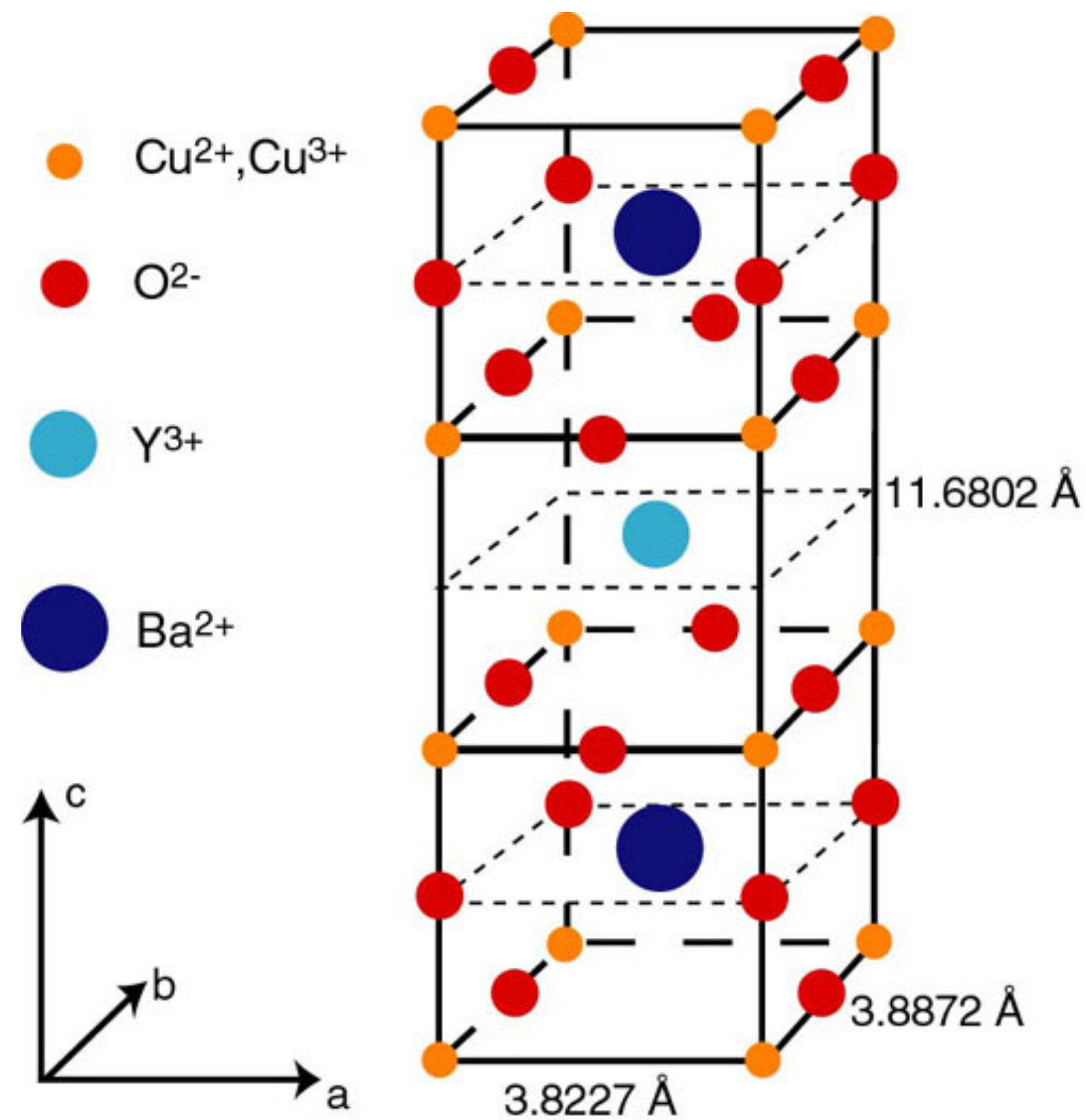
$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$

$\mathcal{D} \rightarrow$  dimer covering of lattice



$$= \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

P.W.Anderson (1987): The key to high temperature superconductivity is the formation of a “resonating valence bond state”.



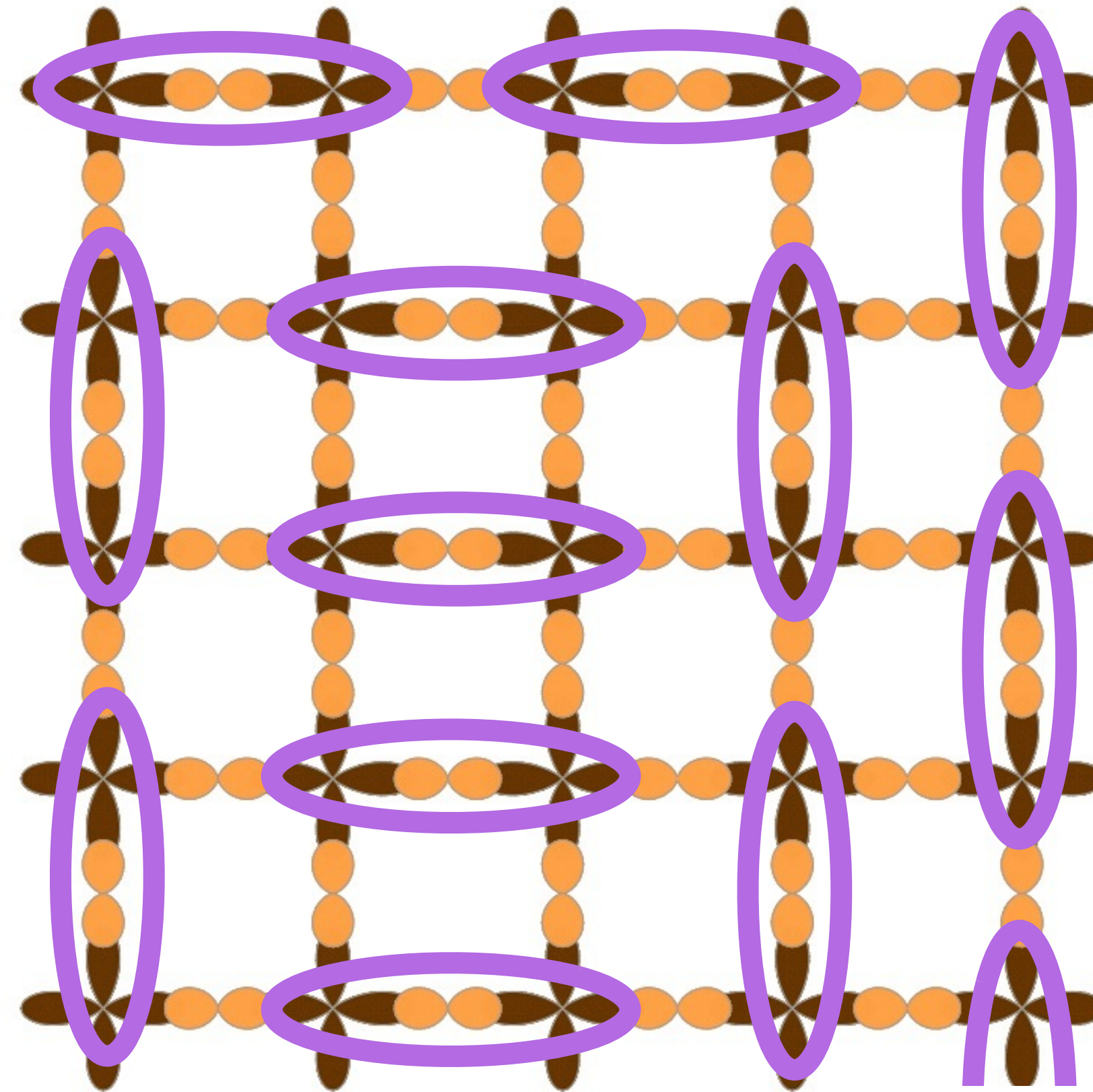
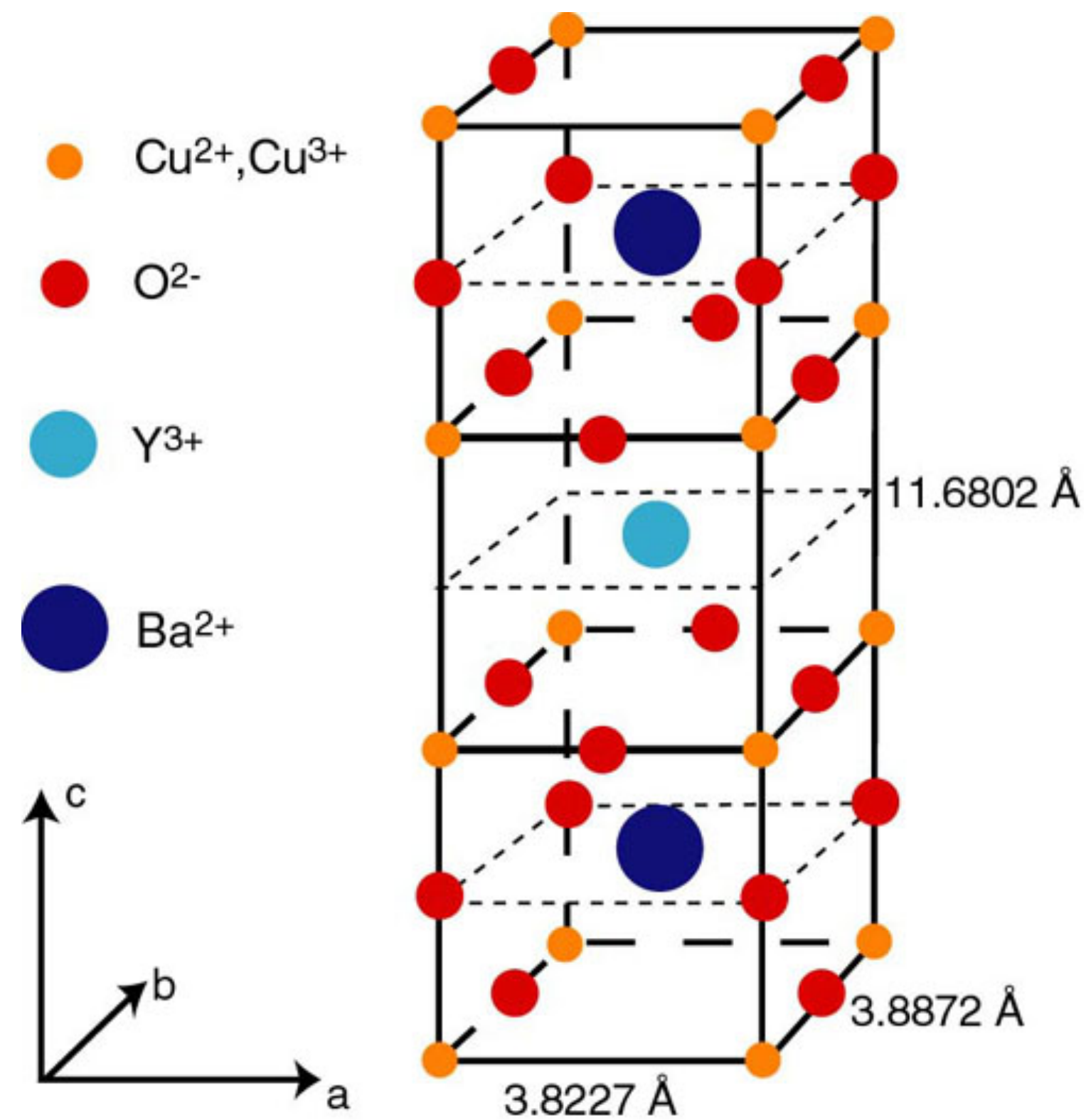
$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$

$\mathcal{D} \rightarrow$  dimer covering  
 of lattice



$$= \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

P.W.Anderson (1987): The key to high temperature superconductivity  
 is the formation of a “resonating valence bond state”.



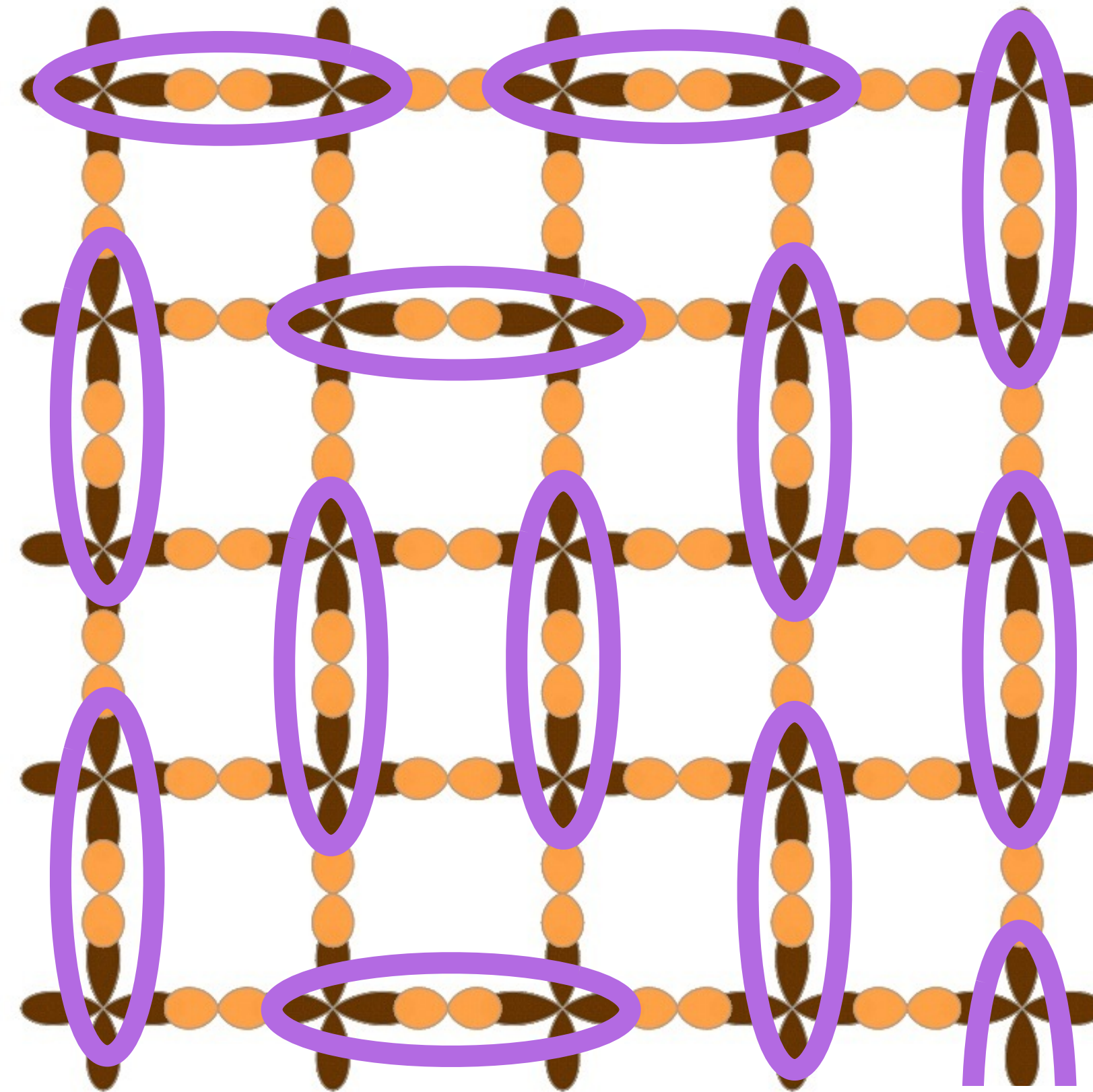
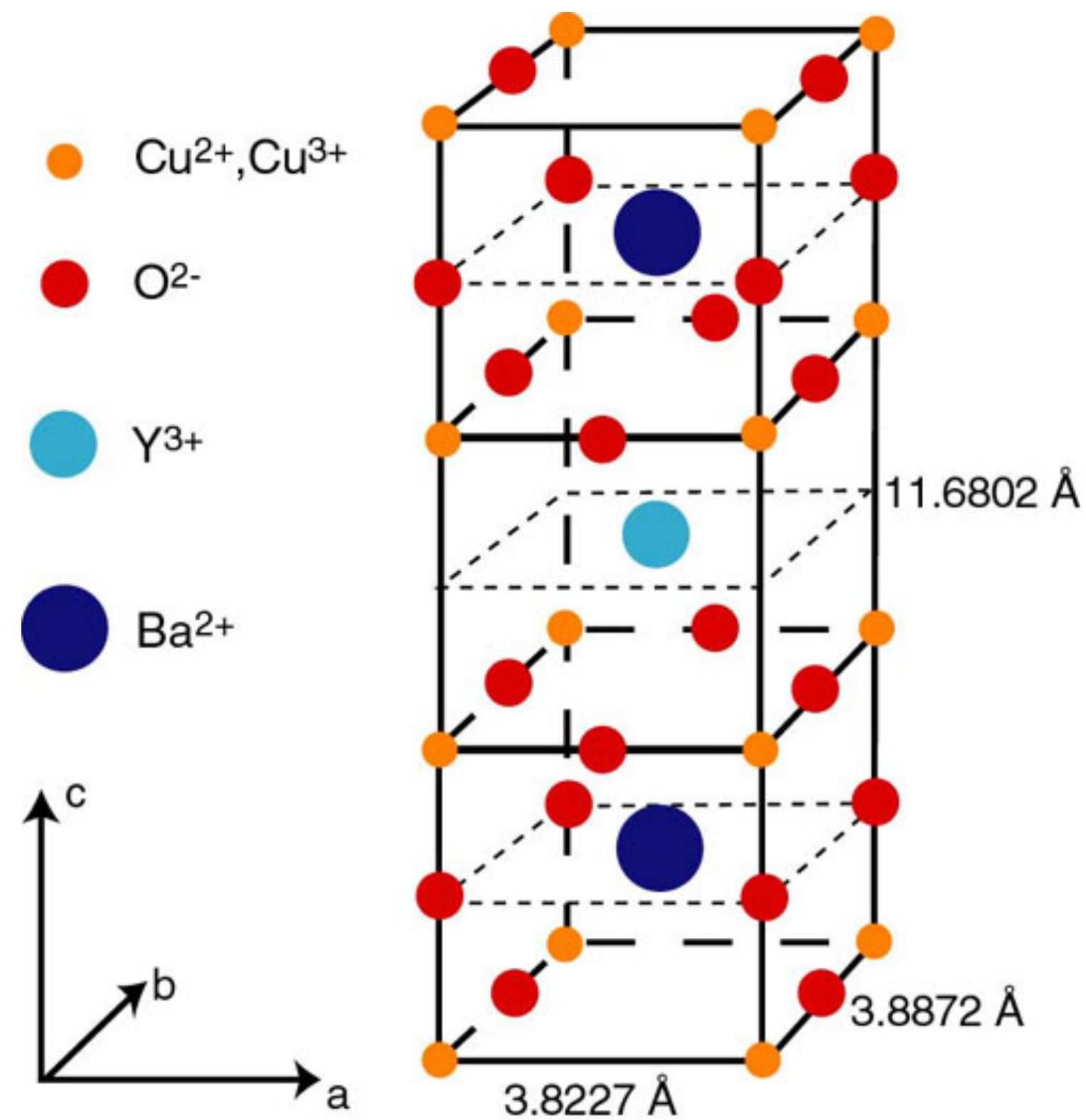
$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$

$\mathcal{D} \rightarrow$  dimer covering  
 of lattice



$$\text{Oval} = \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

P.W.Anderson (1987): The key to high temperature superconductivity  
 is the formation of a “resonating valence bond state”.



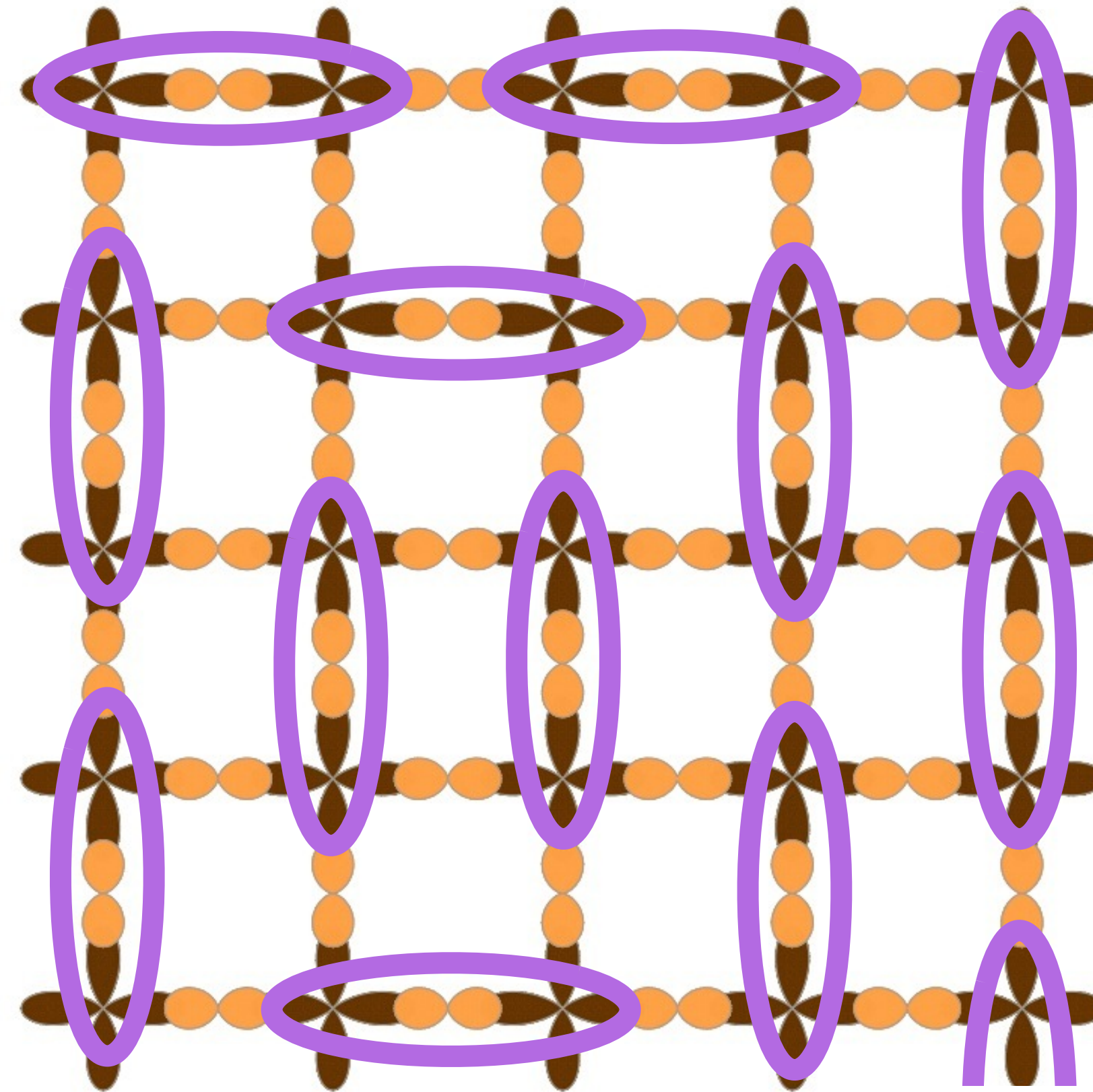
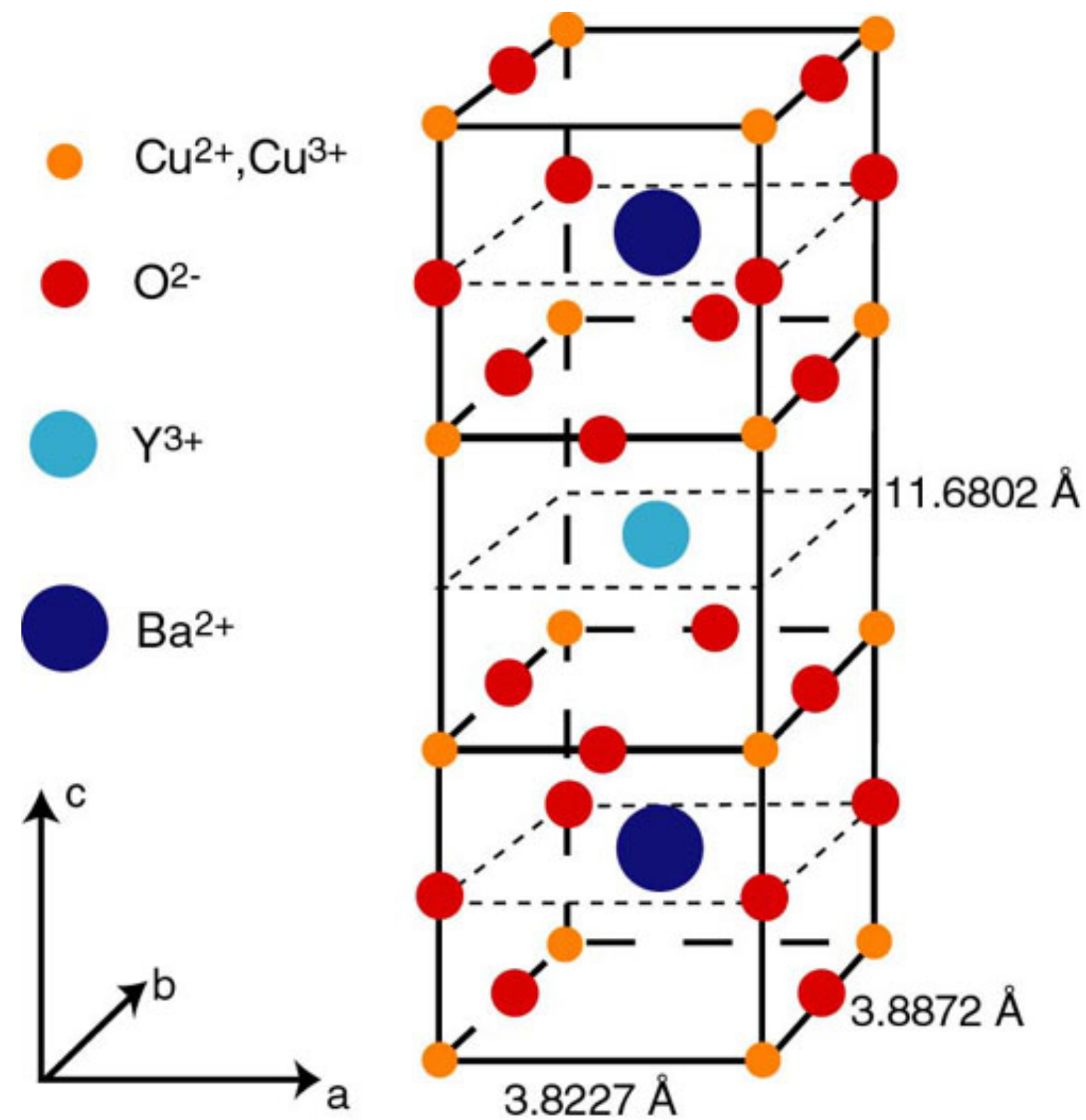
$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$

$\mathcal{D} \rightarrow$  dimer covering  
 of lattice



$$= \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

P.W.Anderson (1987): The key to high temperature superconductivity  
 is the formation of a “resonating valence bond state”.



$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$

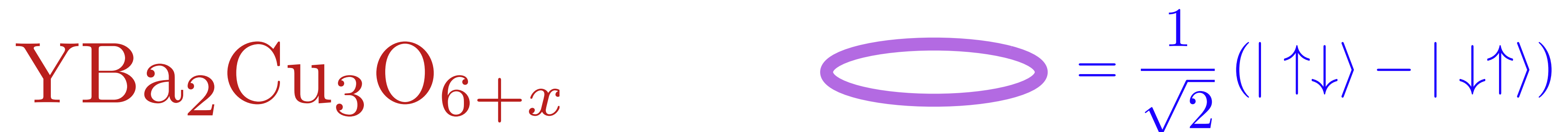
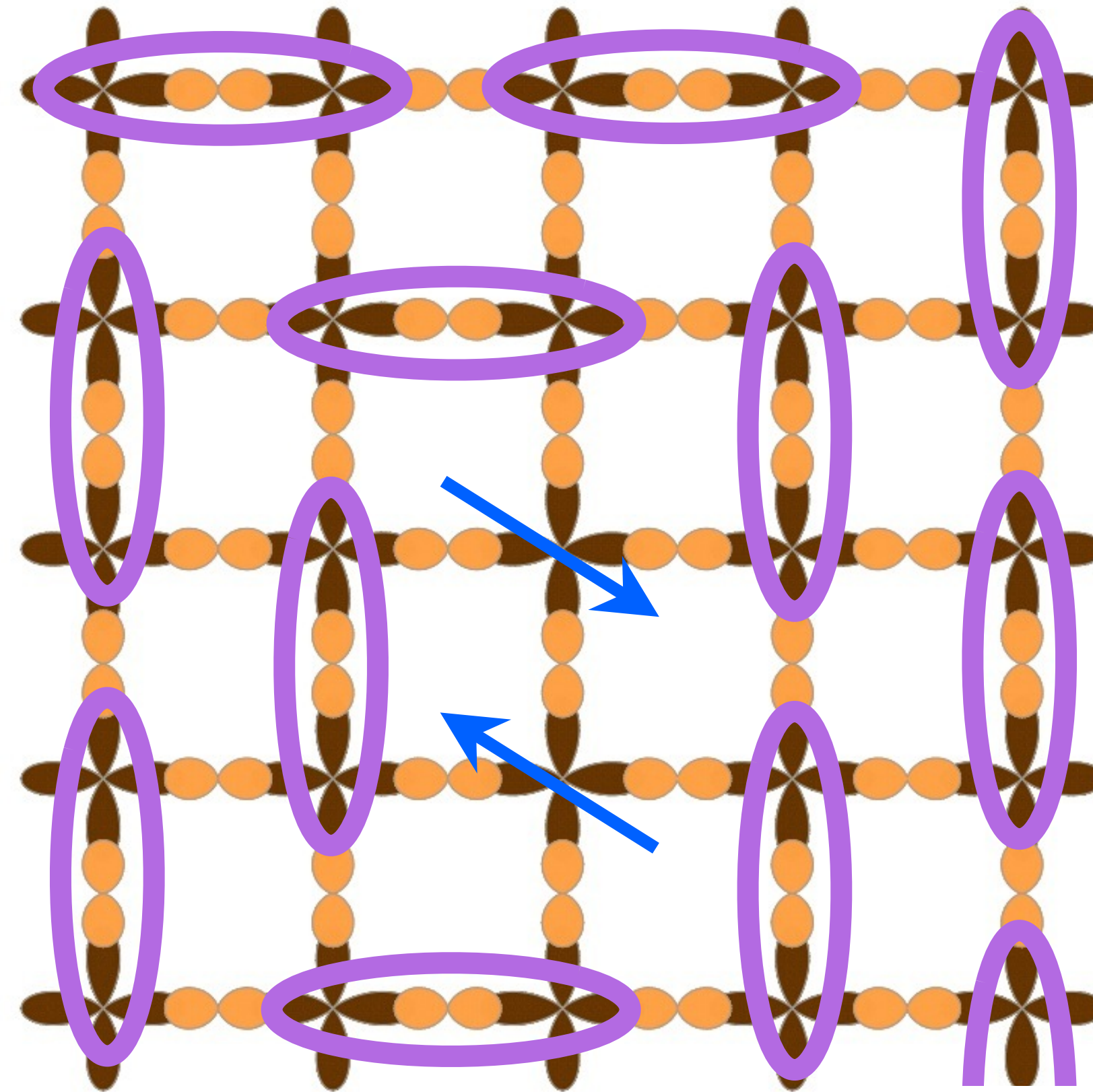
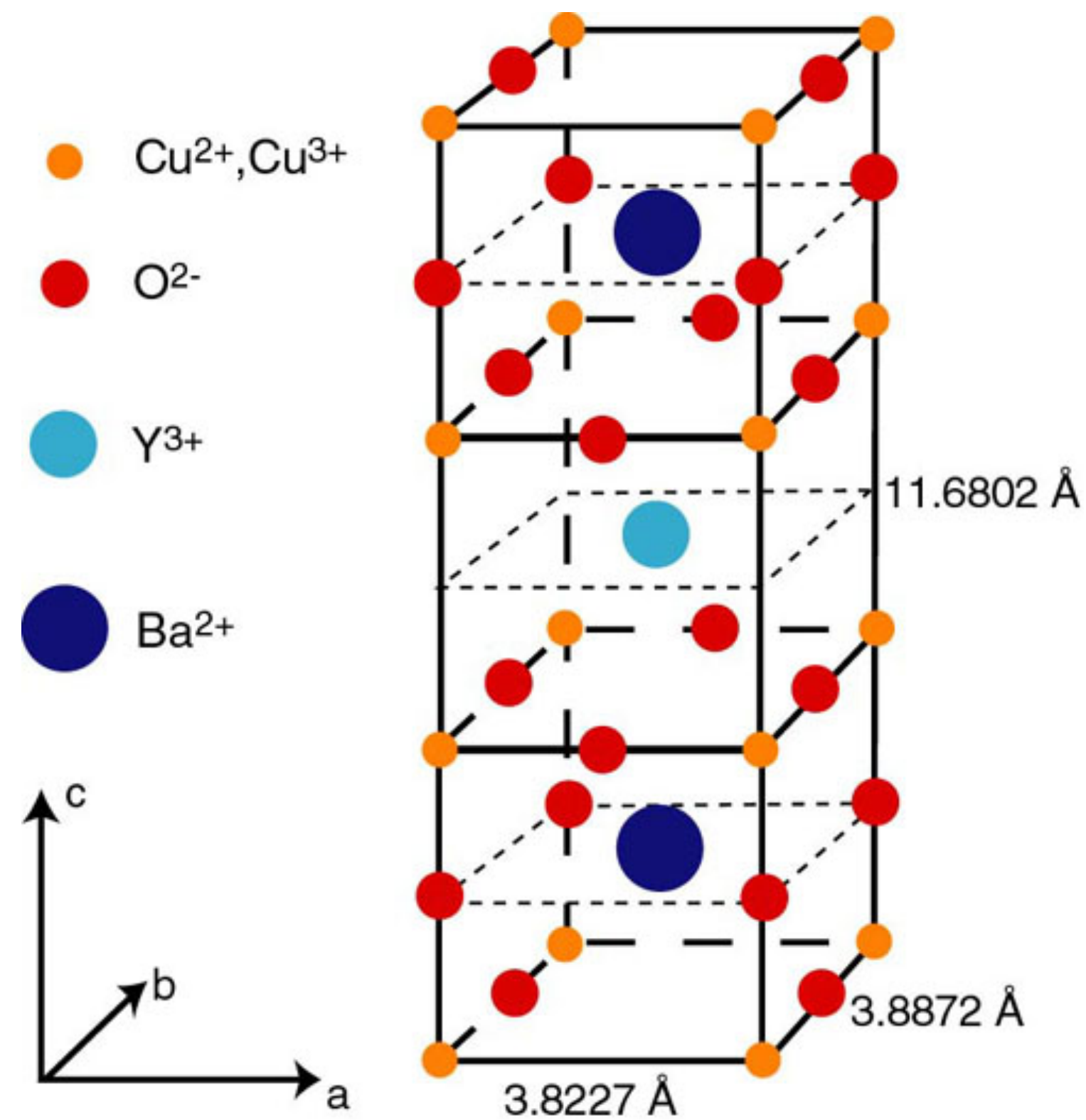
$\mathcal{D} \rightarrow$  dimer covering  
 of lattice



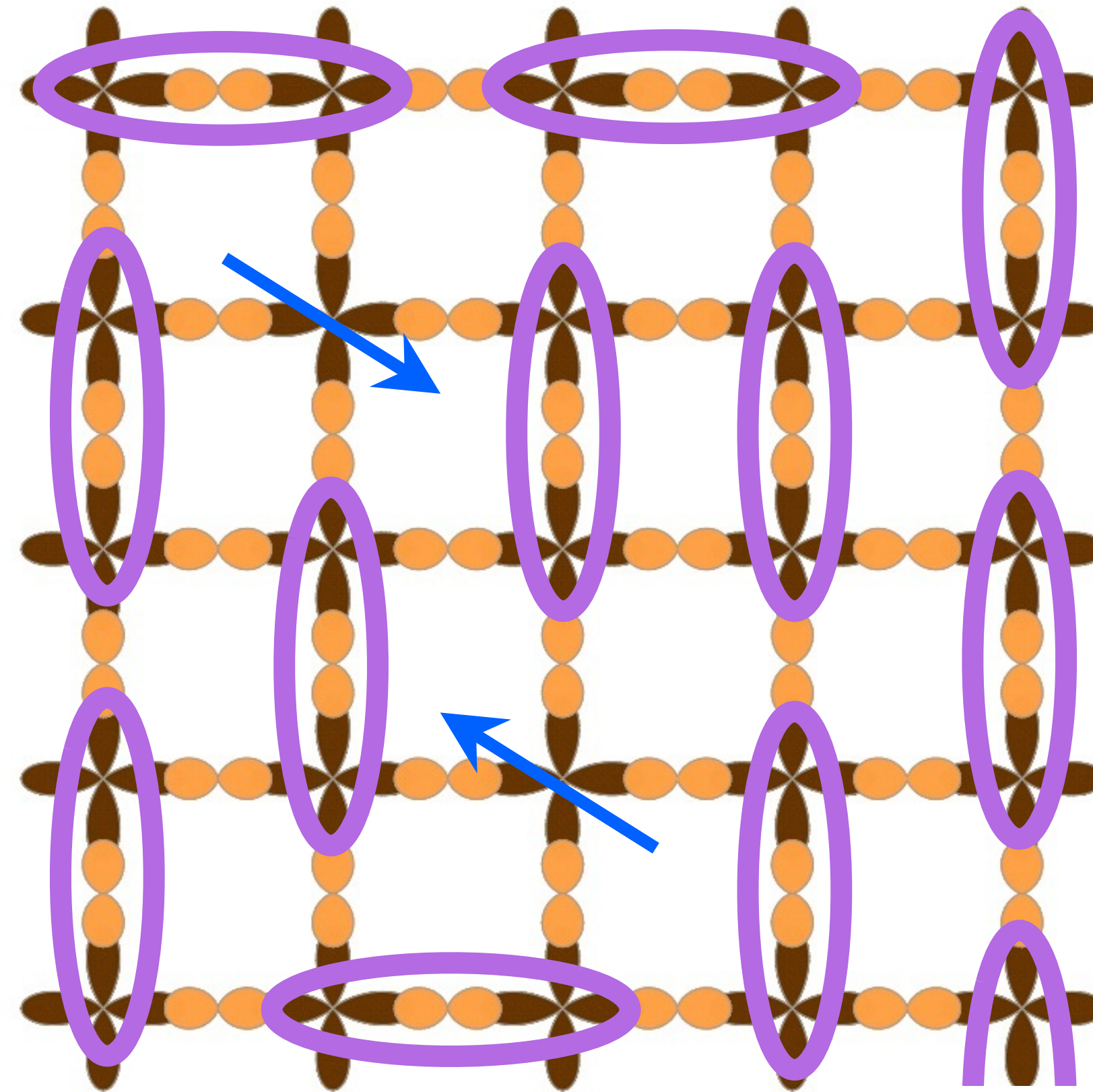
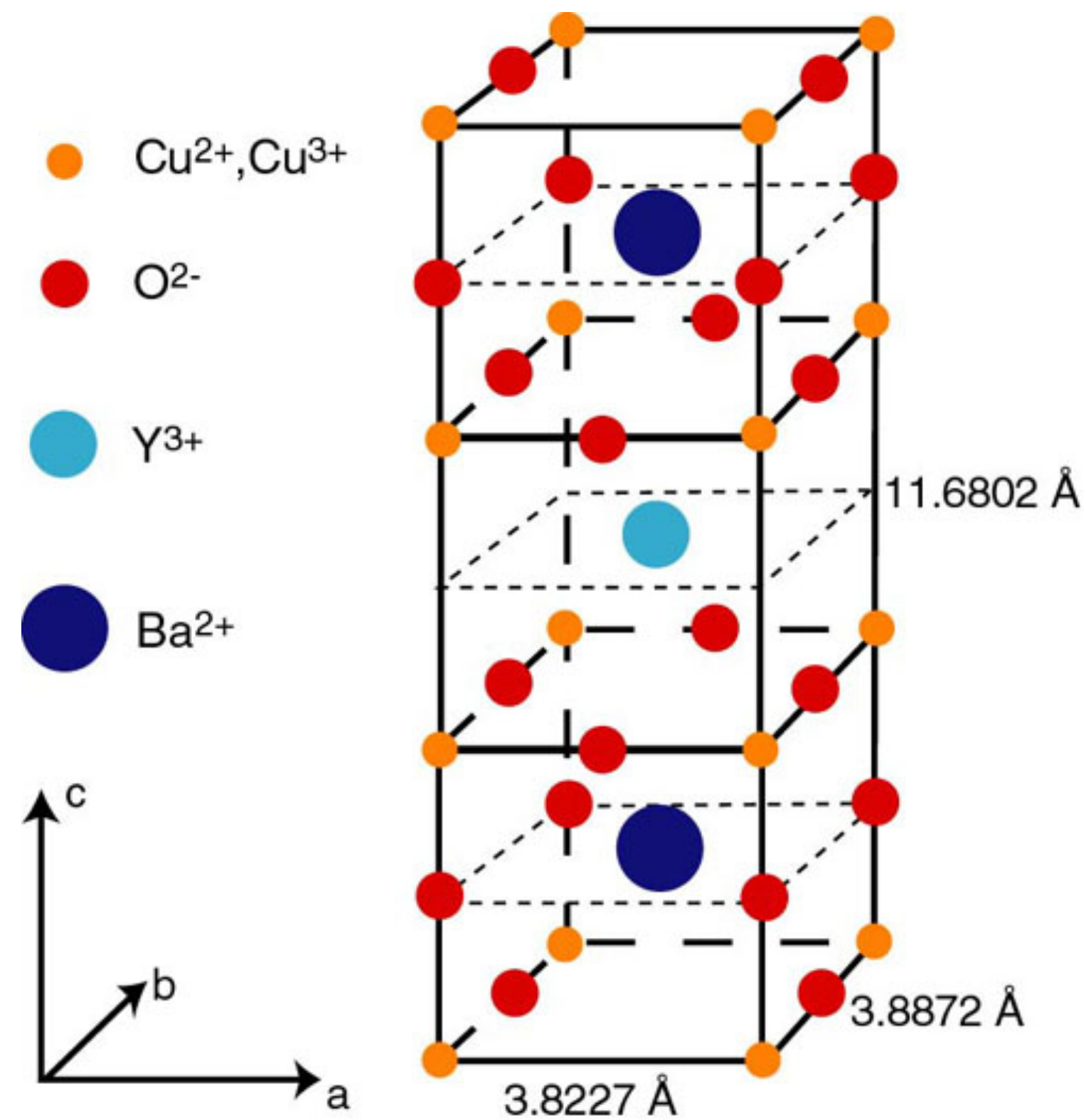
$$= \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

P.W.Anderson (1987): The key to high temperature superconductivity  
 is the formation of a “resonating valence bond state”.

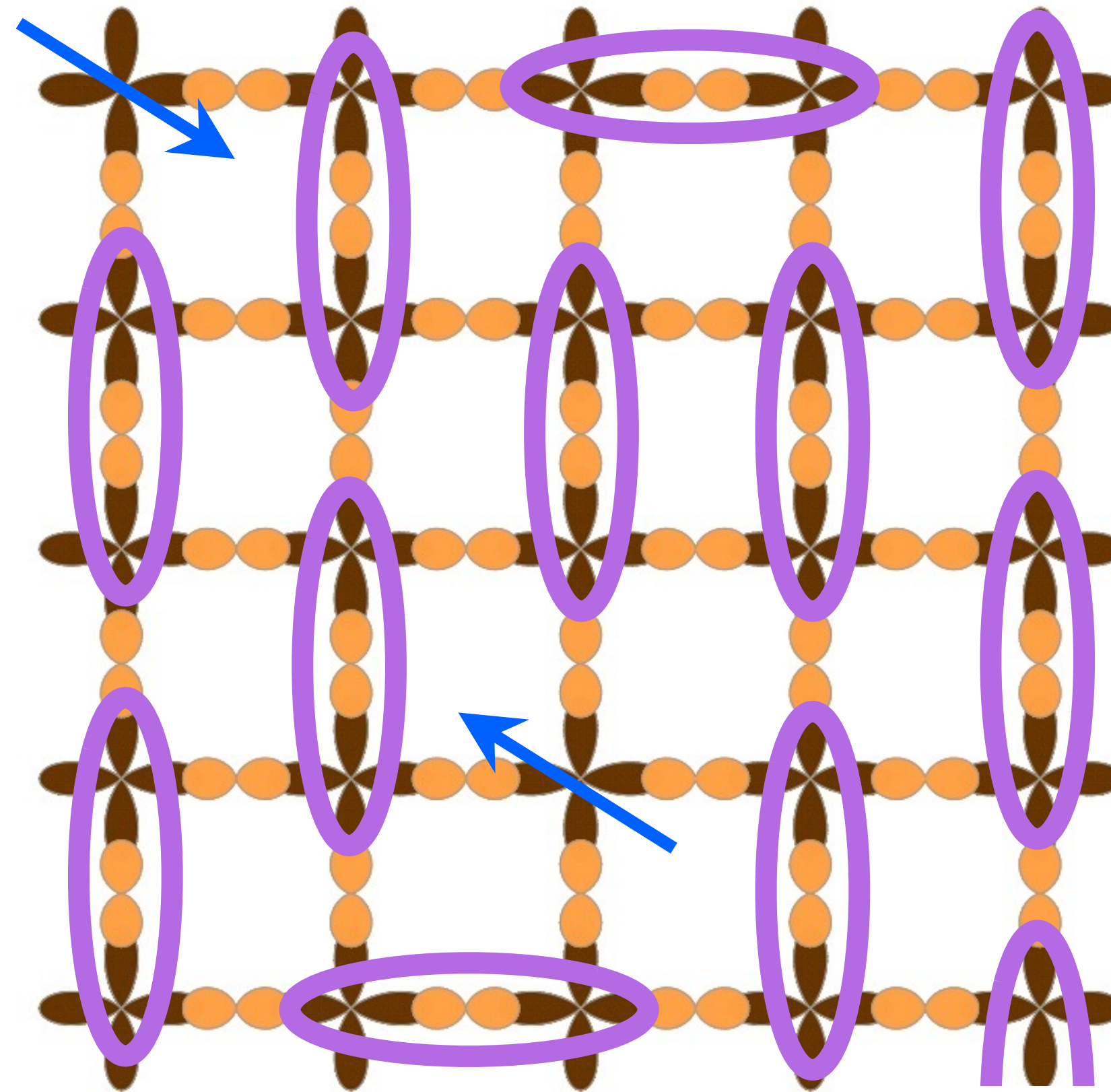
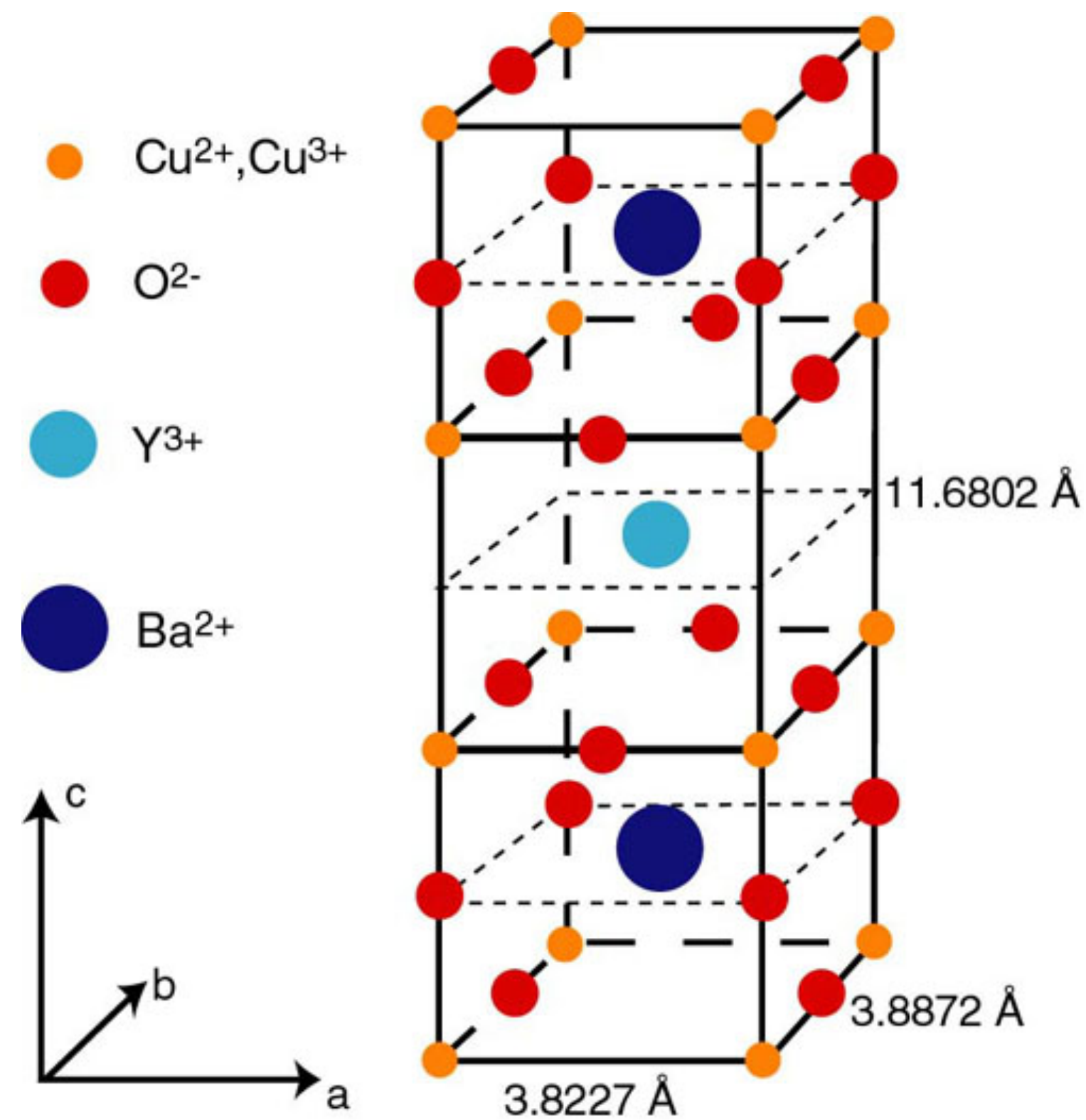
**A quantum spin liquid with many-boson (spins on Cu) entanglement**



Key feature: fractionalization. Excitations are particle-like, but cannot be created by local operators: they are classified under distinct superselection/anyon sectors.

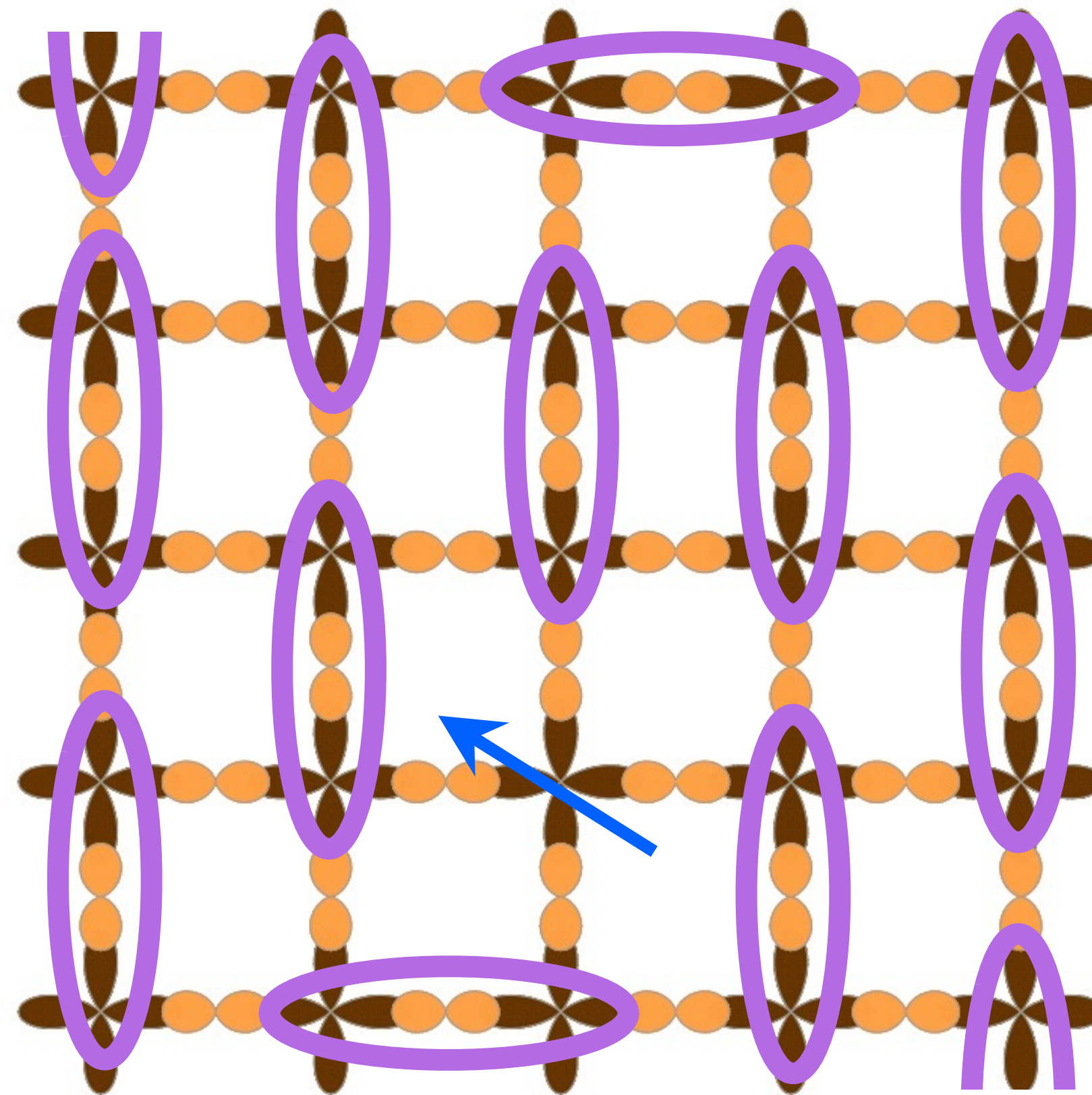
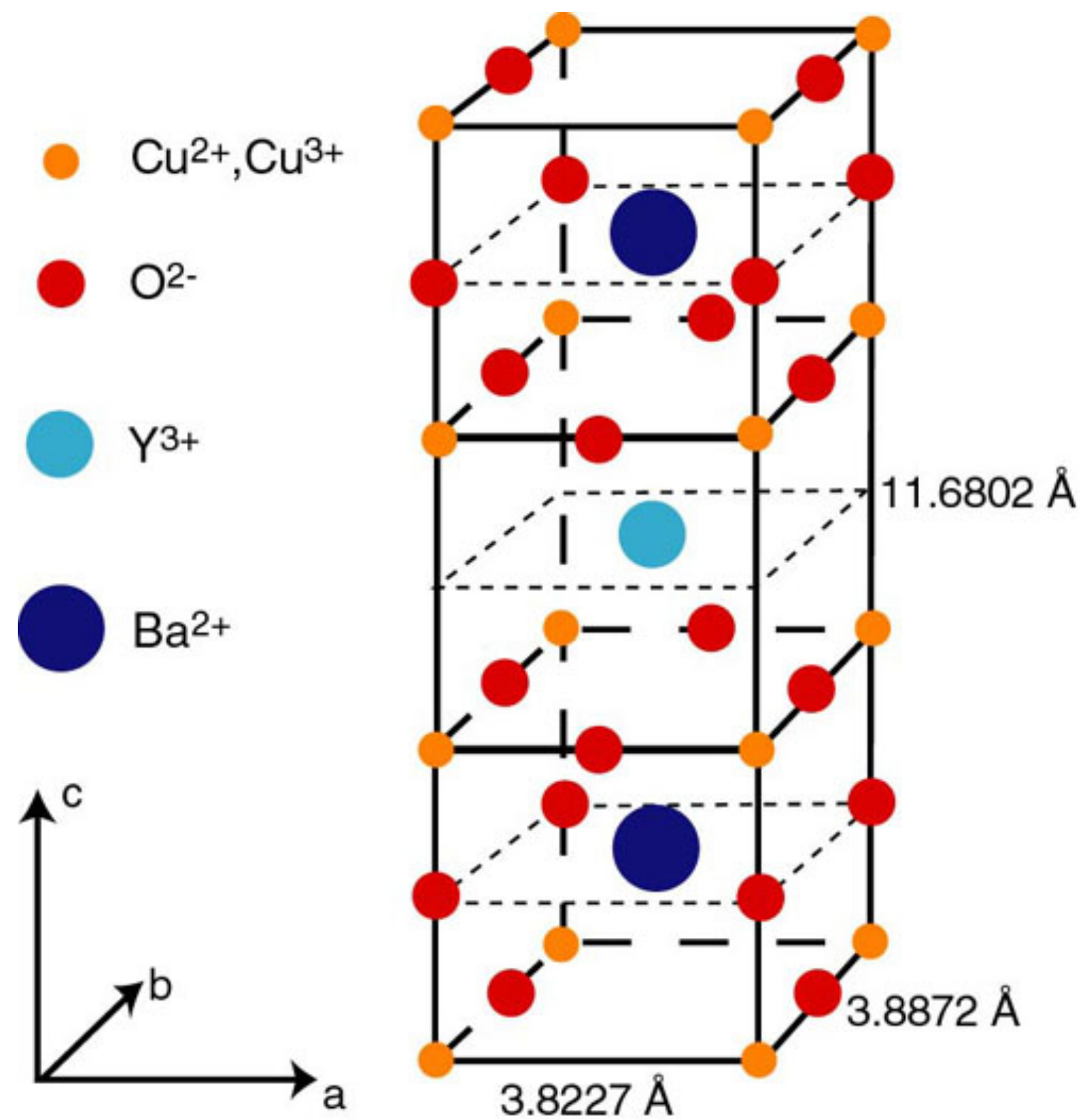


Key feature: fractionalization. Excitations are particle-like, but cannot be created by local operators: they are classified under distinct superselection/anyon sectors.



$$\text{Oval} = \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

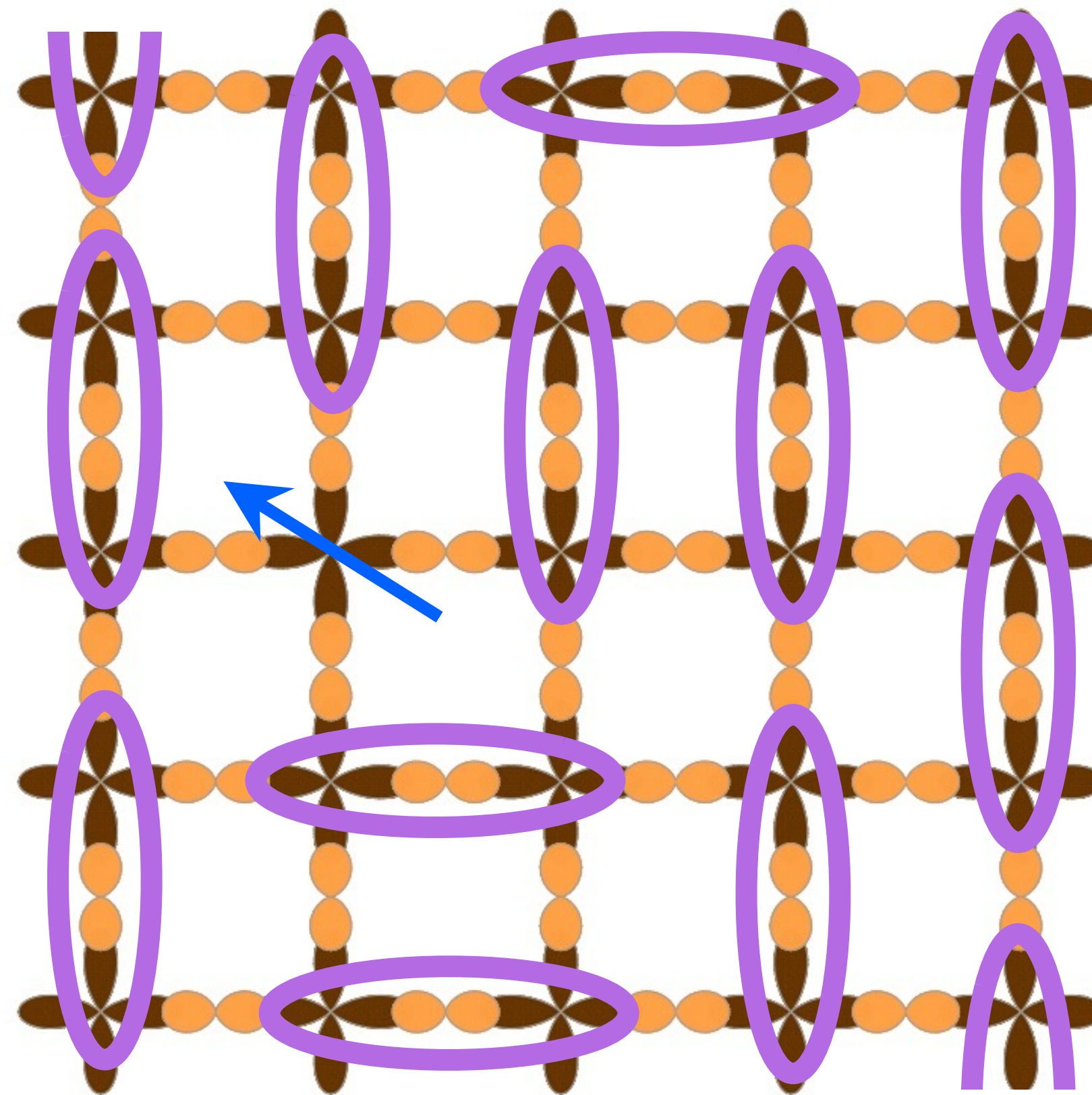
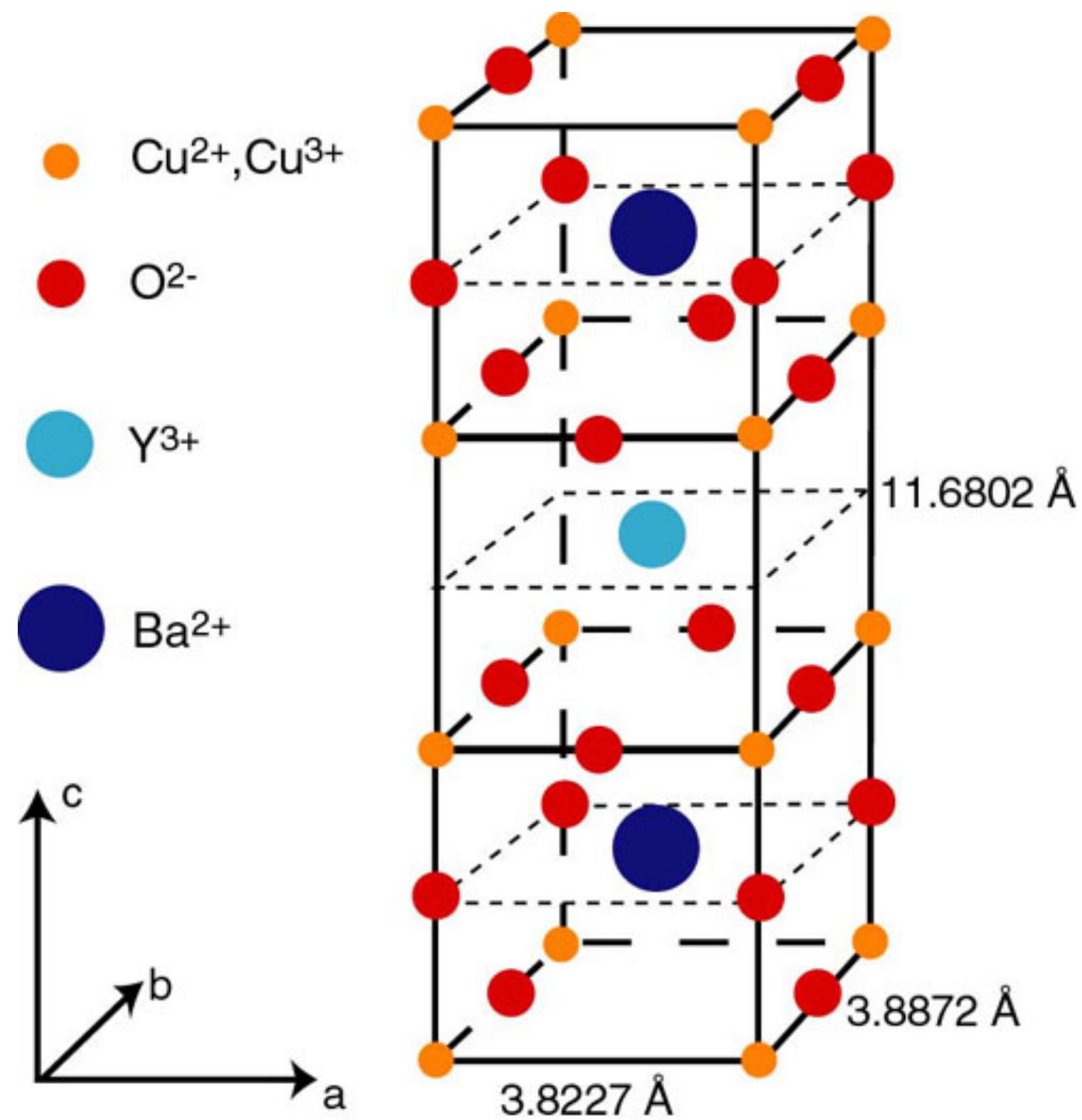
Key feature: fractionalization. Excitations are particle-like, but cannot be created by local operators: they are classified under distinct superselection/anyon sectors.



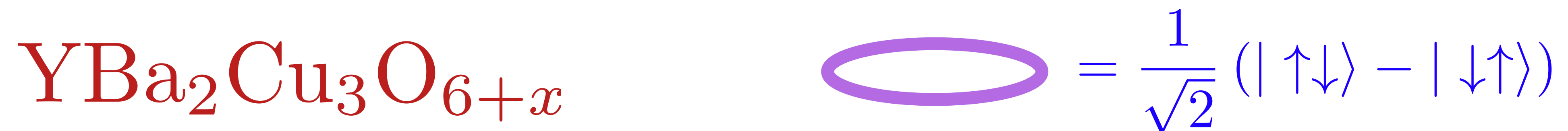
Spin  $S=1/2$ ,  
 charge  
 neutral  
 spinon



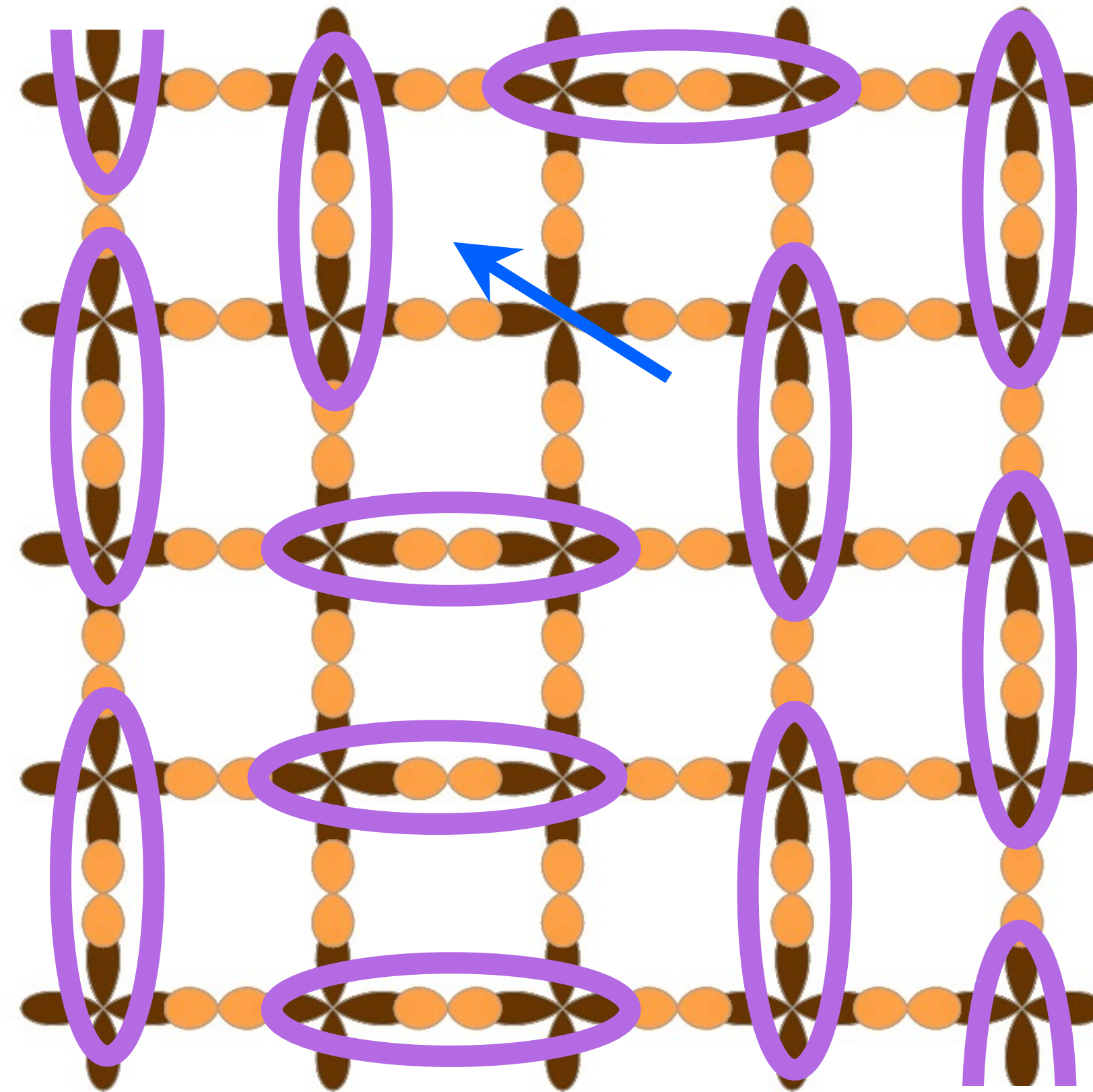
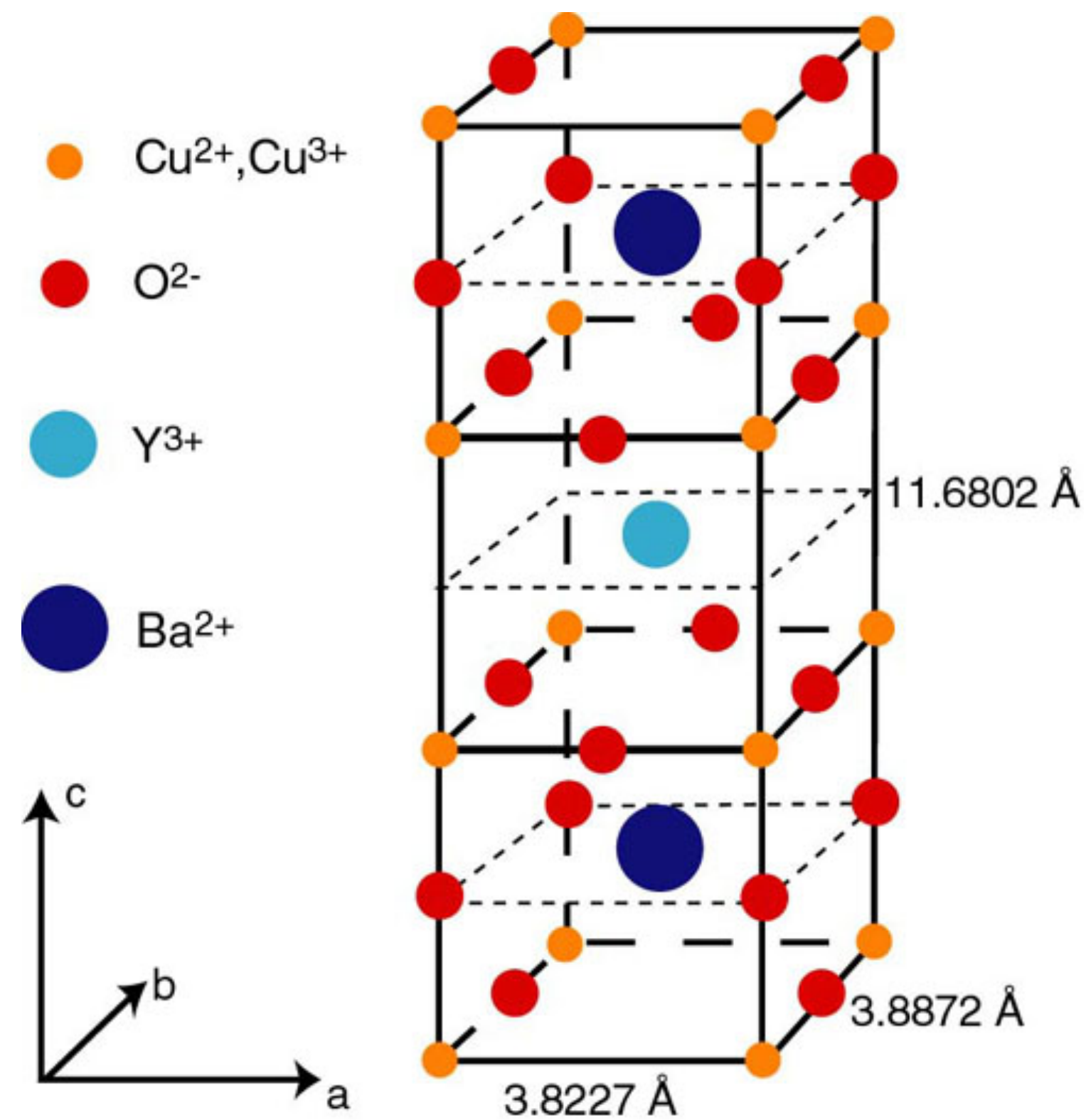
Key feature: fractionalization. Excitations are particle-like, but cannot be created by local operators: they are classified under distinct superselection/anyon sectors.



Spin  $S=1/2$ ,  
 charge  
 neutral  
 spinon



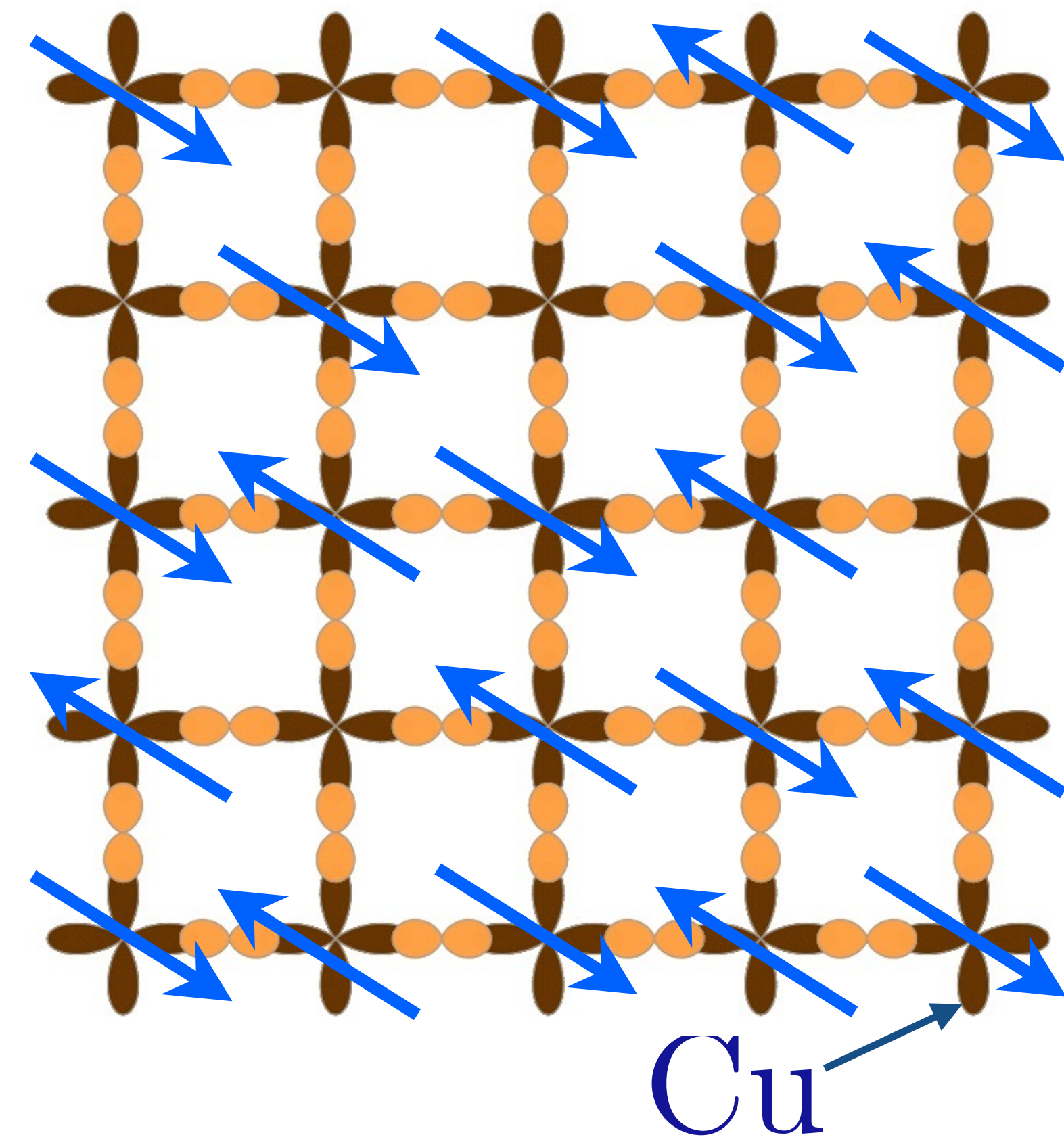
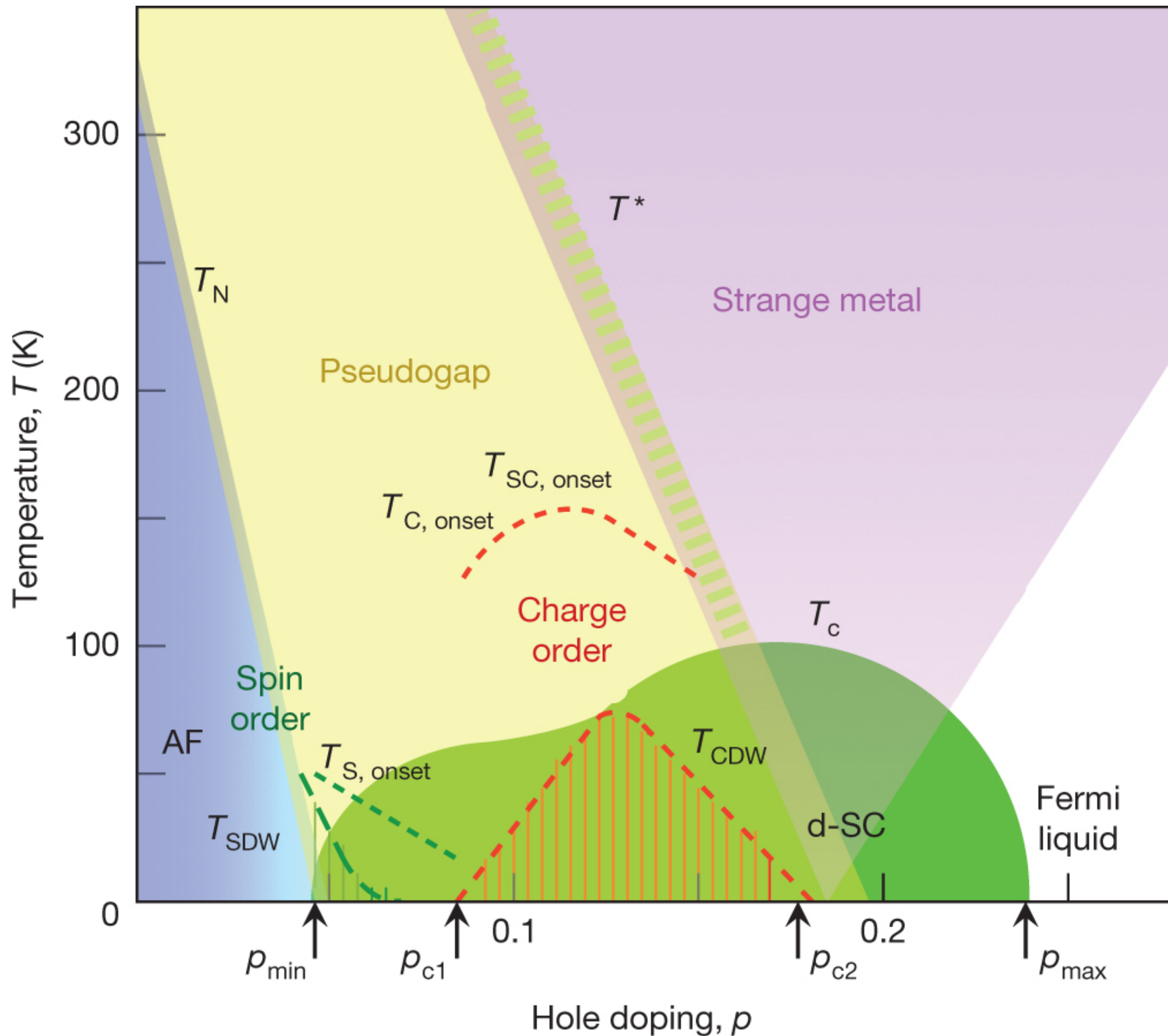
Key feature: fractionalization. Excitations are particle-like, but cannot be created by local operators: they are classified under distinct superselection/anyon sectors.



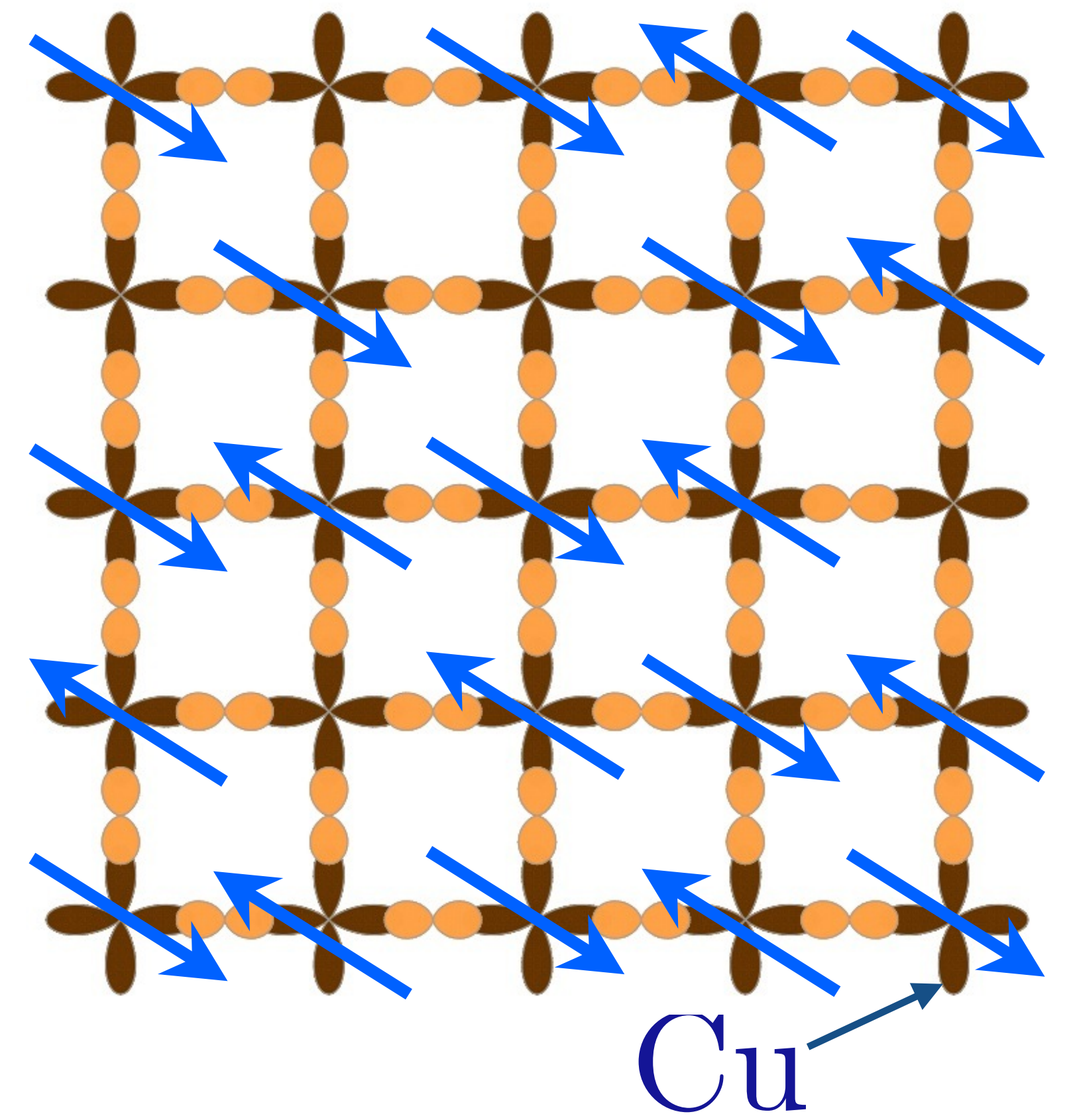
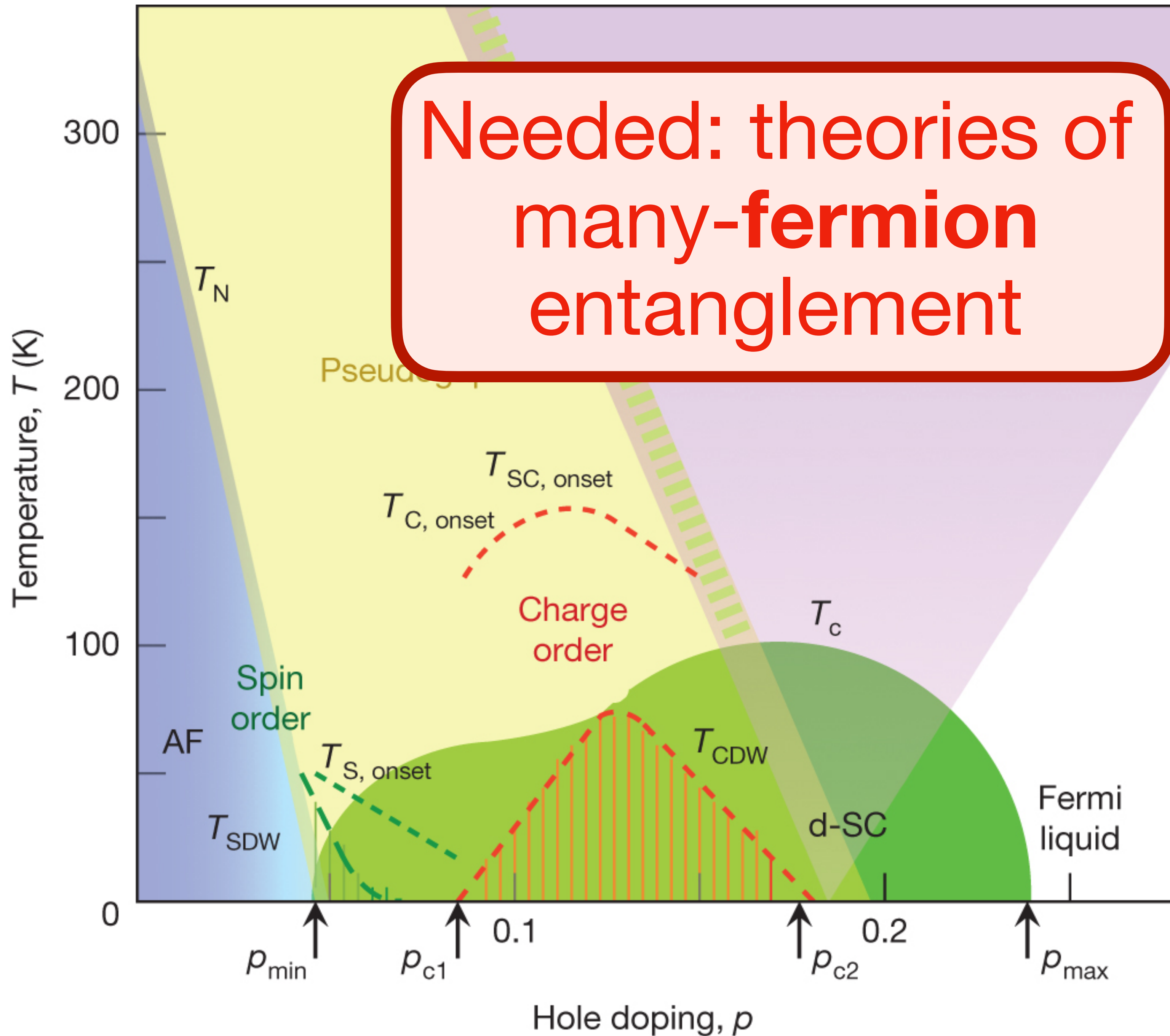
Spin  $S=1/2$ ,  
 charge  
 neutral  
 spinon



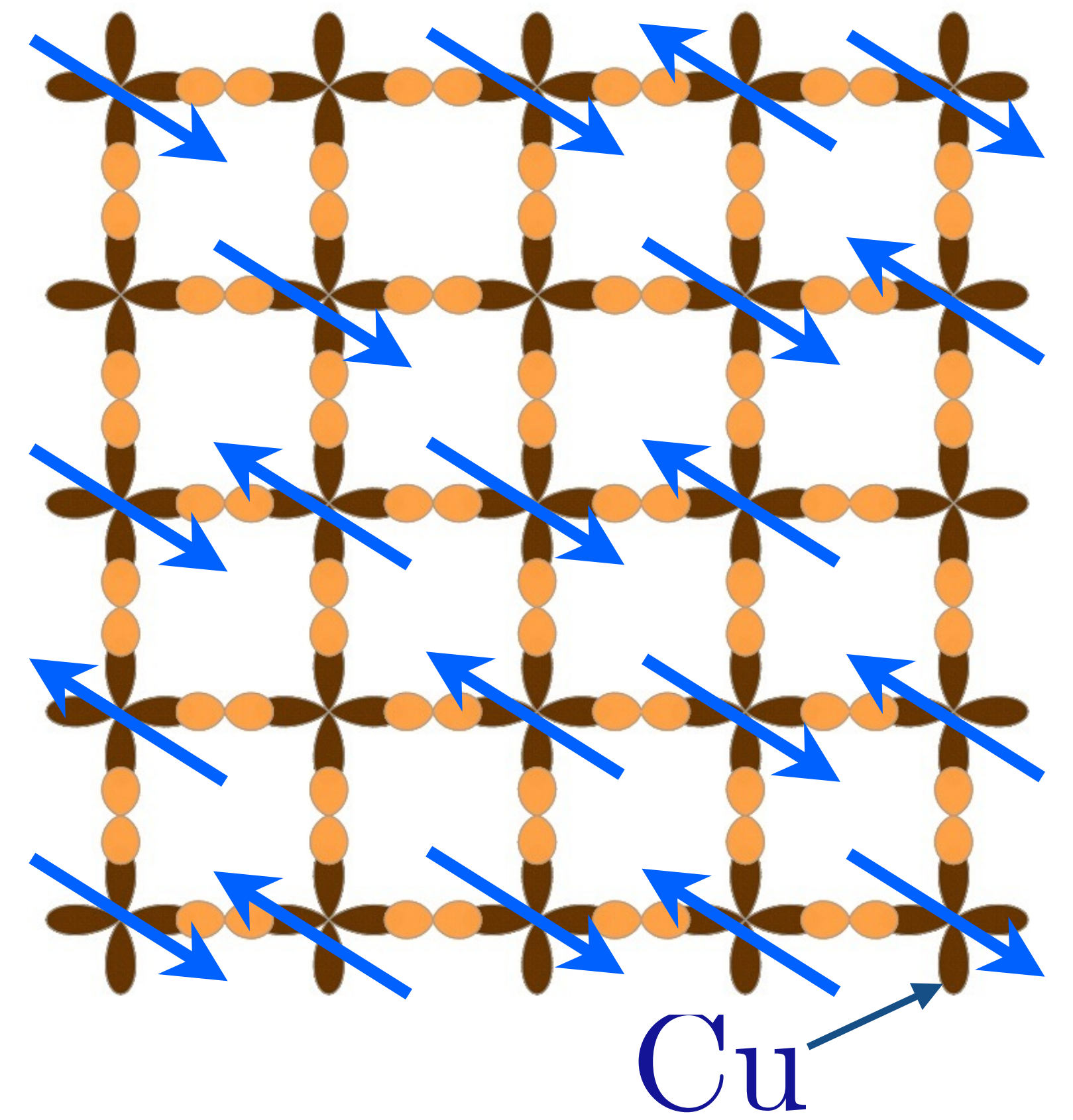
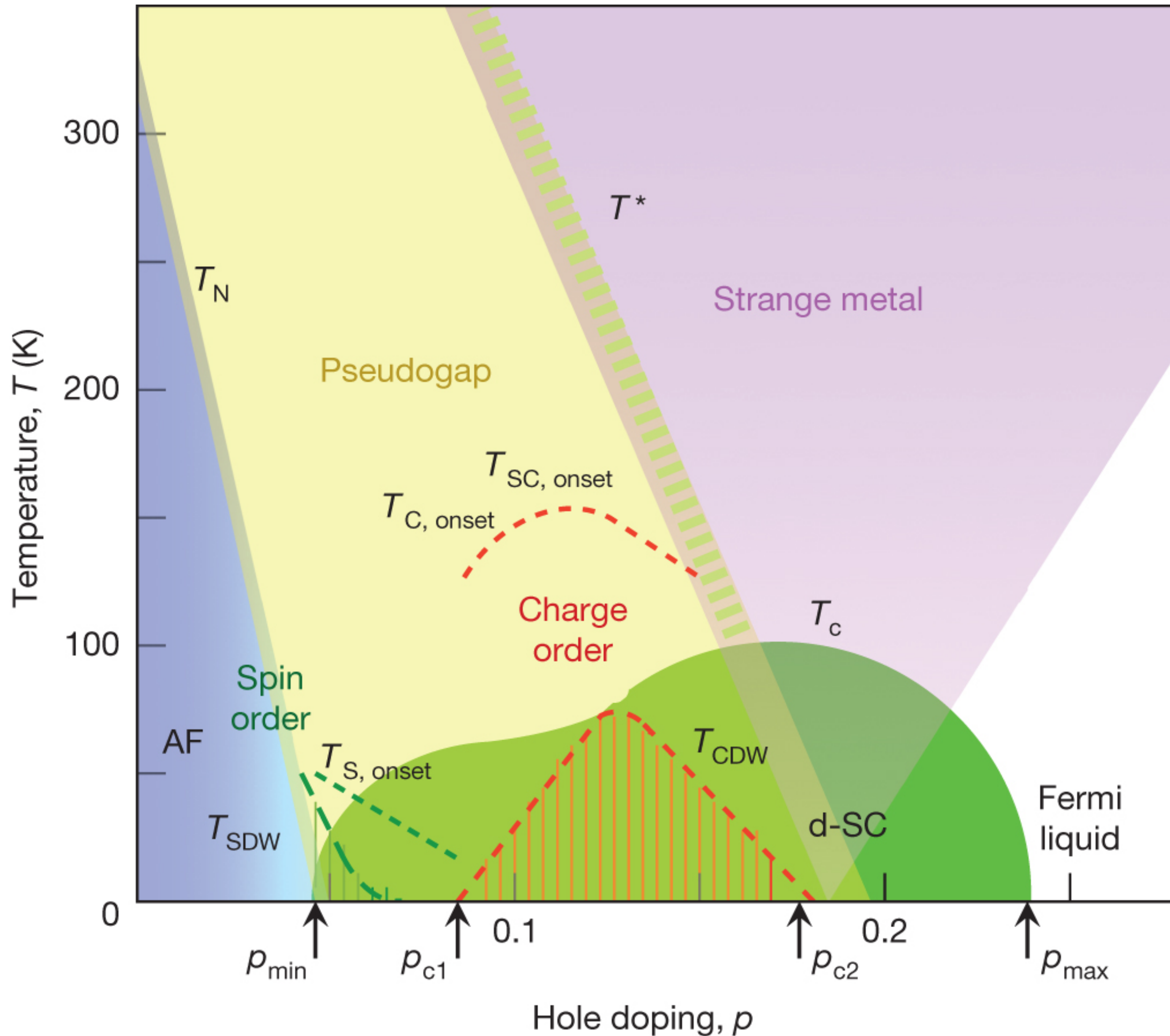
Key feature: fractionalization. Excitations are particle-like, but cannot be created by local operators: they are classified under distinct superselection/anyon sectors.



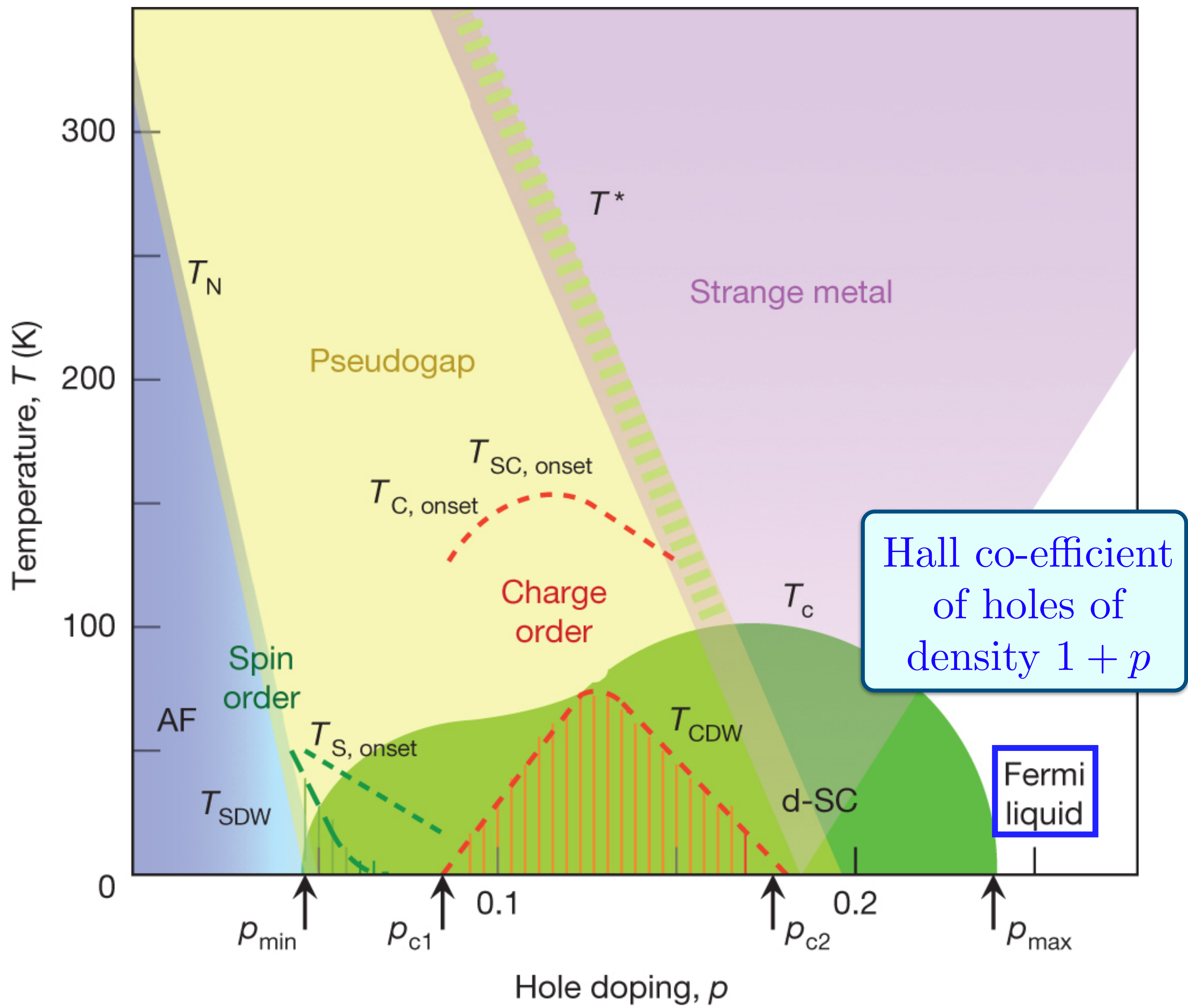
d-SC obtained upon doping AF with density  $p$  holes.

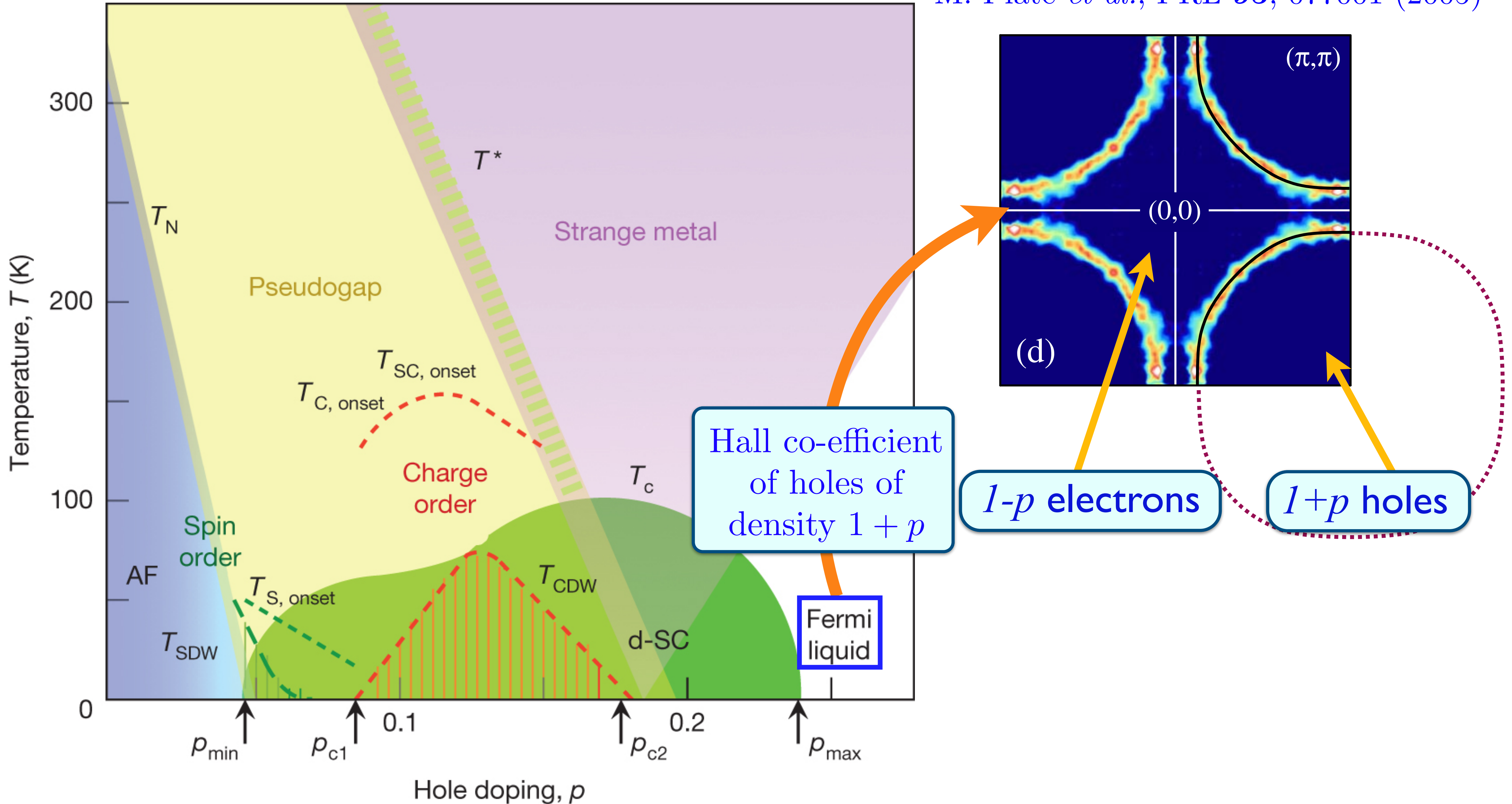


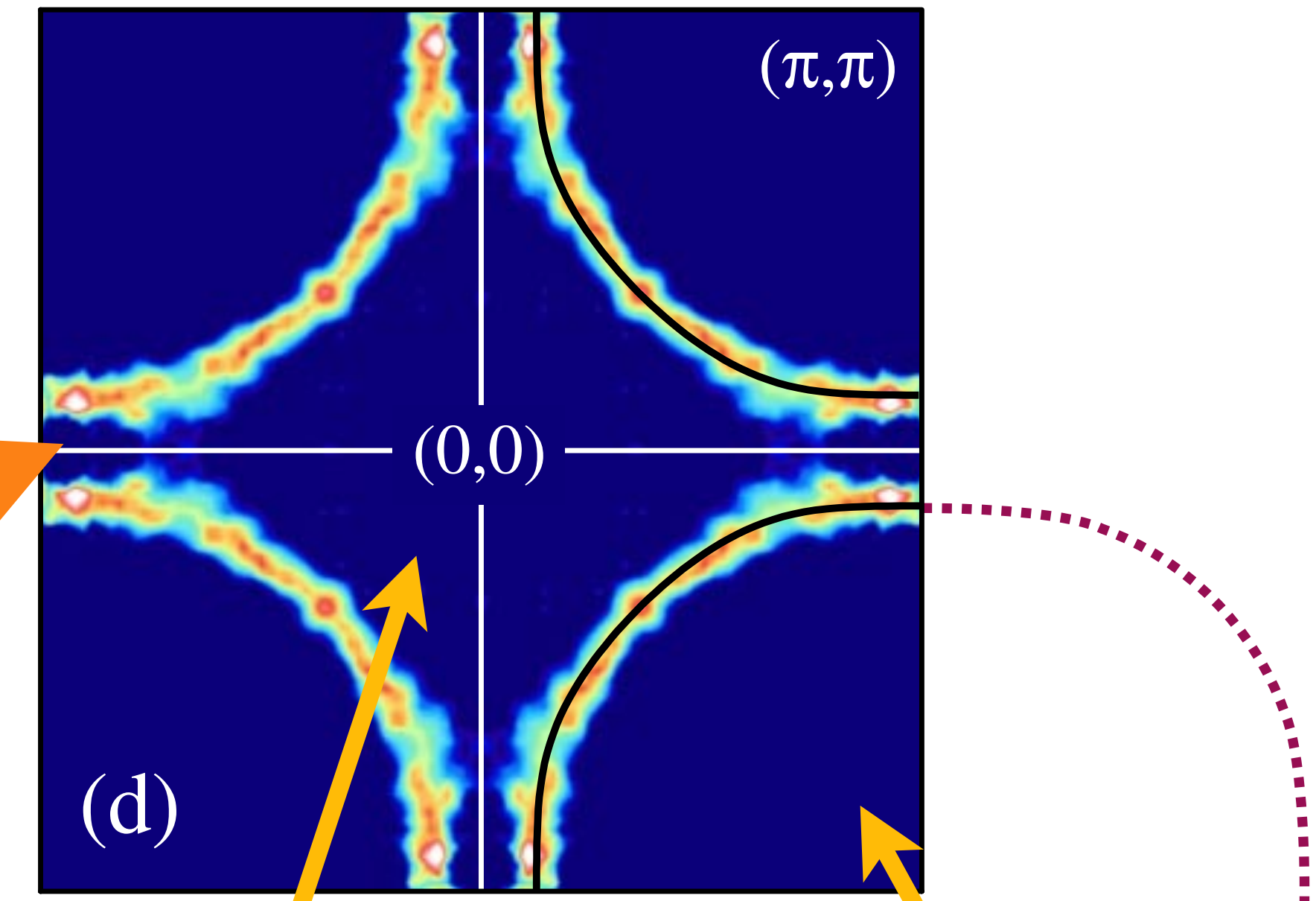
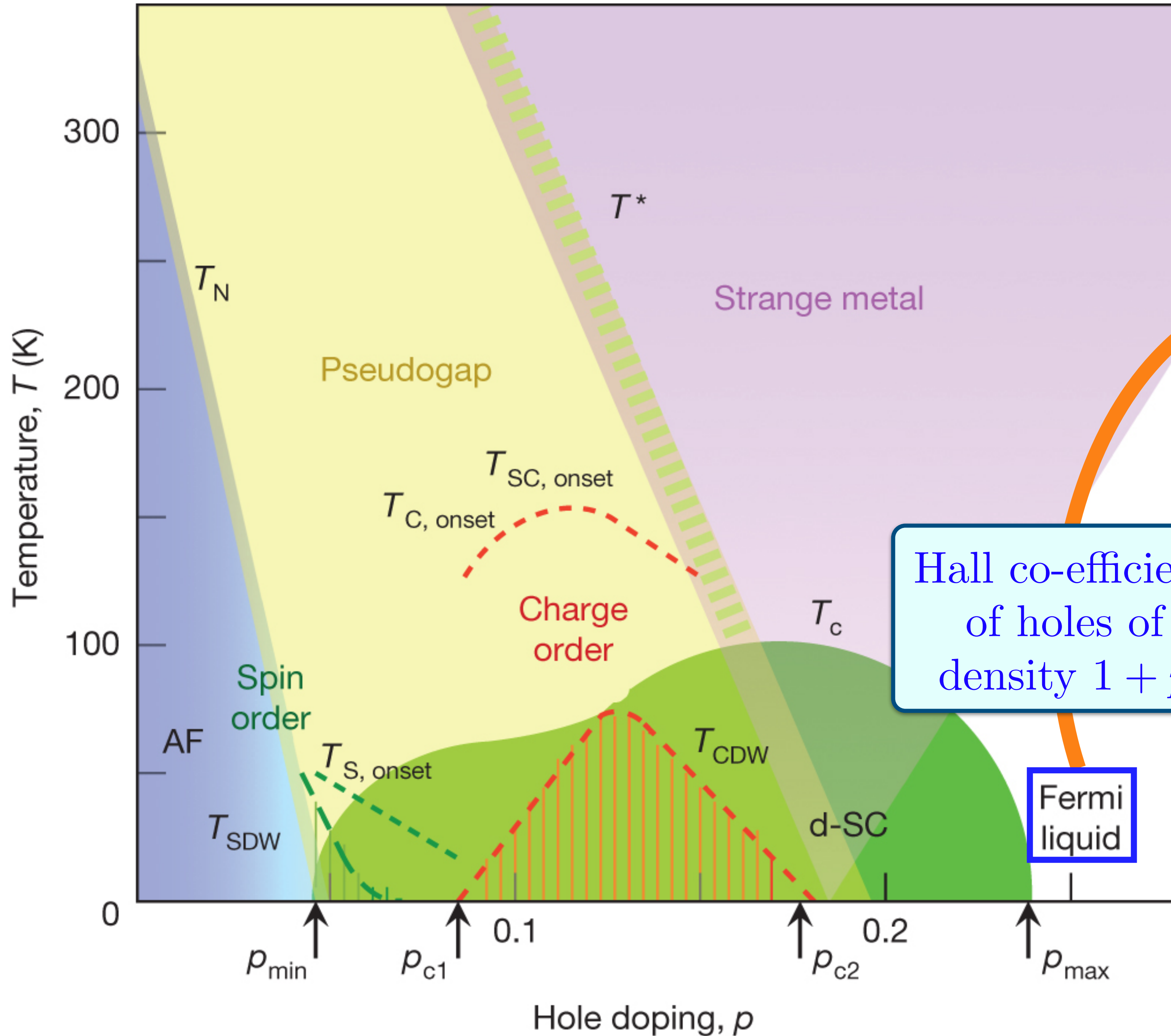
d-SC obtained upon doping AF with density  $p$  holes.



d-SC obtained upon doping AF with density  $p$  holes. Hole density relative to the filled band  $\rho = 1 + p$ . Electron density relative to the empty band  $\rho_e = 1 - p$ .





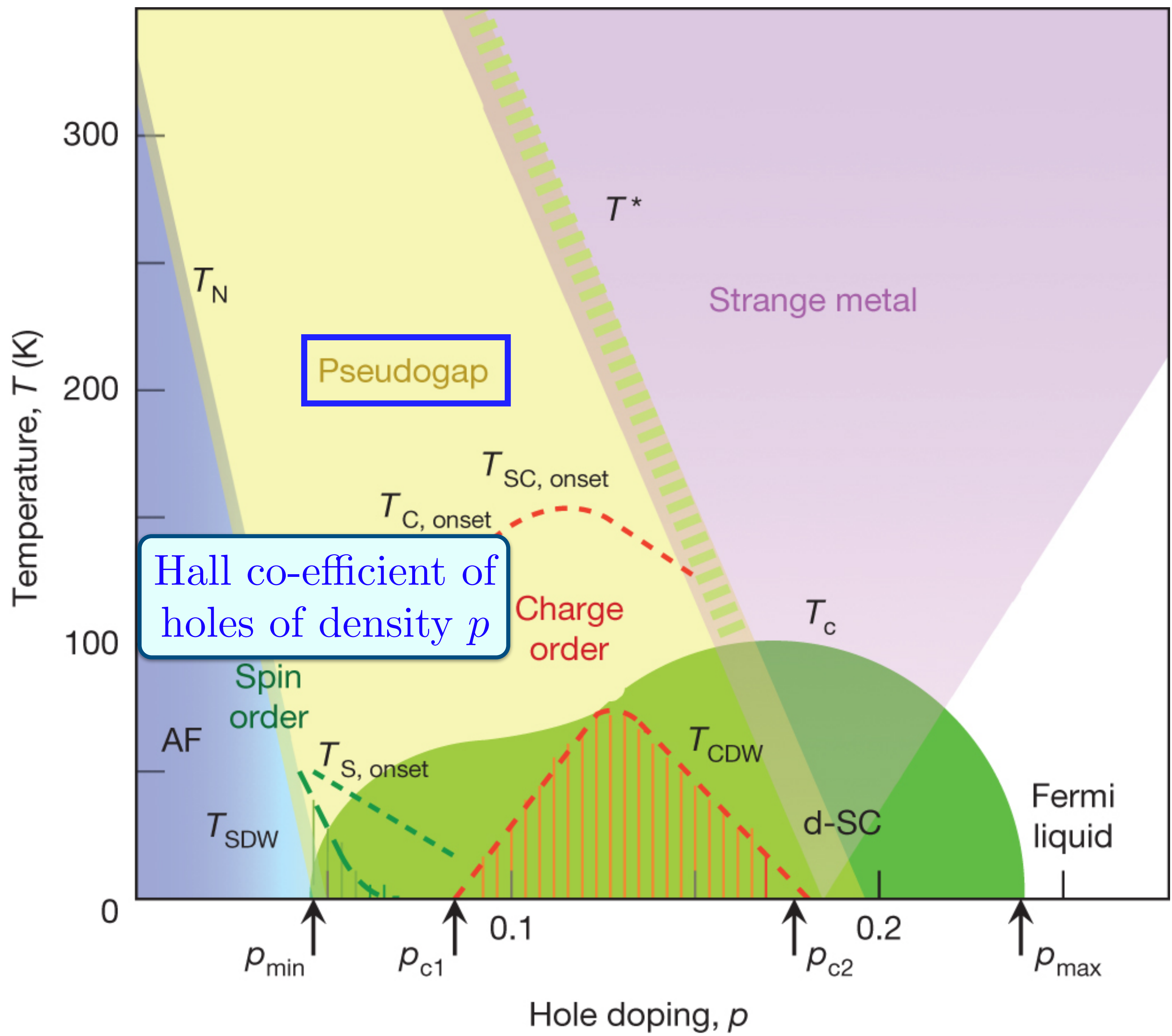


Hall co-efficient of holes of density  $1 + p$

$1-p$  electrons

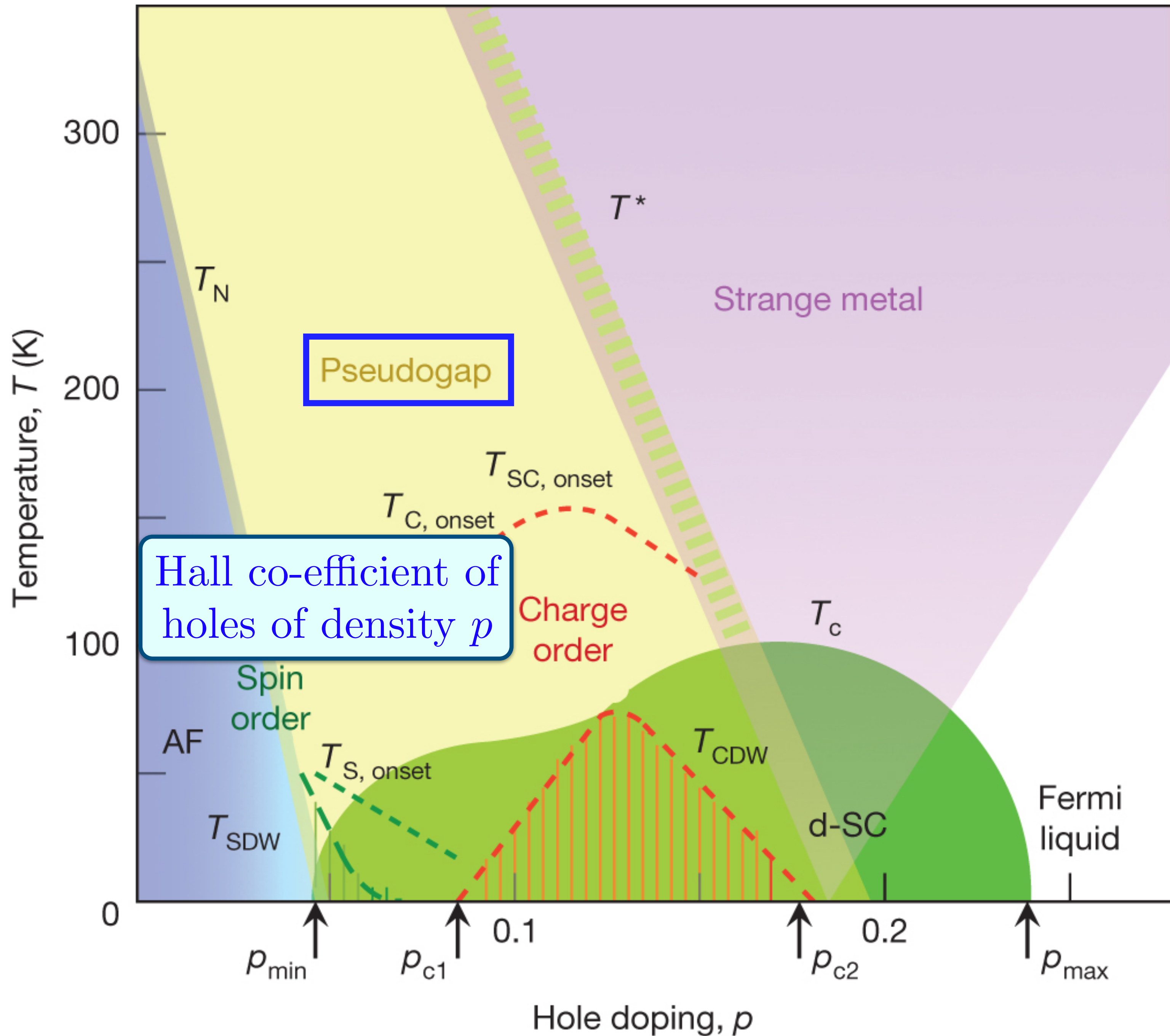
$1+p$  holes

**Luttinger, 1960:** Area enclosed by the Fermi surface is the same as that for free fermions *with the same symmetry*.



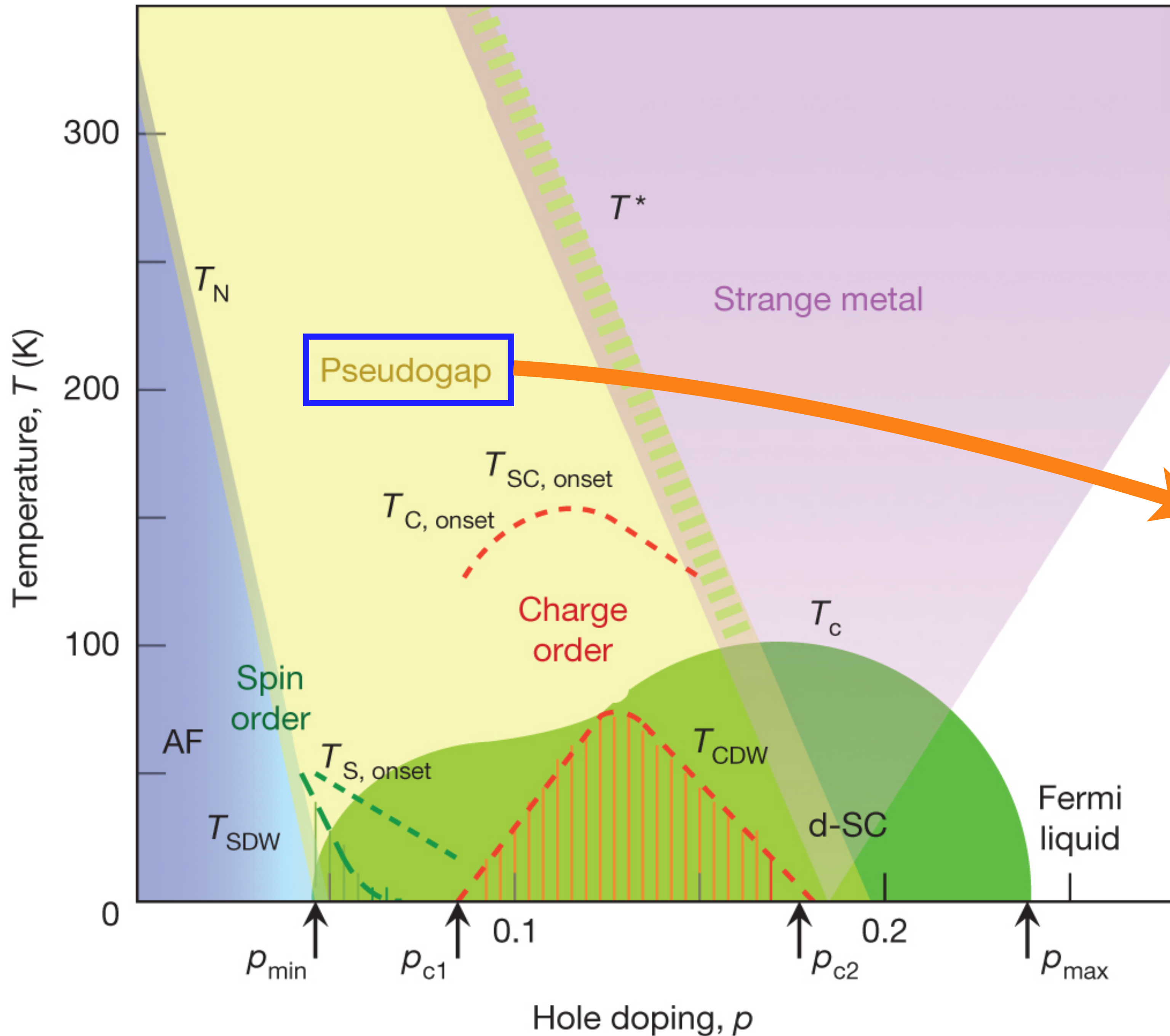
But there is no antiferromagnetic order to justify carrier density  $p$

Many theories with fluctuating and intertwined AFM, d-SC and charge orders.



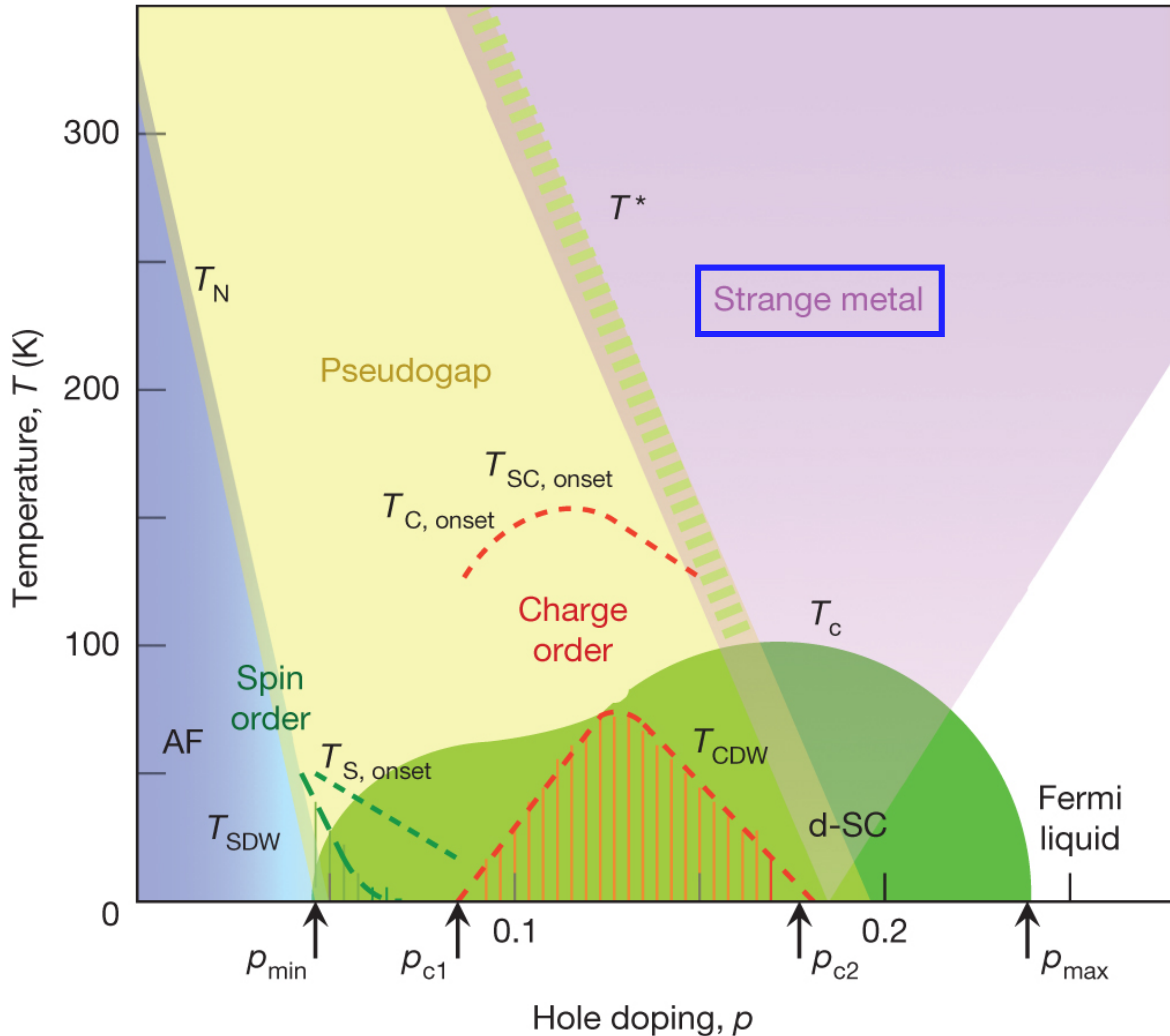
**Quantum entanglement of mobile fermions without an energy gap**

I argue that a better starting point is a novel quantum ground state with no broken symmetry.



**Quantum entanglement of mobile fermions without an energy gap**

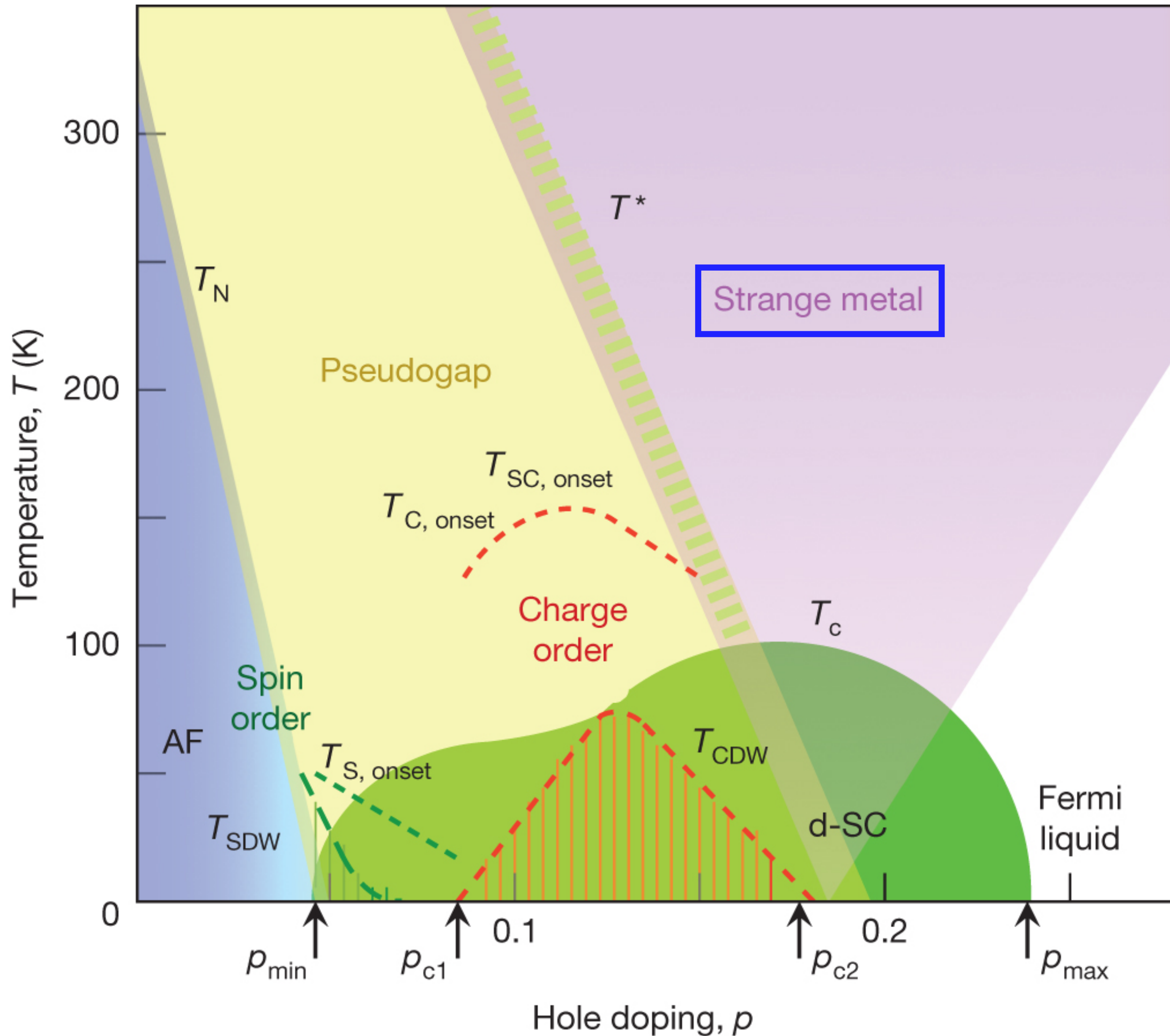
**I. Fractionalized Fermi Liquid (FL\*)**  
Fractionalized (anyonic) spinon excitations co-existing with electron-like quasiparticles on a Fermi surface which can tunnel coherently between layers.



**Quantum entanglement of mobile fermions without an energy gap**

**II. Sachdev-Ye-Kitaev (SYK) liquid**

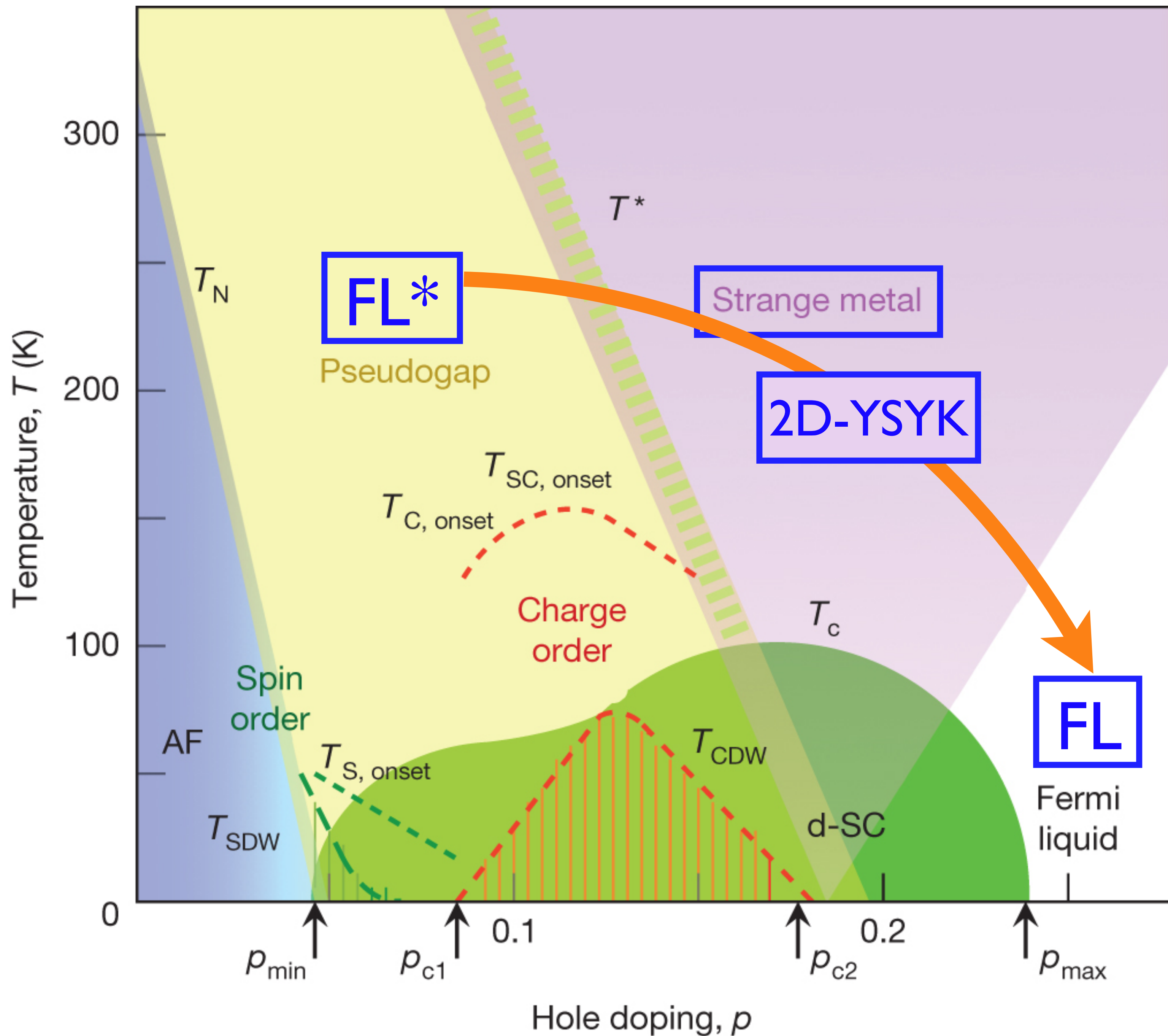
- Compressible state with no quasiparticles.



**Quantum entanglement of mobile fermions without an energy gap**

## II. Sachdev-Ye-Kitaev (SYK) liquid

- Compressible state with no quasiparticles.
- SYK: low energy theory of generic charged black holes in asymptotically flat 3+1 dimensional space.



## Quantum entanglement of mobile fermions without an energy gap

### II. Sachdev-Ye-Kitaev (SYK) liquid

- Compressible state with no quasiparticles.
- SYK: low energy theory of generic charged black holes in asymptotically flat 3+1 dimensional space.
- 2D-YSYK: universal theory of strange metals: FL\*-FL transition in cuprates.

Many fermion entanglement I:

Fractionalized  
Fermi liquids ( $FL^*$ )

# Fermi liquid

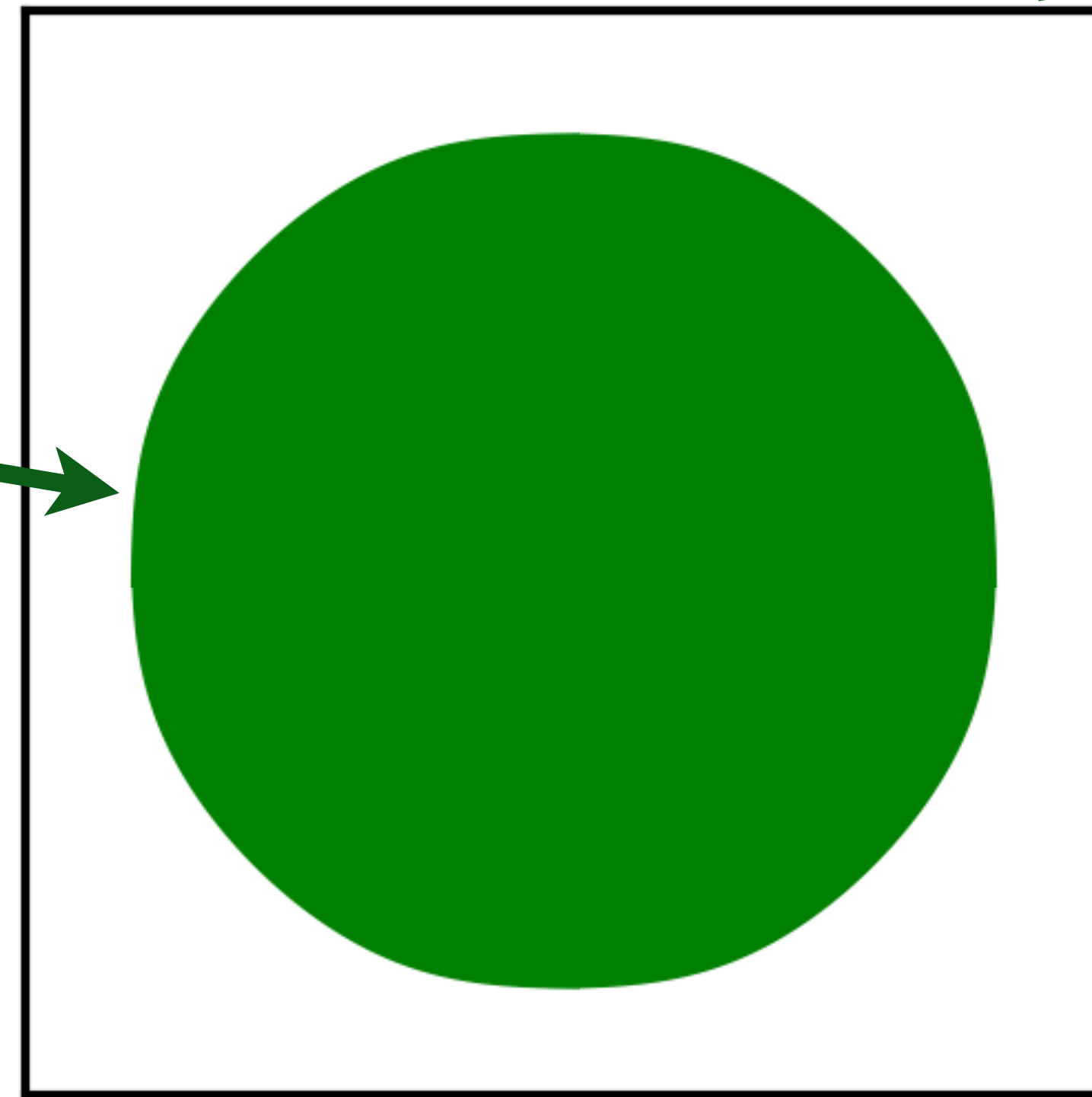
Spin-1/2 holes of density

$$\rho = 1 + p$$

Positive Hall coefficient  
of carrier density  $\rho$

Area  $\rho/2$

Area 1



**Luttinger, 1960:** Area enclosed by the Fermi surface is the same as that for free fermions *with the same symmetry*.

# Fermi liquid

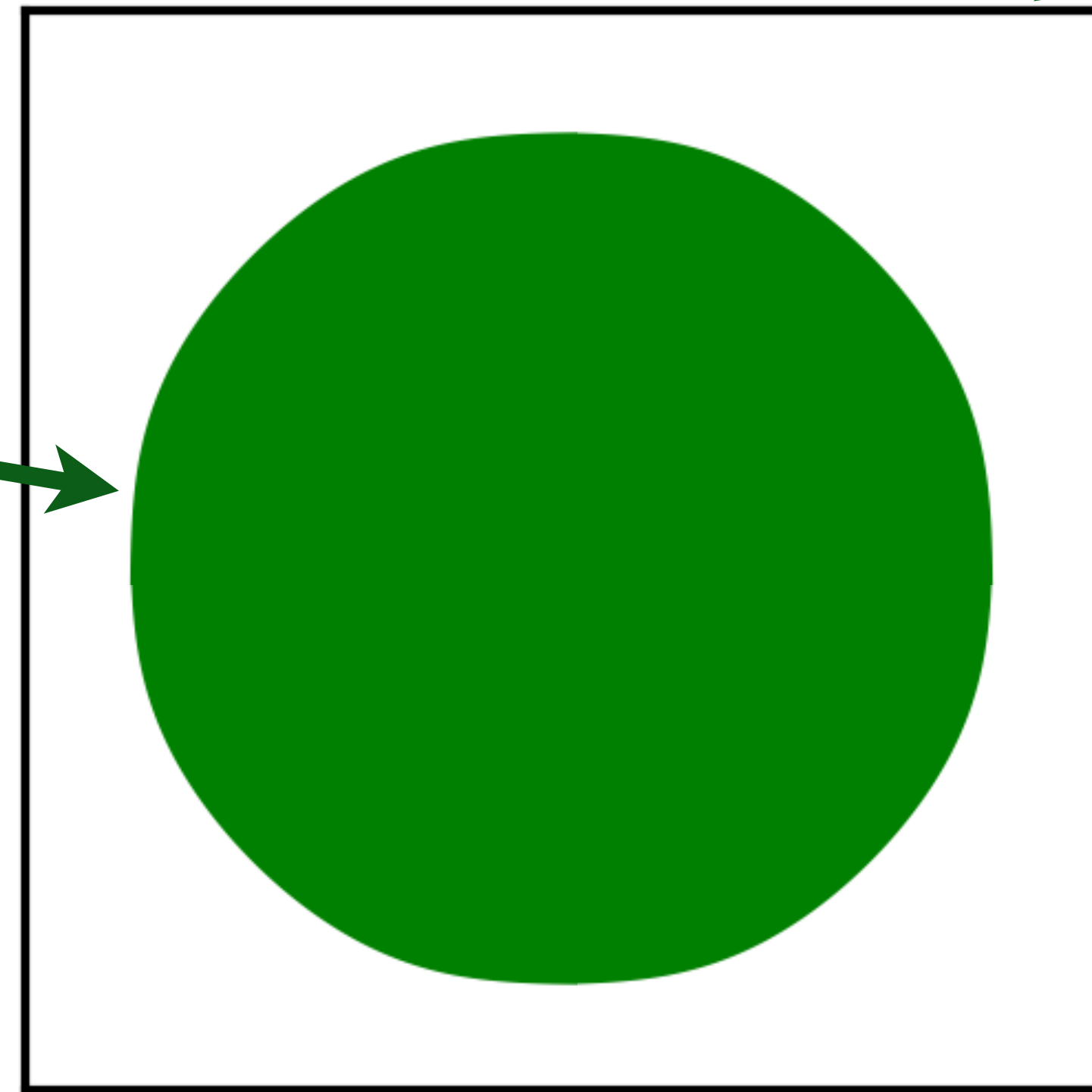
Spin-1/2 holes of density

$$\rho = 1 + p$$

Positive Hall coefficient  
of carrier density  $\rho$

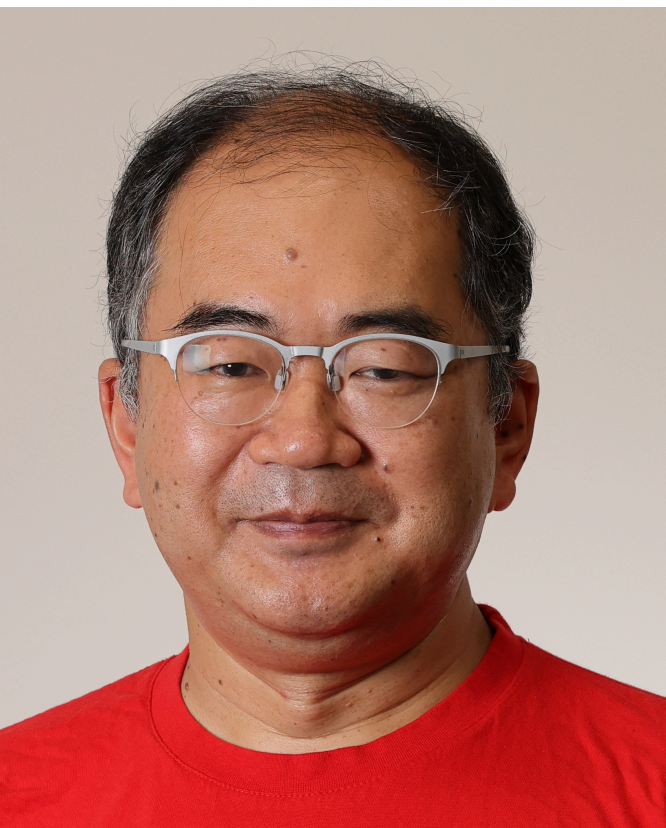
Area  $\rho/2$

Area 1



**Luttinger, 1960:** Area enclosed by the Fermi surface is the same as that for free fermions *with the same symmetry*.

**Oshikawa, 2000:** Area constrained by an anomaly-argument of global U(1) and translations



# Fractionalized Fermi liquid (FL\*)

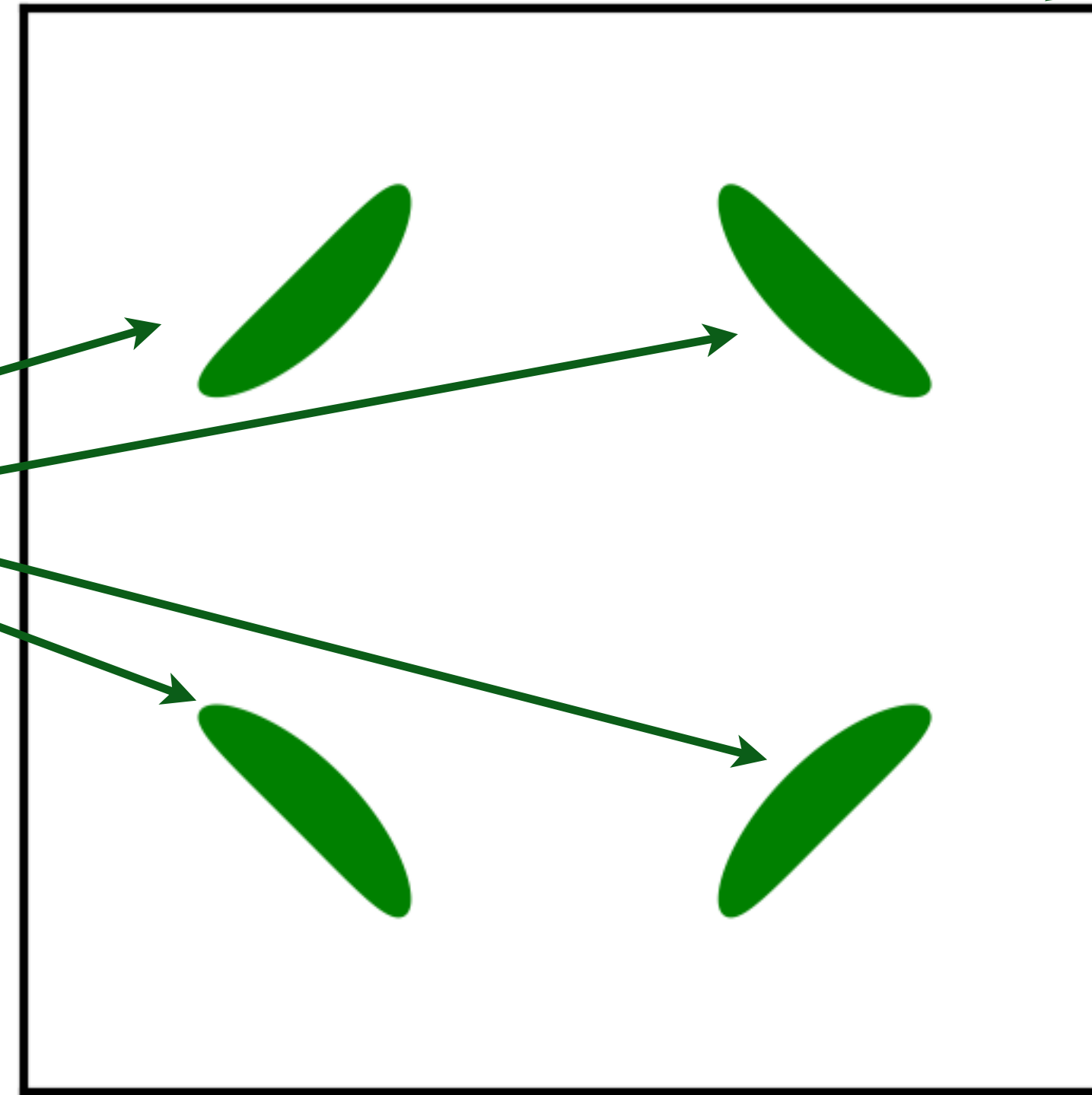
Area 1

Spin-1/2 holes of density

$$\rho = 1 + p$$

Positive Hall coefficient  
of carrier density  $\rho - 1$

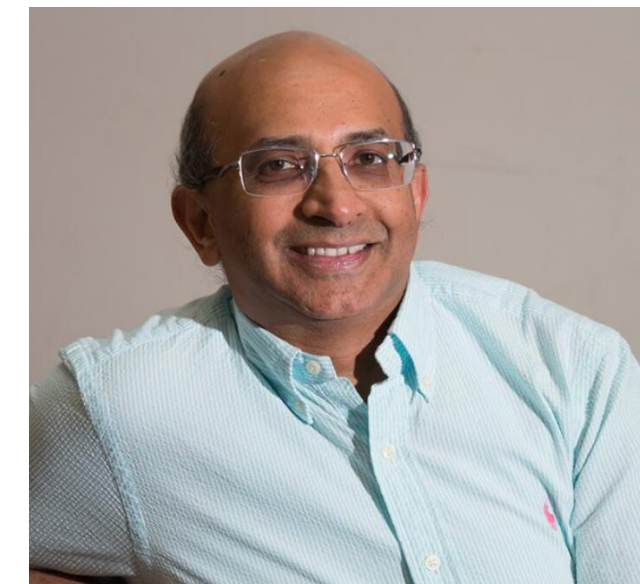
Total area  
 $(\rho - 1)/2$



No  
broken  
symmetry.

Area per  
pocket  
 $= p/8$

Oshikawa anomaly-argument is satisfied by  
the sum of spin liquid (1) and  
Fermi surface anomalies  $(\rho - 1)$



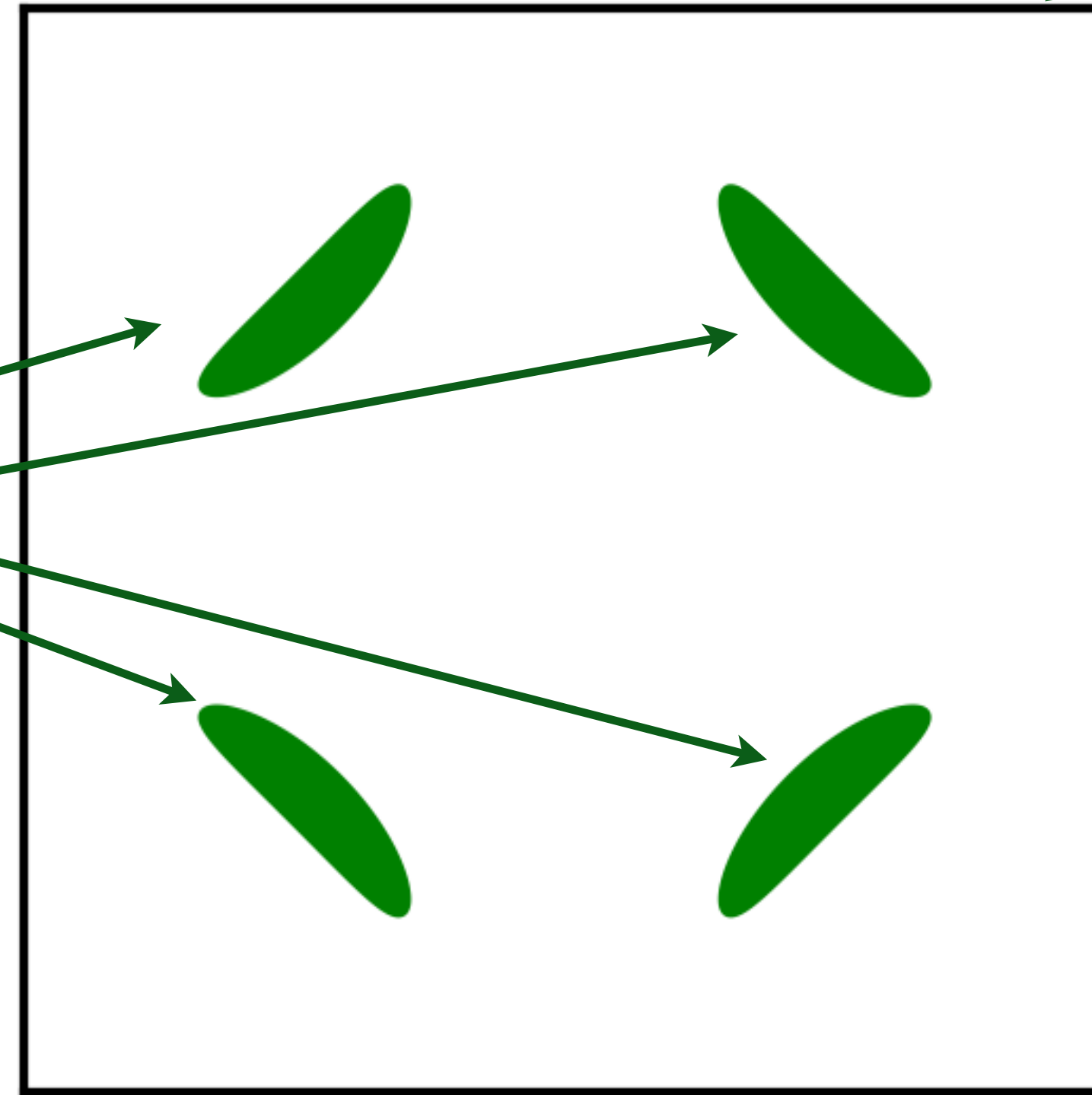
# Fractionalized Fermi liquid (FL\*)

Area 1

Spin-1/2 holes of density  
 $\rho = 1 + p$

Positive Hall coefficient  
of carrier density  $\rho - 1$

Total area  
 $(\rho - 1)/2$



The density deficit (1) in the area is quantized by rigid structure of the spin liquid.

Oshikawa anomaly-argument is satisfied by the sum of spin liquid (1) and Fermi surface anomalies  $(\rho - 1)$



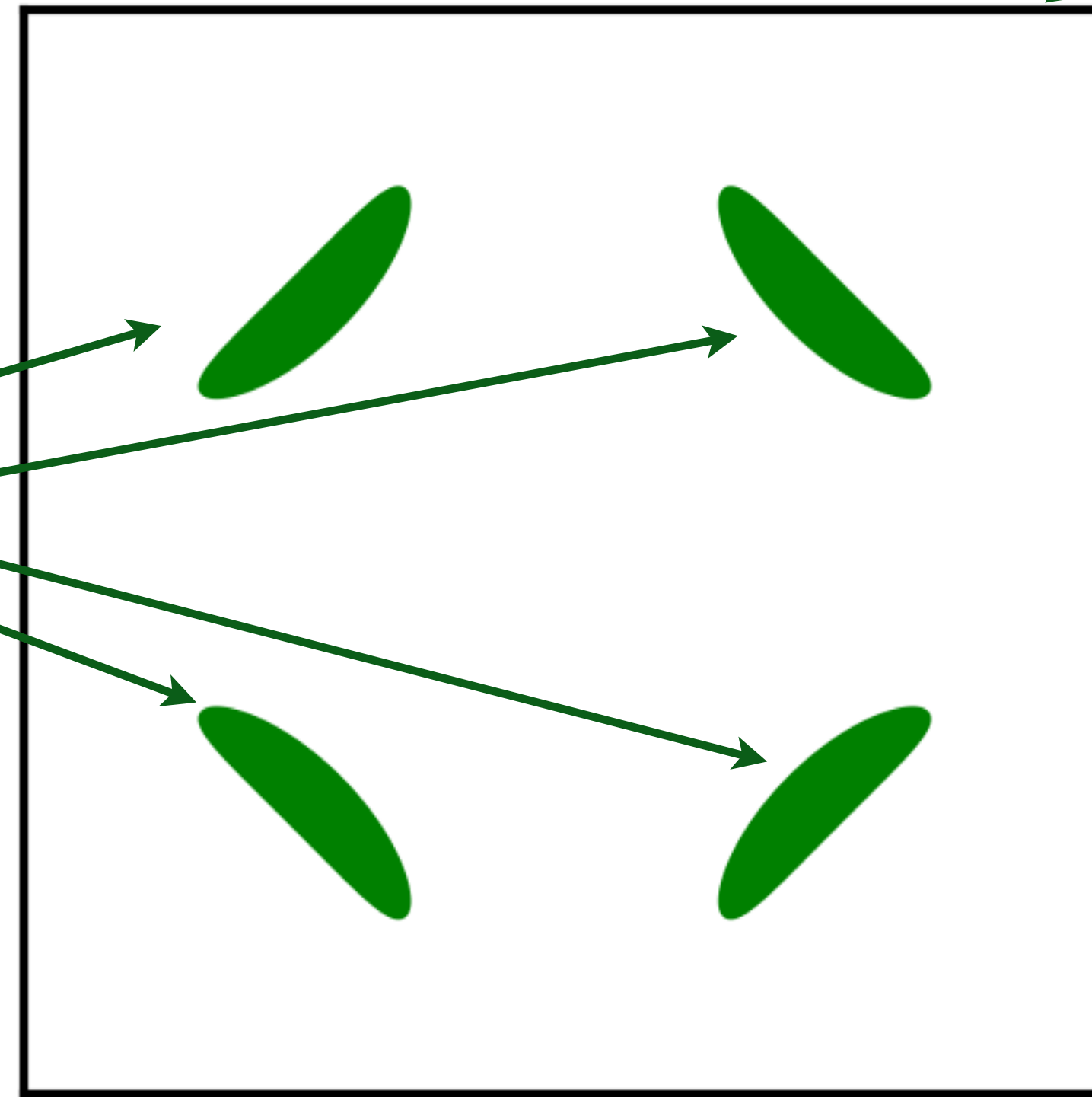
# Fractionalized Fermi liquid (FL\*)

Area 1

Spin-1/2 holes of density  
 $\rho = 1 + p$

Positive Hall coefficient  
of carrier density  $\rho - 1$

Total area  
 $(\rho - 1)/2$

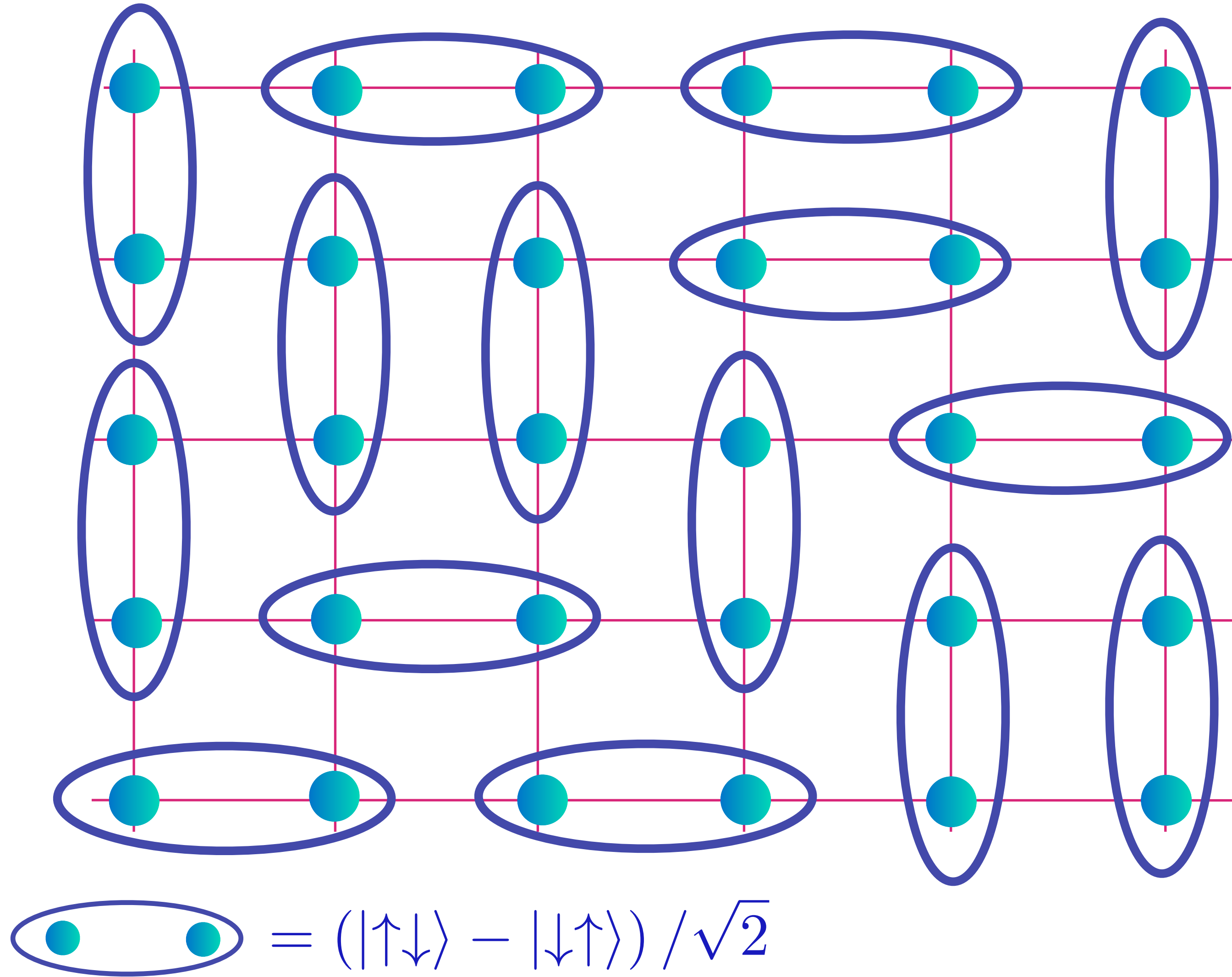


Measuring non-Luttinger Fermi surface area is direct evidence for multi-fermion quantum entanglement.

Oshikawa anomaly-argument is satisfied by  
the sum of spin liquid (1) and  
Fermi surface anomalies  $(\rho - 1)$



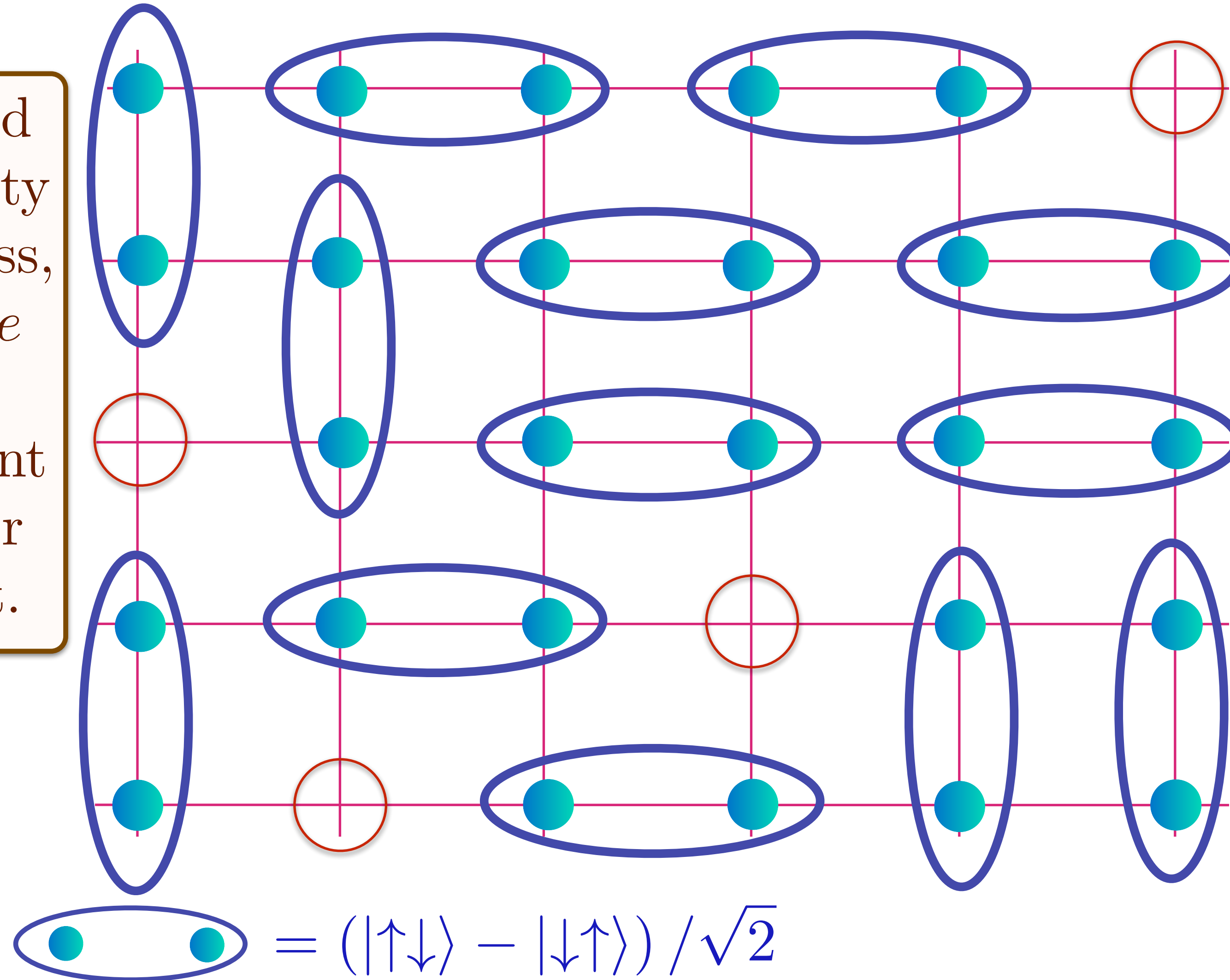
# Anderson's RVB



# Doping an insulating antiferromagnet with holes of density $p$

## Mobile Holons

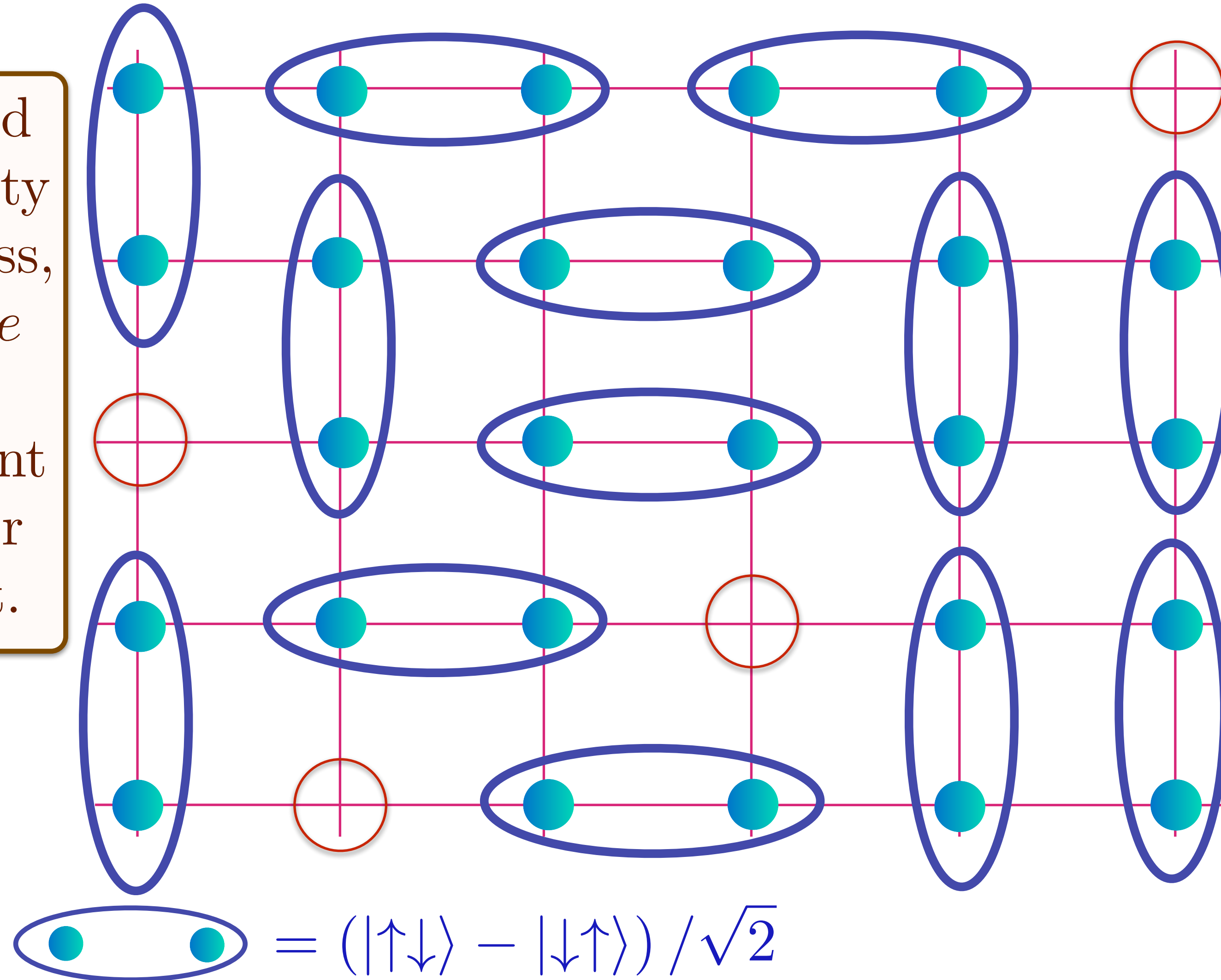
Spin liquid  
with density  
 $p$  of spinless,  
charge  $+e$   
holons.  
No coherent  
inter-layer  
transport.



# Doping an insulating antiferromagnet with holes of density $p$

## Mobile Holons

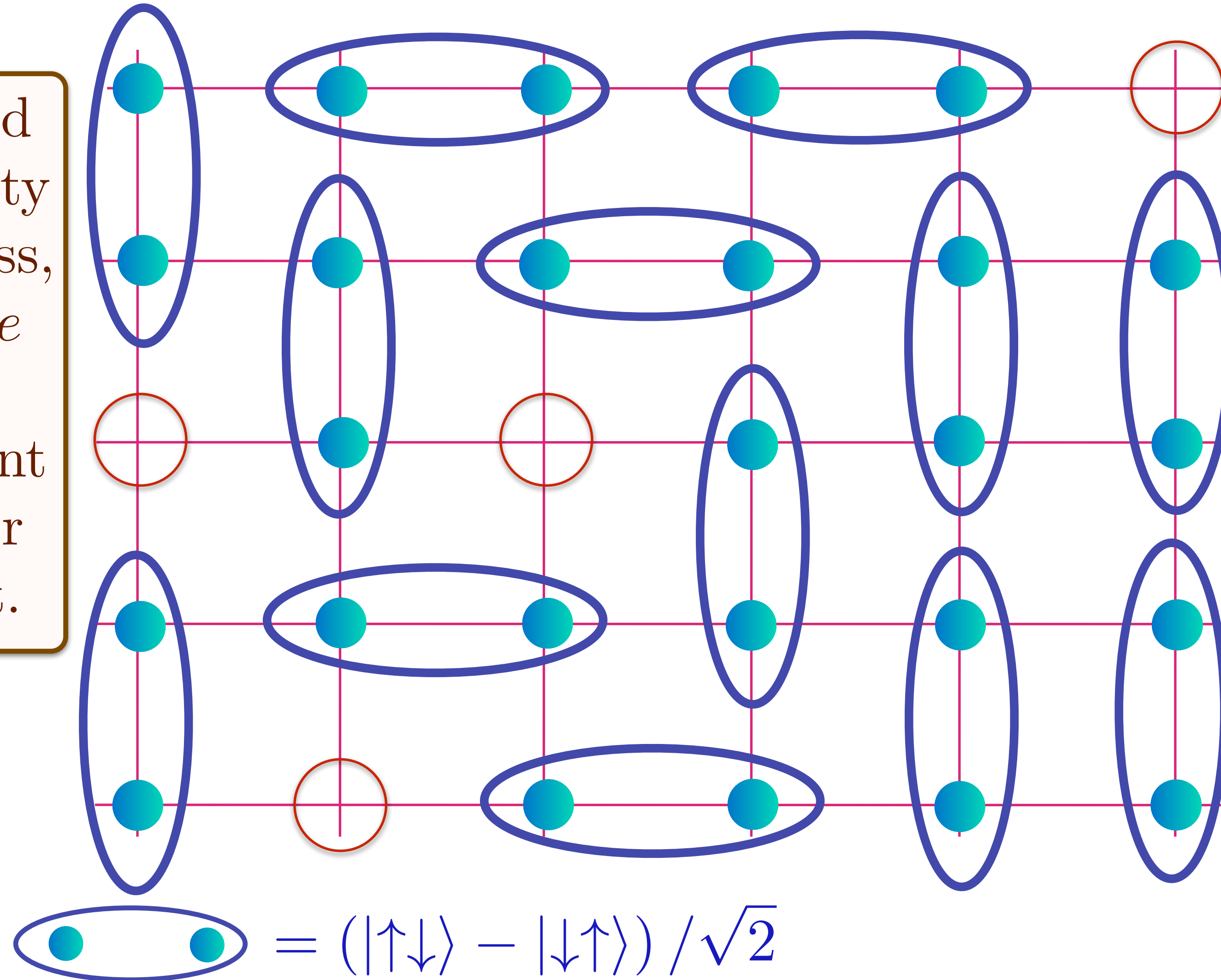
Spin liquid  
with density  
 $p$  of spinless,  
charge  $+e$   
holons.  
No coherent  
inter-layer  
transport.



# Doping an insulating antiferromagnet with holes of density $p$

## Mobile Holons

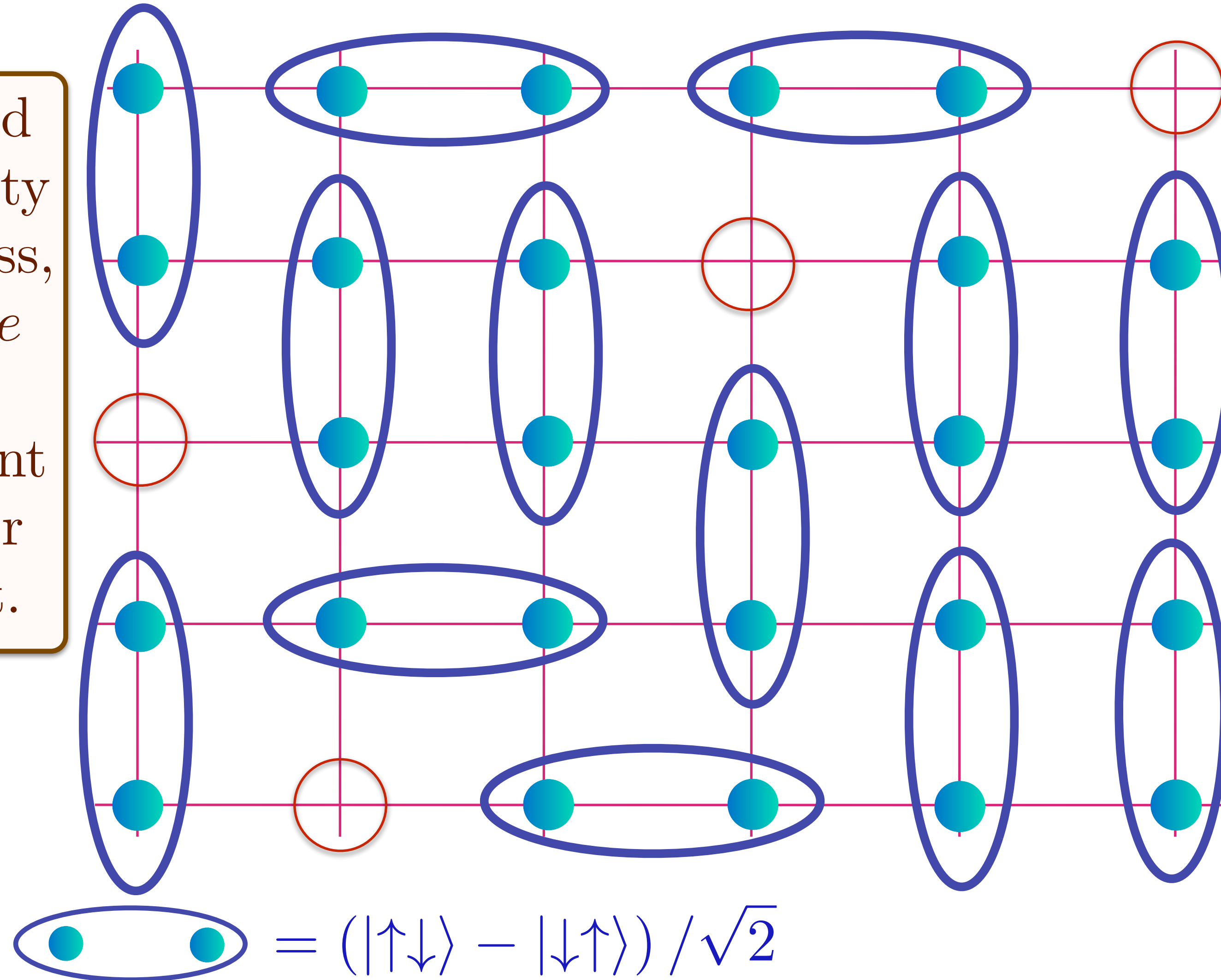
Spin liquid  
with density  
 $p$  of spinless,  
charge  $+e$   
holons.  
No coherent  
inter-layer  
transport.



# Doping an insulating antiferromagnet with holes of density $p$

## Mobile Holons

Spin liquid  
with density  
 $p$  of spinless,  
charge  $+e$   
holons.  
No coherent  
inter-layer  
transport.

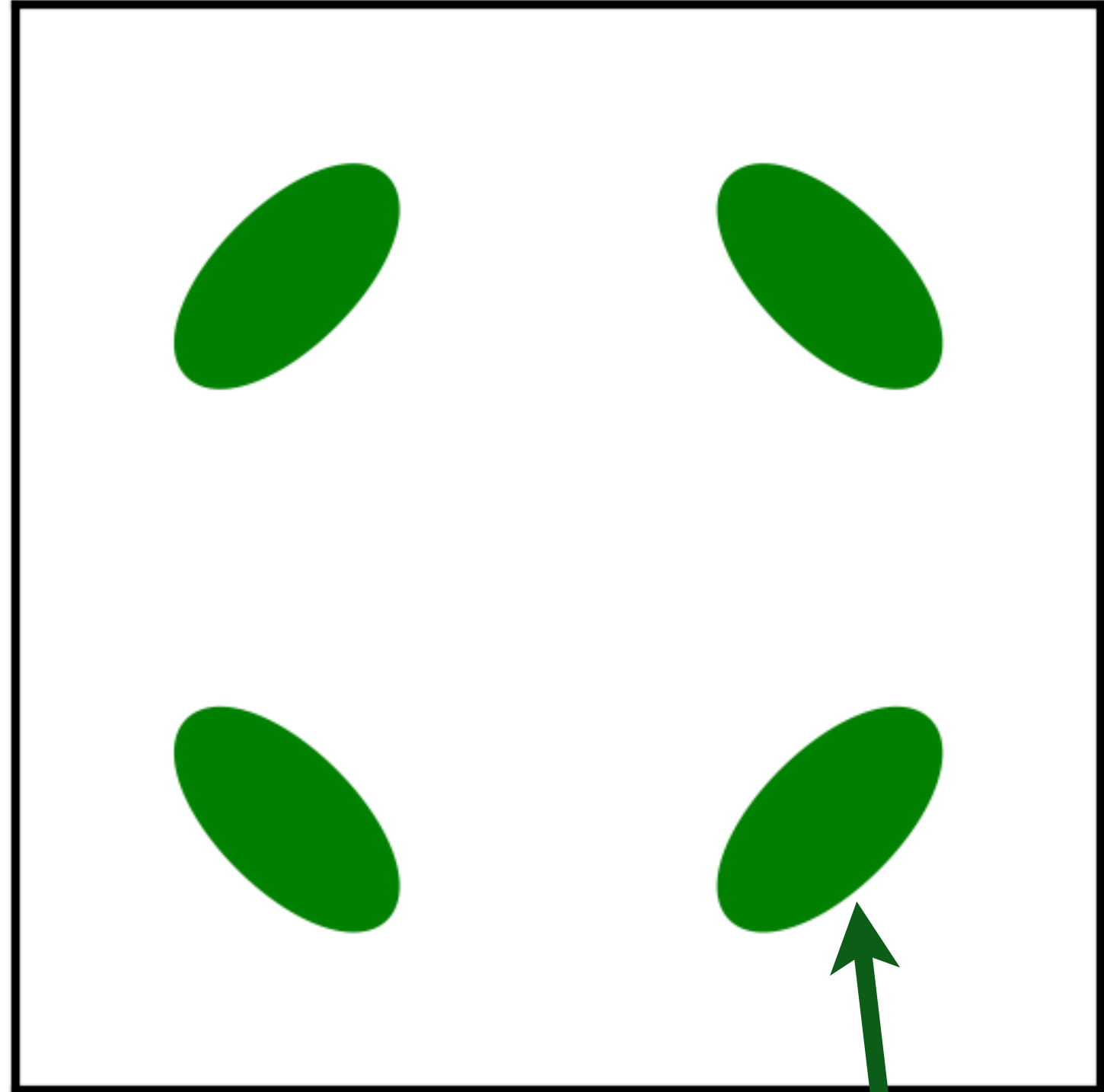
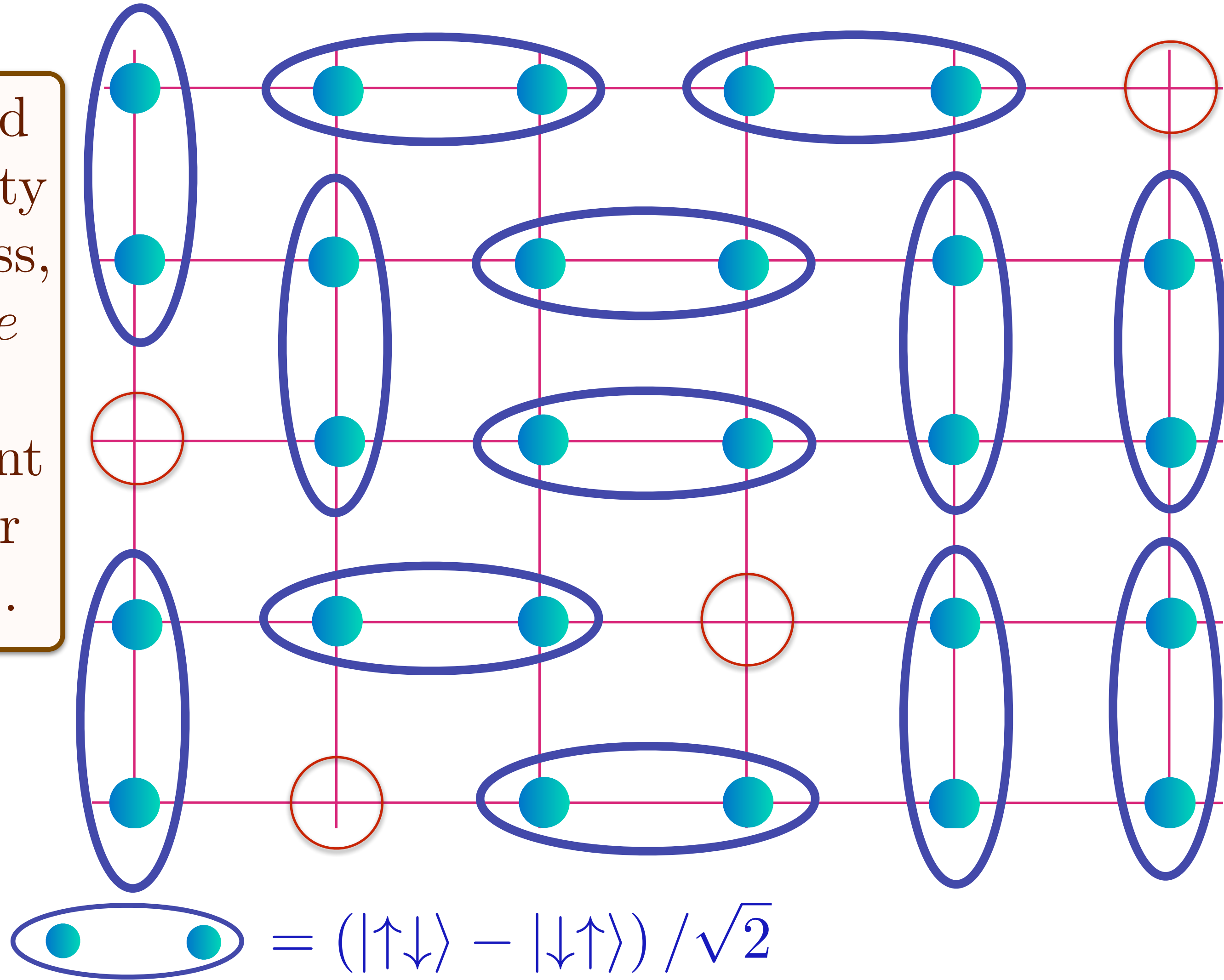


# Doping an insulating antiferromagnet with holes of density $p$

## Holon metal

Oshikawa anomaly is satisfied by sum of spin liquid (1) and Fermi surface anomalies ( $p$ )

Spin liquid with density  $p$  of spinless, charge  $+e$  holons.  
No coherent inter-layer transport.

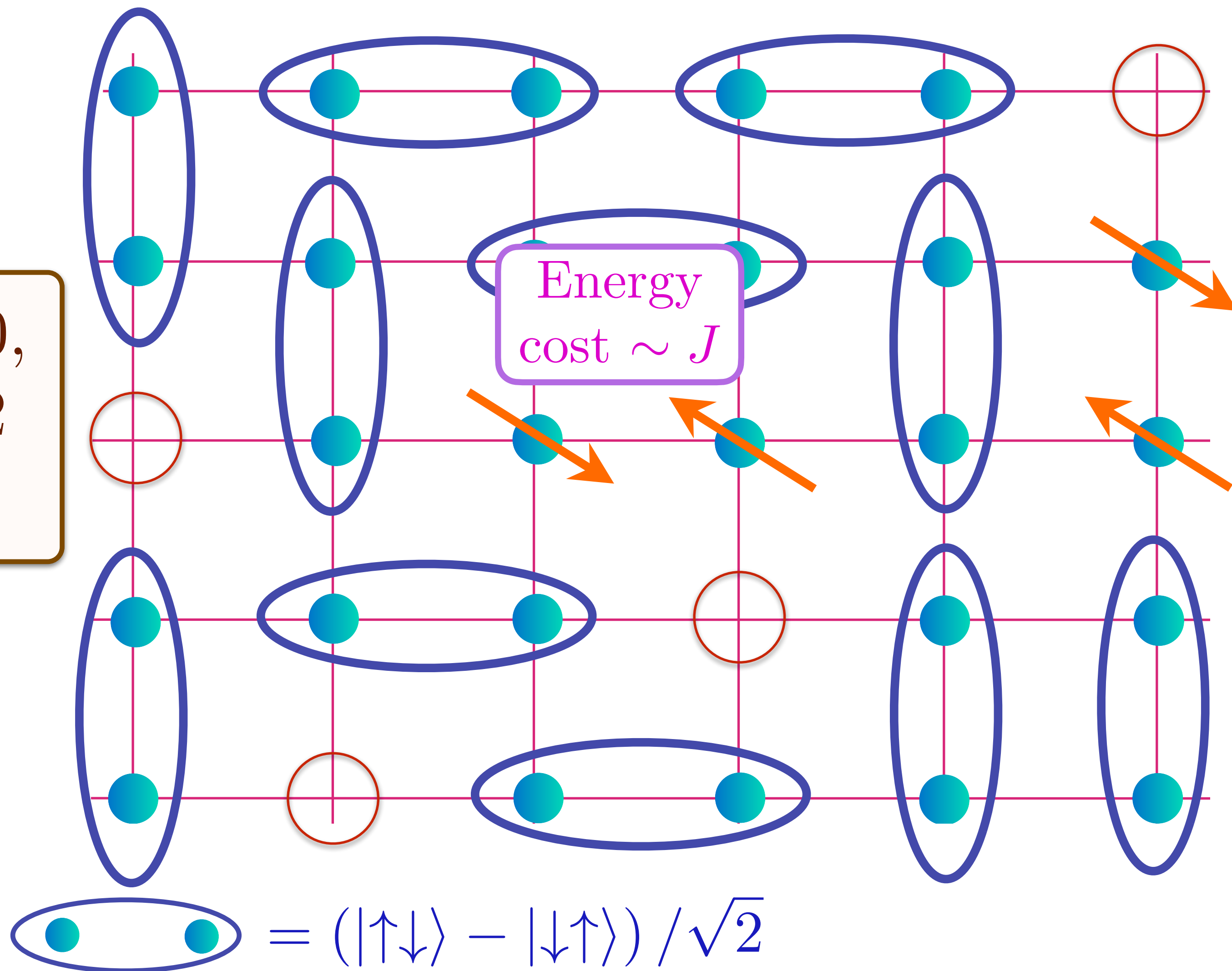


Area  $p/4$

Doping an insulating antiferromagnet with holes of density  $p$

## Excited states

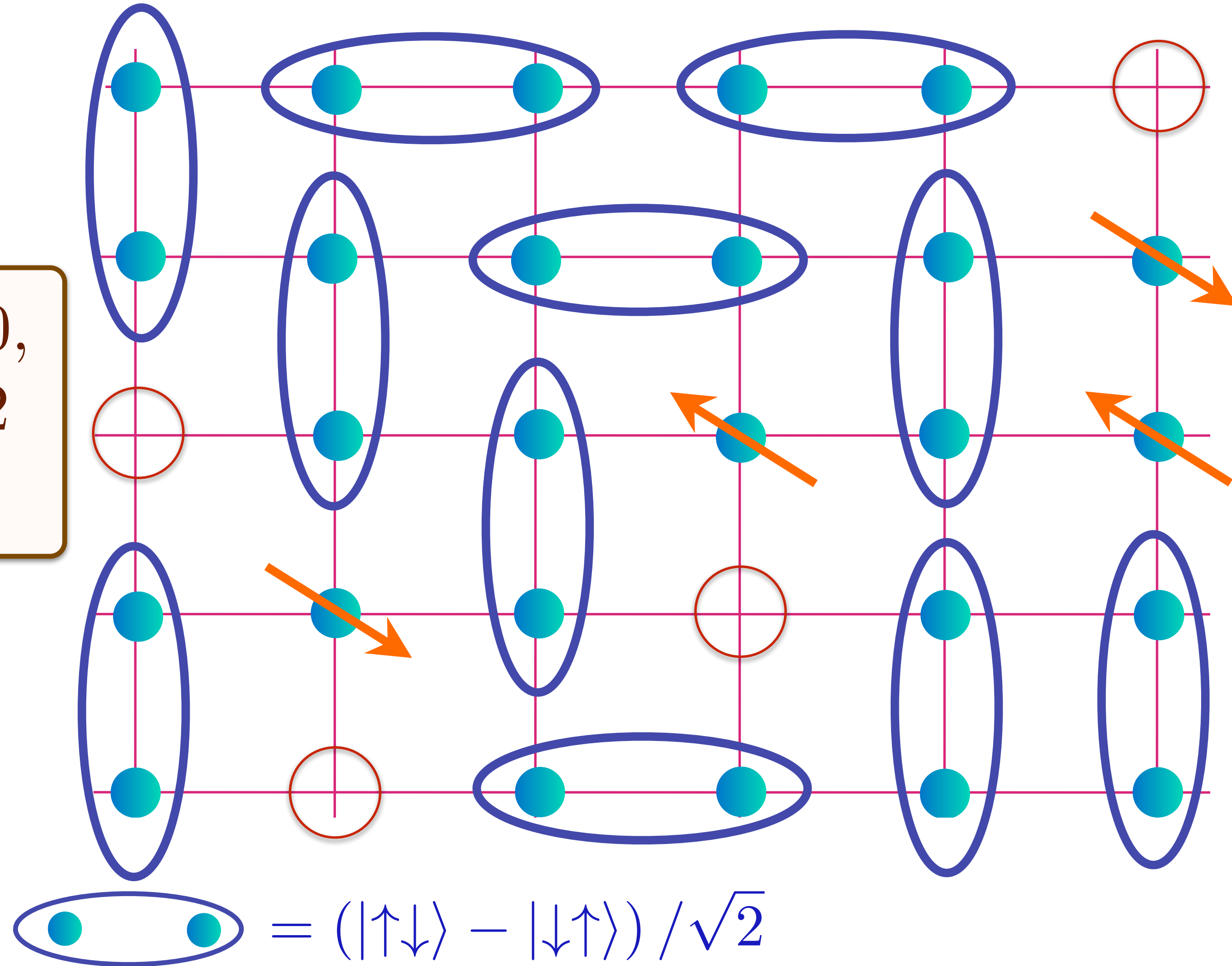
Charge 0,  
spin-1/2  
spinons



Doping an insulating antiferromagnet with holes of density  $p$

## Excited states

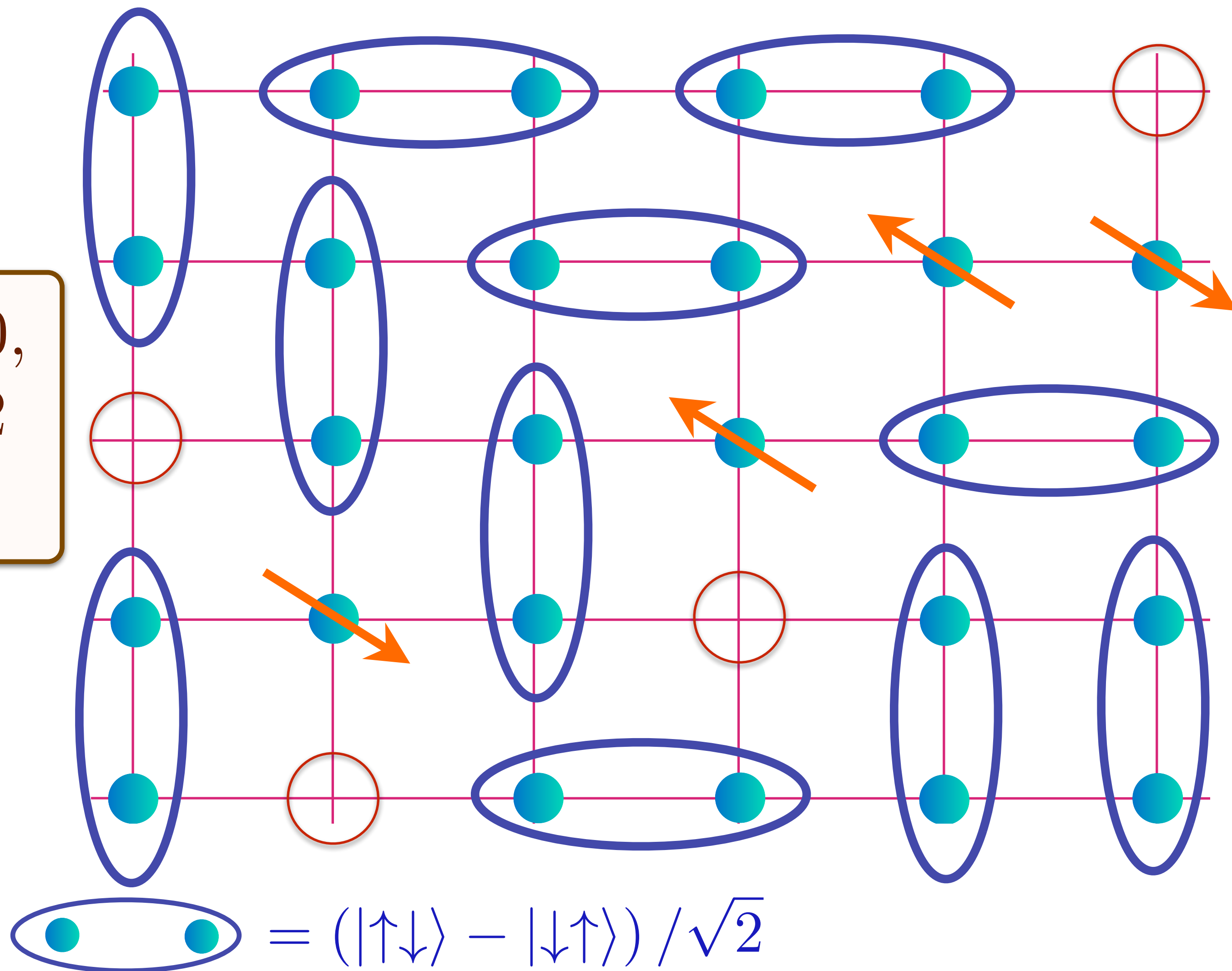
Charge 0,  
spin-1/2  
spinons



Doping an insulating antiferromagnet with holes of density  $p$

## Excited states

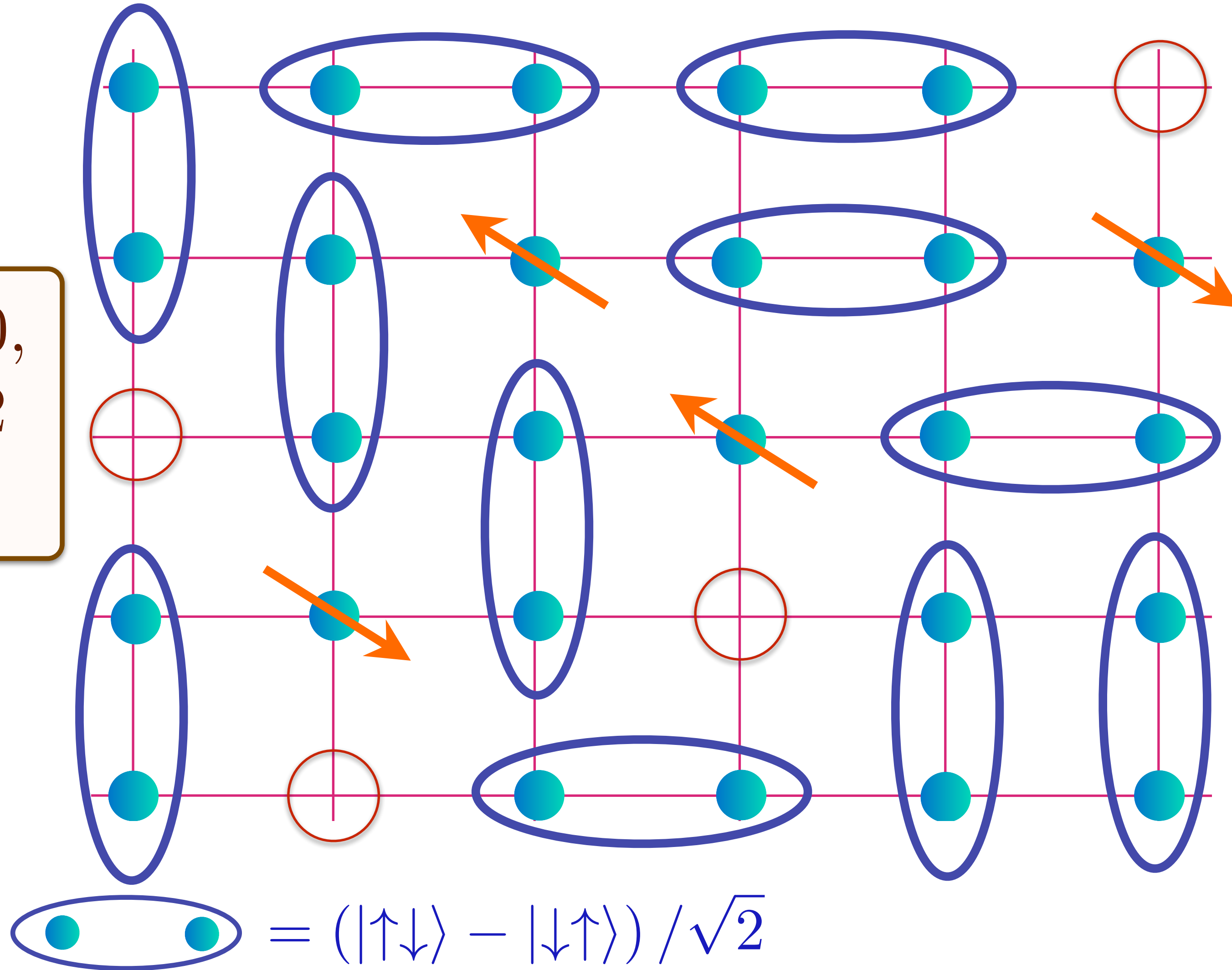
Charge 0,  
spin-1/2  
spinons



Doping an insulating antiferromagnet with holes of density  $p$

## Excited states

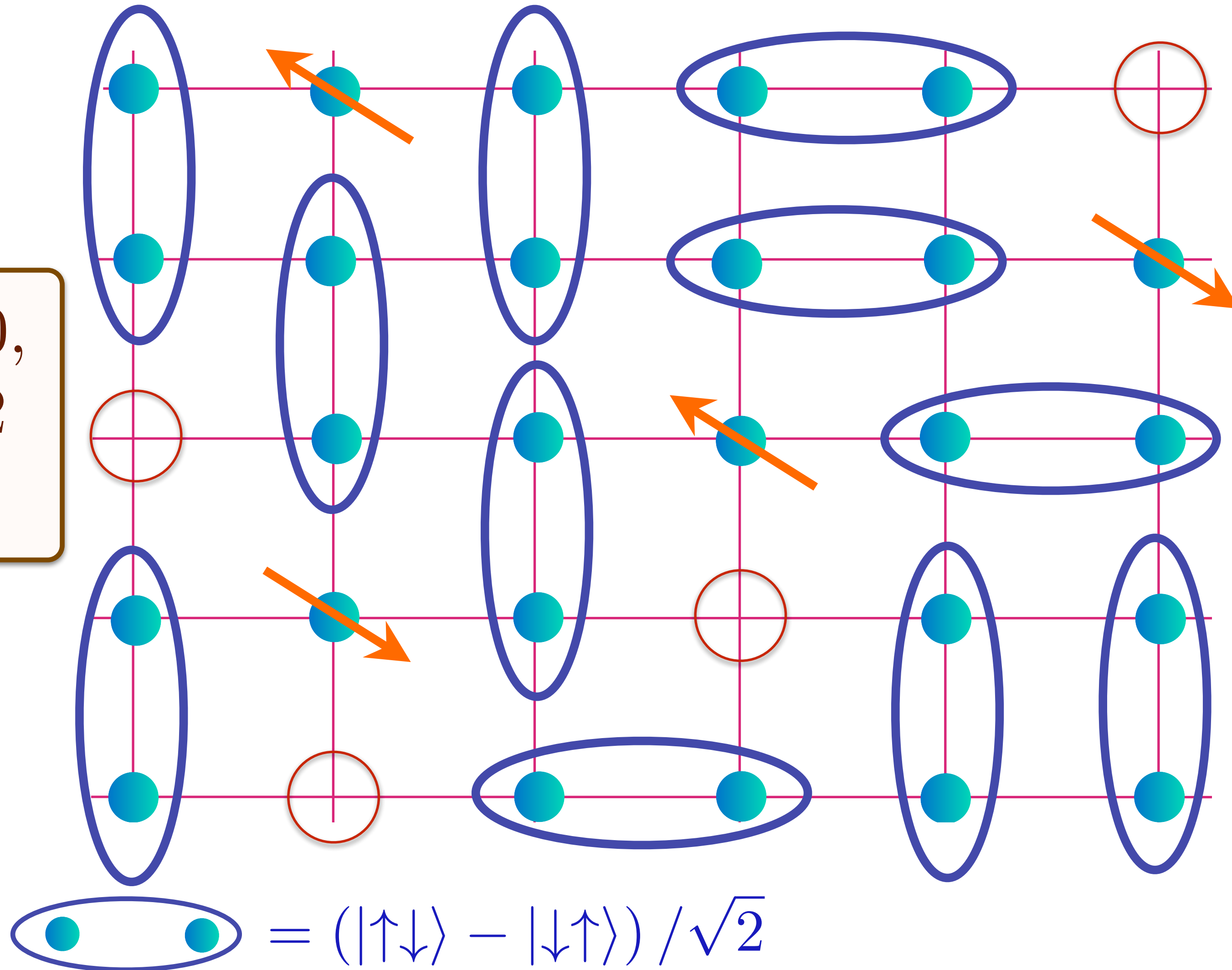
Charge 0,  
spin-1/2  
spinons



Doping an insulating antiferromagnet with holes of density  $p$

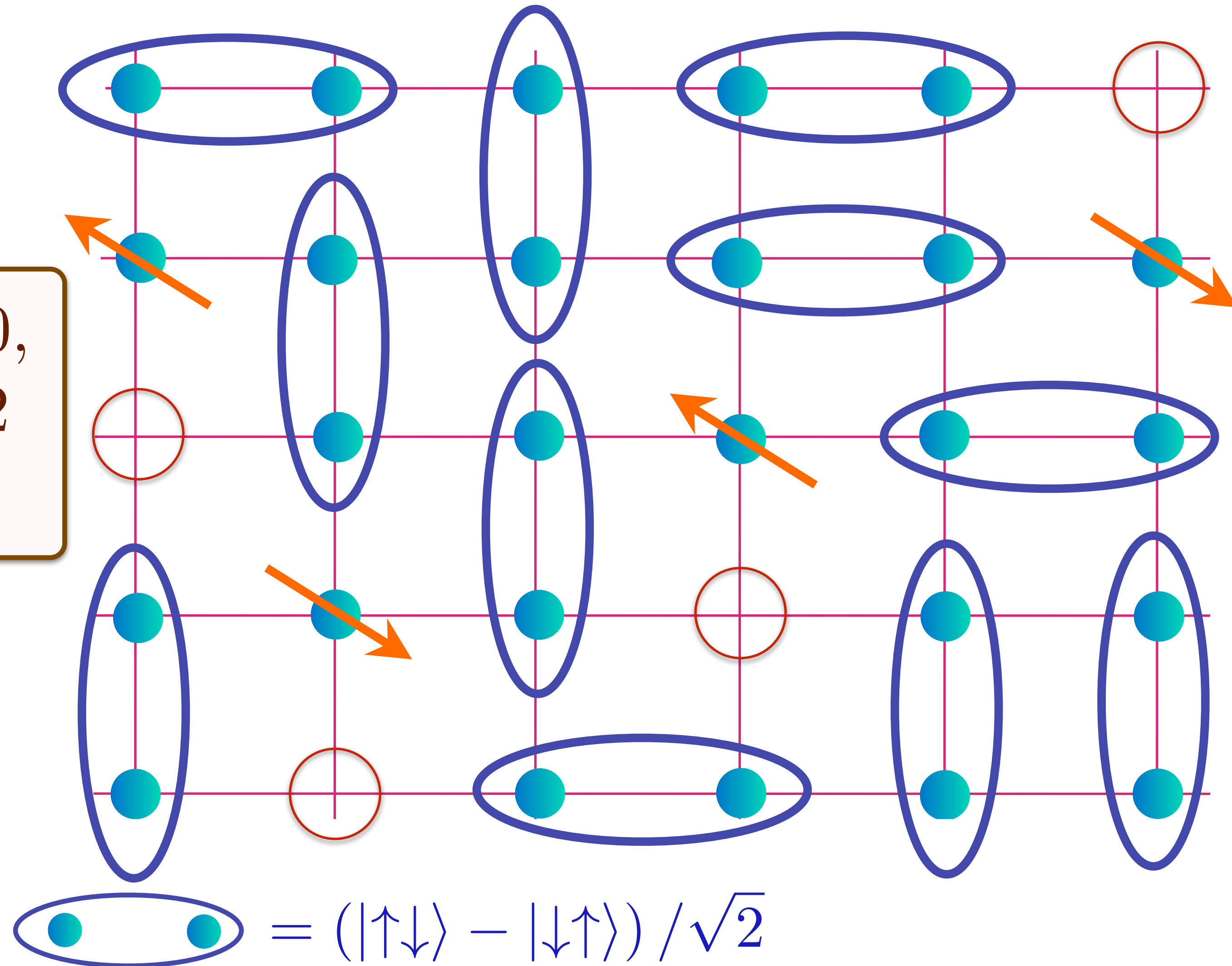
## Excited states

Charge 0,  
spin-1/2  
spinons



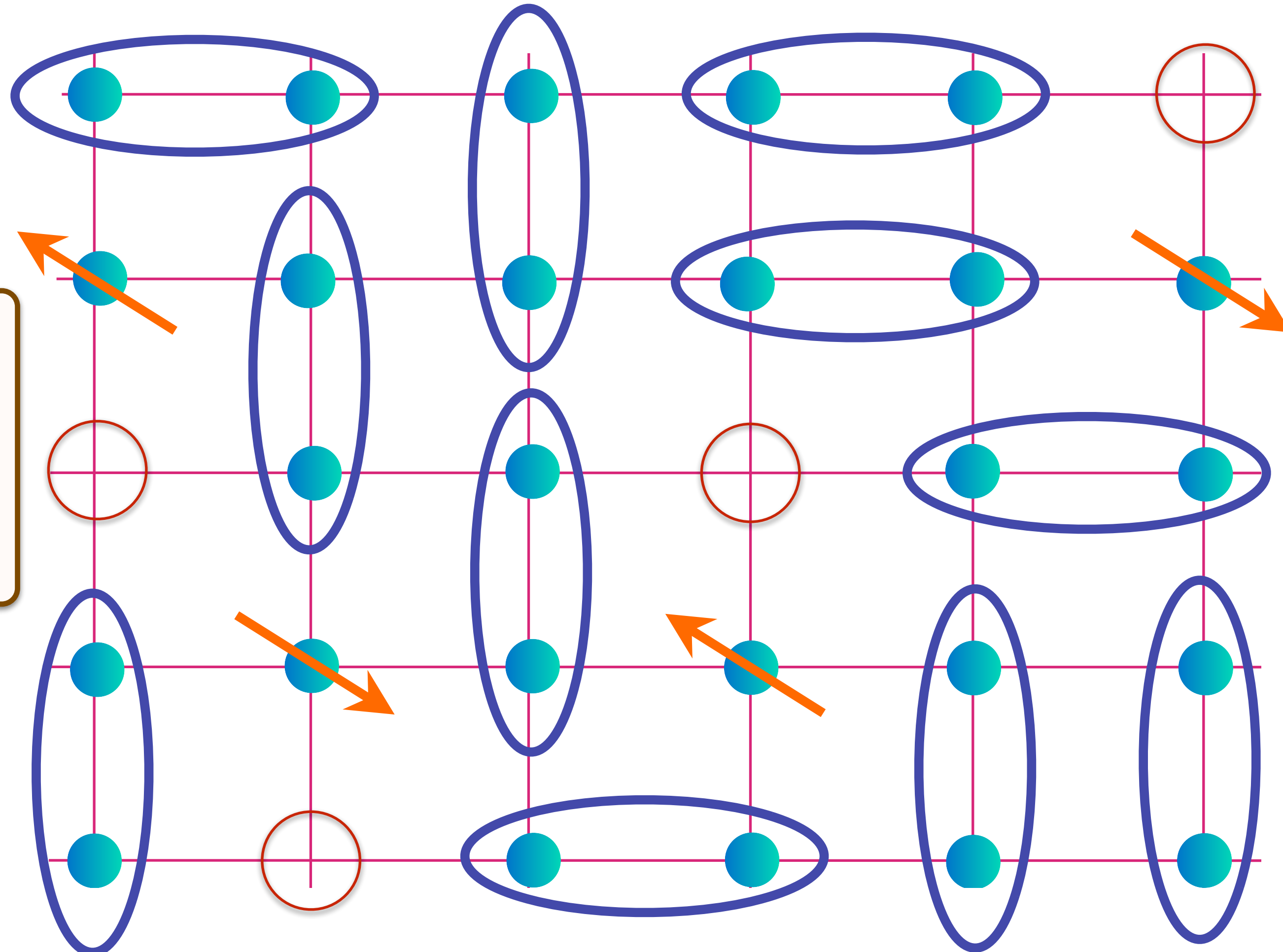
Doping an insulating antiferromagnet with holes of density  $p$

## Excited states



Doping an insulating antiferromagnet with holes of density  $p$

## Excited states

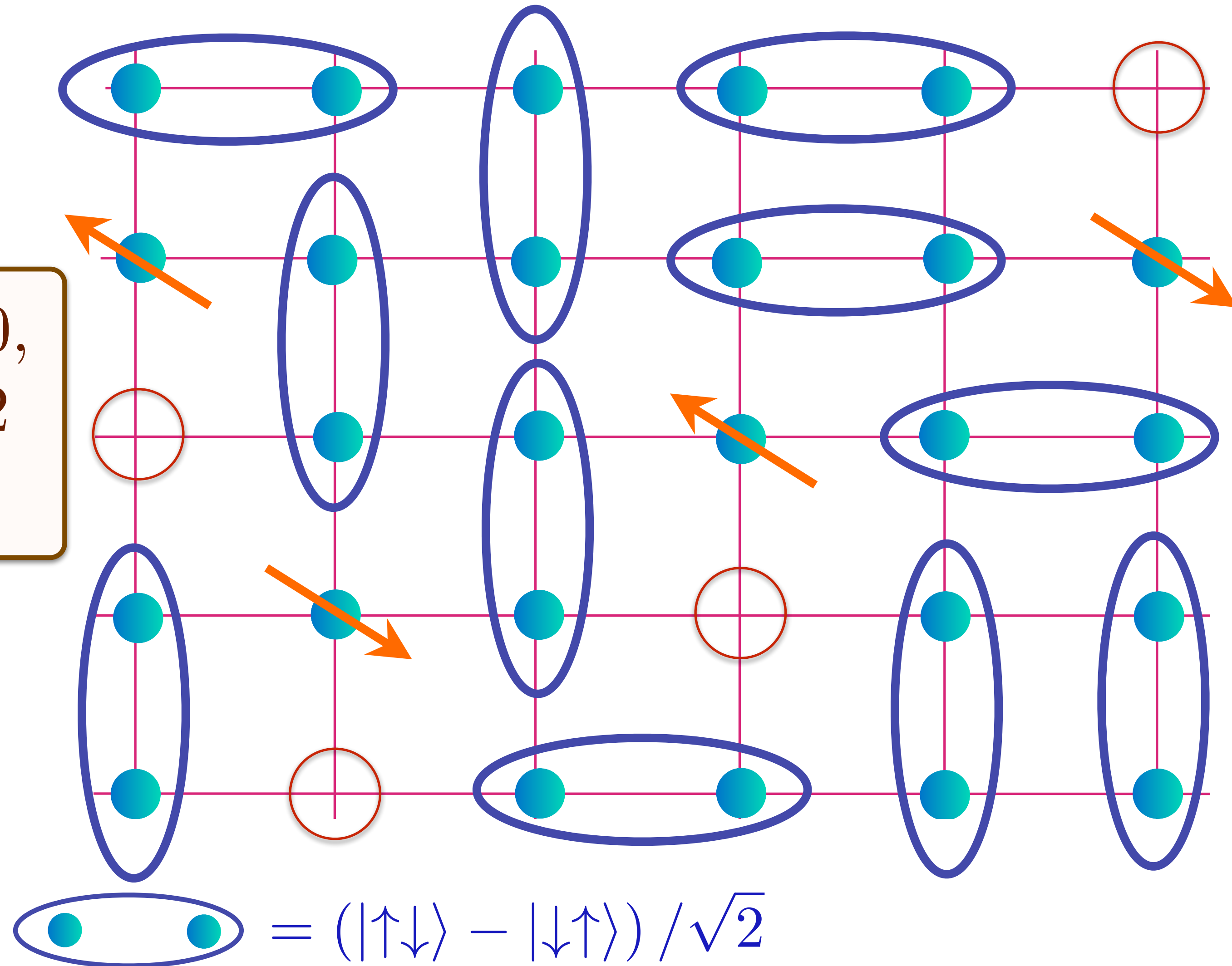


Charge 0,  
spin-1/2  
spinons

$$\text{[Diagram of two teal circles in a blue oval]} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2}$$

Doping an insulating antiferromagnet with holes of density  $p$

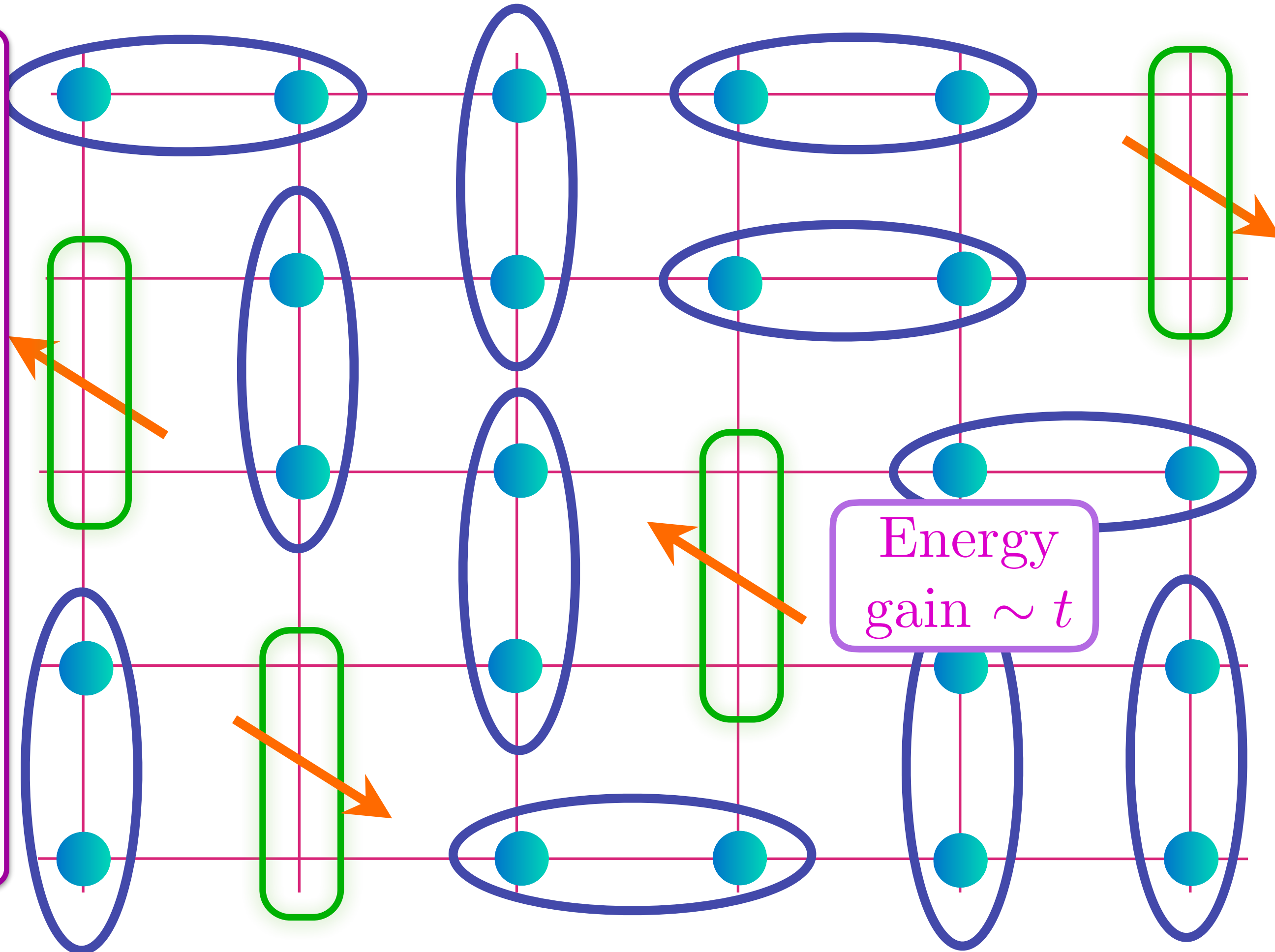
## Excited states



# Doping an insulating antiferromagnet with holes of density $p$

FL\*

Metal with density  $p$  of spin-1/2, charge  $+e$  'holes' (or 'magnetic polarons') with coherent inter-layer transport.



$$\text{Blue oval} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2} \quad \text{Green oval} = (|\uparrow\circ\rangle + |\circ\uparrow\rangle) / \sqrt{2}$$

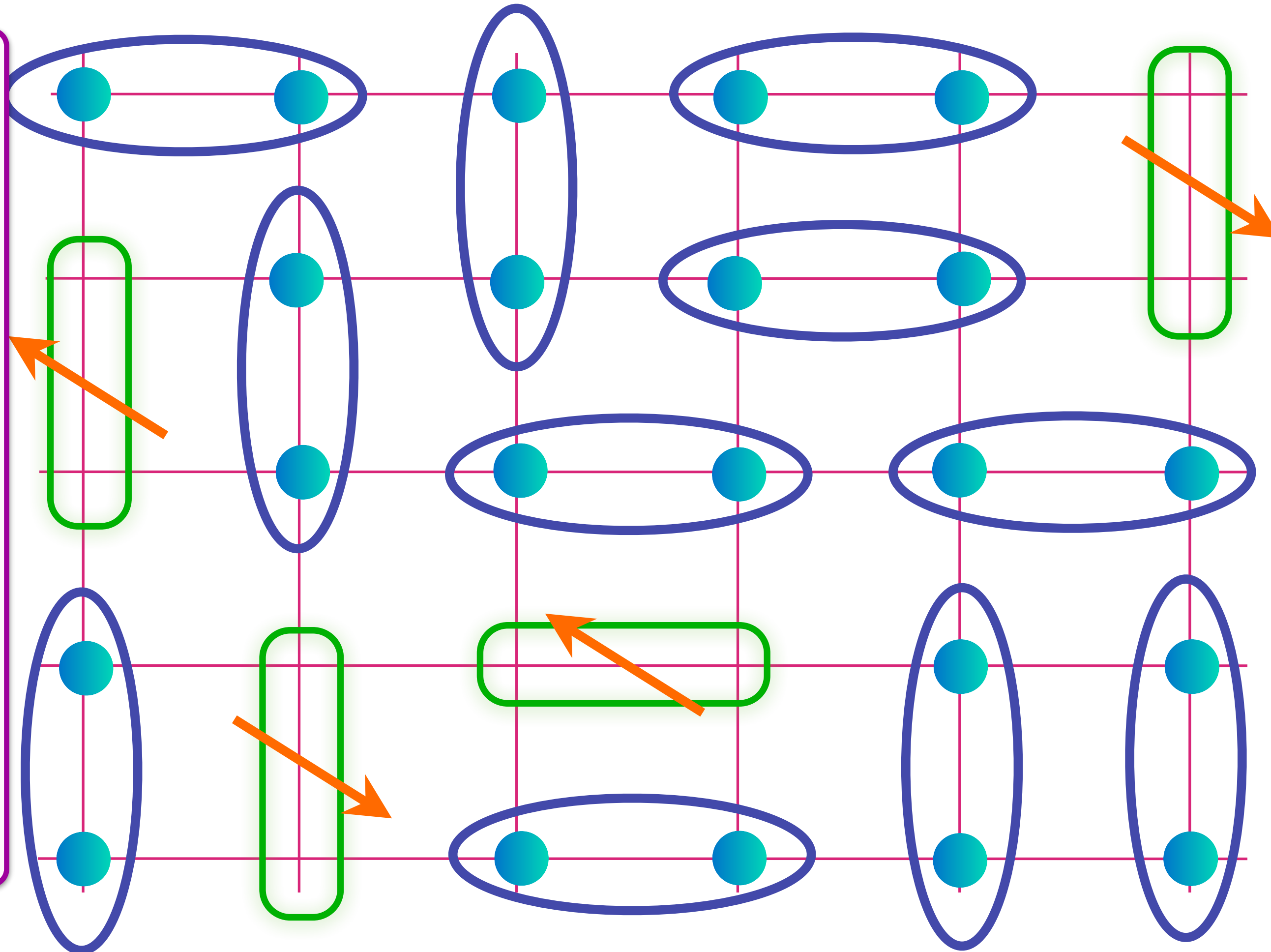
T. Senthil, S. S., M. Vojta, PRL **90**, 216403 (2003); R. K. Kaul, A. Kolezhuk, M. Levin, S.S., T. Senthil, PRB **75**, 235122 (2007)

M. Punk, A. Allais, and S. Sachdev, PNAS **112**, 9552 (2015)

# Doping an insulating antiferromagnet with holes of density $p$

FL\*

Metal with density  $p$  of spin-1/2, charge  $+e$  'holes' (or 'magnetic polarons') with coherent inter-layer transport.



$$\begin{array}{|c|c|} \hline \bullet & \bullet \\ \hline \end{array} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2} \quad \begin{array}{|c|} \hline \bullet \\ \hline \end{array} = (|\uparrow\circ\rangle + |\circ\uparrow\rangle) / \sqrt{2}$$

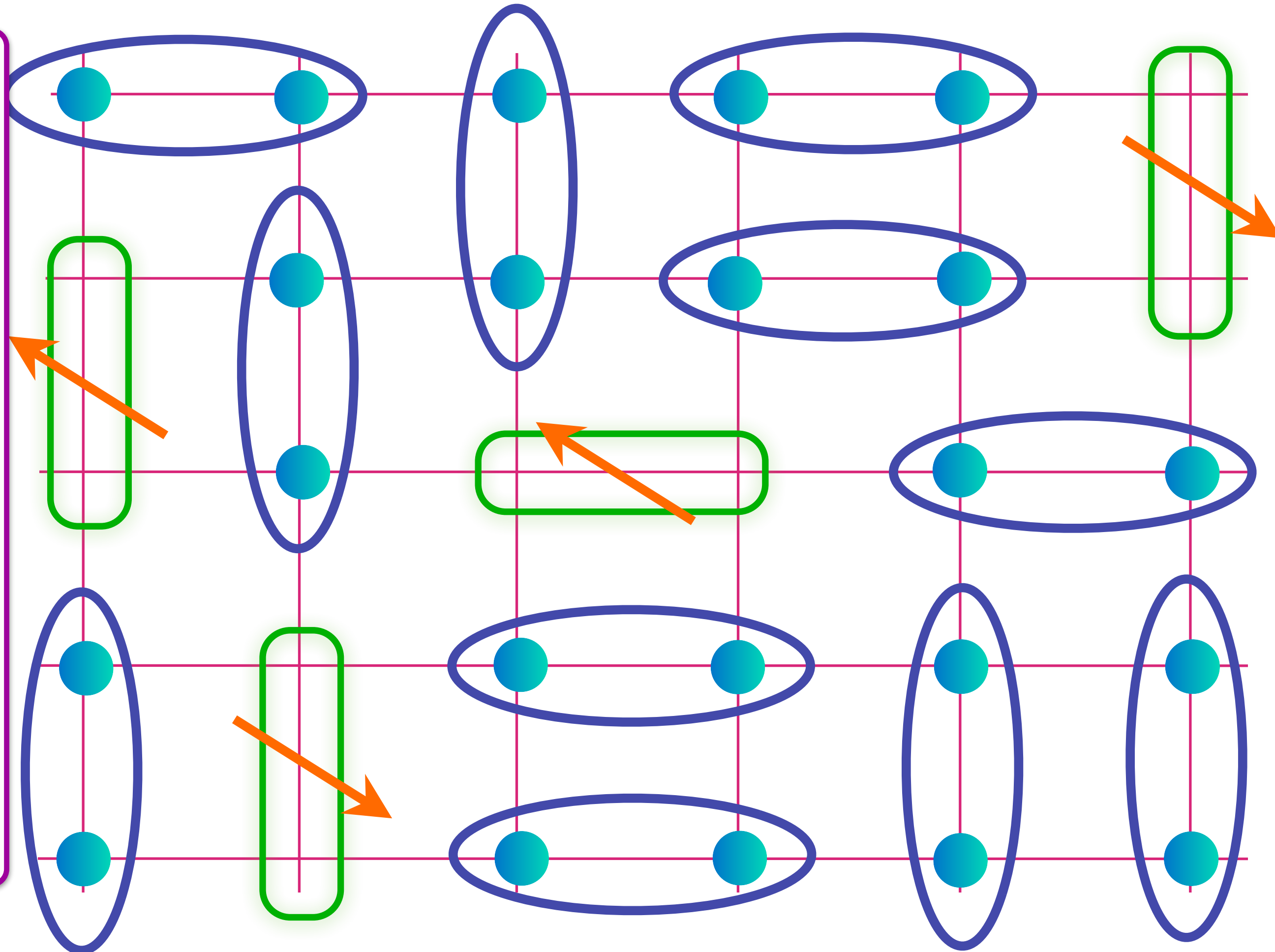
T. Senthil, S. S., M. Vojta, PRL **90**, 216403 (2003); R. K. Kaul, A. Kolezhuk, M. Levin, S.S., T. Senthil, PRB **75**, 235122 (2007)

M. Punk, A. Allais, and S. Sachdev, PNAS **112**, 9552 (2015)

# Doping an insulating antiferromagnet with holes of density $p$

FL\*

Metal with density  $p$  of spin-1/2, charge  $+e$  'holes' (or 'magnetic polarons') with coherent inter-layer transport.



$$\text{Blue oval} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2} \quad \text{Green oval with arrow} = (|\uparrow\circ\rangle + |\circ\uparrow\rangle) / \sqrt{2}$$

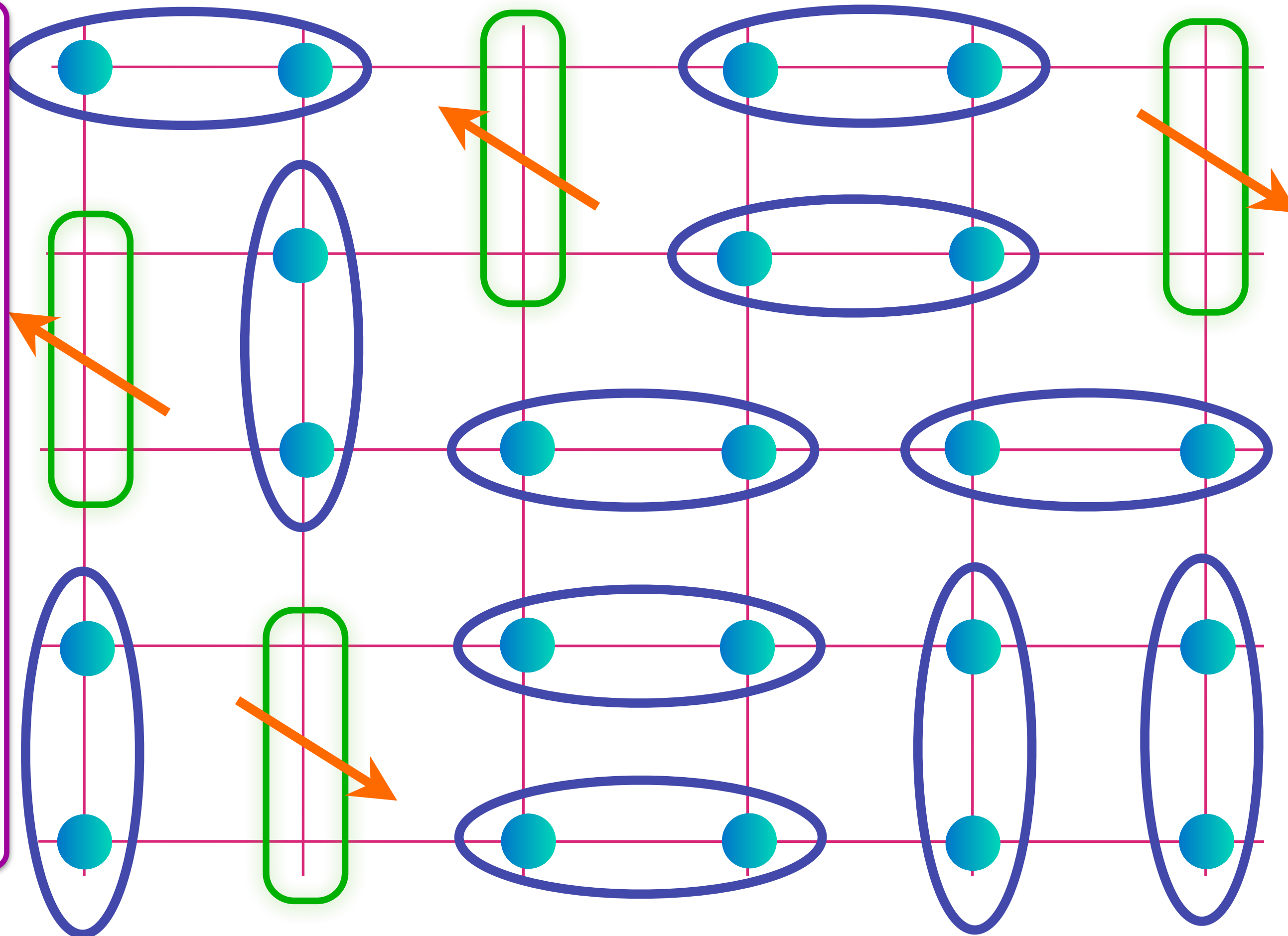
T. Senthil, S. S., M. Vojta, PRL **90**, 216403 (2003); R. K. Kaul, A. Kolezhuk, M. Levin, S.S., T. Senthil, PRB **75**, 235122 (2007)

M. Punk, A. Allais, and S. Sachdev, PNAS **112**, 9552 (2015)

# Doping an insulating antiferromagnet with holes of density $p$

FL\*

Metal with density  $p$  of spin-1/2, charge  $+e$  'holes' (or 'magnetic polarons') with coherent inter-layer transport.



$$\text{Blue oval with two dots} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2} \quad \text{Green oval with arrow} = (|\uparrow\circ\rangle + |\circ\uparrow\rangle) / \sqrt{2}$$

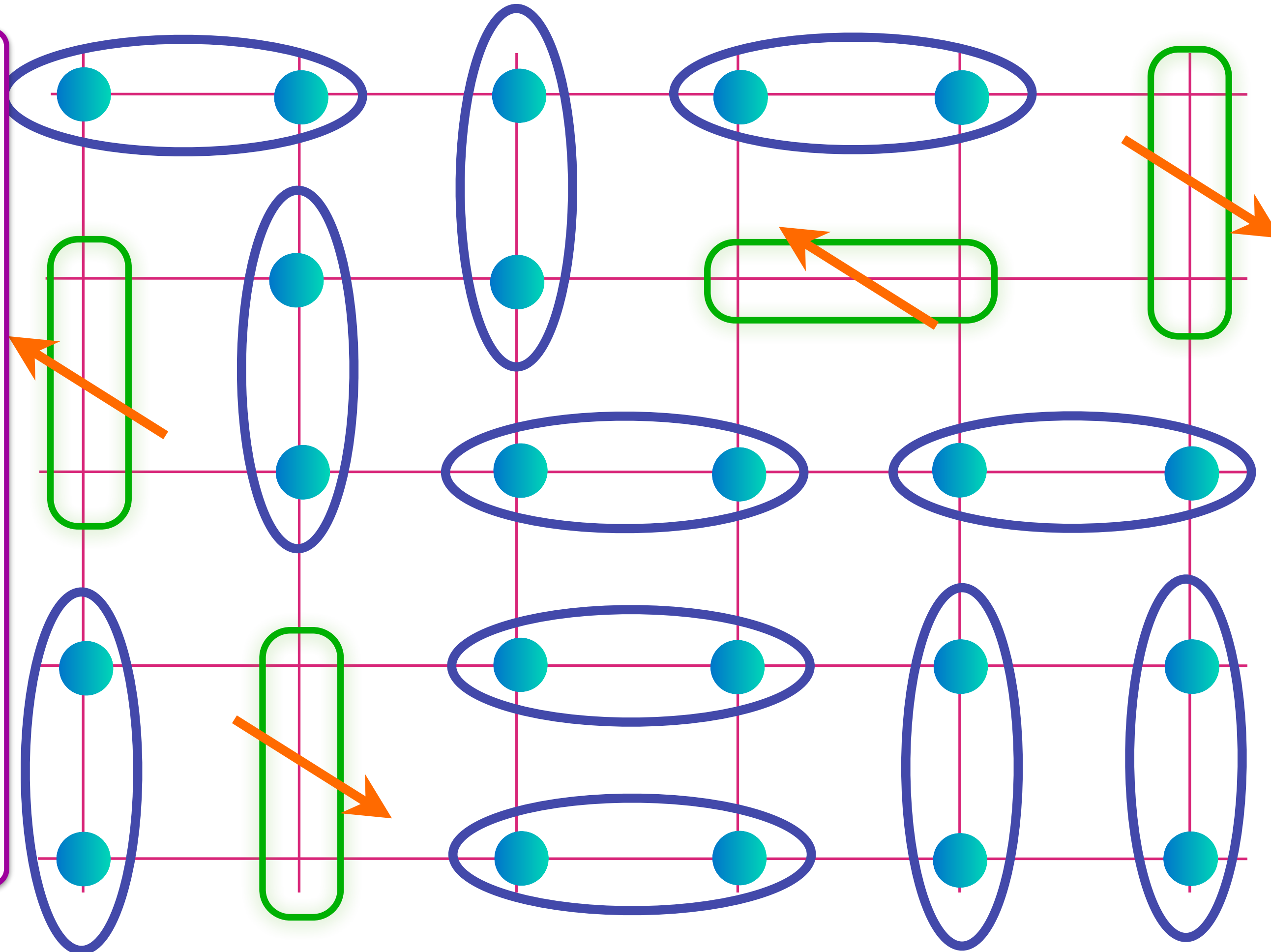
T. Senthil, S. S., M. Vojta, PRL **90**, 216403 (2003); R. K. Kaul, A. Kolezhuk, M. Levin, S.S., T. Senthil, PRB **75**, 235122 (2007)

M. Punk, A. Allais, and S. Sachdev, PNAS **112**, 9552 (2015)

# Doping an insulating antiferromagnet with holes of density $p$

FL\*

Metal with density  $p$  of spin-1/2, charge  $+e$  'holes' (or 'magnetic polarons') with coherent inter-layer transport.



$$\text{Dimer} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2} \quad \text{Hole} = (|\uparrow\circ\rangle + |\circ\uparrow\rangle) / \sqrt{2}$$

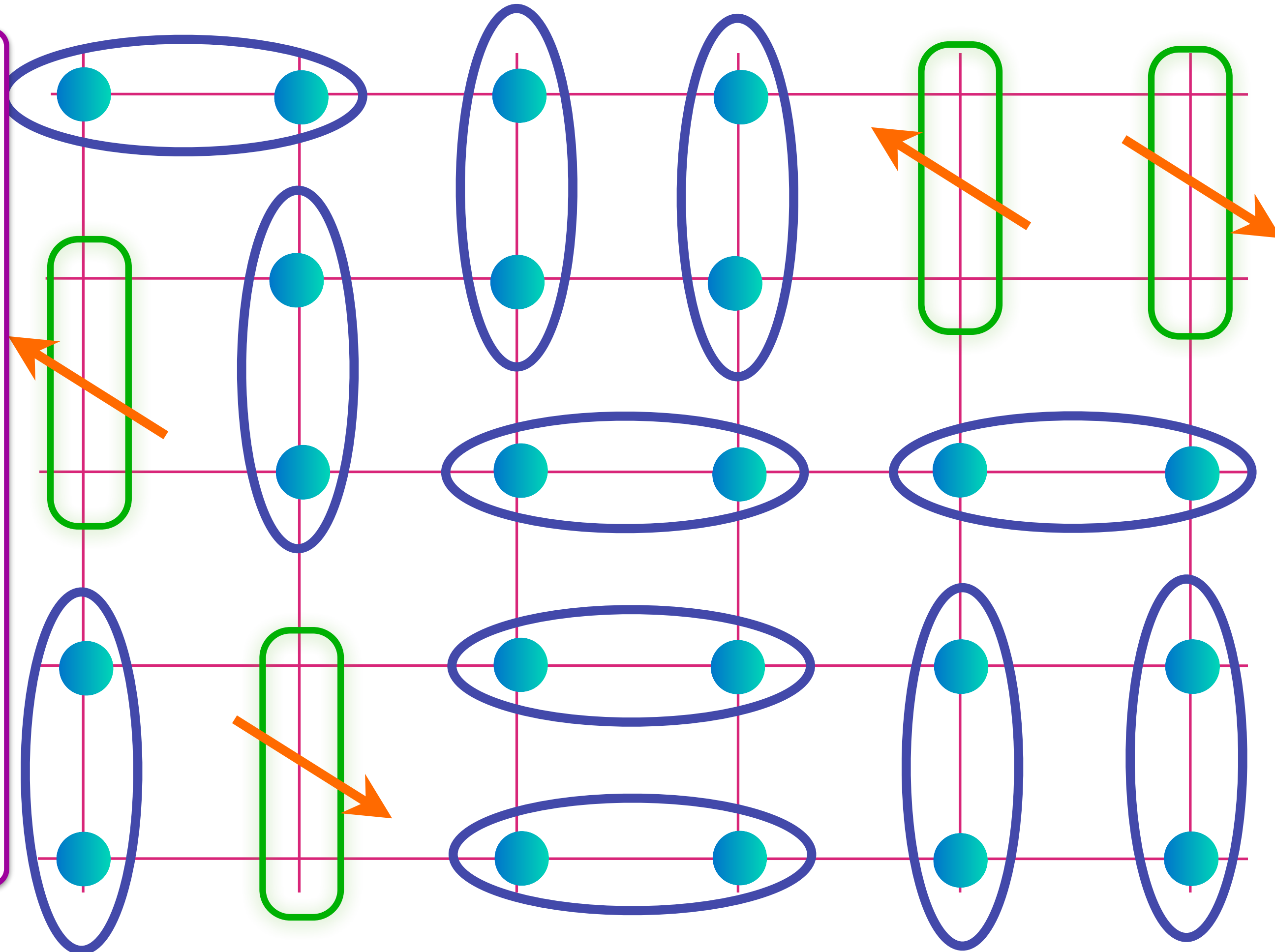
T. Senthil, S. S., M. Vojta, PRL **90**, 216403 (2003); R. K. Kaul, A. Kolezhuk, M. Levin, S.S., T. Senthil, PRB **75**, 235122 (2007)

M. Punk, A. Allais, and S. Sachdev, PNAS **112**, 9552 (2015)

# Doping an insulating antiferromagnet with holes of density $p$

FL\*

Metal with density  $p$  of spin-1/2, charge  $+e$  'holes' (or 'magnetic polarons') with coherent inter-layer transport.



$$\text{Blue oval} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2} \quad \text{Green oval} = (|\uparrow\circ\rangle + |\circ\uparrow\rangle) / \sqrt{2}$$

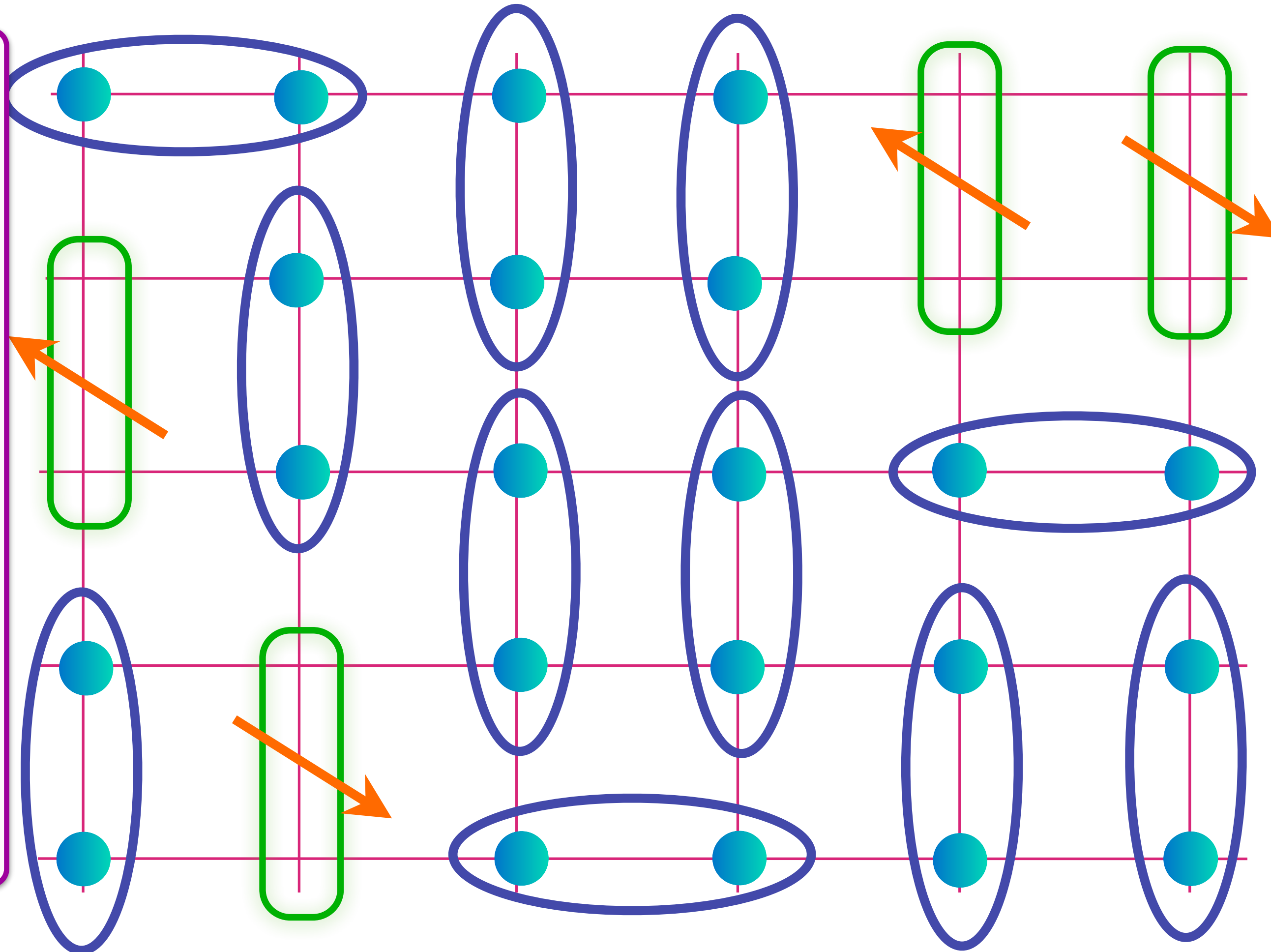
T. Senthil, S. S., M. Vojta, PRL **90**, 216403 (2003); R. K. Kaul, A. Kolezhuk, M. Levin, S.S., T. Senthil, PRB **75**, 235122 (2007)

M. Punk, A. Allais, and S. Sachdev, PNAS **112**, 9552 (2015)

# Doping an insulating antiferromagnet with holes of density $p$

FL\*

Metal with density  $p$  of spin-1/2, charge  $+e$  'holes' (or 'magnetic polarons') with coherent inter-layer transport.



$$\text{Blue oval} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2} \quad \text{Green rounded rectangle} = (|\uparrow\circ\rangle + |\circ\uparrow\rangle) / \sqrt{2}$$

T. Senthil, S. S., M. Vojta, PRL **90**, 216403 (2003); R. K. Kaul, A. Kolezhuk, M. Levin, S.S., T. Senthil, PRB **75**, 235122 (2007)

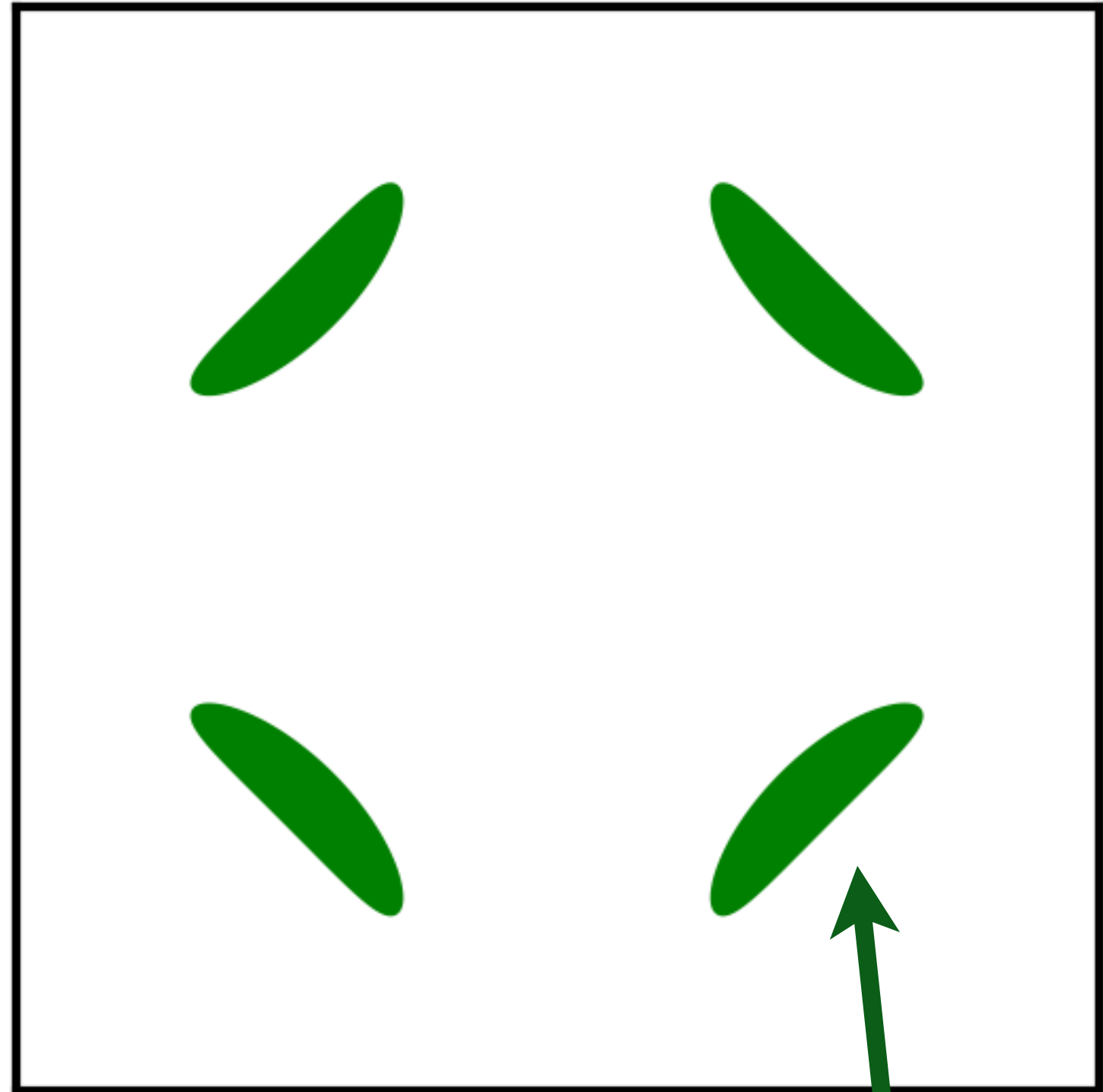
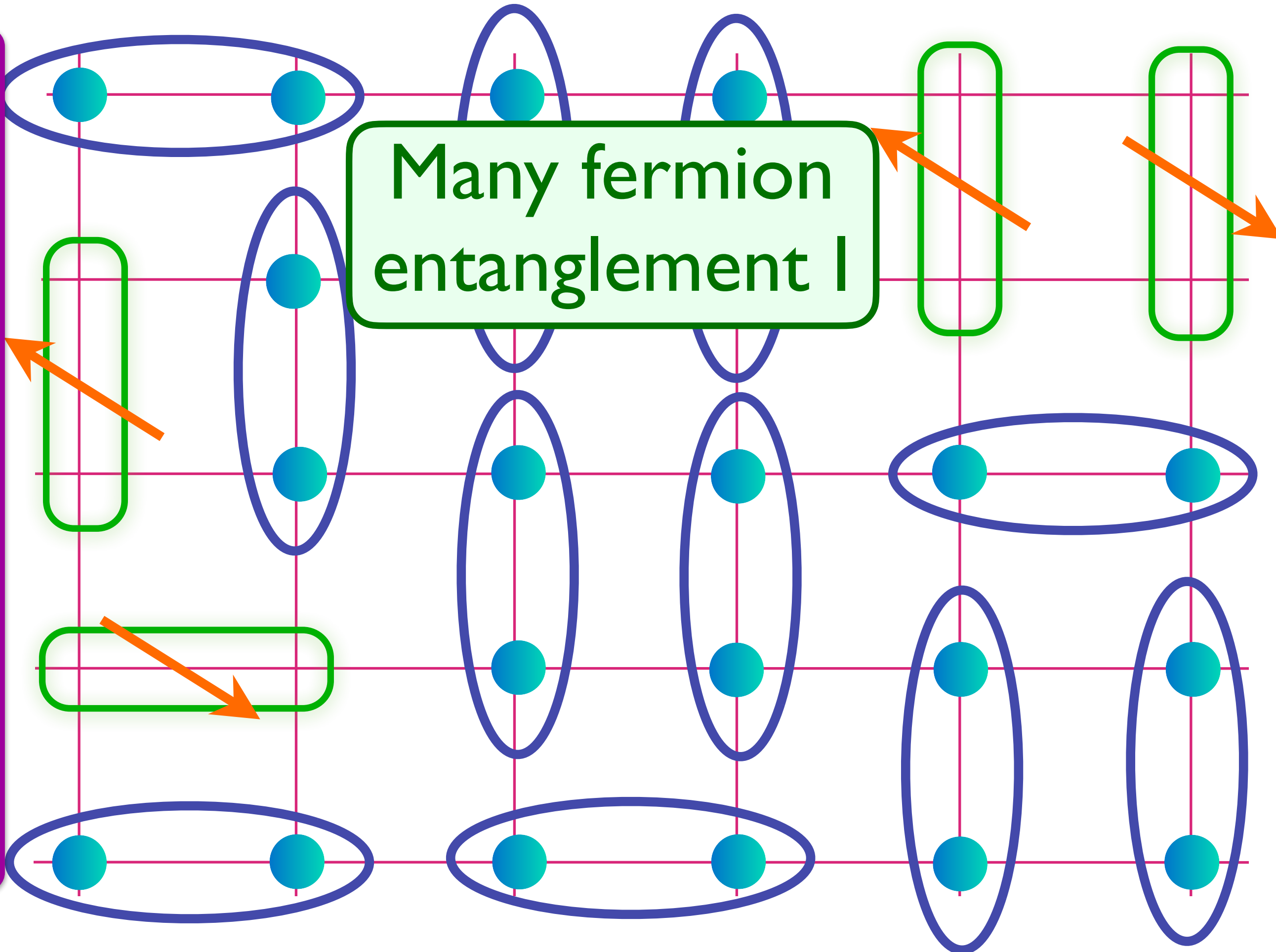
M. Punk, A. Allais, and S. Sachdev, PNAS **112**, 9552 (2015)

# Doping an insulating antiferromagnet with holes of density $p$

FL\*

Oshikawa anomaly is satisfied by sum of spin liquid (1) and Fermi surface anomalies ( $p$ )

Metal with density  $p$  of spin-1/2, charge  $+e$  'holes' (or 'magnetic polarons') with coherent inter-layer transport.



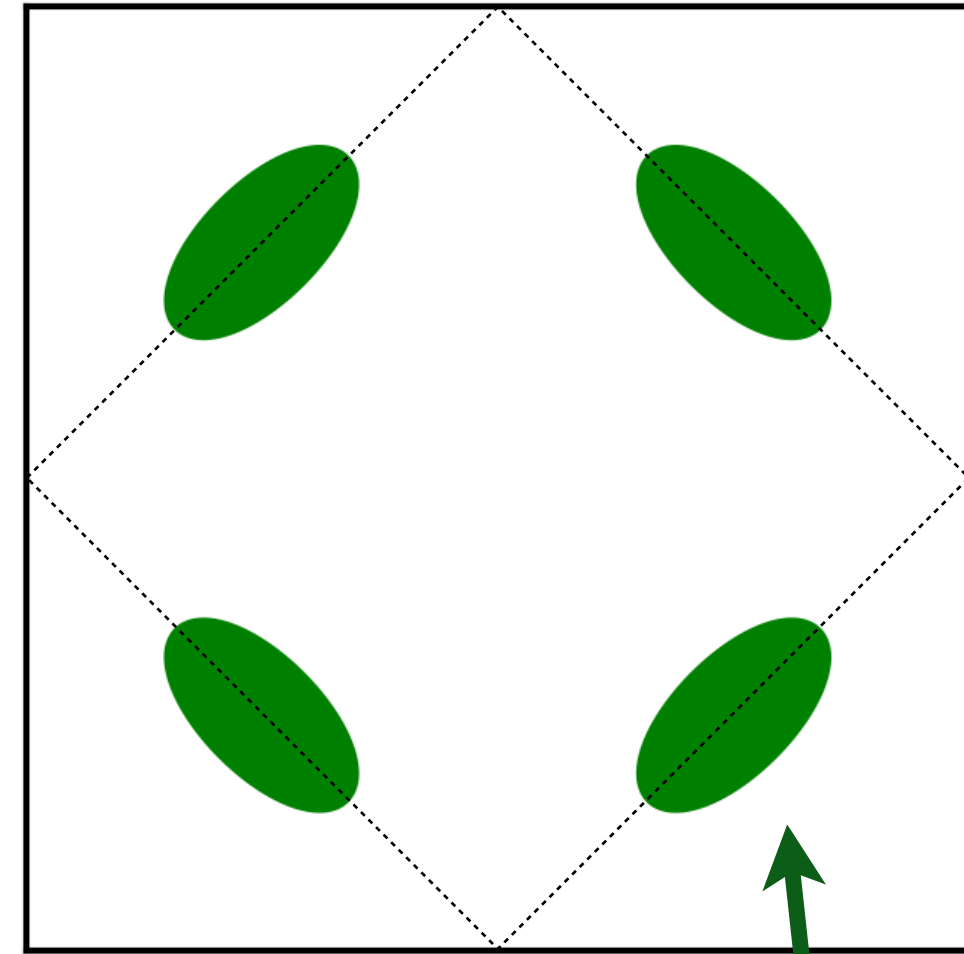
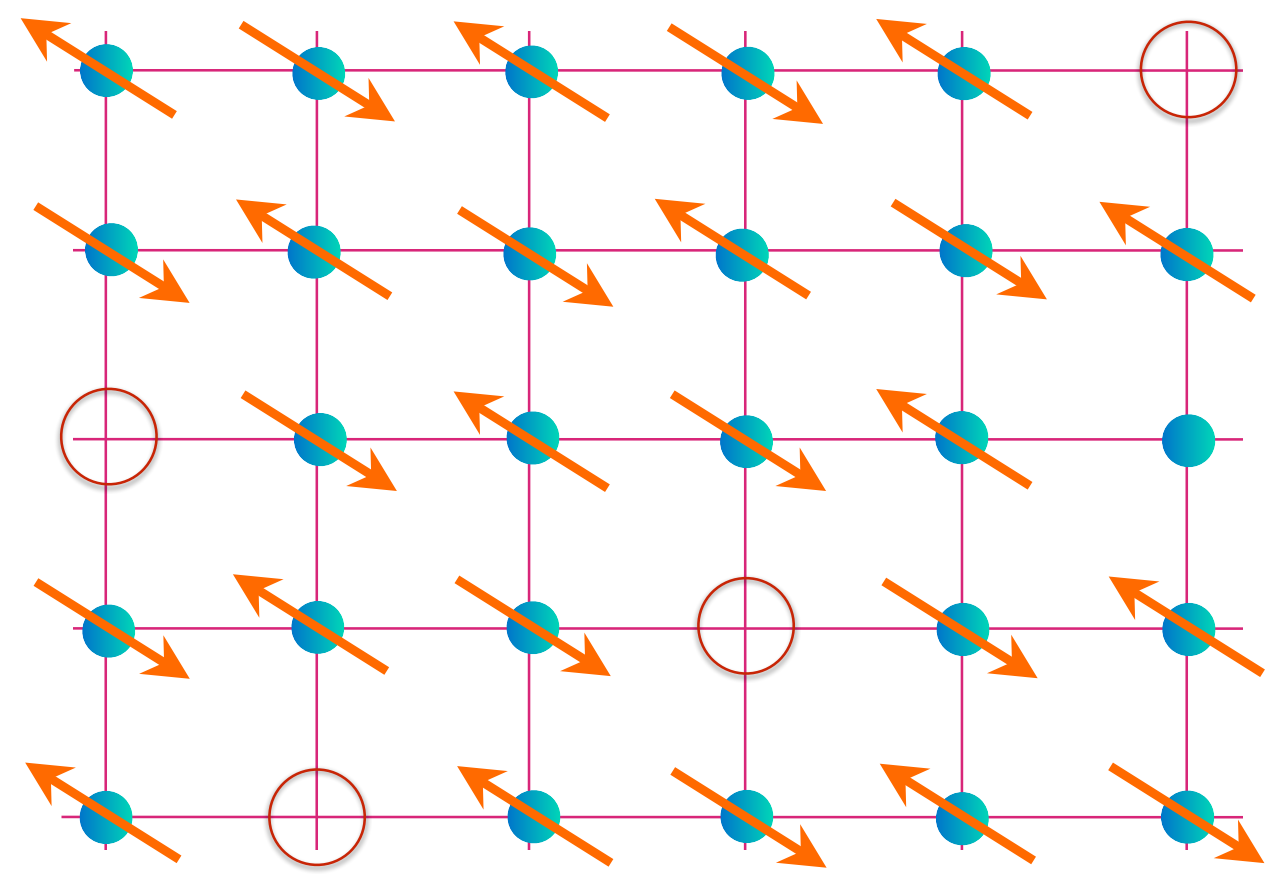
$$\text{Blue oval} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2} \quad \text{Green rectangle} = (|\uparrow\circ\rangle + |\circ\uparrow\rangle) / \sqrt{2}$$

Area  $p/8$

T. Senthil, S. S., M. Vojta, PRL **90**, 216403 (2003); R. K. Kaul, A. Kolezhuk, M. Levin, S.S., T. Senthil, PRB **75**, 235122 (2007)

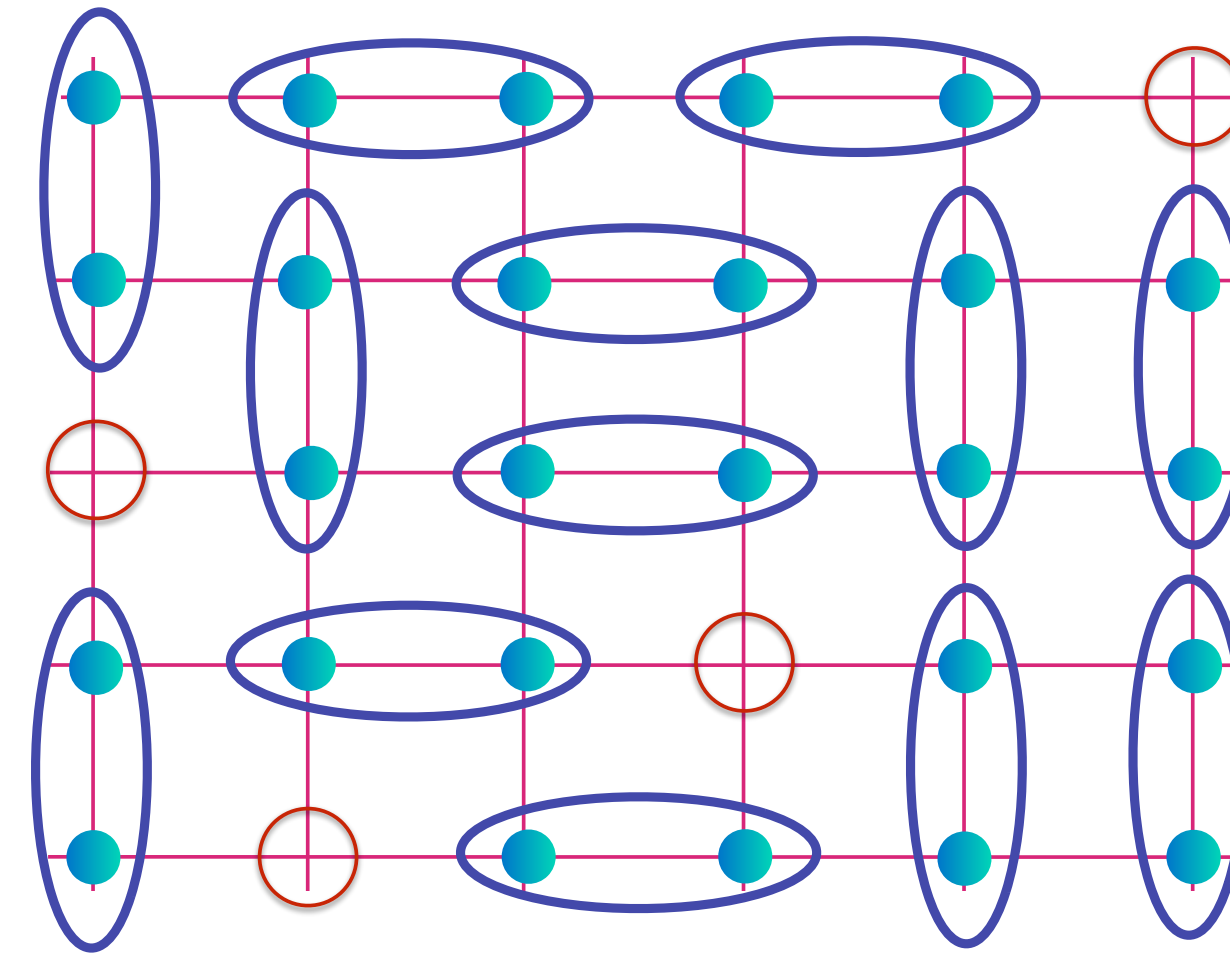
M. Punk, A. Allais, and S. Sachdev, PNAS **112**, 9552 (2015)

# Doping an insulating antiferromagnet with holes of density $p$



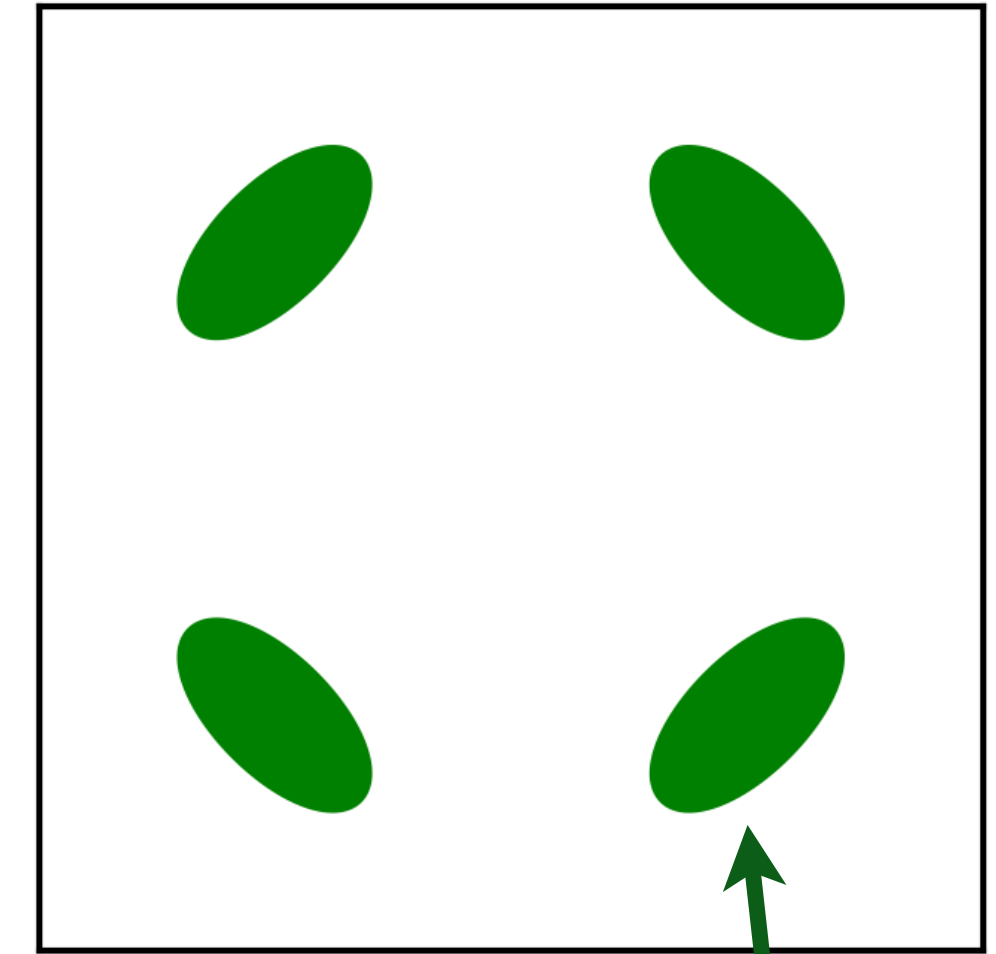
Area  $p/4$

AF metal and SDW fluctuation

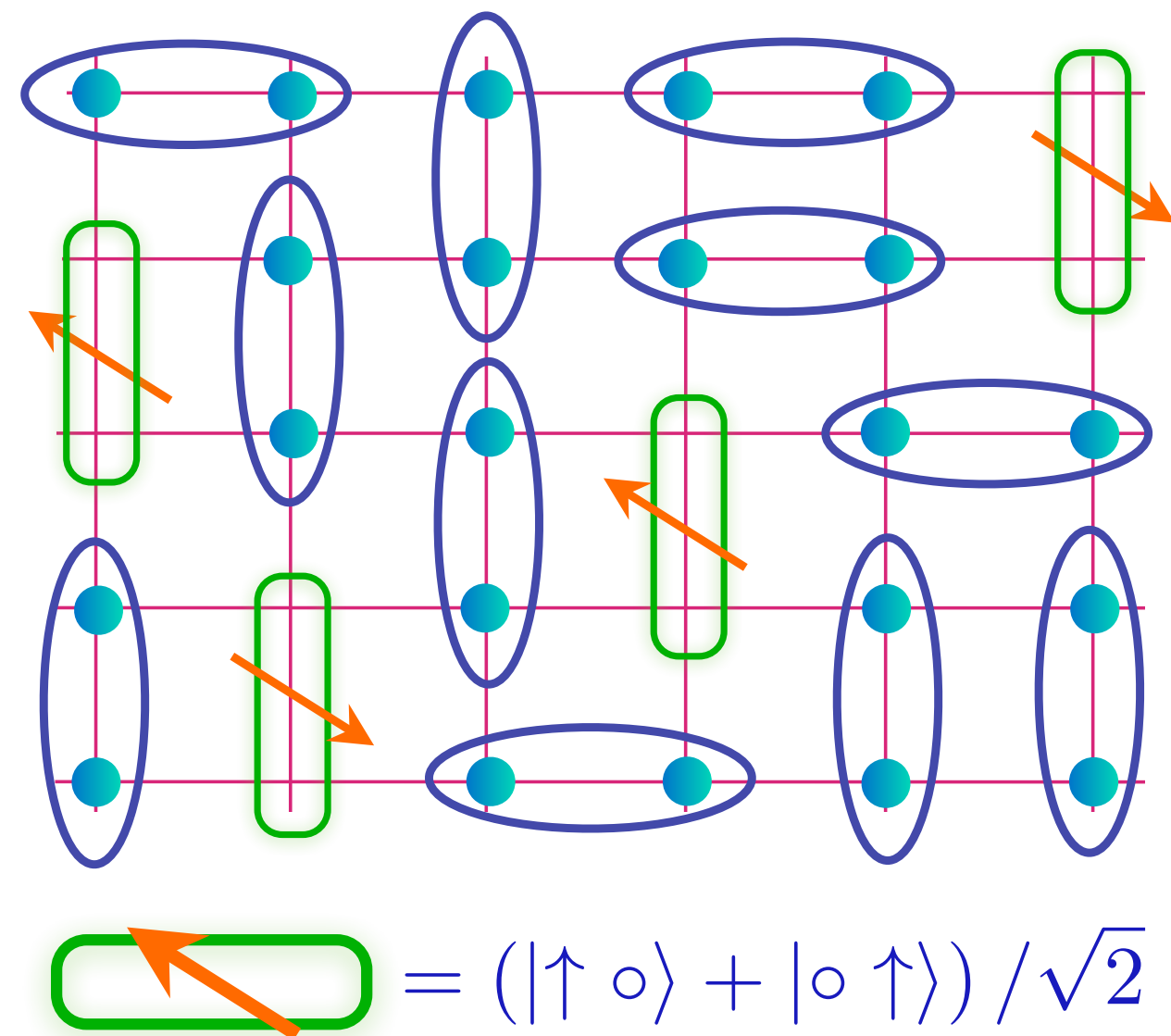


$$\text{Blue oval} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2}$$

Holon metal

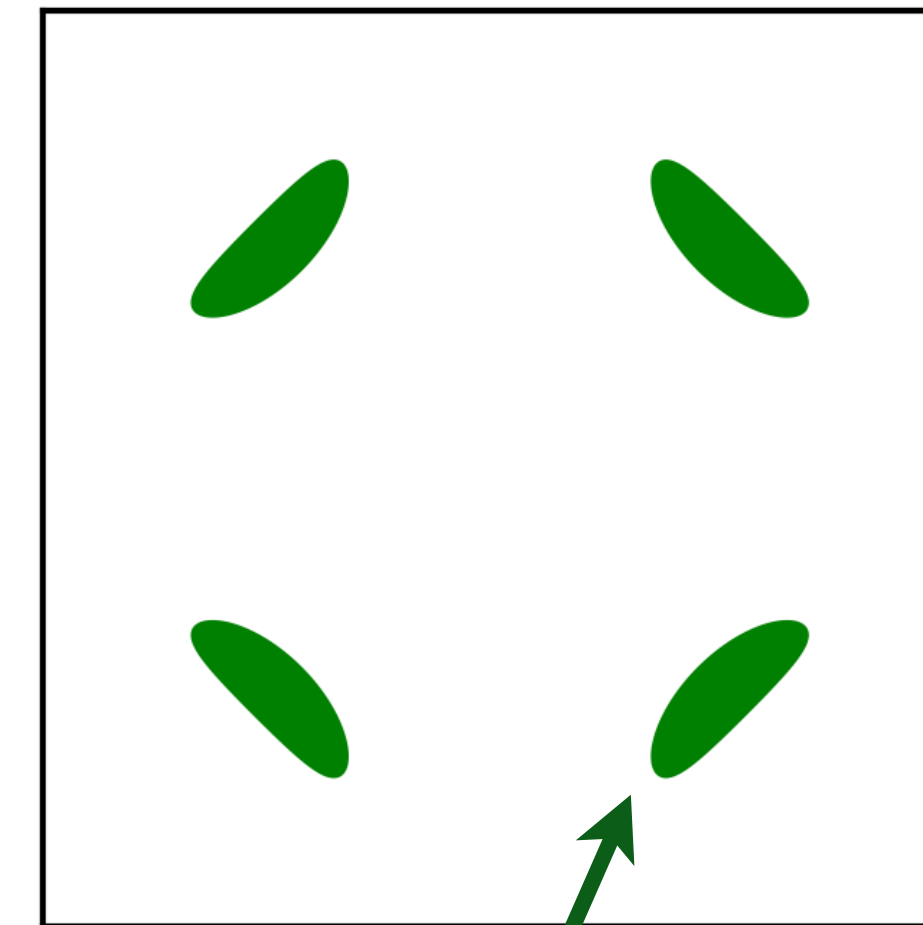


Area  $p/4$



FL\*

$$\text{Green oval} = (|\uparrow\circ\rangle + |\circ\uparrow\rangle) / \sqrt{2}$$



Area  $p/8$

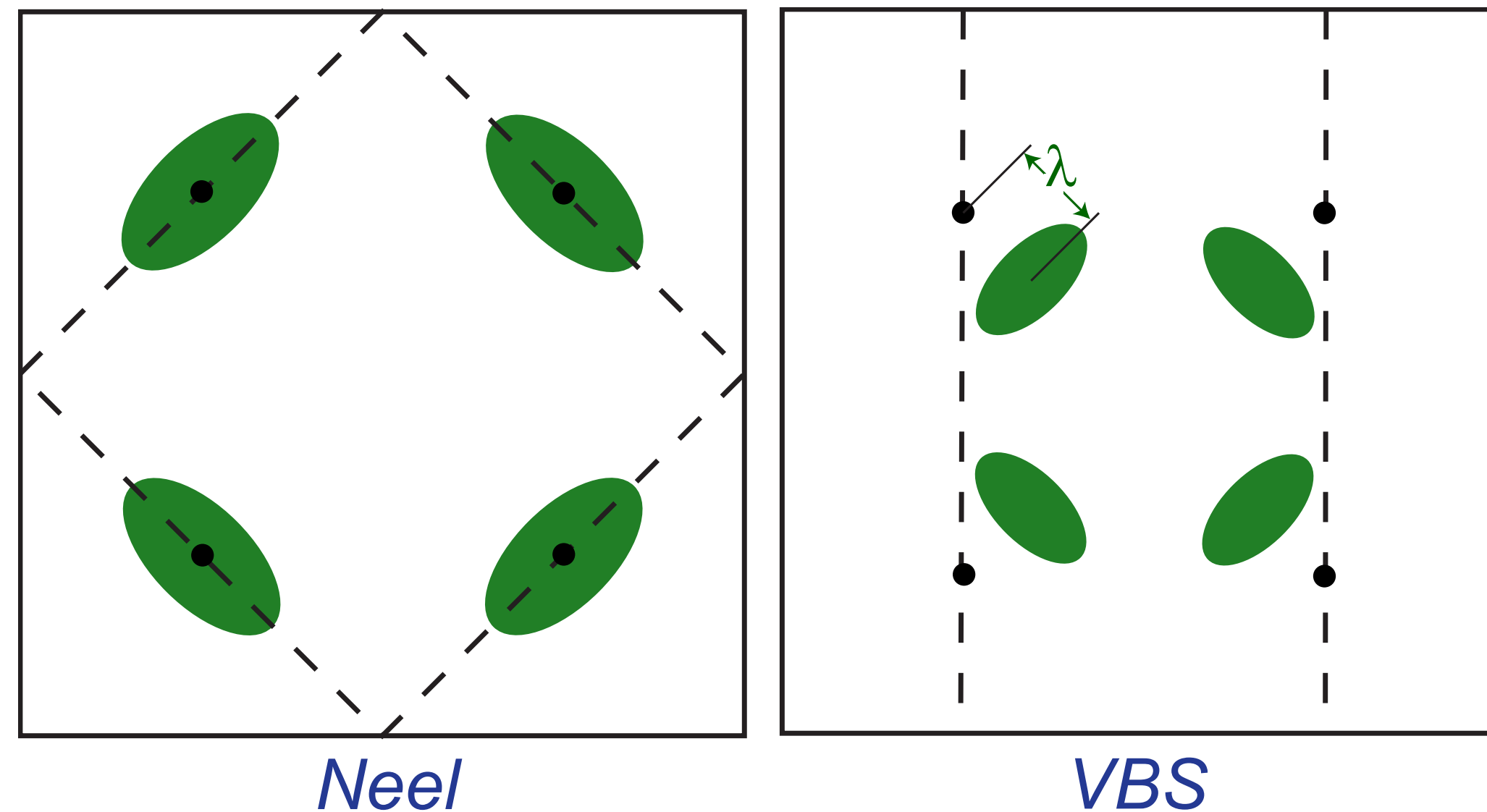
Area 1

Quantization of spin liquid anomaly implies Fermi surface areas are also quantized and robust to all corrections.

T. Senthil, S. S., M. Vojta, PRL **90**, 216403 (2003);  
 R. K. Kaul, A. Kolezhuk, M. Levin, S.S., T. Senthil, PRB **75**, 235122 (2007)  
 M. Punk, A. Allais, and S. S., PNAS **112**, 9552 (2015)  
 E. Mascot, A. Nikolaenko, M. Tikhonovskaya, Ya-Hui Zhang, D. K. Morr, S. S., PRB **105**, 075146 (2022)

# Hole dynamics in an antiferromagnet across a deconfined quantum critical point

Ribhu K. Kaul,<sup>1</sup> Alexei Kolezhuk,<sup>1,2</sup> Michael Levin,<sup>1</sup> Subir Sachdev,<sup>1</sup> and T. Senthil<sup>3,4</sup>



The dashed line in the Néel phase indicates the boundary of the magnetic Brillouin zone. Only the Fermi surfaces within this zone contribute to the Luttinger counting, and so the area of each ellipse is  $\mathcal{A}_F = (2\pi)^2 \delta/4$ . In the VBS phase, all four pockets are inequivalent, and so the area of each ellipse is  $\mathcal{A}_F = (2\pi)^2 \delta/8$ .

Factor of 2 between  
SDW fluctuation  
and FL\*

# Many fermion entanglement I:

## Observation of the Yamaji effect in the cuprate pseudogap

**See also:**

**Fermi surface transformation at the pseudogap critical point of a cuprate superconductor**

Yawen Fang, Gaël Grissonnache, Anaëlle Legros, Simon Verret, Francis Laliberté, Clément Collignon, Amirreza Ataei, Maxime Dion, Jianshi Zhou, David Graf, M. J. Lawler, Paul Goddard, Louis Taillefer, and B. J. Ramshaw, *Nature Physics* **18**, 558 (2022)

Angle-dependent magnetoresistance (ADMR) of  $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$

# Observation of the Yamaji effect in a cuprate superconductor

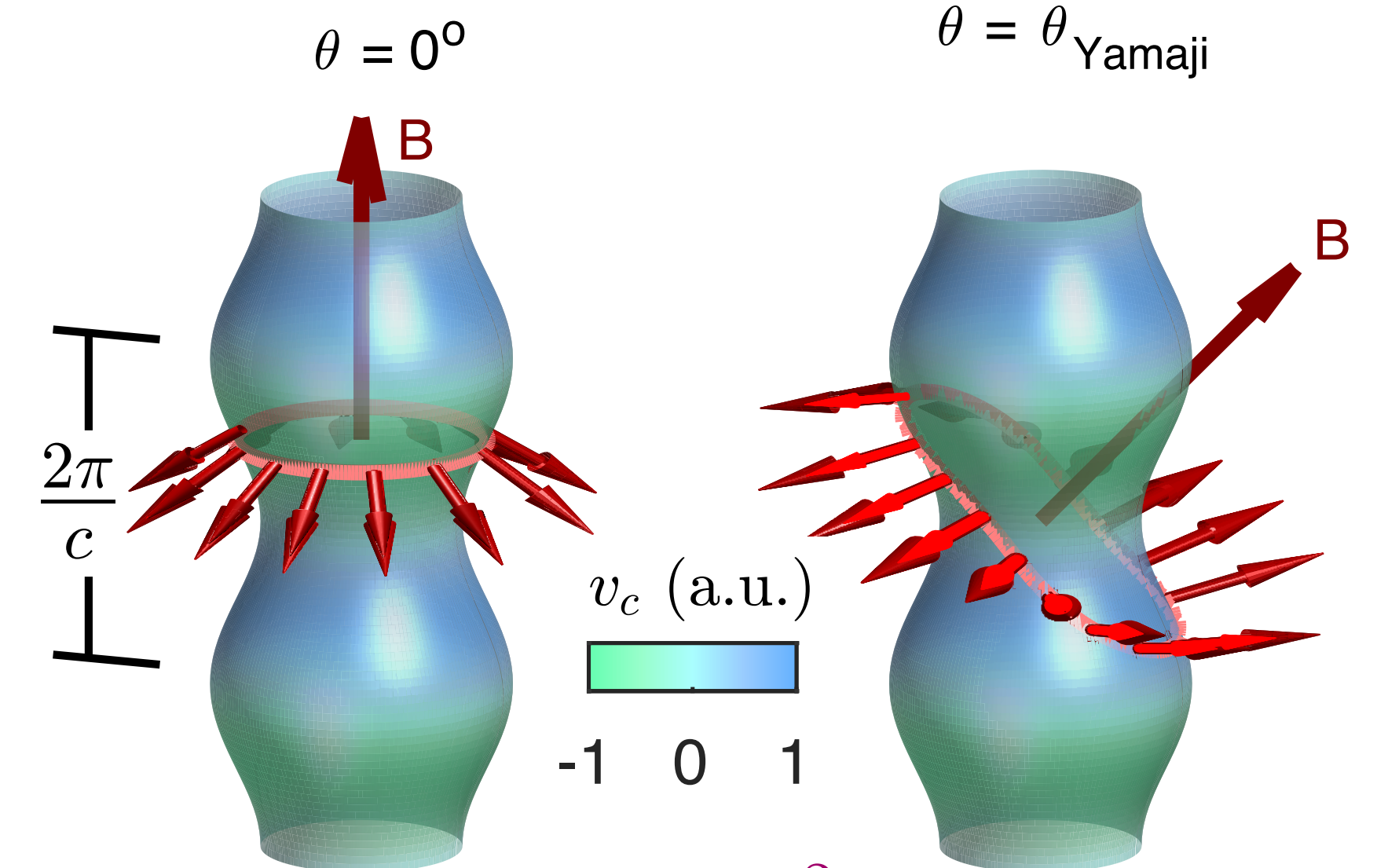
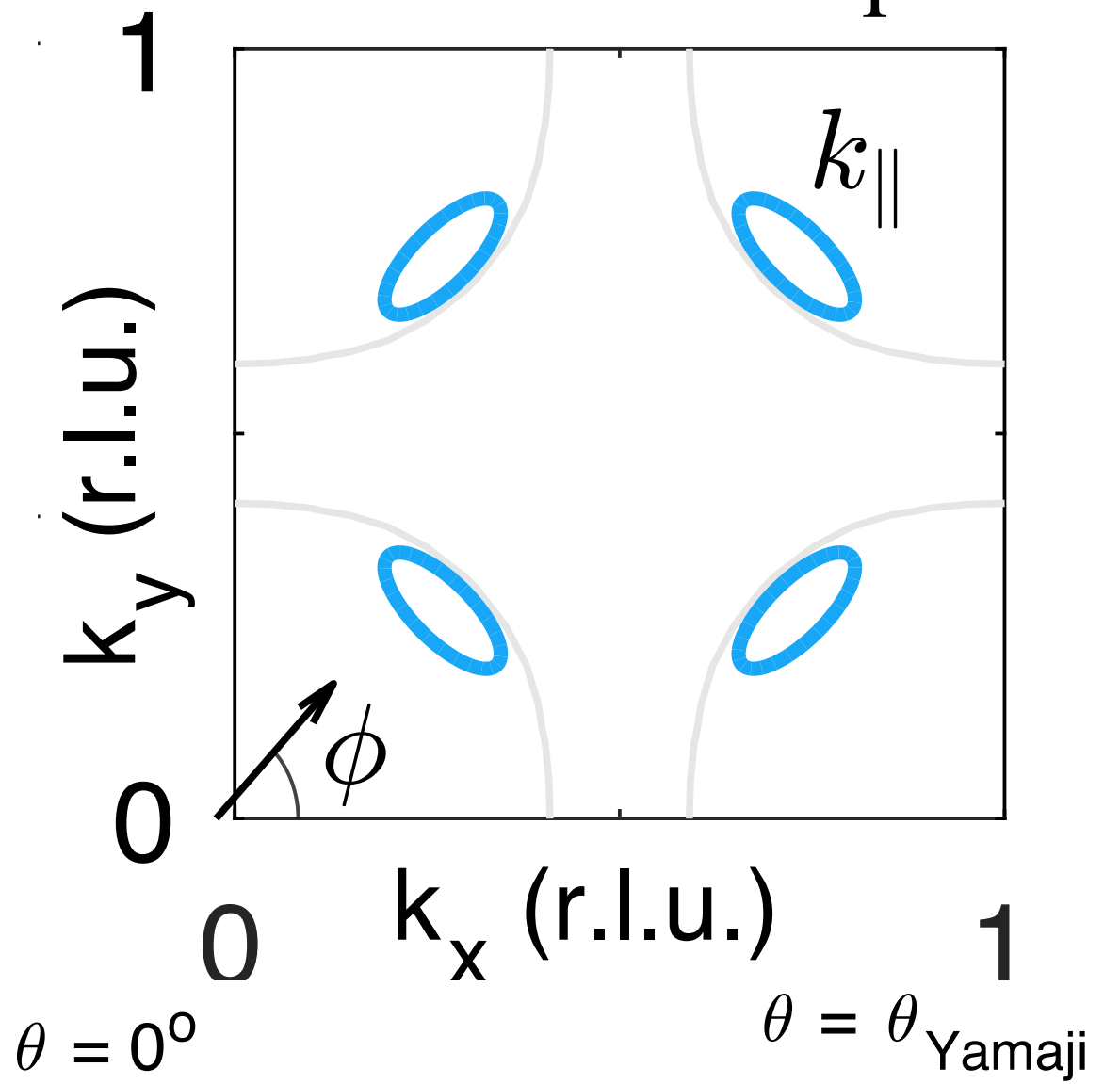
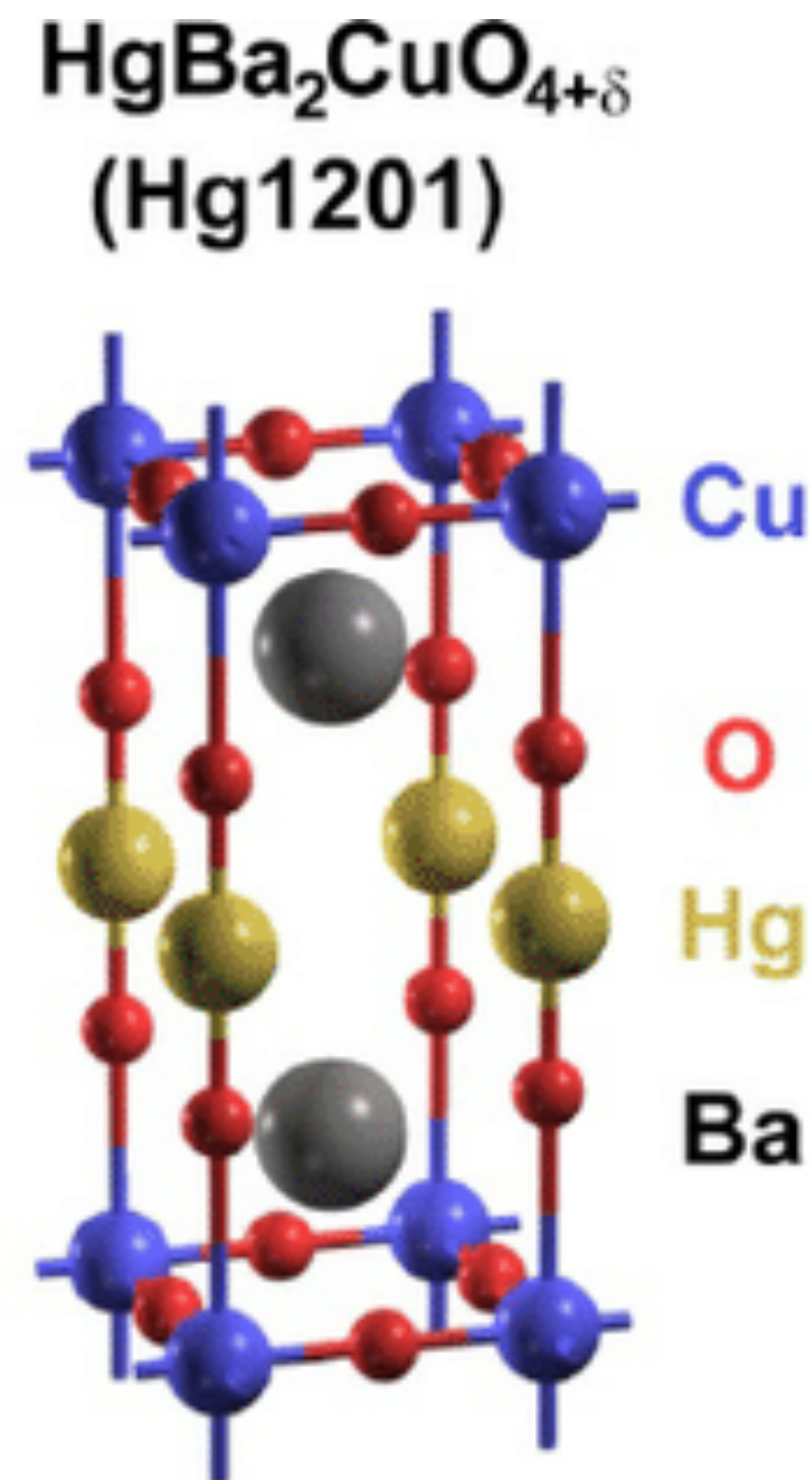
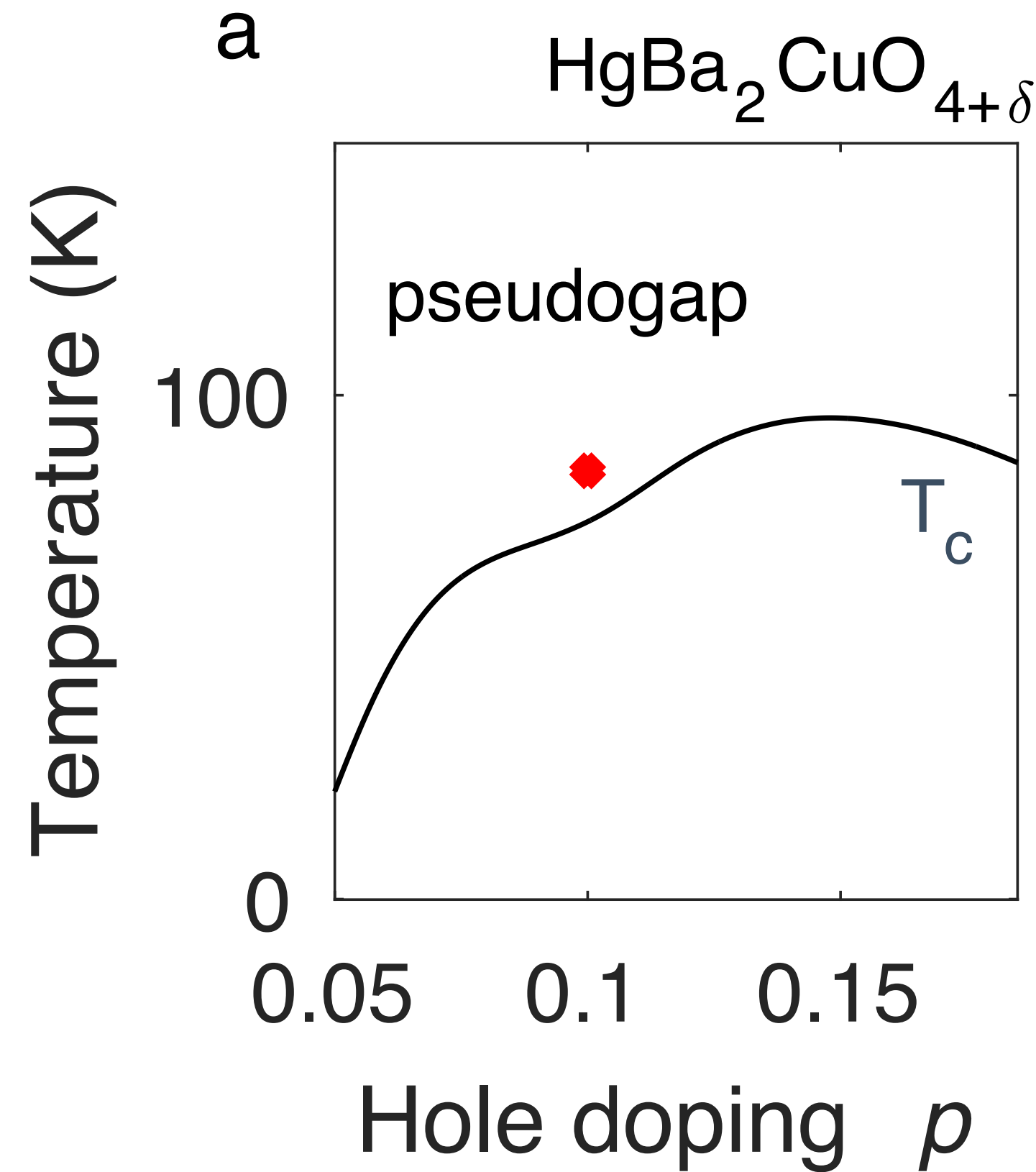
superconductor

Mun K. Chan<sup>1</sup>✉, Katherine A. Schreiber<sup>1</sup>, Oscar E. Ayala-Valenzuela<sup>1</sup>,  
Eric D. Bauer<sup>2</sup>, Arkady Shekhter<sup>1</sup> & Neil Harrison<sup>1</sup>

nature physics

21, 1753 (2025)

Published online: 16 September 2025



$$\epsilon(\mathbf{k}) = \frac{k_x^2}{2m_1} + \frac{k_y^2}{2m_2} - 2t_\perp \cos(k_z c)$$

At the Yamaji angle, the orbits in the plane orthogonal to  $\mathbf{B}$  have an area which is independent of momentum in the  $c$  direction, to first order in the hopping along the  $c$  direction.

K. Yamaji JPSJ **58**, 1520 (1989)

# Observation of the Yamaji effect in a cuprate superconductor

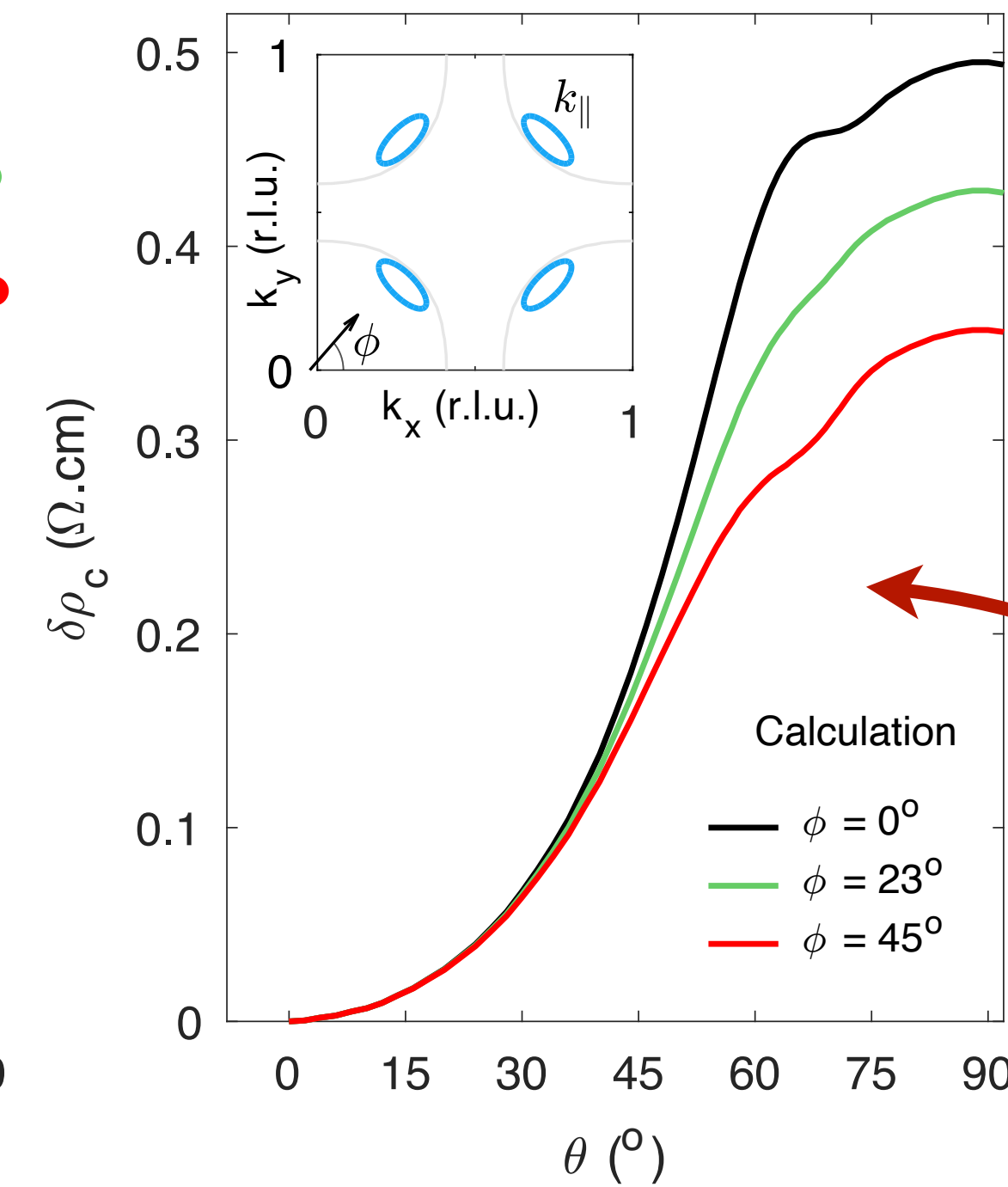
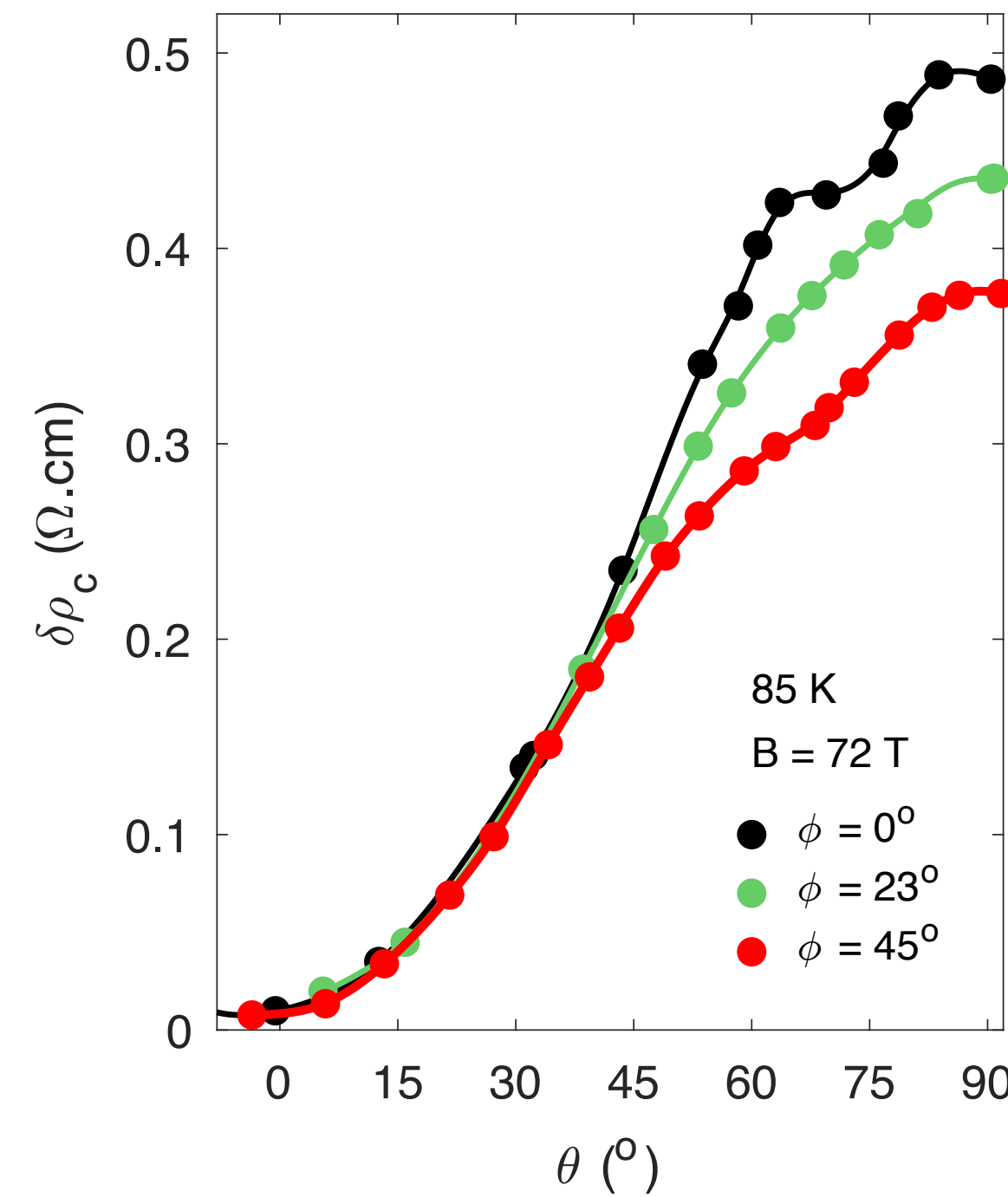
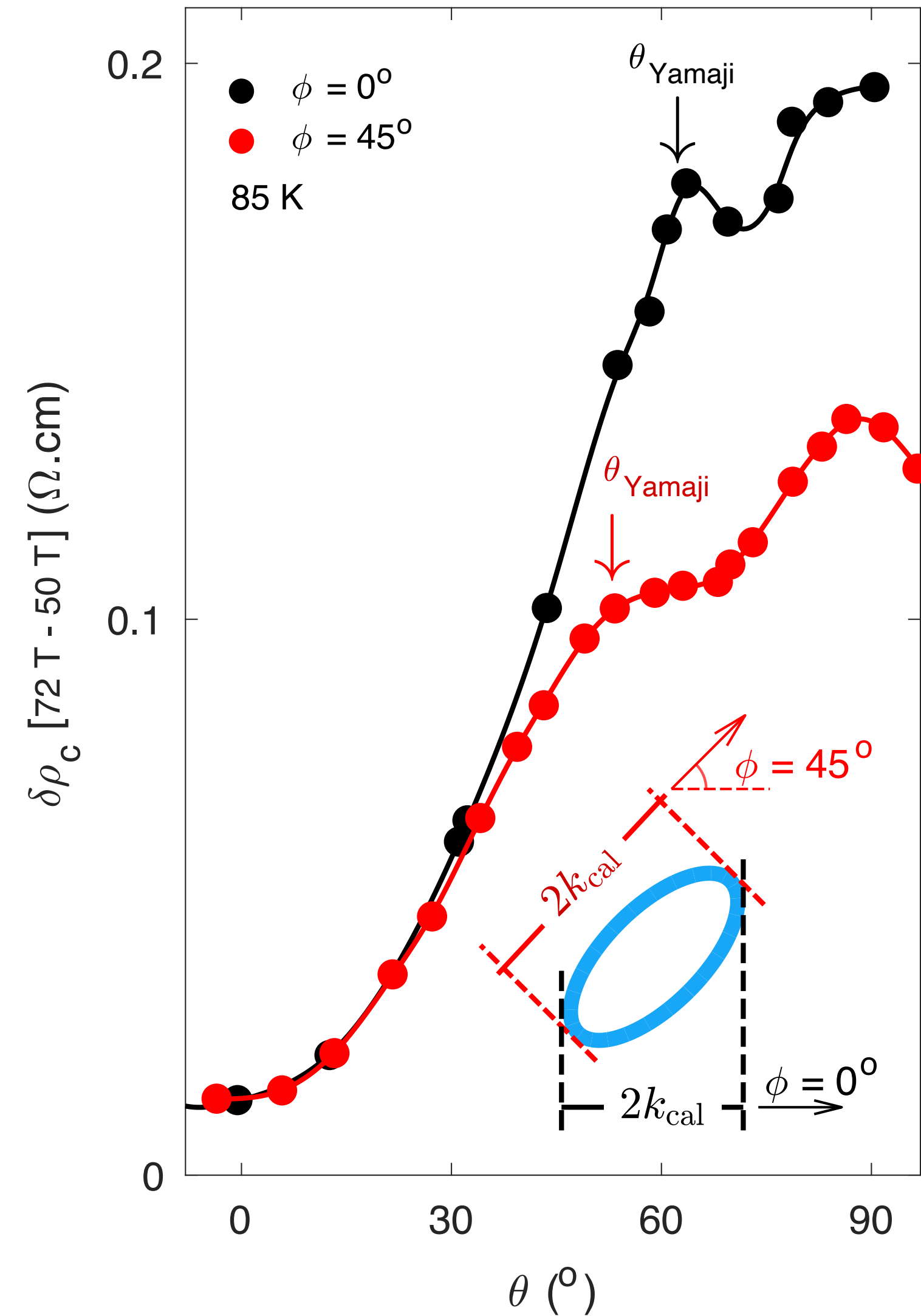
superconductor

Mun K. Chan <sup>1</sup>✉, Katherine A. Schreiber<sup>1</sup>, Oscar E. Ayala-Valenzuela <sup>1</sup>,  
Eric D. Bauer <sup>2</sup>, Arkady Shekhter <sup>1</sup> & Neil Harrison <sup>1</sup>

nature physics

21, 1753 (2025)

Published online: 16 September 2025



Doping  
 $p = 0.1$

The observation of the Yamaji peak is evidence for small Fermi-surface pockets in the normal state of the pseudogap phase.

$$\frac{\partial f}{\partial t} + e(\mathbf{E} + \mathbf{v} \times \mathbf{B}) \cdot \mathbf{v} \left( -\frac{\partial f}{\partial \epsilon} \right) = -\frac{f - f_0}{\tau}$$

$$\mathbf{v} = \nabla_{\mathbf{k}} \epsilon(\mathbf{k}) ; f_0(\epsilon) = \frac{1}{e^{(\epsilon - \mu)/T} + 1}$$

# Observation of the Yamaji effect in a cuprate superconductor

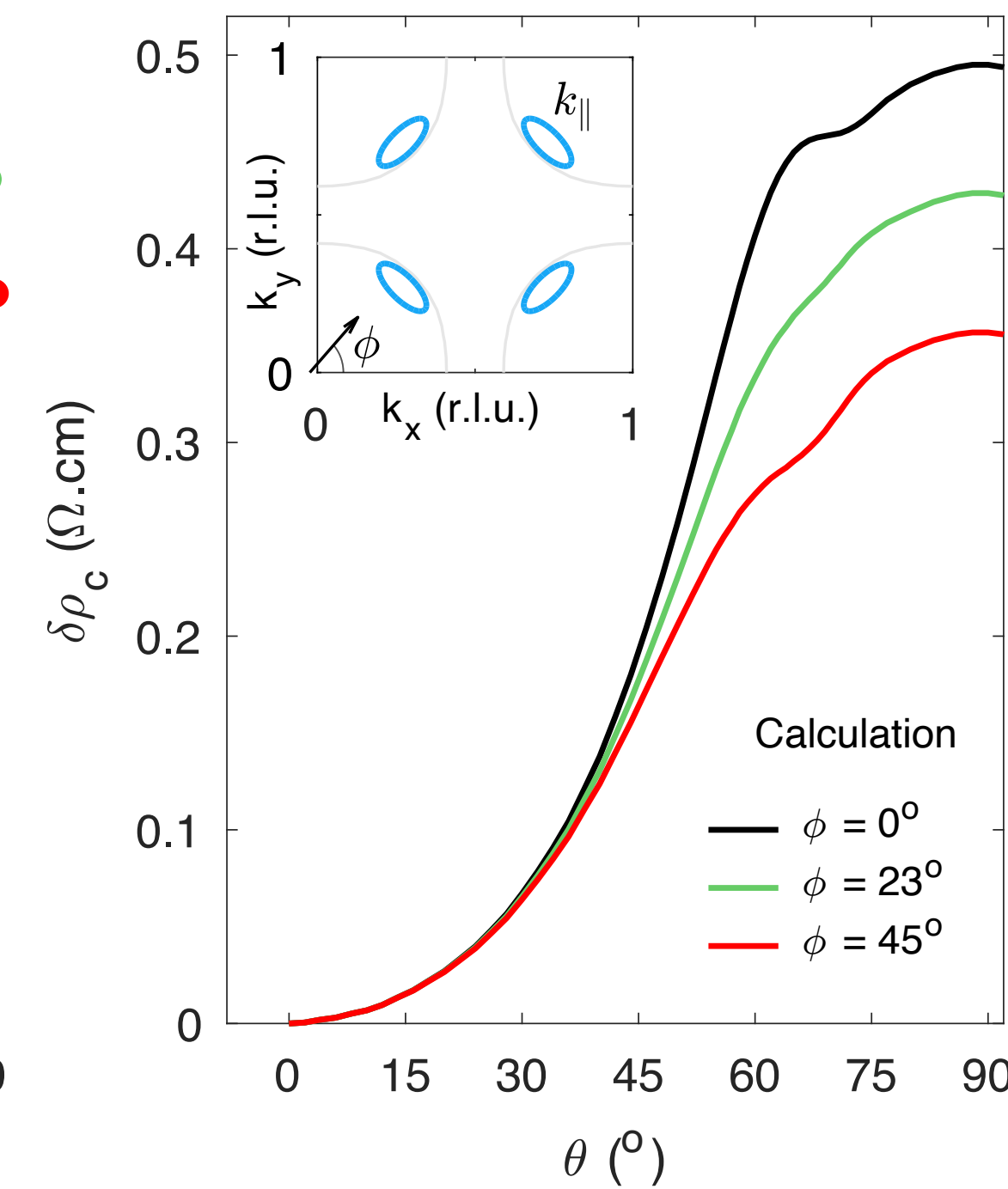
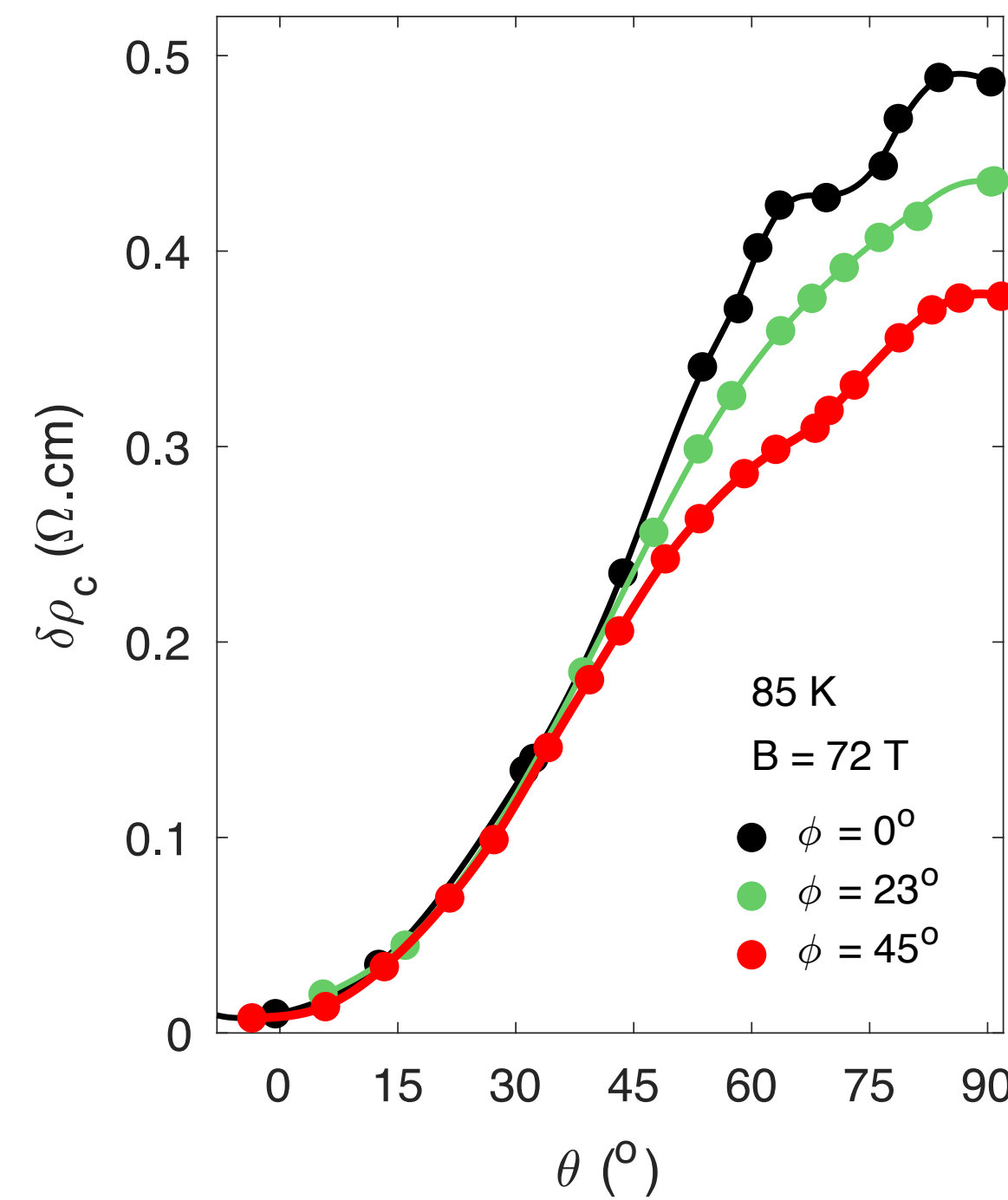
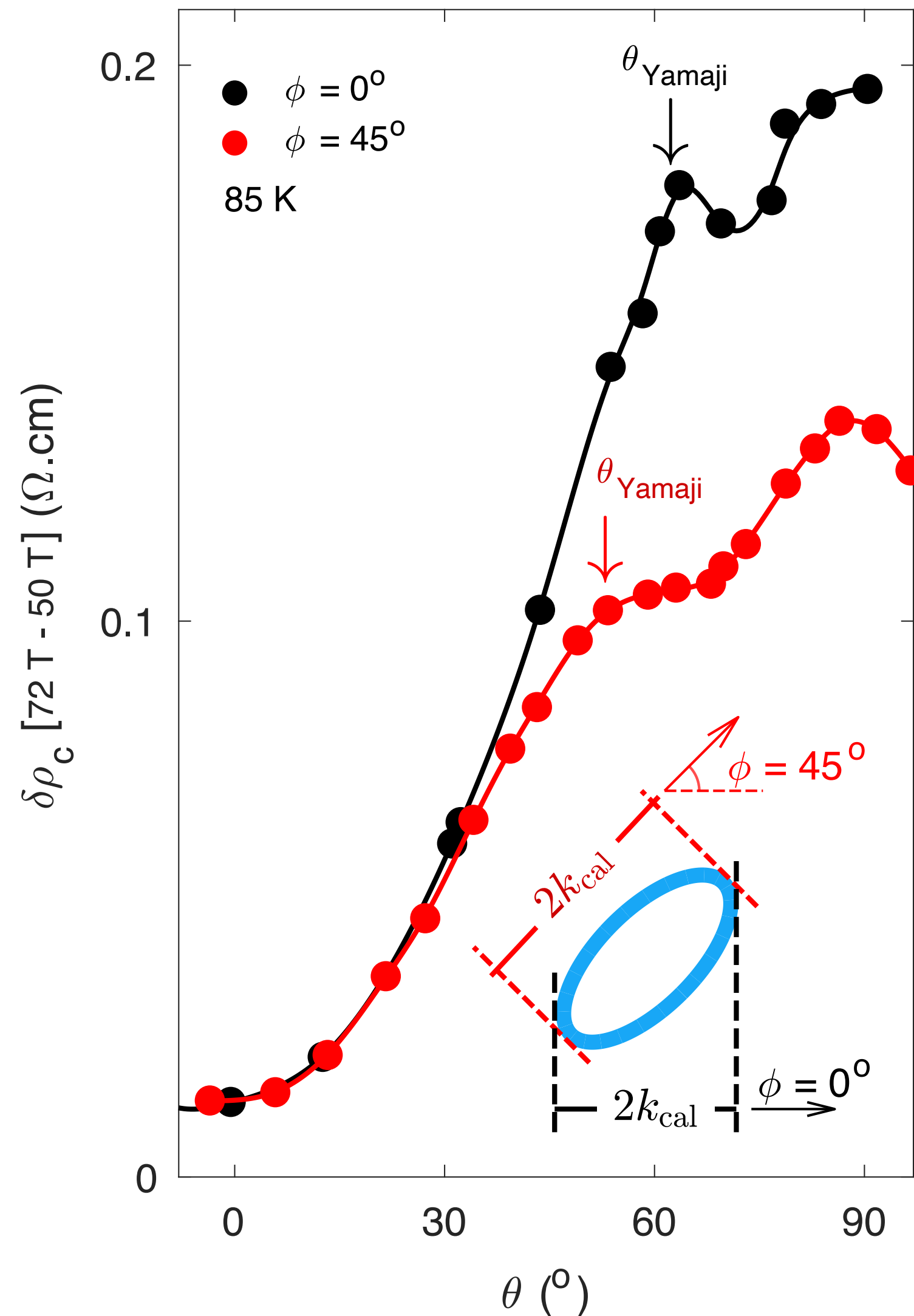
superconductor

Mun K. Chan<sup>1</sup>✉, Katherine A. Schreiber<sup>1</sup>, Oscar E. Ayala-Valenzuela<sup>1</sup>,  
Eric D. Bauer<sup>2</sup>, Arkady Shekhter<sup>1</sup> & Neil Harrison<sup>1</sup>

nature physics

21, 1753 (2025)

Published online: 16 September 2025



Doping  
 $p = 0.1$

The observation of the Yamaji peak is evidence for small Fermi-surface pockets in the normal state of the pseudogap phase.

Excellent evidence for hole pockets with coherent interlayer-transport.

# Observation of the Yamaji effect in a cuprate superconductor

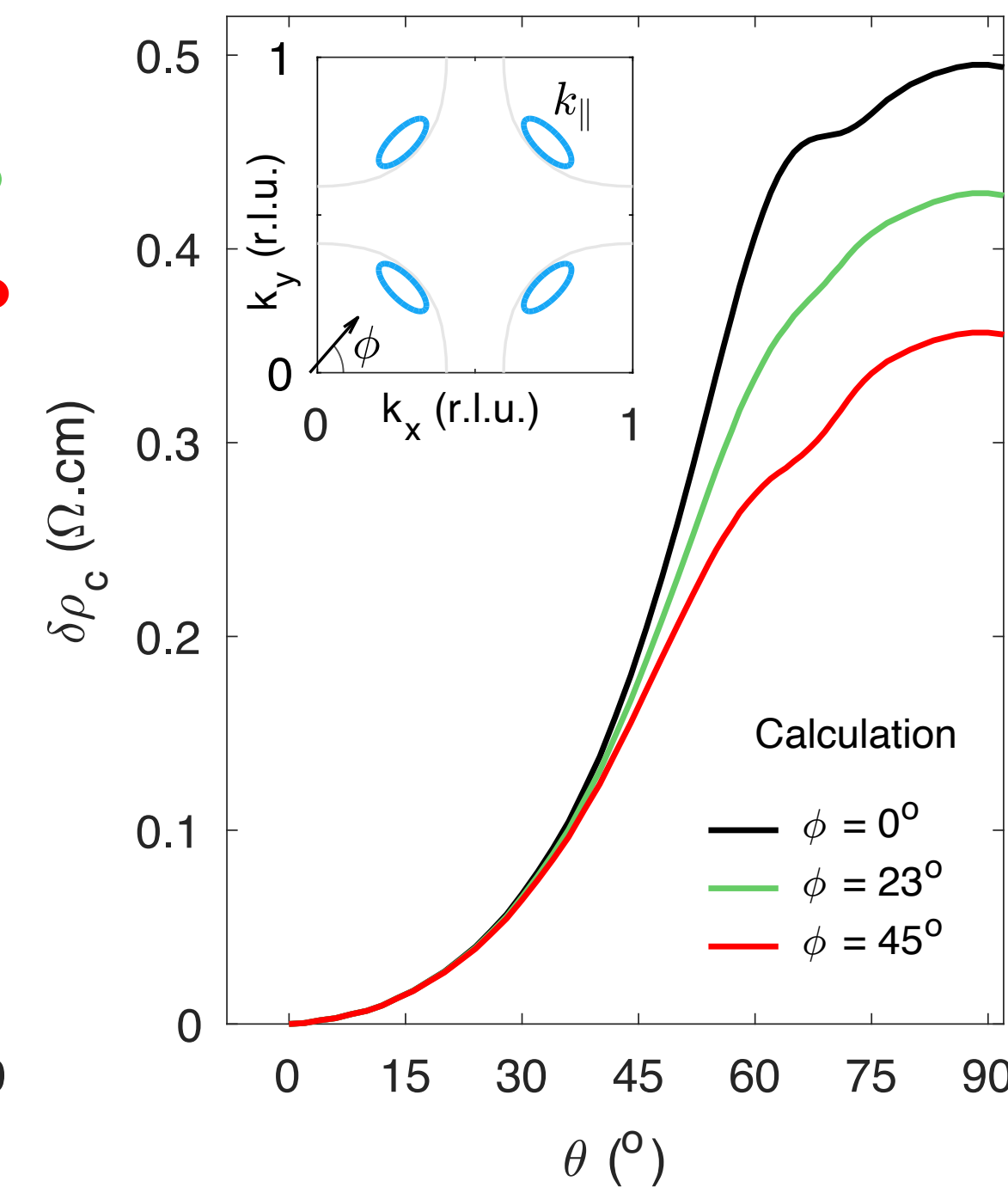
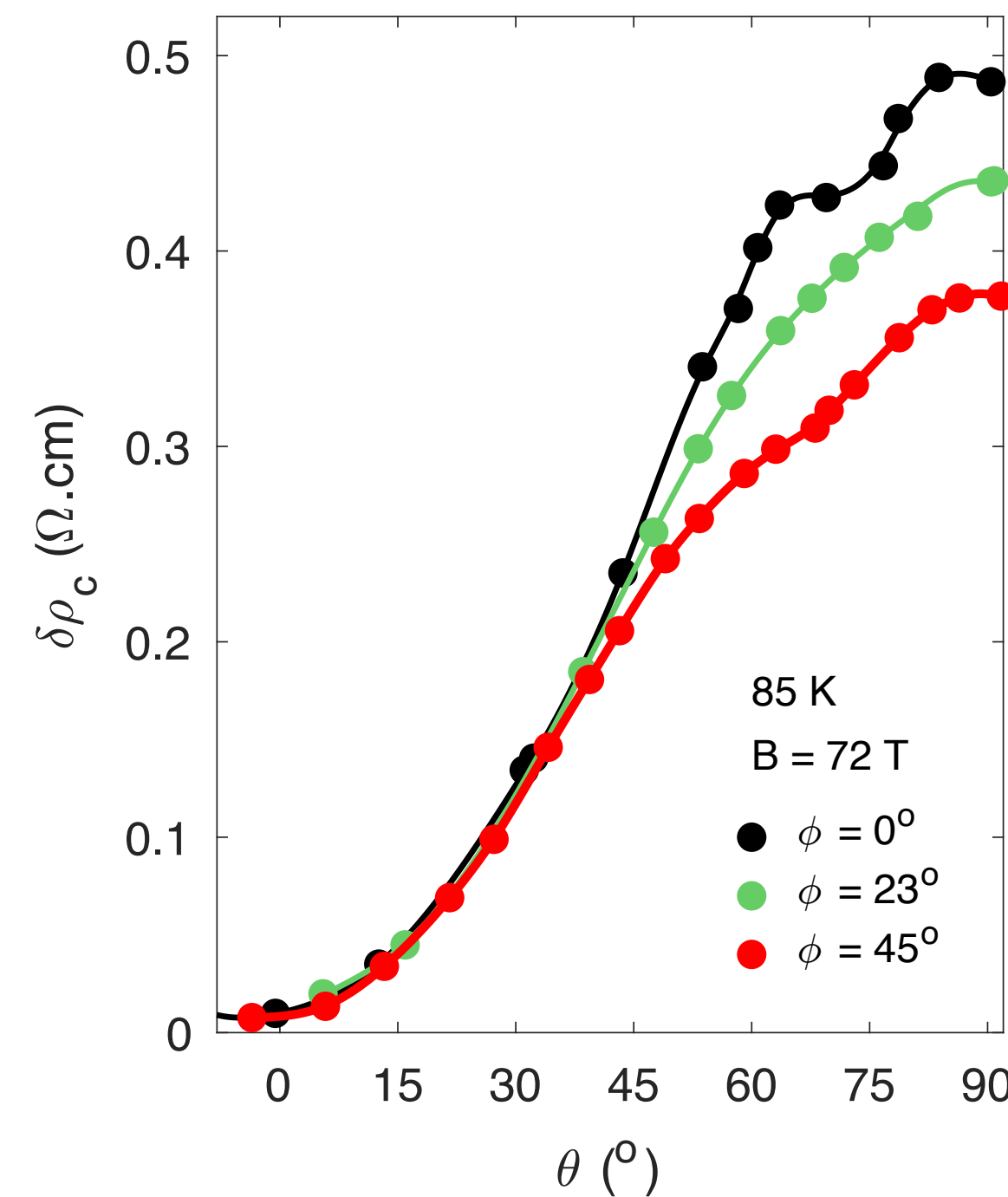
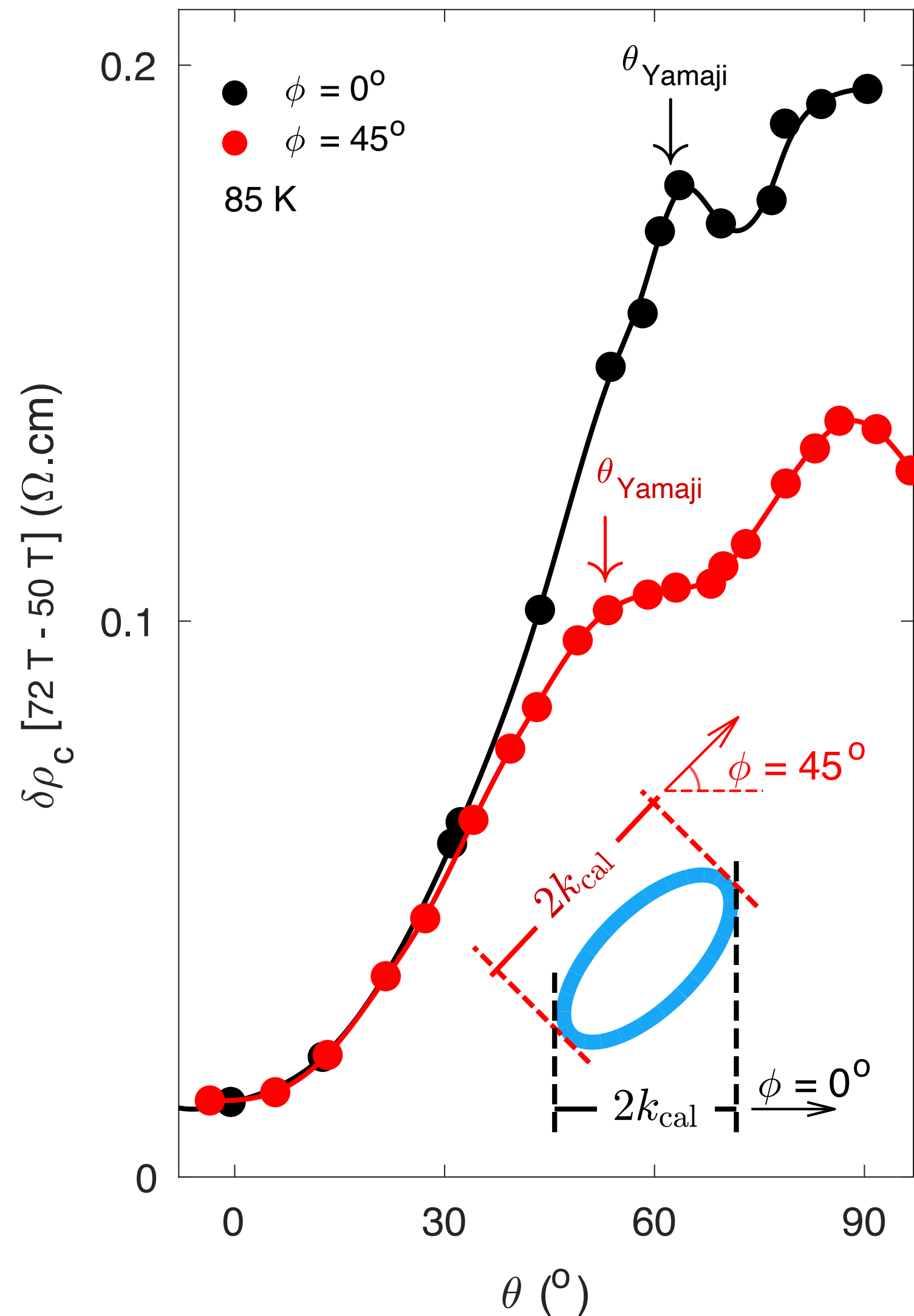
superconductor

Mun K. Chan<sup>1</sup>✉, Katherine A. Schreiber<sup>1</sup>, Oscar E. Ayala-Valenzuela<sup>1</sup>,  
Eric D. Bauer<sup>2</sup>, Arkady Shekhter<sup>1</sup> & Neil Harrison<sup>1</sup>

nature physics

21, 1753 (2025)

Published online: 16 September 2025



Doping  
 $p = 0.1$

The observation of the Yamaji peak is evidence for small Fermi-surface pockets in the normal state of the pseudogap phase.

Excellent evidence for hole pockets with coherent interlayer-transport.  
Rules out holon metal

# Observation of the Yamaji effect in a cuprate superconductor

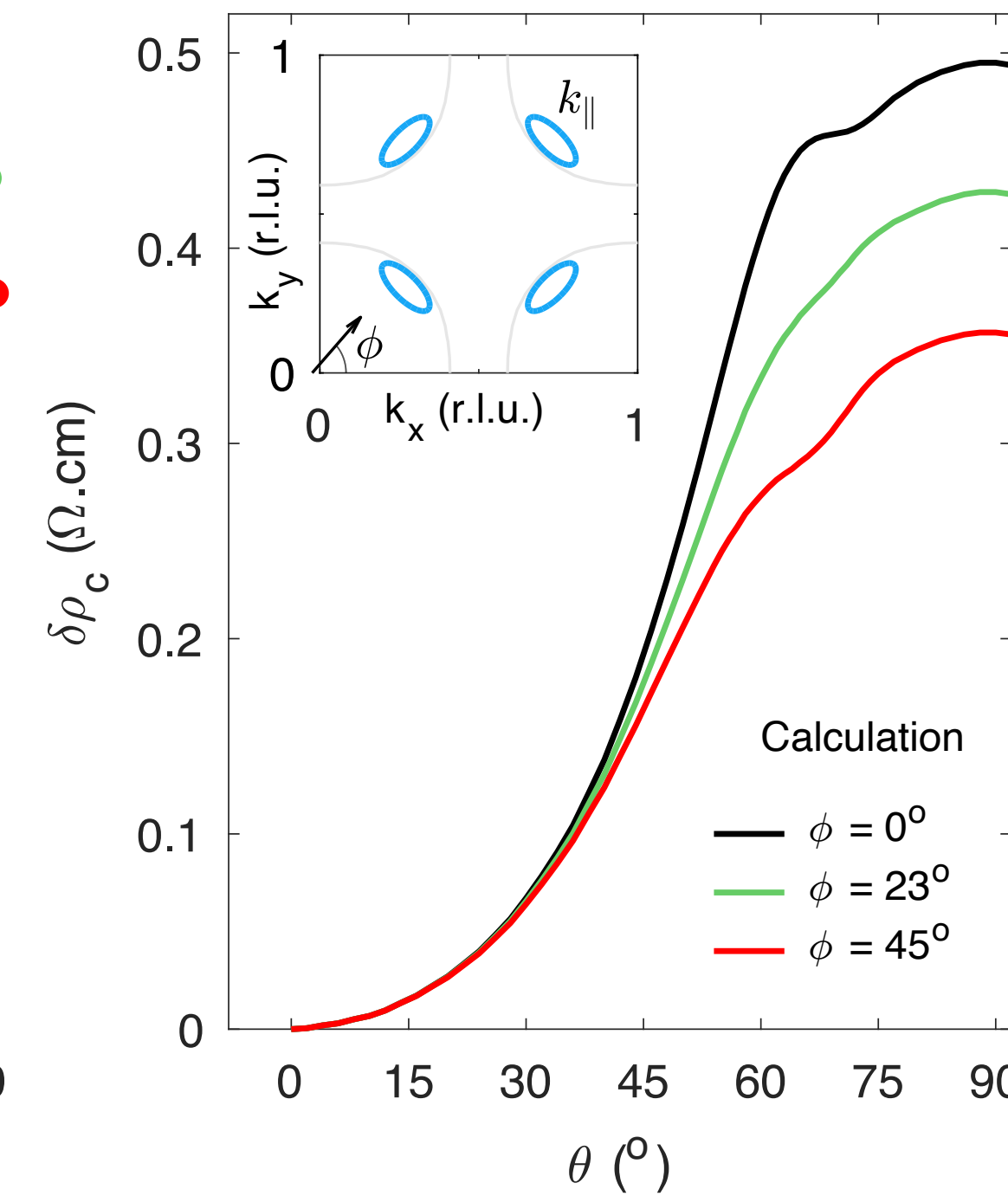
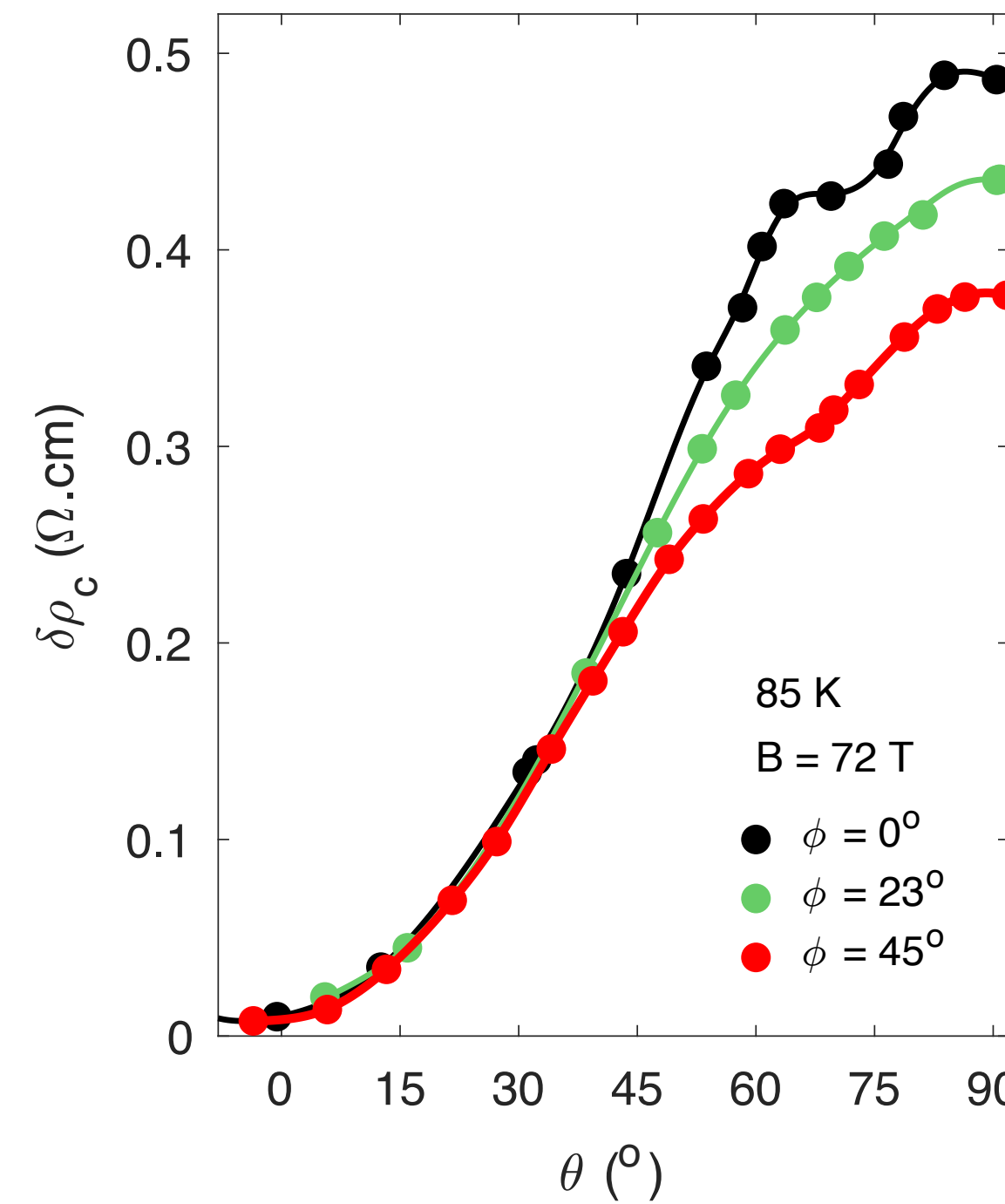
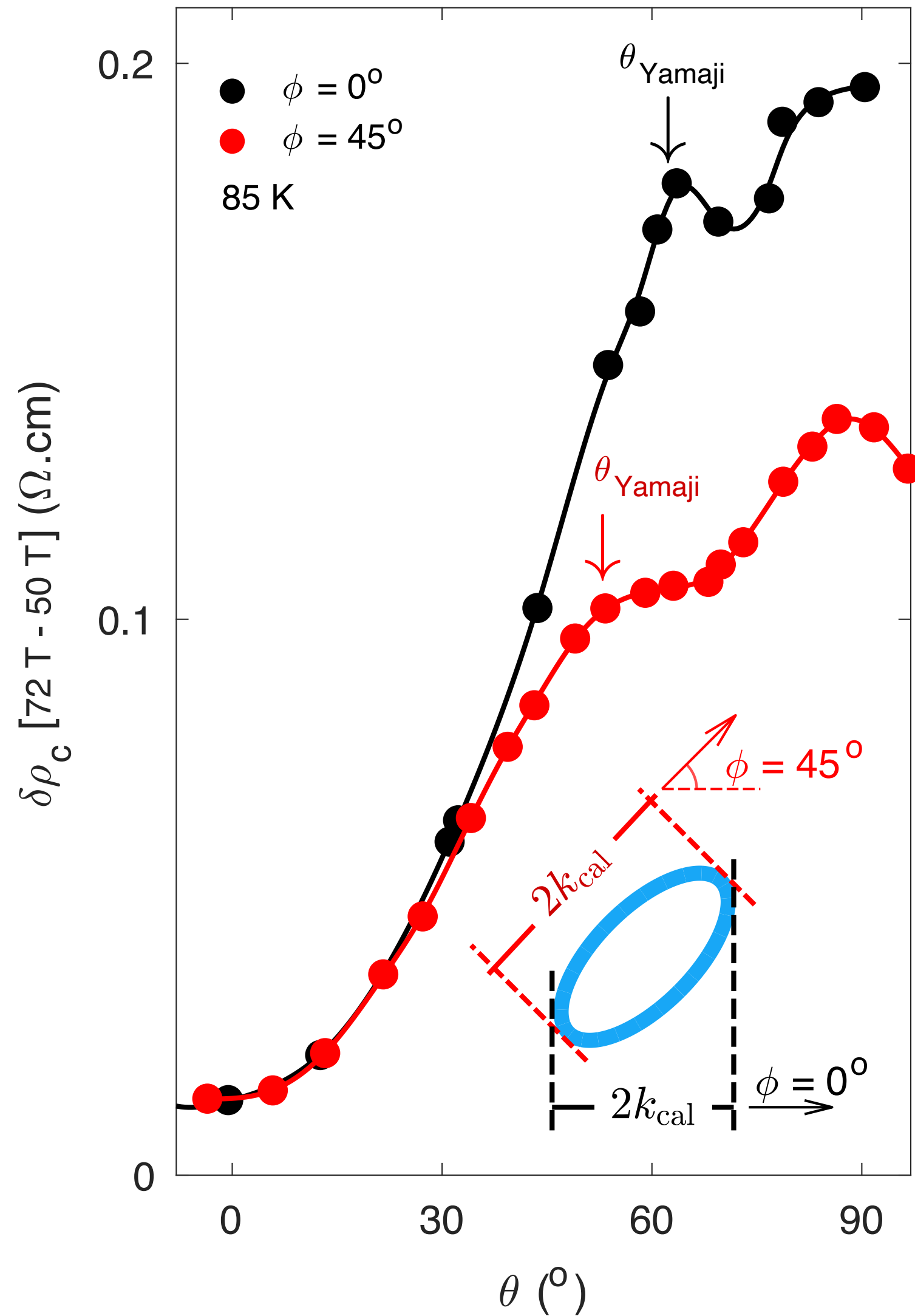
superconductor

Mun K. Chan<sup>1</sup>✉, Katherine A. Schreiber<sup>1</sup>, Oscar E. Ayala-Valenzuela<sup>1</sup>,  
Eric D. Bauer<sup>2</sup>, Arkady Shekhter<sup>1</sup> & Neil Harrison<sup>1</sup>

nature physics

21, 1753 (2025)

Published online: 16 September 2025



Doping  
 $p = 0.1$

The observation of the Yamaji peak is evidence for small Fermi-surface pockets in the normal state of the pseudogap phase.

Excellent evidence for hole pockets with coherent interlayer-transport. Rules out holon metal and possibly SDW metal

# Observation of the Yamaji effect in a cuprate superconductor

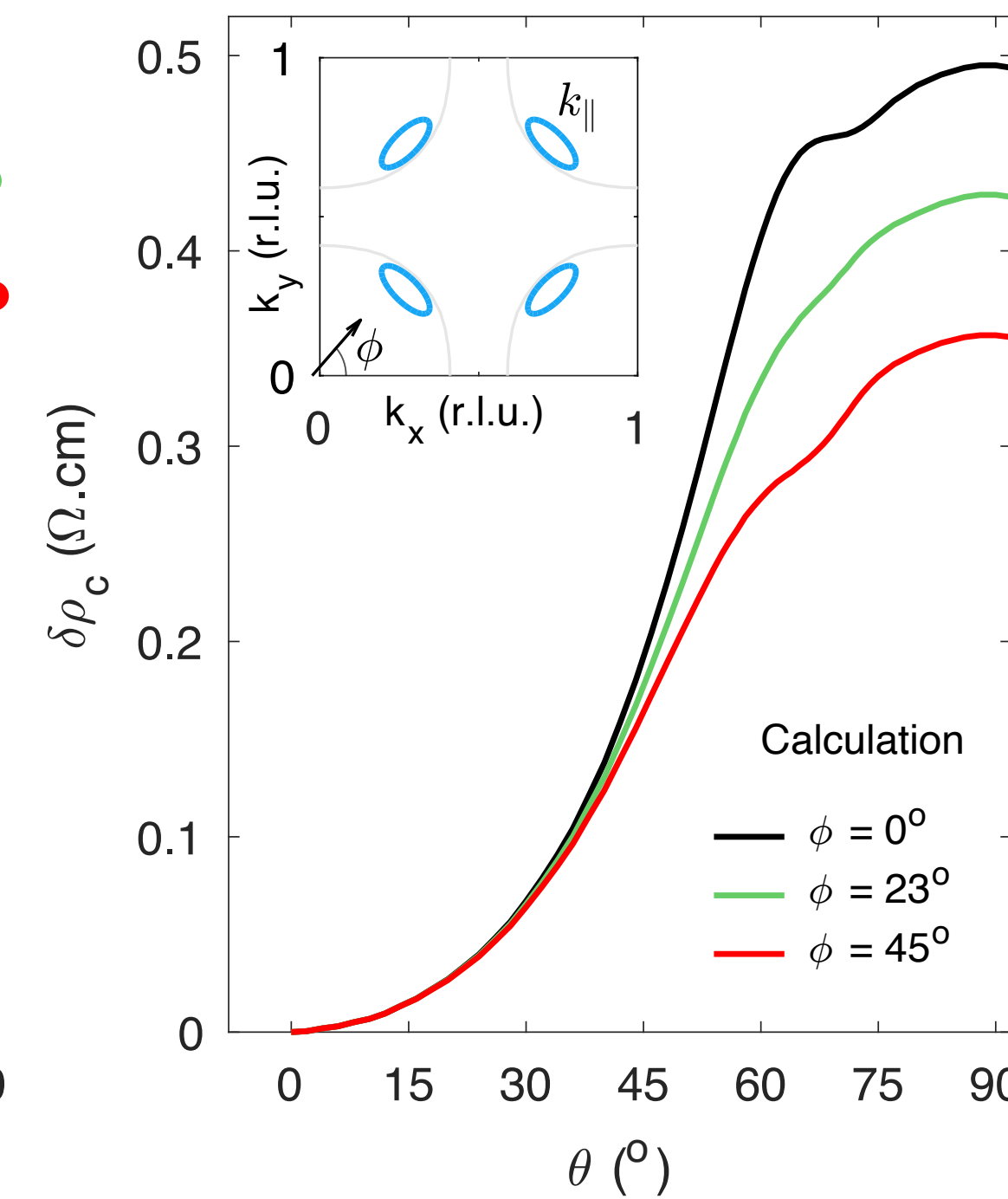
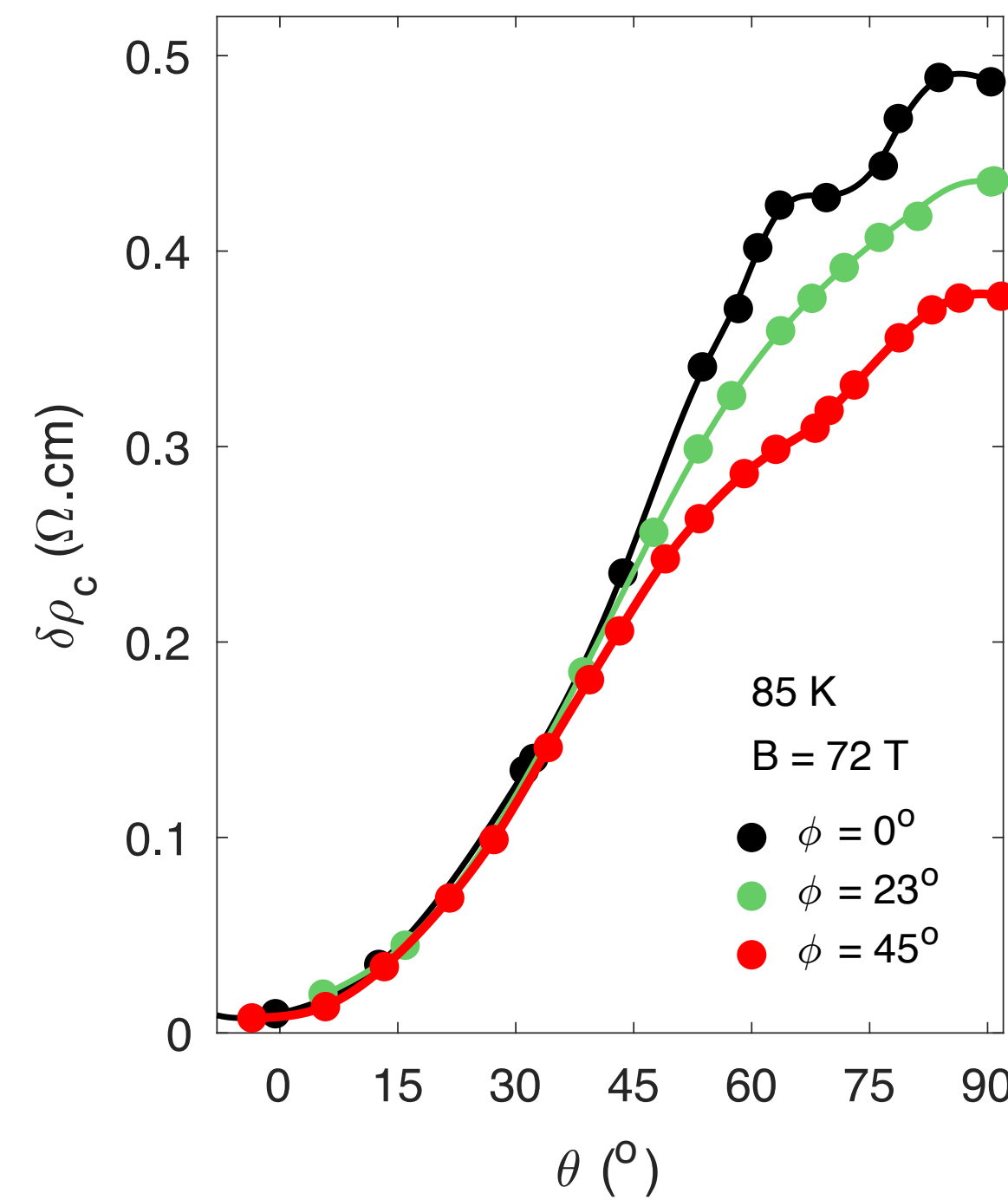
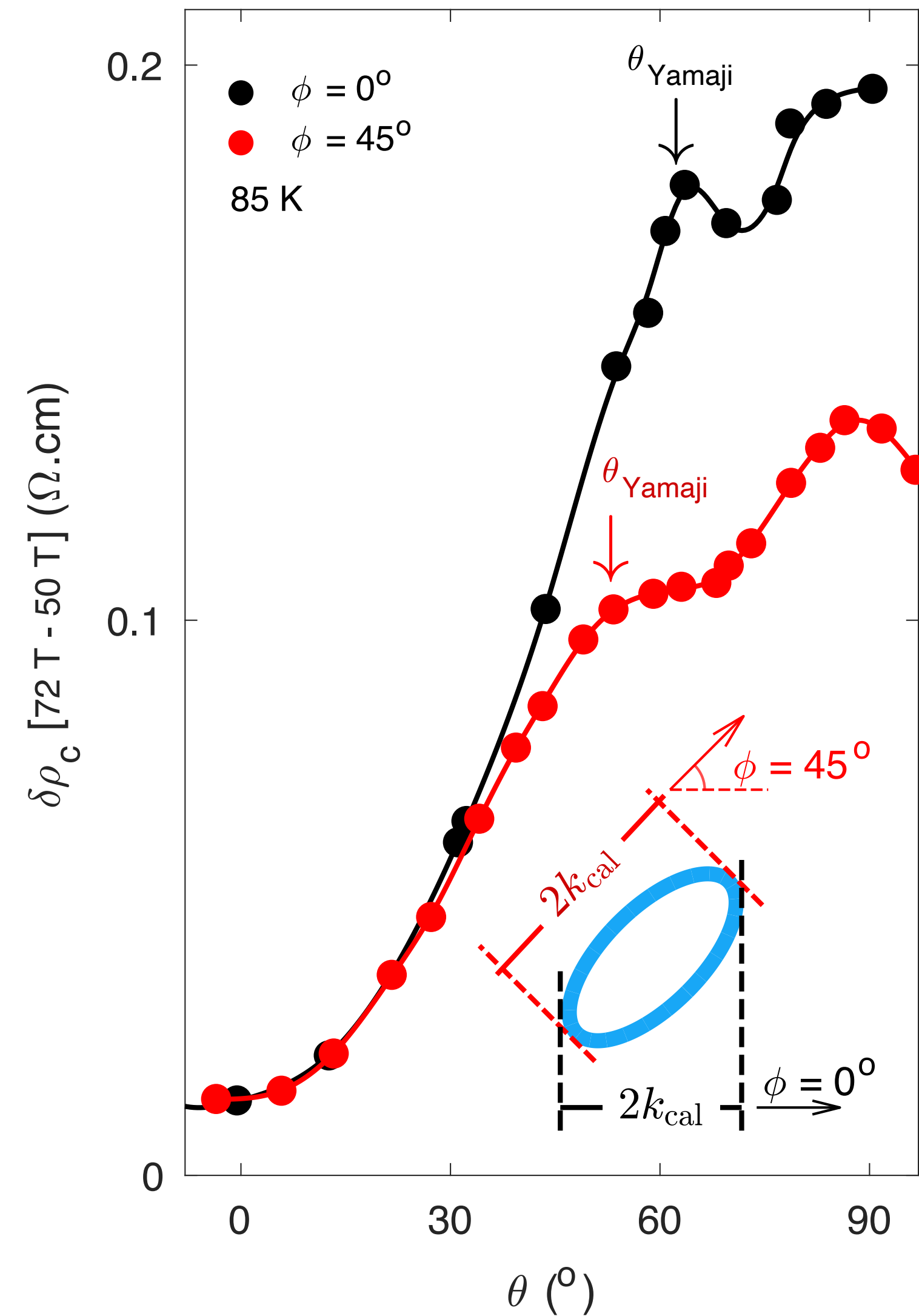
superconductor

Mun K. Chan <sup>1</sup>✉, Katherine A. Schreiber<sup>1</sup>, Oscar E. Ayala-Valenzuela <sup>1</sup>,  
Eric D. Bauer <sup>2</sup>, Arkady Shekhter <sup>1</sup> & Neil Harrison <sup>1</sup>

nature physics

21, 1753 (2025)

Published online: 16 September 2025



Doping  
 $p = 0.1$

The observation of the Yamaji peak is evidence for small Fermi-surface pockets in the normal state of the pseudogap phase. The small size of the pockets, each estimated to occupy only 1.3% of the Brillouin zone area, is not expected given the absence of long-range broken translational symmetry.

# Observation of the Yamaji effect in a cuprate superconductor

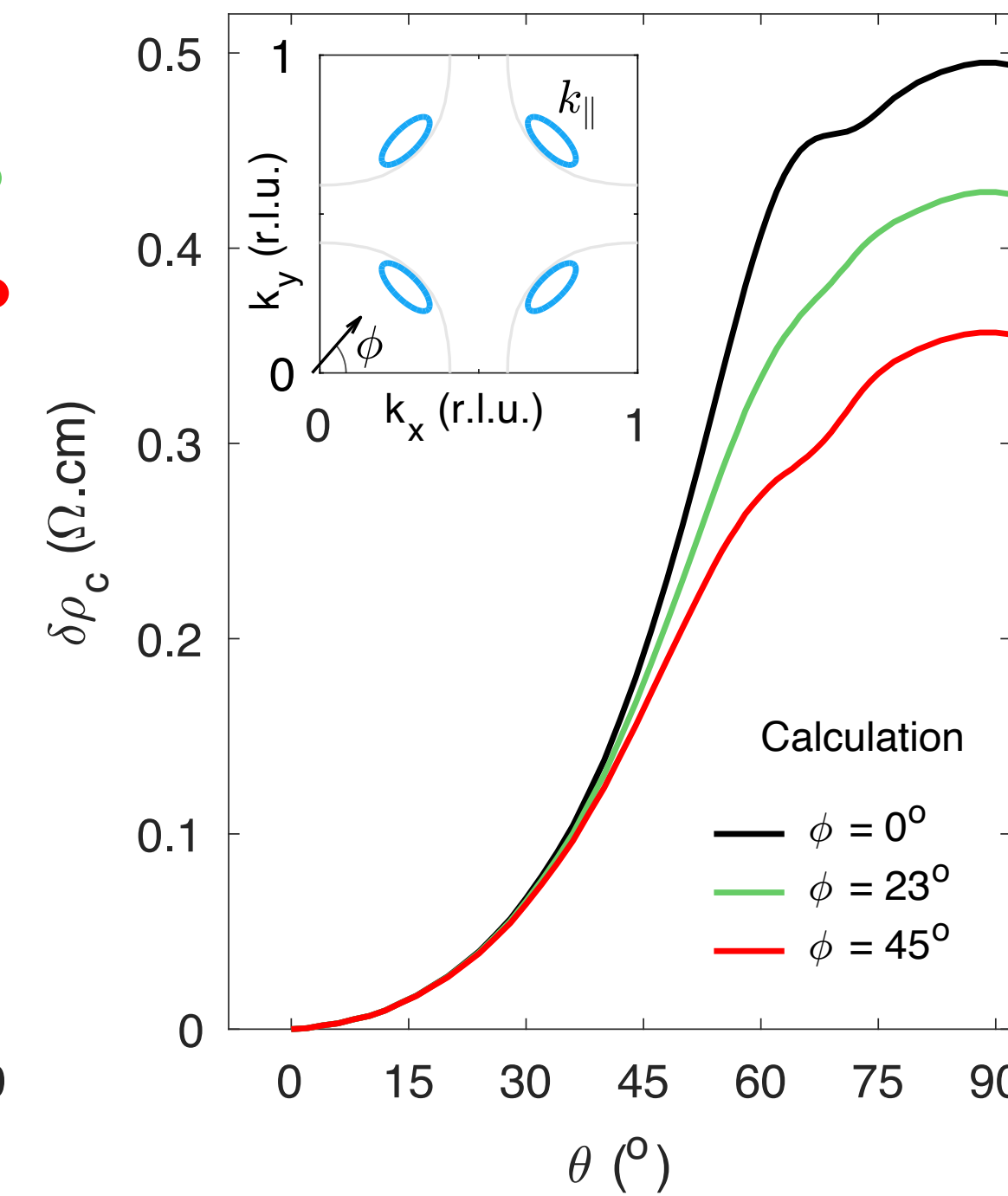
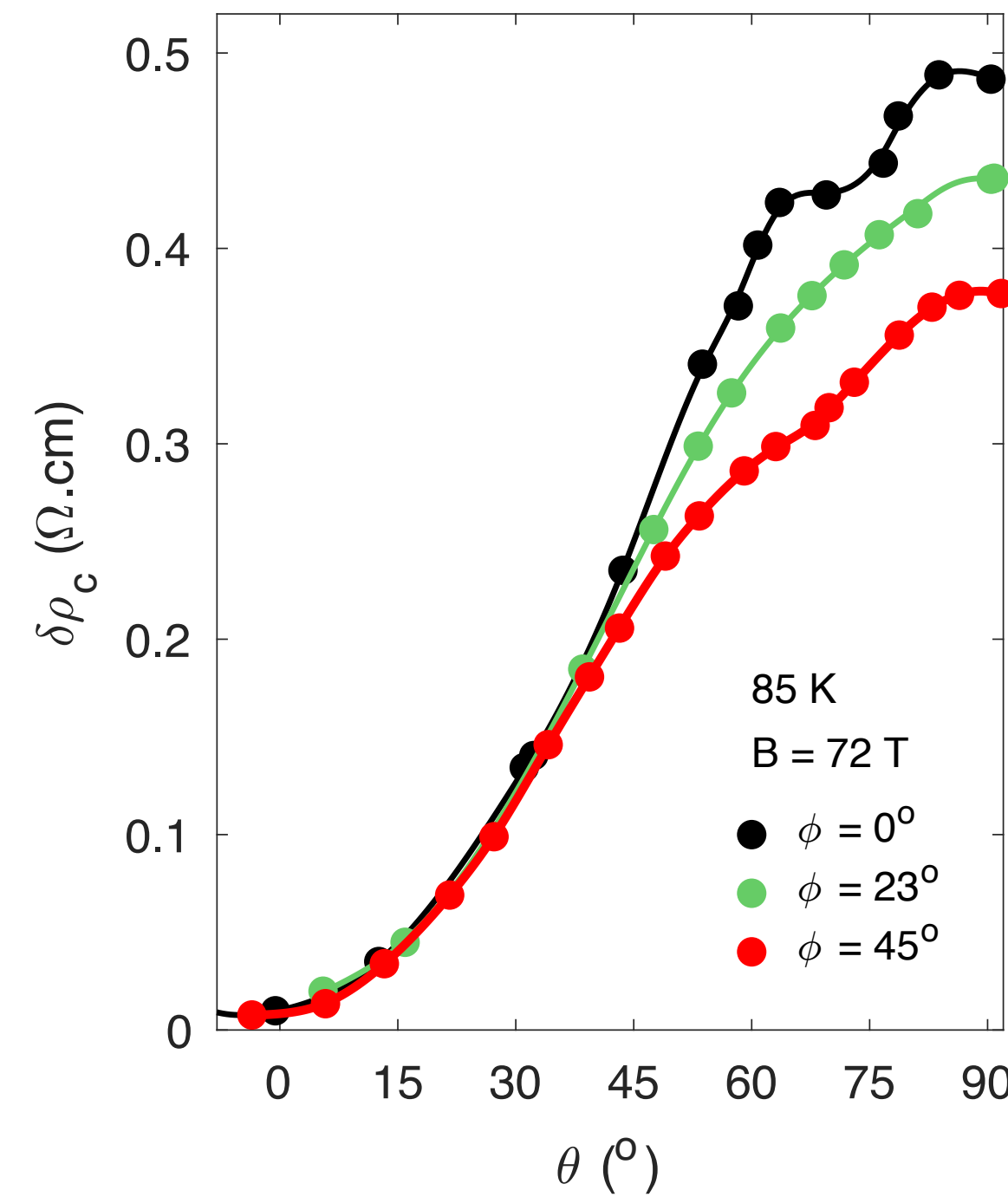
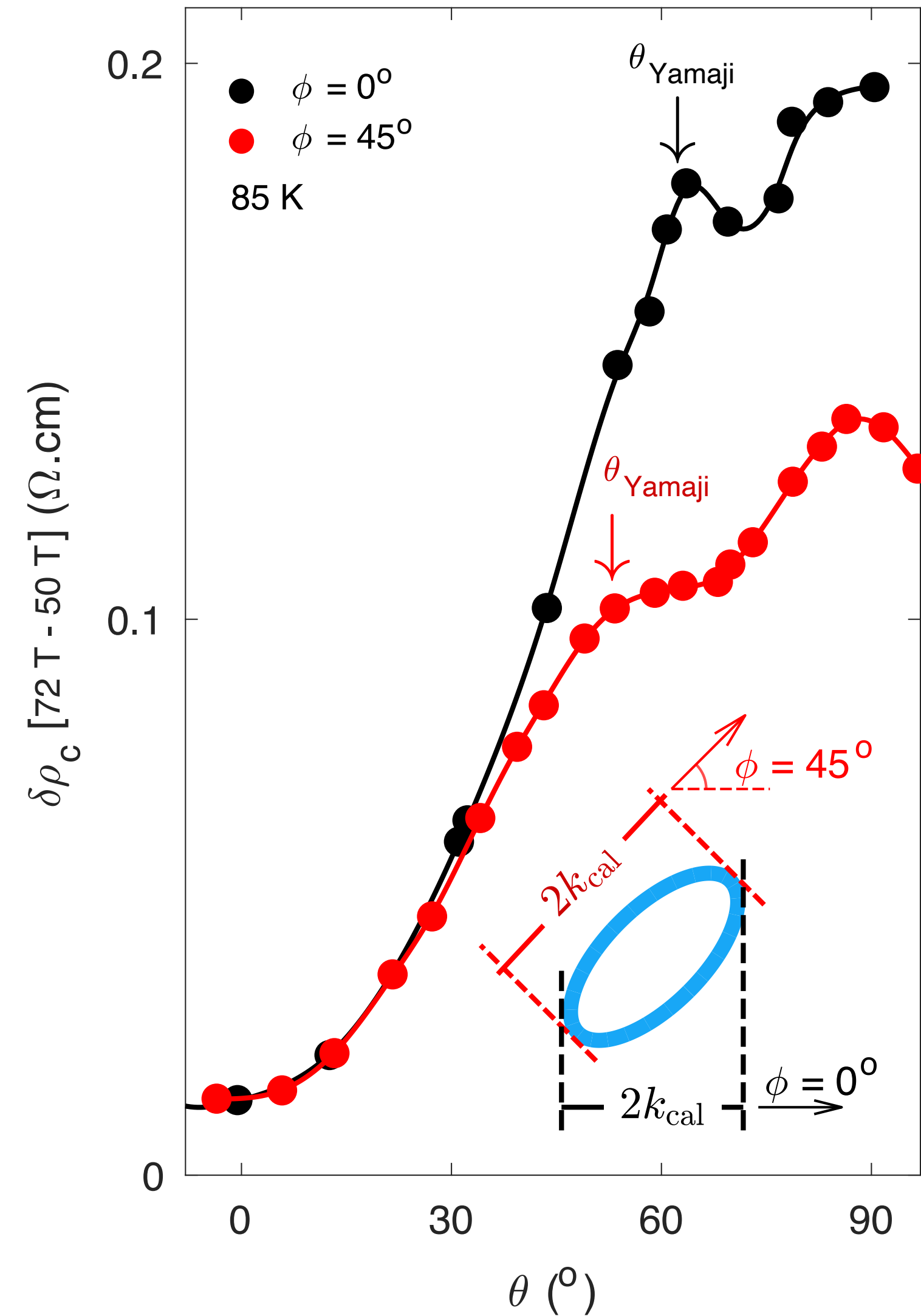
superconductor

Mun K. Chan<sup>1</sup>✉, Katherine A. Schreiber<sup>1</sup>, Oscar E. Ayala-Valenzuela<sup>1</sup>,  
Eric D. Bauer<sup>2</sup>, Arkady Shekhter<sup>1</sup> & Neil Harrison<sup>1</sup>

nature physics

21, 1753 (2025)

Published online: 16 September 2025



Doping  
 $p = 0.1$

The observation of the Yamaji peak is evidence for small Fermi-surface pockets in the normal state of the pseudogap phase. The small size of the pockets, each estimated to occupy only 1.3% of the Brillouin zone area, **is not expected** given the absence of long-range broken translational symmetry.

(was expected by us!)

# Observation of the Yamaji effect in a cuprate superconductor

nature physics

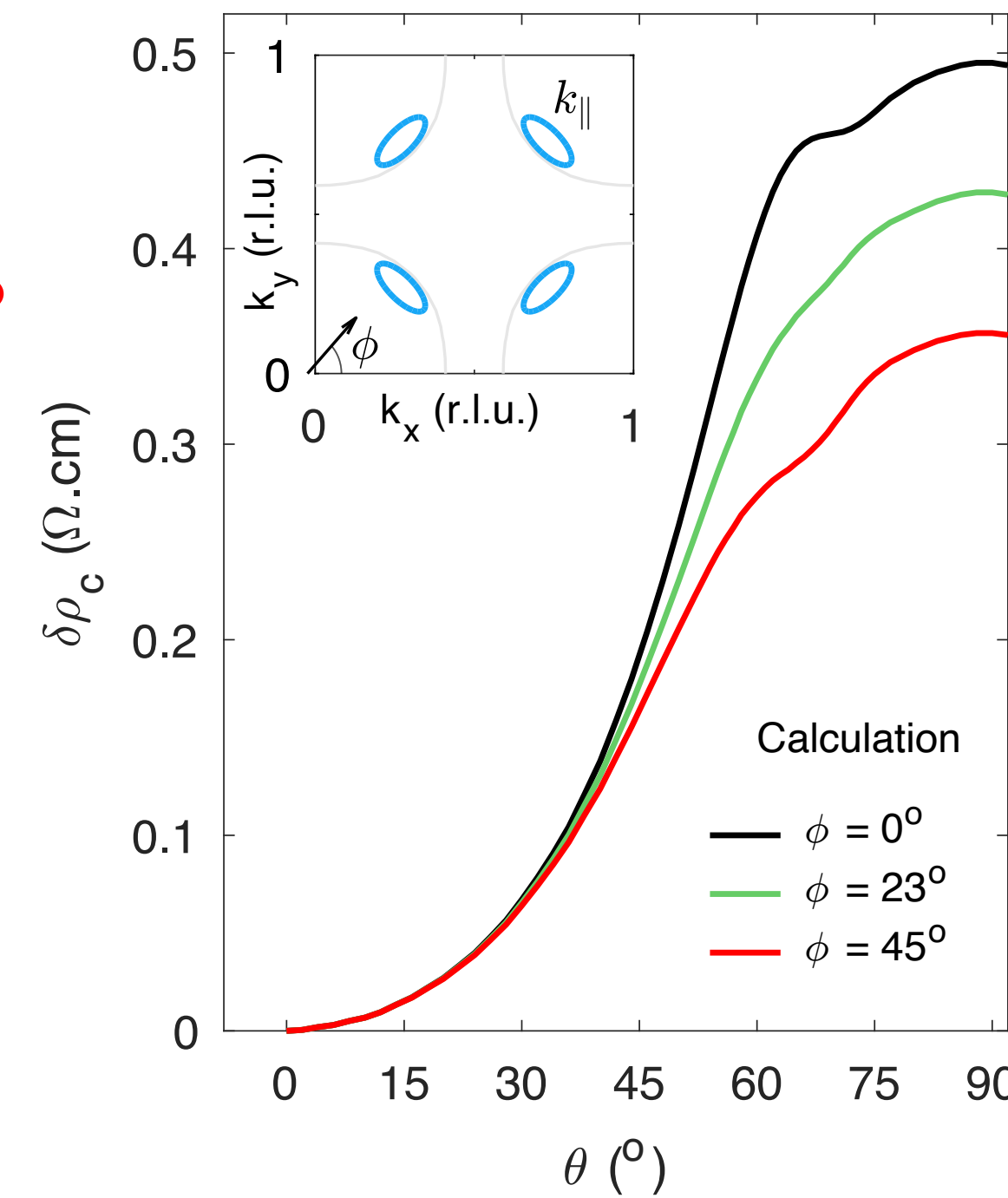
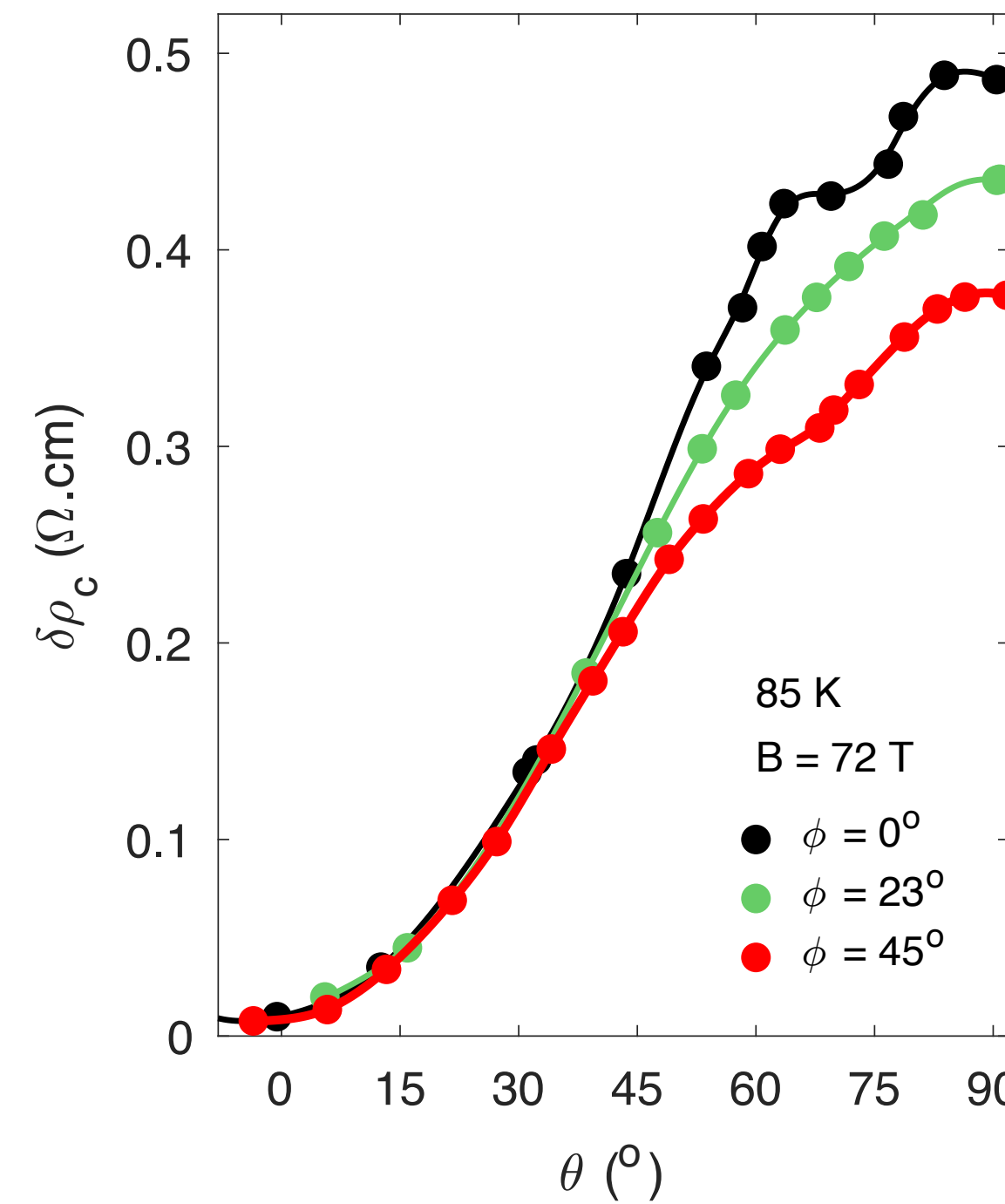
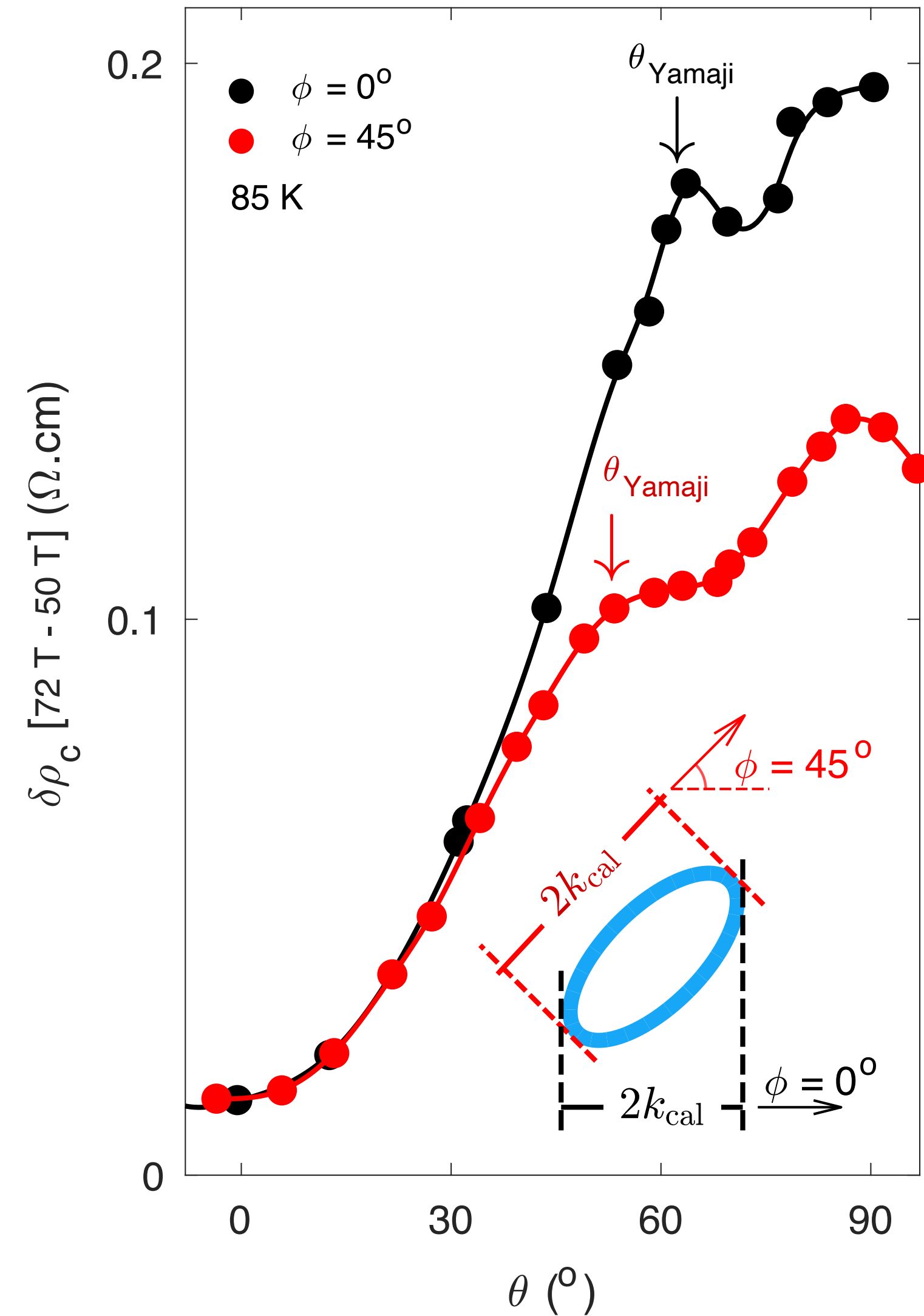
21, 1753 (2025)

superconductor

Mun K. Chan<sup>1</sup>, Katherine A. Schreiber<sup>1</sup>, Oscar E. Ayala-Valenzuela<sup>1</sup>,

Eric D. Bauer<sup>2</sup>, Arkady Shekhter<sup>1</sup> & Neil Harrison<sup>1</sup>

Published online: 16 September 2025



Doping  
 $p = 0.1$

The observation of the Yamaji peak is evidence for small Fermi-surface pockets in the normal state of the pseudogap phase. The small size of the pockets, each estimated to occupy only 1.3% of the Brillouin zone area, is not expected given the absence of long-range broken translational symmetry.

Predicted FL\* pocket fraction =  $p/8 = 1.25\%$  !

Fluctuating AF metal fraction =  $p/4 = 2.5\%$ .

( $p/8$  also in Yang-Rice-Zhang ansatz, Peter Johnson photoemission, and Jenny Hoffman and Seamus Davis STMs; Stanescu-Kotliar)

Jing-Yu Zhao, S. Chatterjee, S. S., Ya-Hui Zhang, arXiv:2510.13943

# Observation of the Yamaji effect in a cuprate superconductor

nature physics

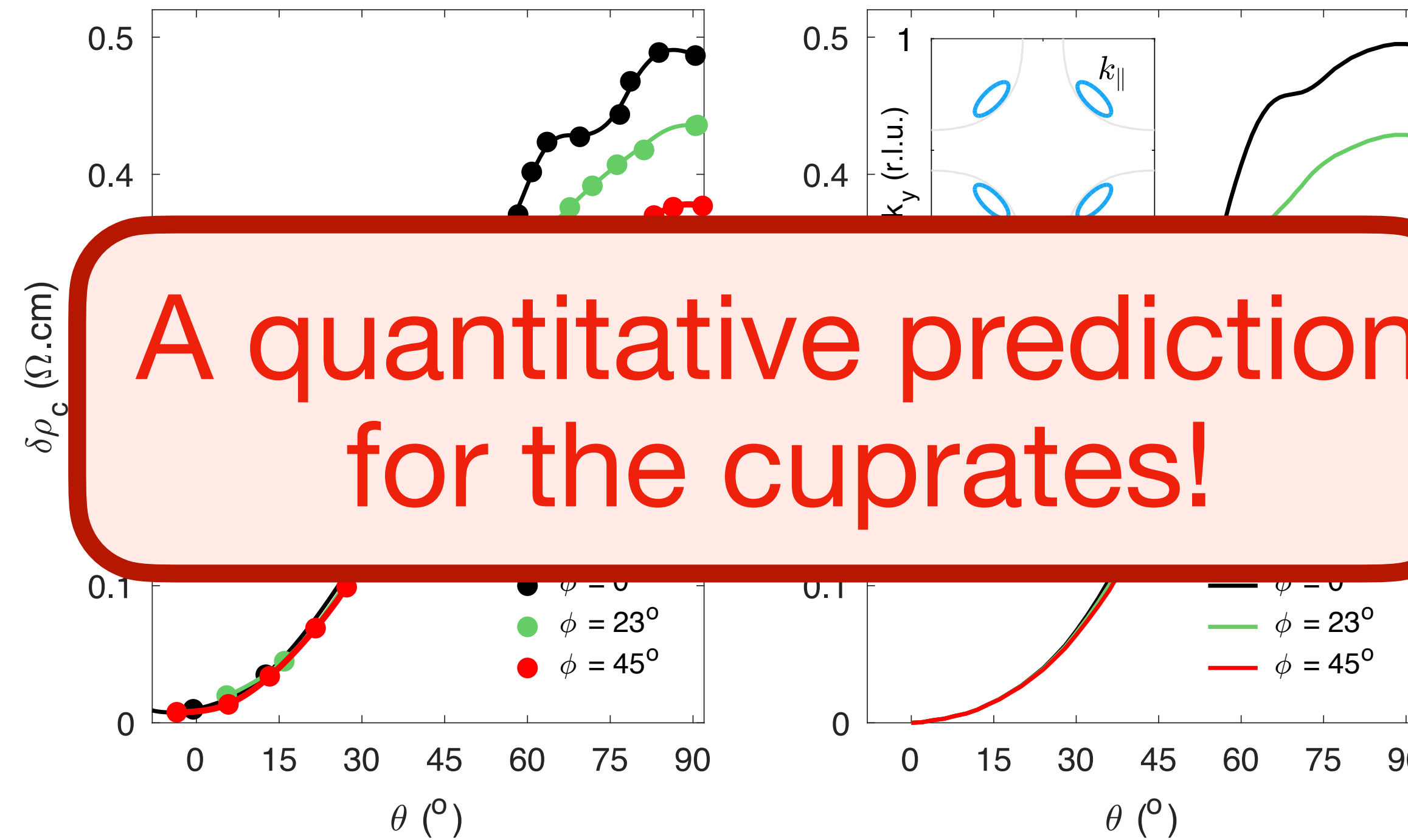
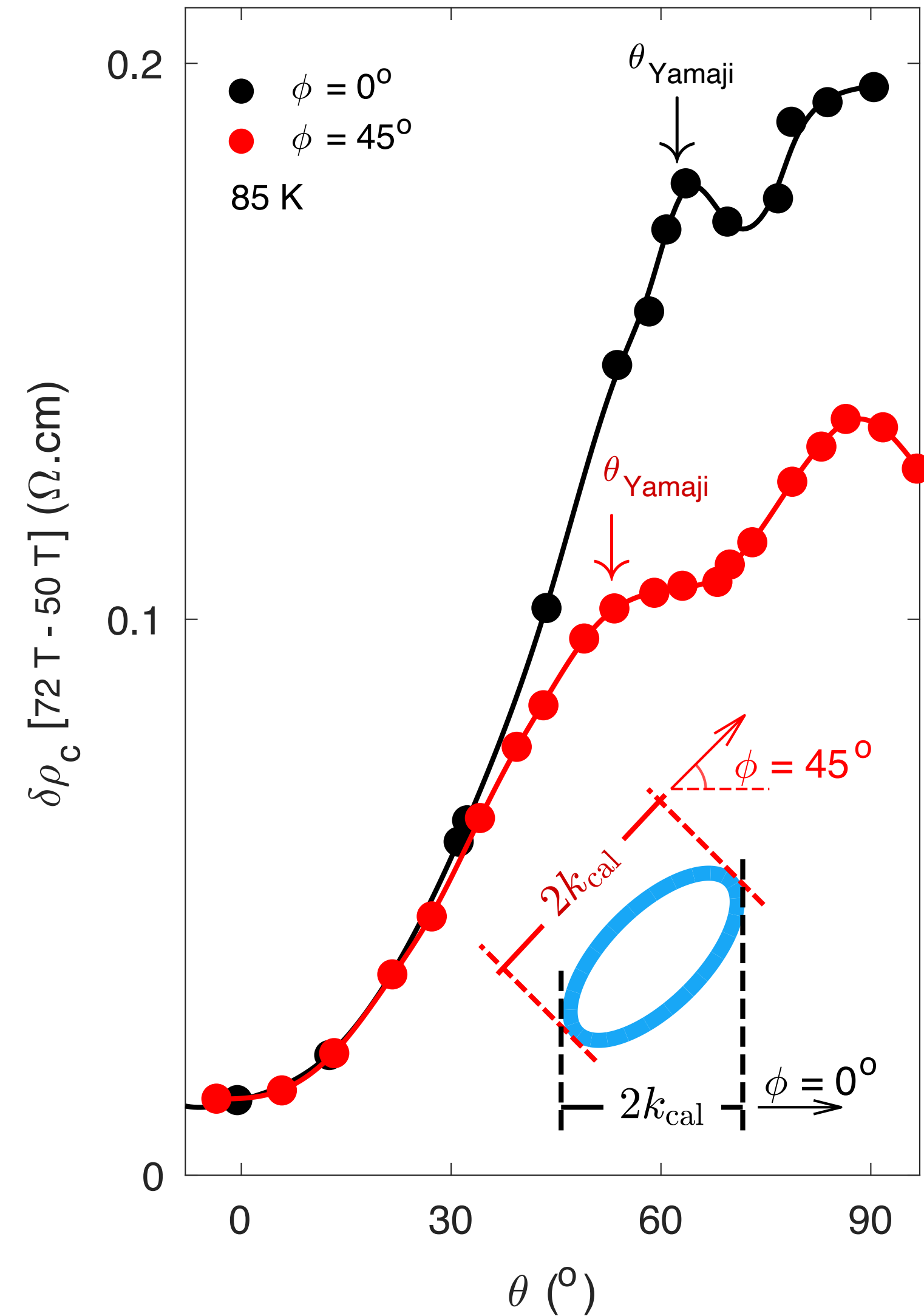
21, 1753 (2025)

superconductor

Mun K. Chan<sup>1</sup>, Katherine A. Schreiber<sup>1</sup>, Oscar E. Ayala-Valenzuela<sup>1</sup>,

Eric D. Bauer<sup>2</sup>, Arkady Shekhter<sup>1</sup> & Neil Harrison<sup>1</sup>

Published online: 16 September 2025



A quantitative prediction for the cuprates!

Doping  $p = 0.1$

The observation of the Yamaji peak is evidence for small Fermi-surface pockets in the normal state of the pseudogap phase. The small size of the pockets, each estimated to occupy only 1.3% of the Brillouin zone area, is not expected given the absence of long-range broken translational symmetry.

Predicted FL\* pocket fraction =  $p/8 = 1.25\%$  !

Fluctuating AF metal fraction =  $p/4 = 2.5\%$ .

( $p/8$  also in Yang-Rice-Zhang ansatz, Peter Johnson photoemission, and Jenny Hoffman and Seamus Davis STMs; Stanescu-Kotliar)

Jing-Yu Zhao, S. Chatterjee, S. S., Ya-Hui Zhang, arXiv:2510.13943

# Observation of the Yamaji effect in a cuprate superconductor

nature physics

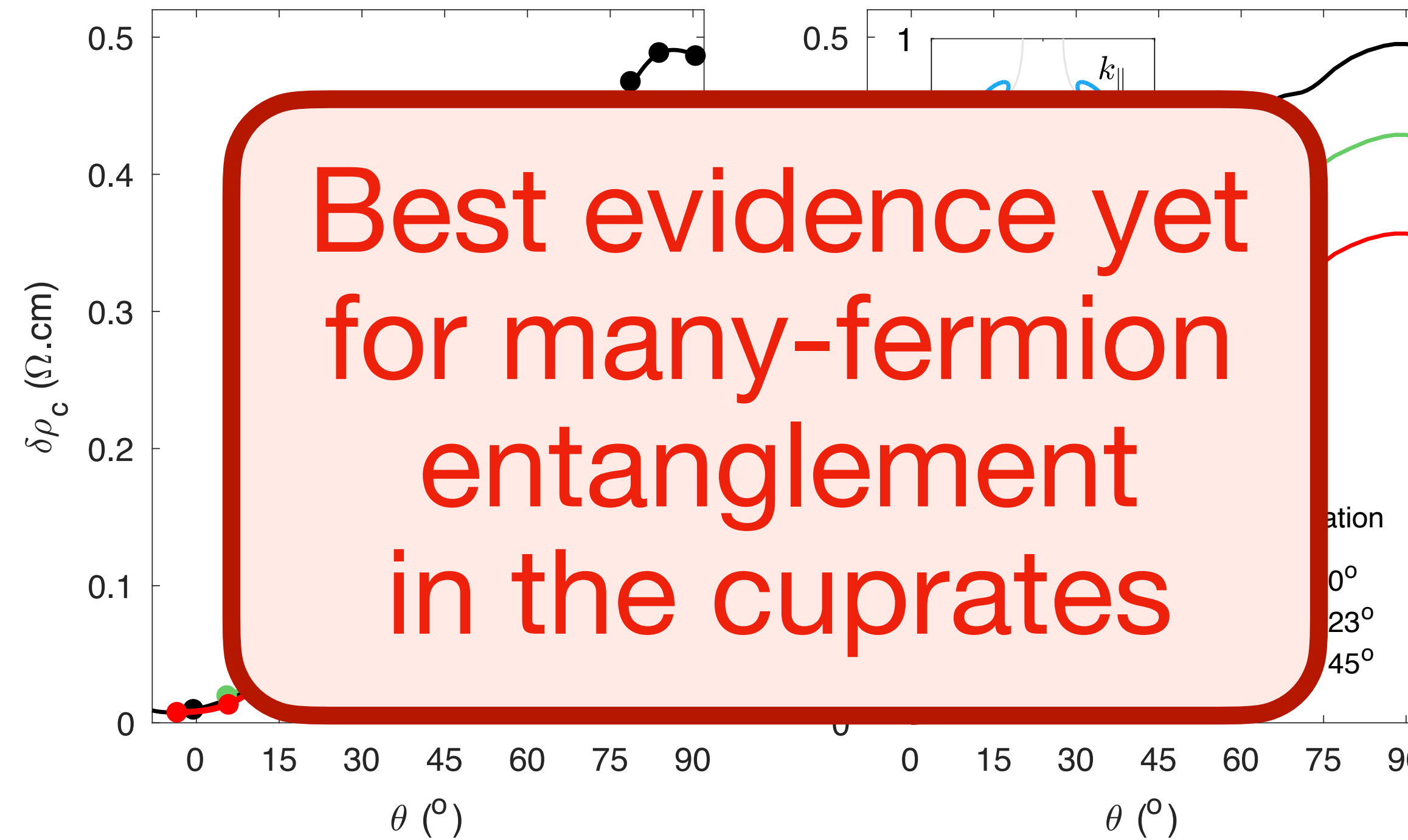
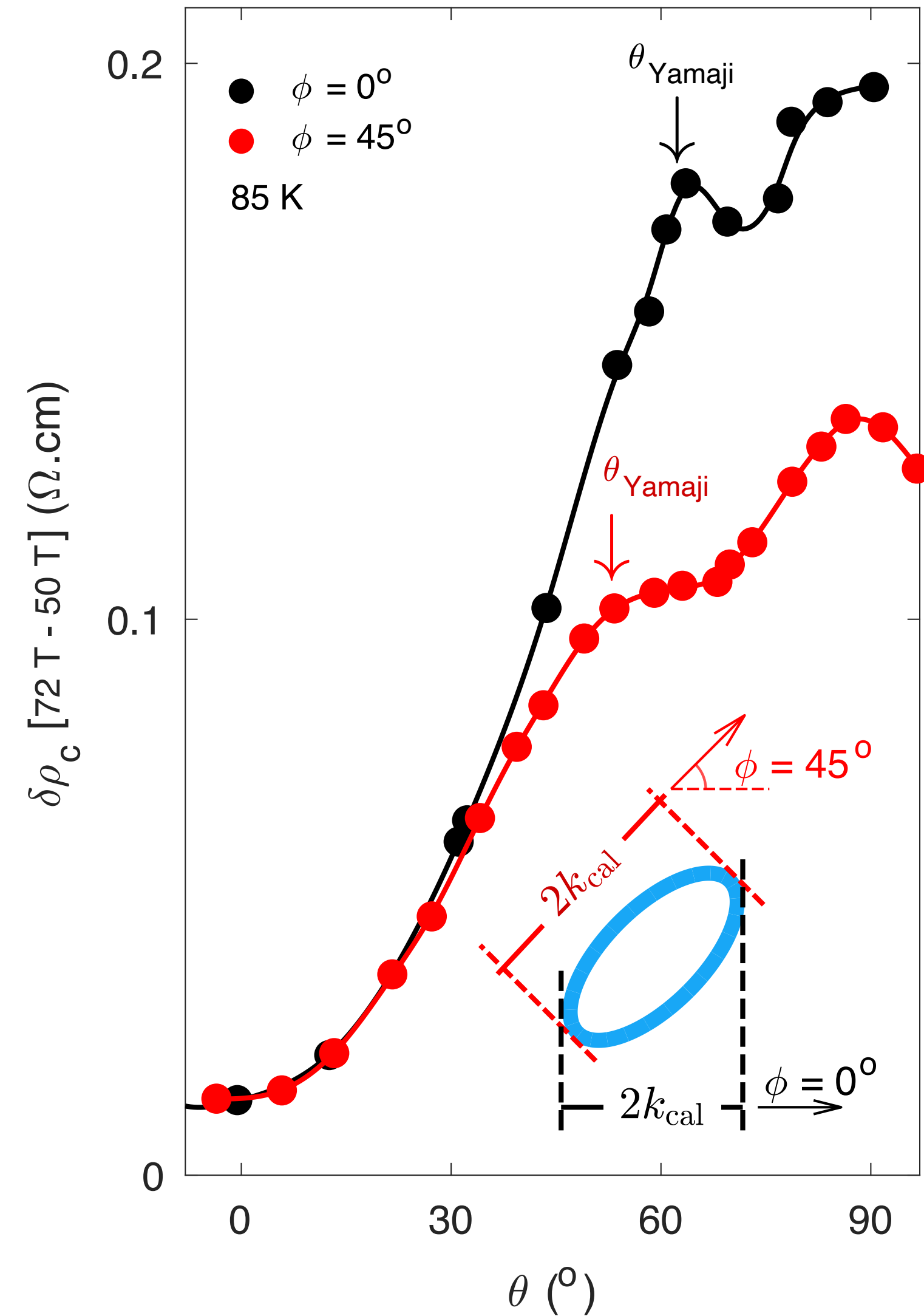
21, 1753 (2025)

superconductor

Mun K. Chan <sup>1</sup>✉, Katherine A. Schreiber<sup>1</sup>, Oscar E. Ayala-Valenzuela <sup>1</sup>,

Eric D. Bauer <sup>2</sup>, Arkady Shekhter <sup>1</sup> & Neil Harrison <sup>1</sup>

Published online: 16 September 2025



Doping  
 $p = 0.1$

The observation of the Yamaji peak is evidence for small Fermi-surface pockets in the normal state of the pseudogap phase. The small size of the pockets, each estimated to occupy only 1.3% of the Brillouin zone area, is not expected given the absence of long-range broken translational symmetry.

Predicted FL\* pocket fraction =  $p/8 = 1.25\%$  !

Fluctuating AF metal fraction =  $p/4 = 2.5\%$ .

( $p/8$  also in Yang-Rice-Zhang ansatz, Peter Johnson photoemission, and Jenny Hoffman and Seamus Davis STMs; Stanescu-Kotliar)

Jing-Yu Zhao, S. Chatterjee, S. S., Ya-Hui Zhang, arXiv:2510.13943

Many fermion entanglement I:

Wavefunction for  $FL^*$

and

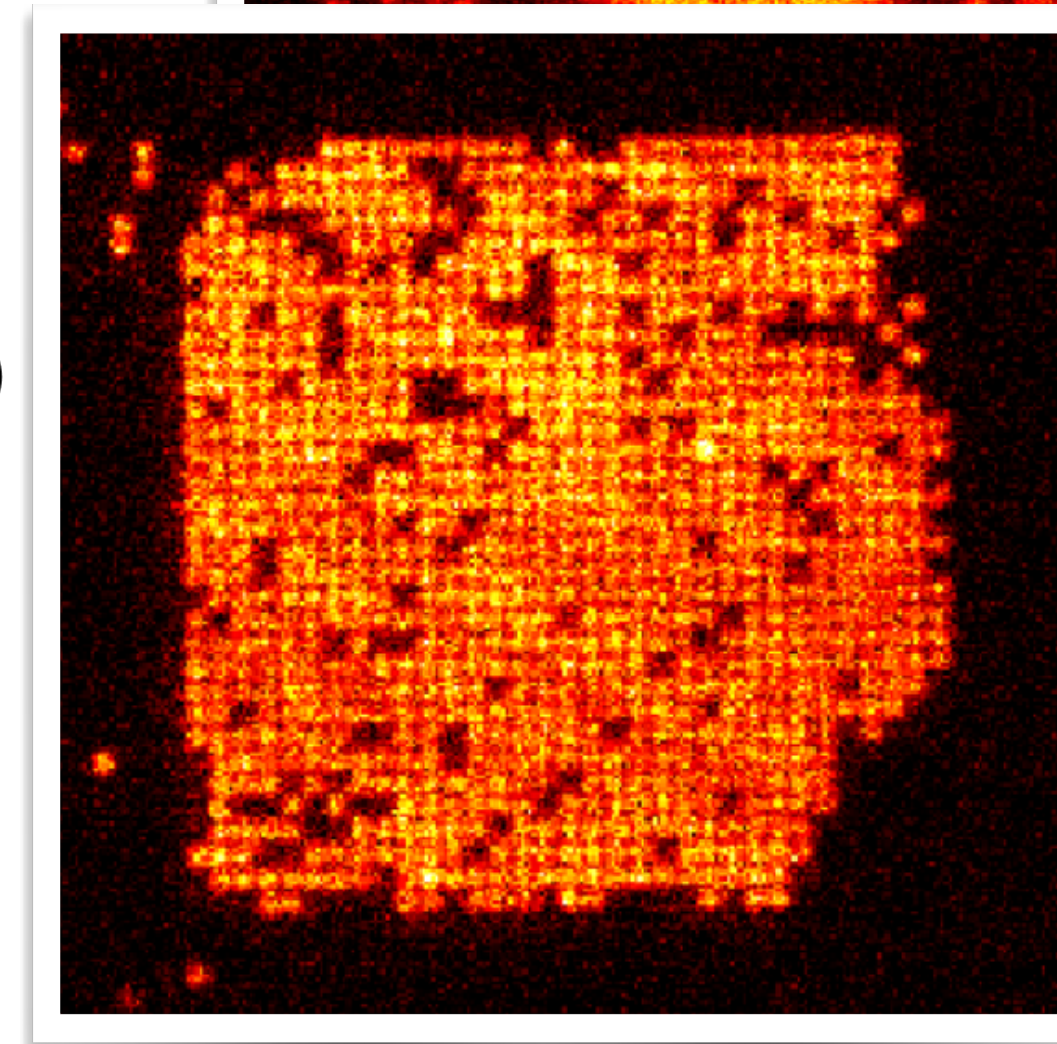
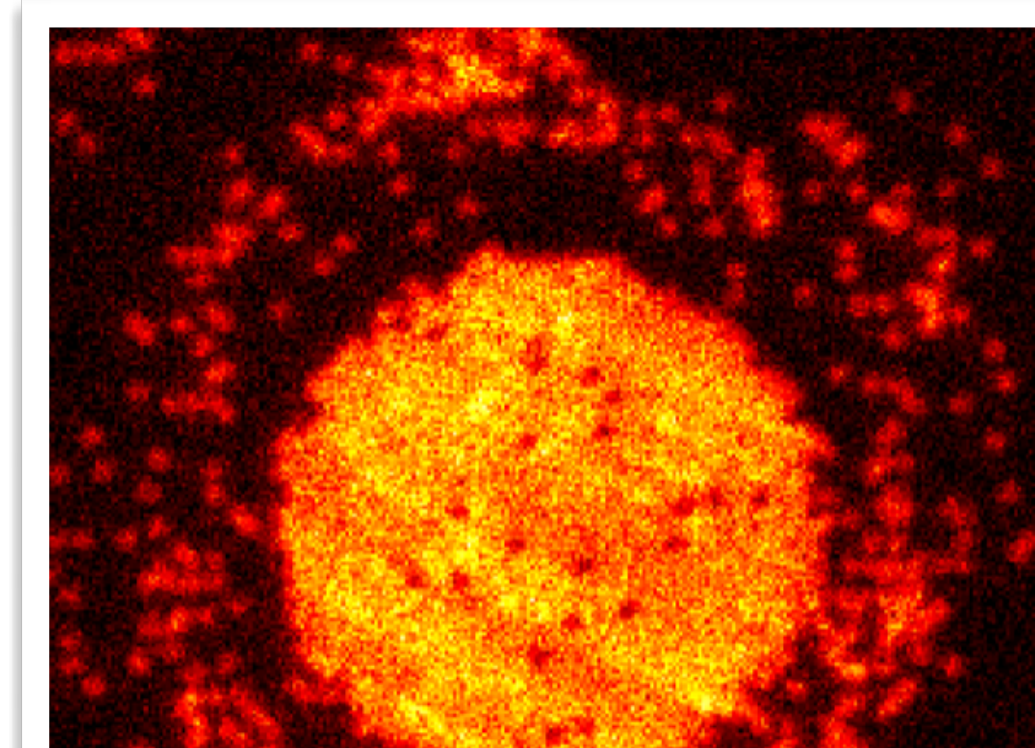
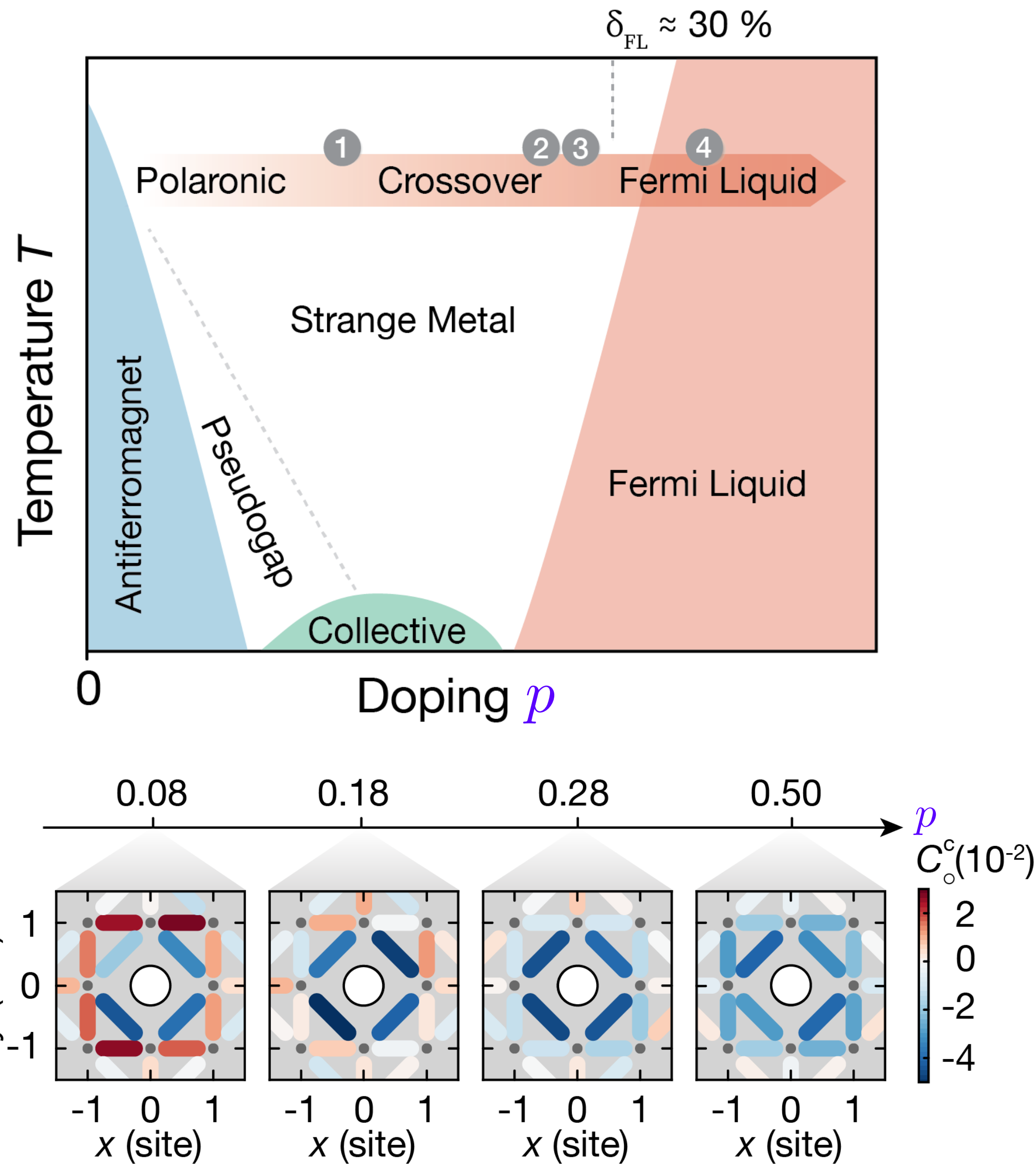
observations on ultracold atoms

# Microscopic evolution of doped Mott insulators from polaronic metal to Fermi liquid

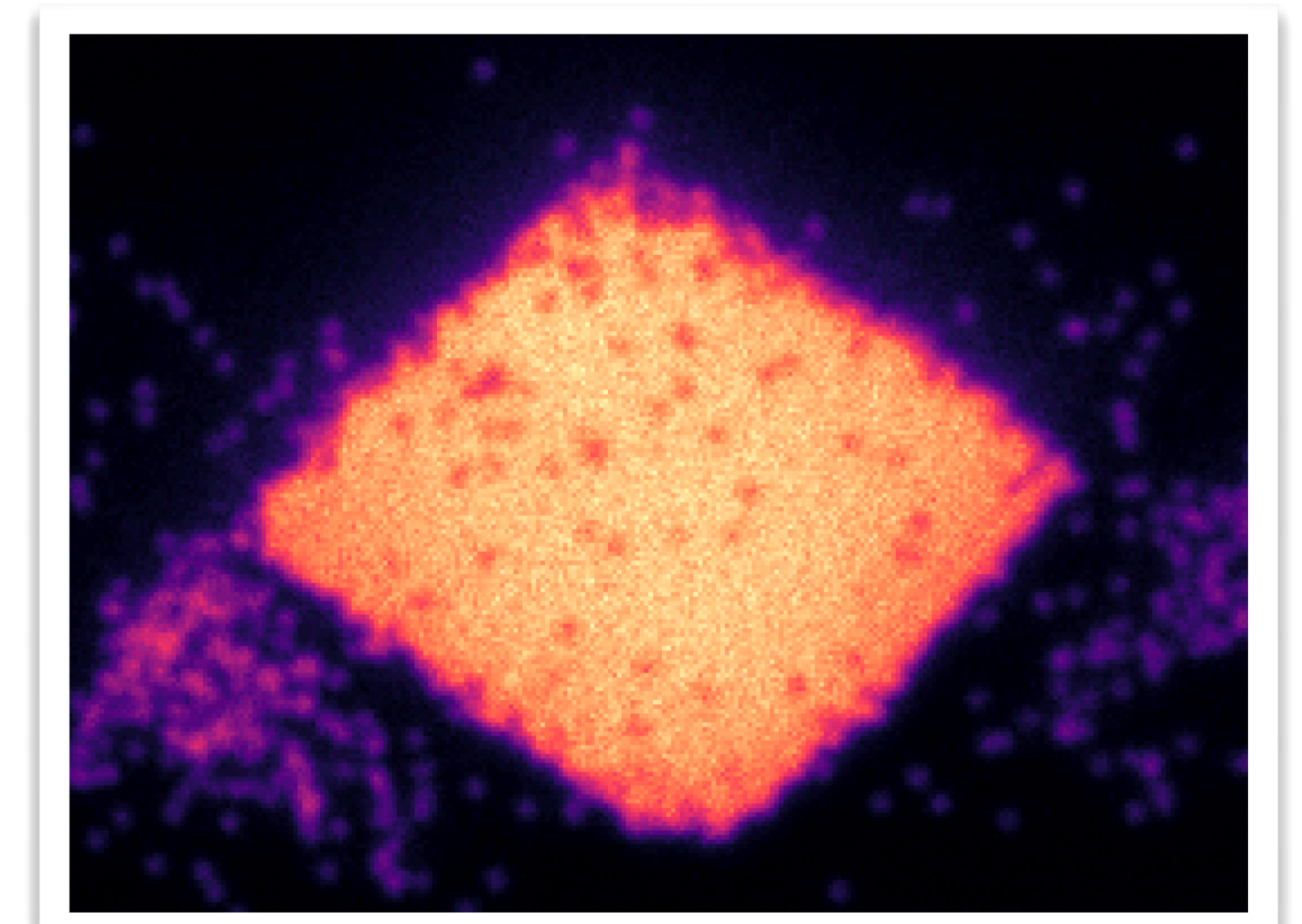
Joannis Koepsell, Dominik Bourgund, Pimonpan Sompert, Sarah Hirthe, Annabelle Bohrdt, Yao Wang, Fabian Grusdt, Eugene Demler, Guillaume Salomon, Christian Gross, Immanuel Bloch

*Science* **374** (2021) 82

Chalopin...Bloch, *PNAS* **123**, e2525539123 (2026)



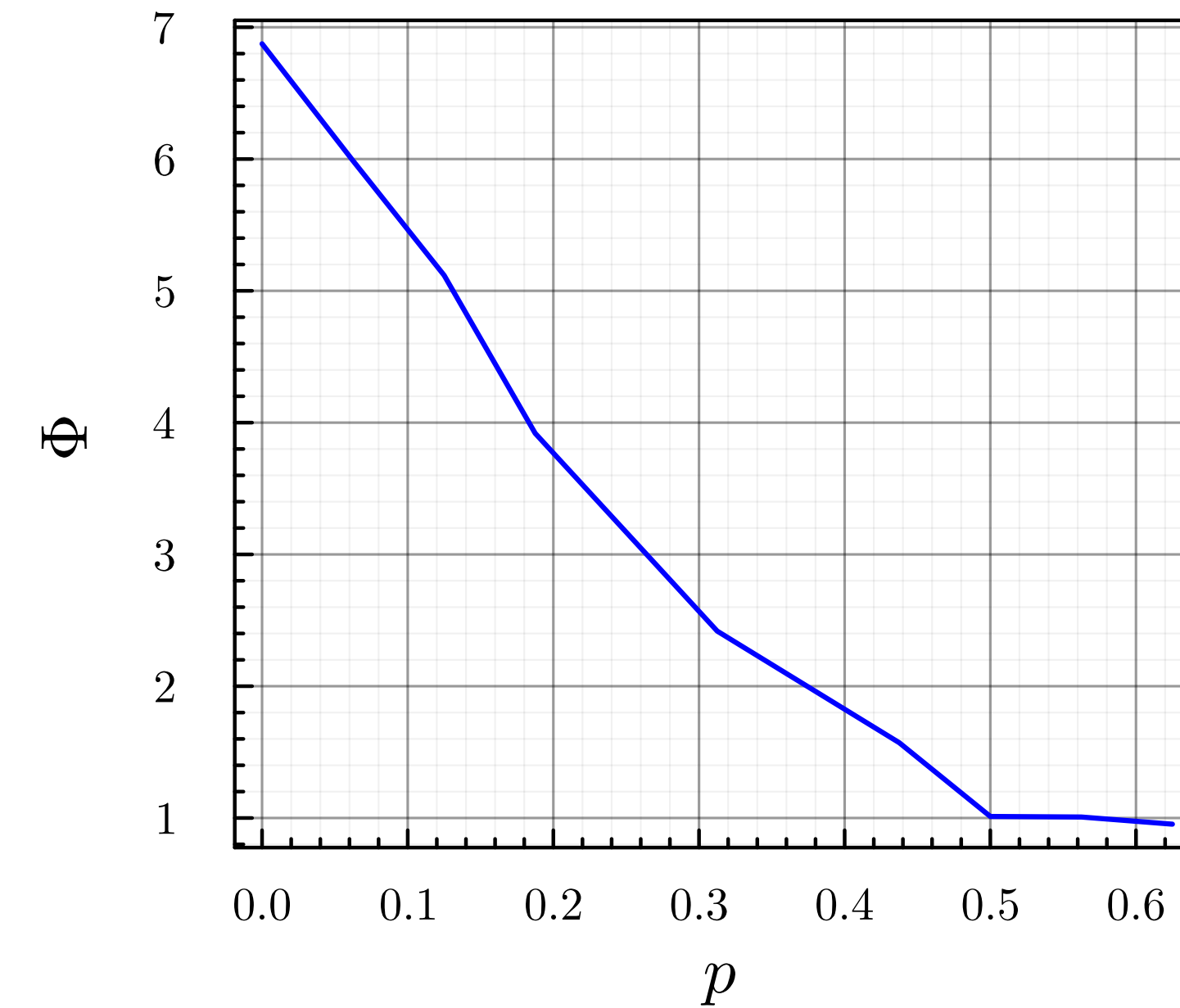
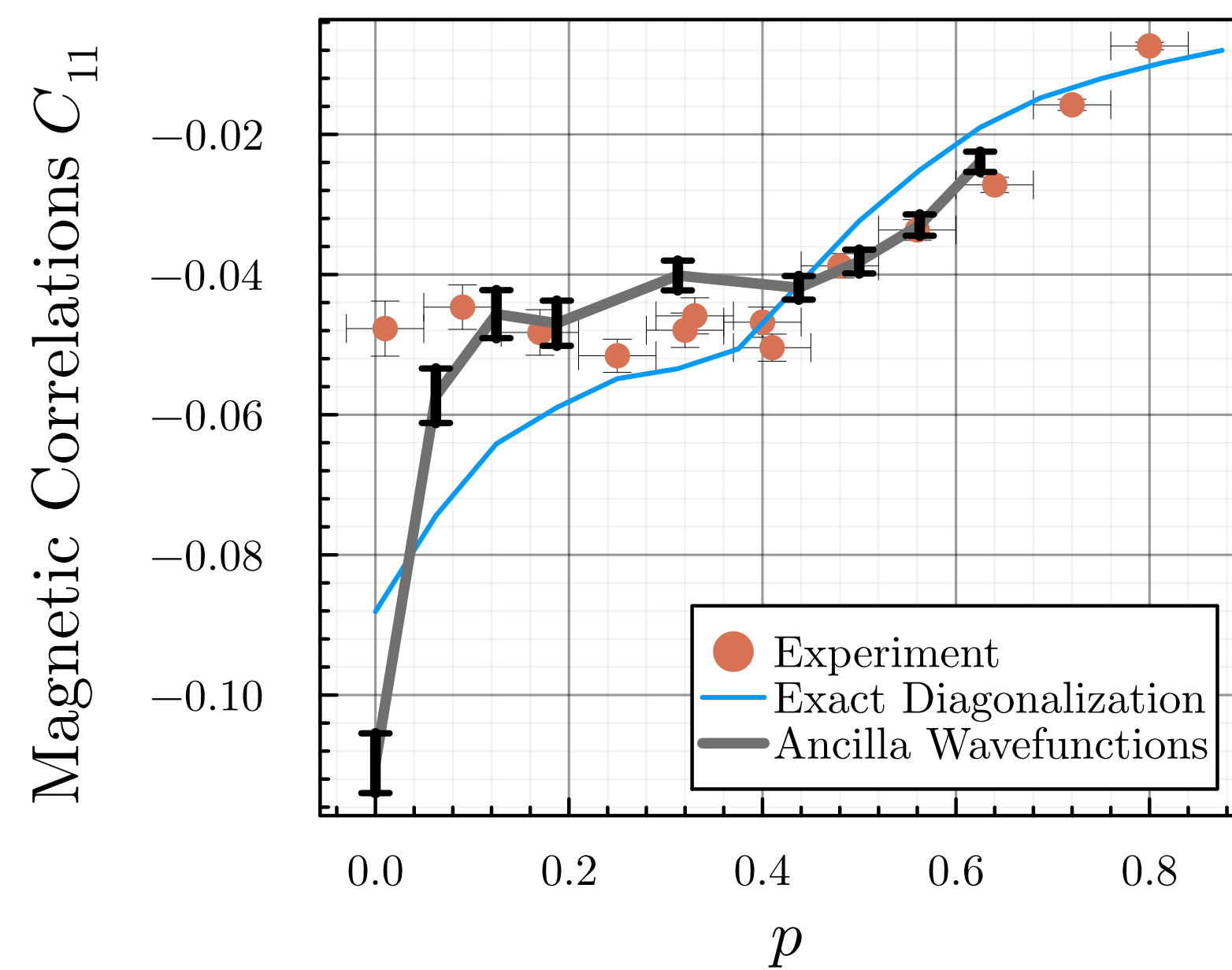
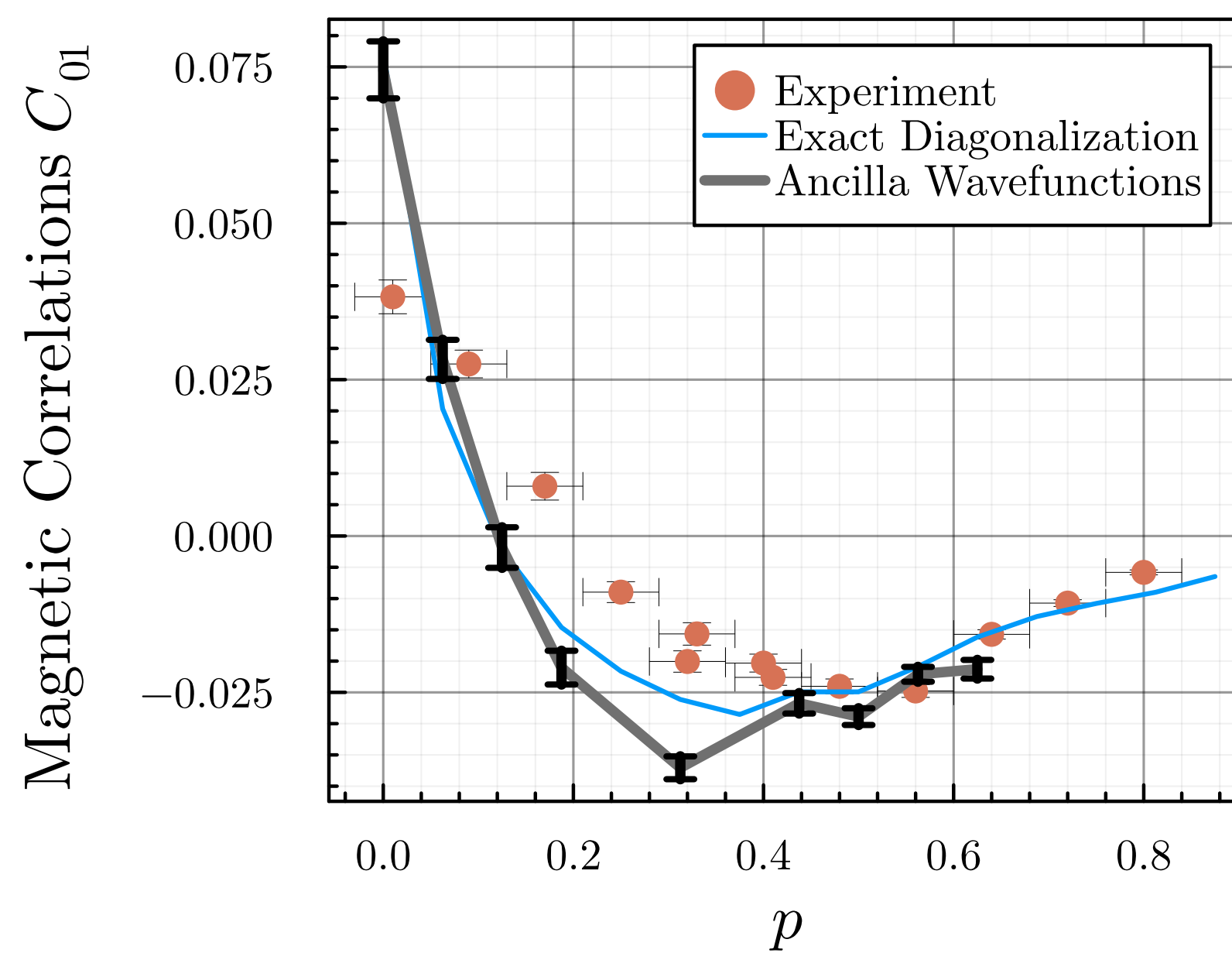
Rb Quantum Gas Microscope



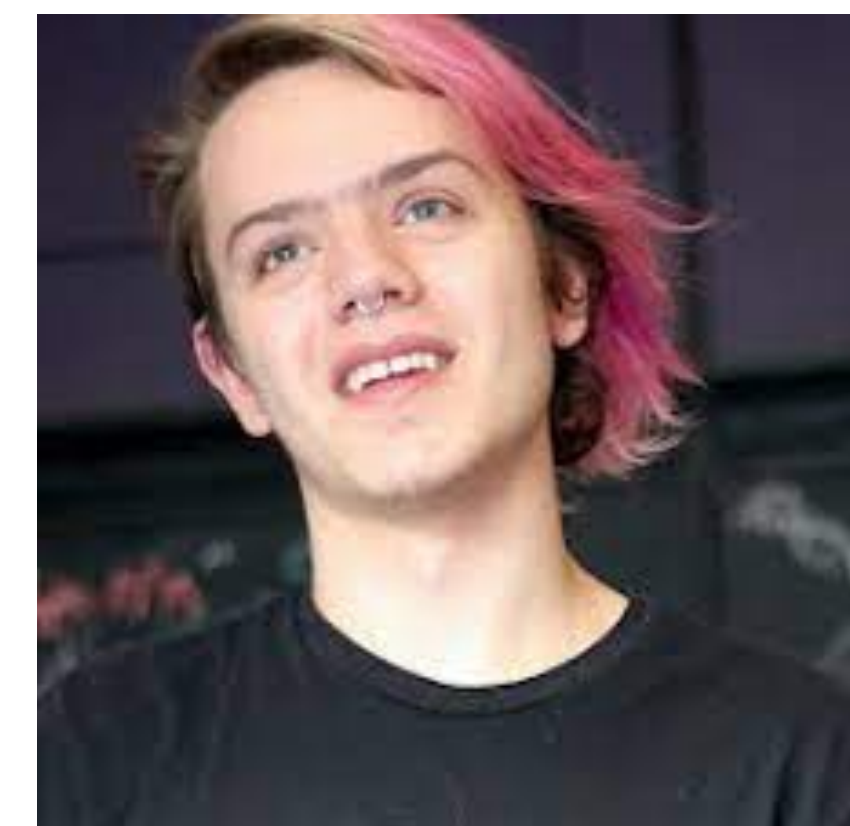
Cs Quantum Gas Microscope

see also: C. Chiu *et al.* *Phys. Rev. Lett.* **120**, 243201 (2018)  
 Idea: J.-S. Bernier *et al.* *Phys. Rev. A* **79**, 061601 (2009)  
 T.-L. Ho & Q. Zhou arXiv:0911.5506

# QMC for FL\* of Hubbard model



Quantum Monte Carlo on  
Ancilla Layer trial wavefunction  
with  $\Phi$  a variational parameter  
minimizing Hubbard Hamiltonian  
FL\*:  $\Phi \neq 0$  ; FL:  $\Phi = 0$



L. Shackleton and Shiwei Zhang, arXiv:2408.02190

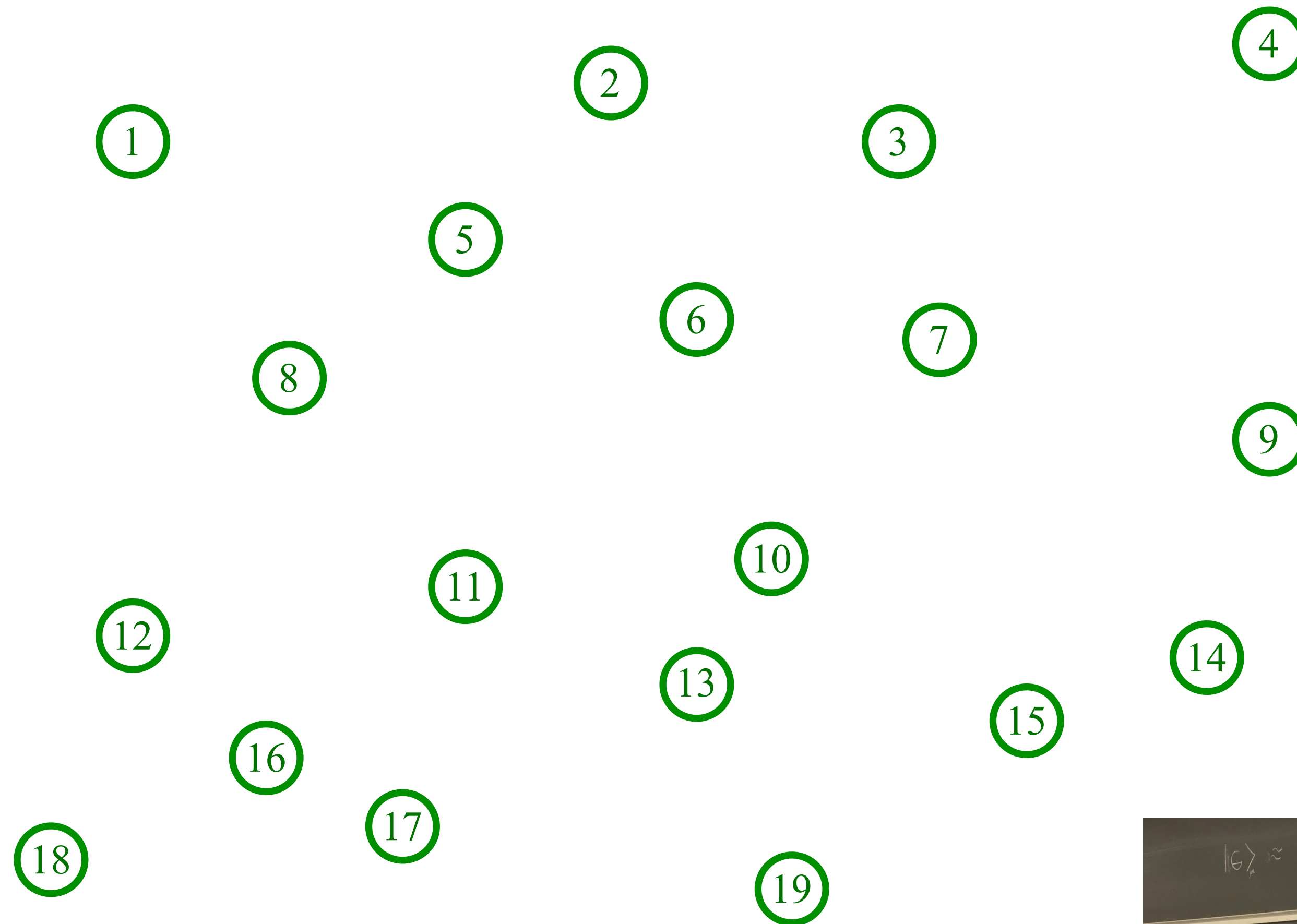
Tobias Müller, Yasir Iqbal, S.S., Ronny Thomale, PNAS **122**, e2504261122 (2025)

Many fermion entanglement II:

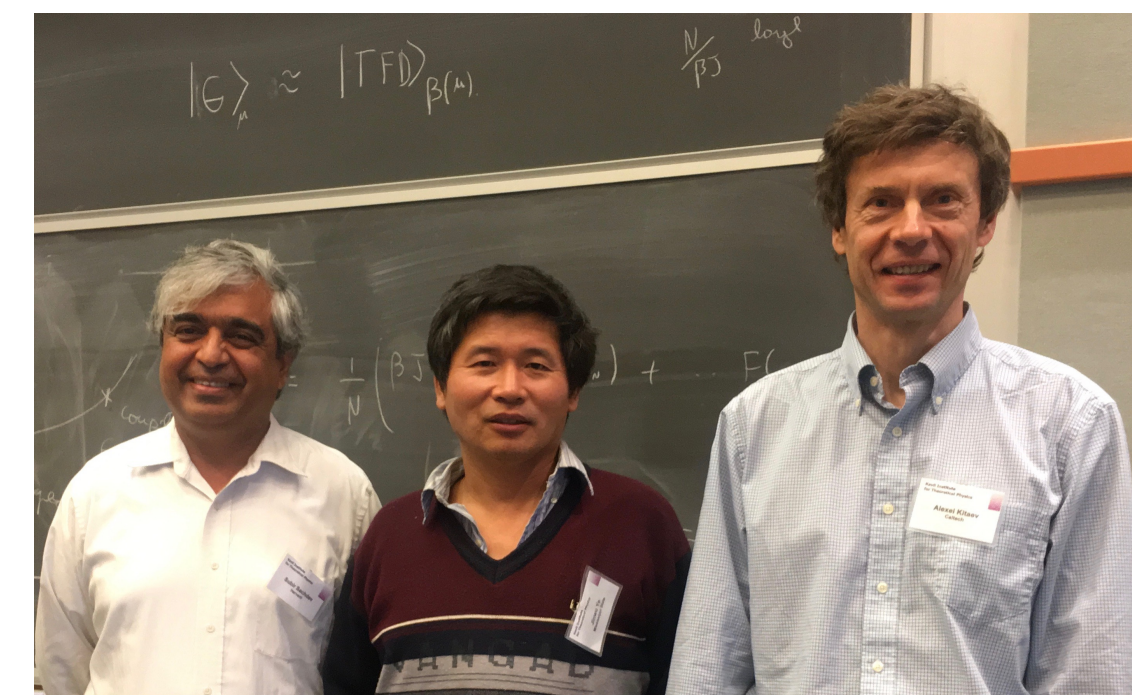
Sachdev-Ye-Kitaev  
model

# The SYK model

Sachdev, Ye (1993); Kitaev (2015)

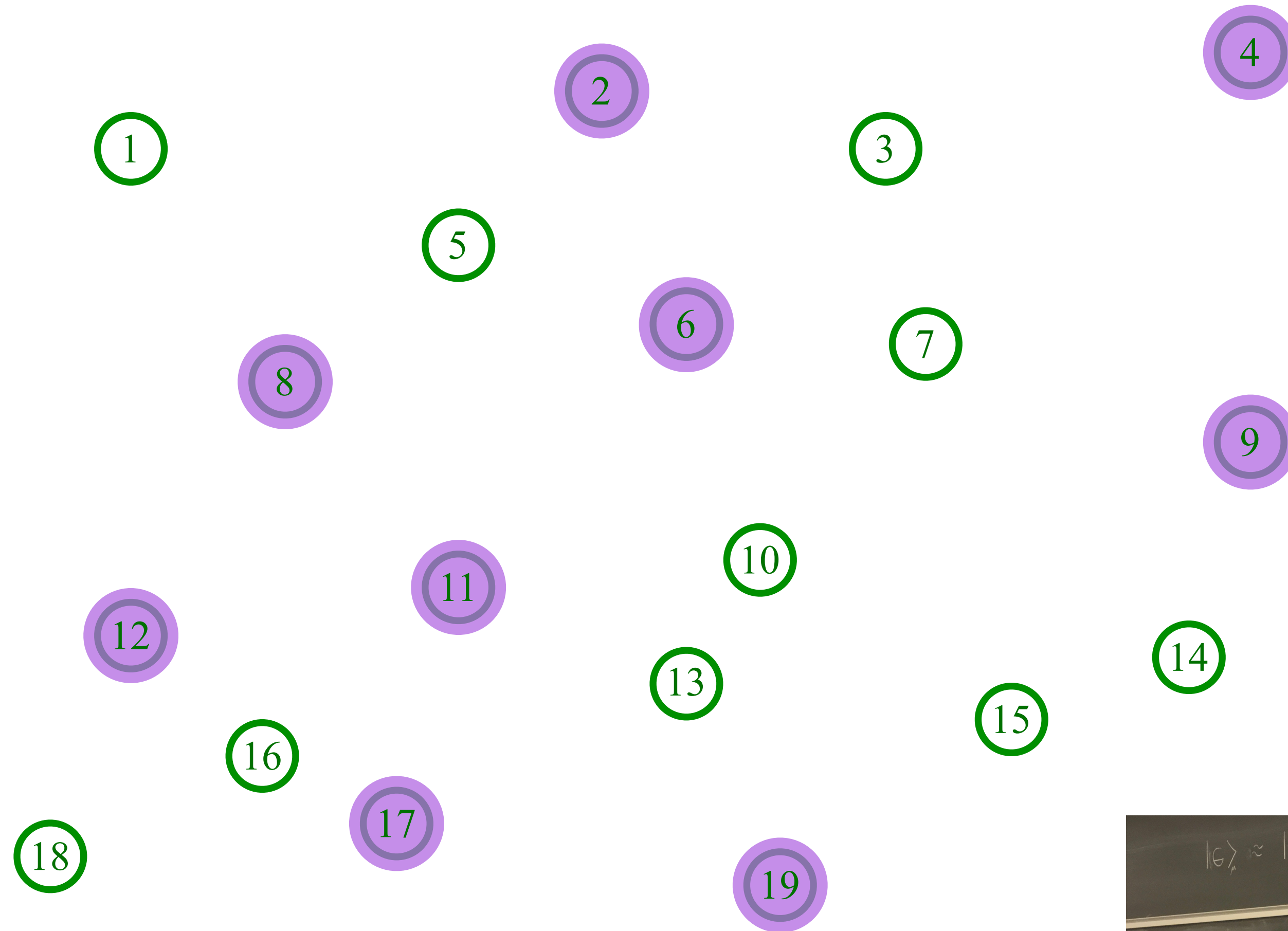


Pick a set of random positions

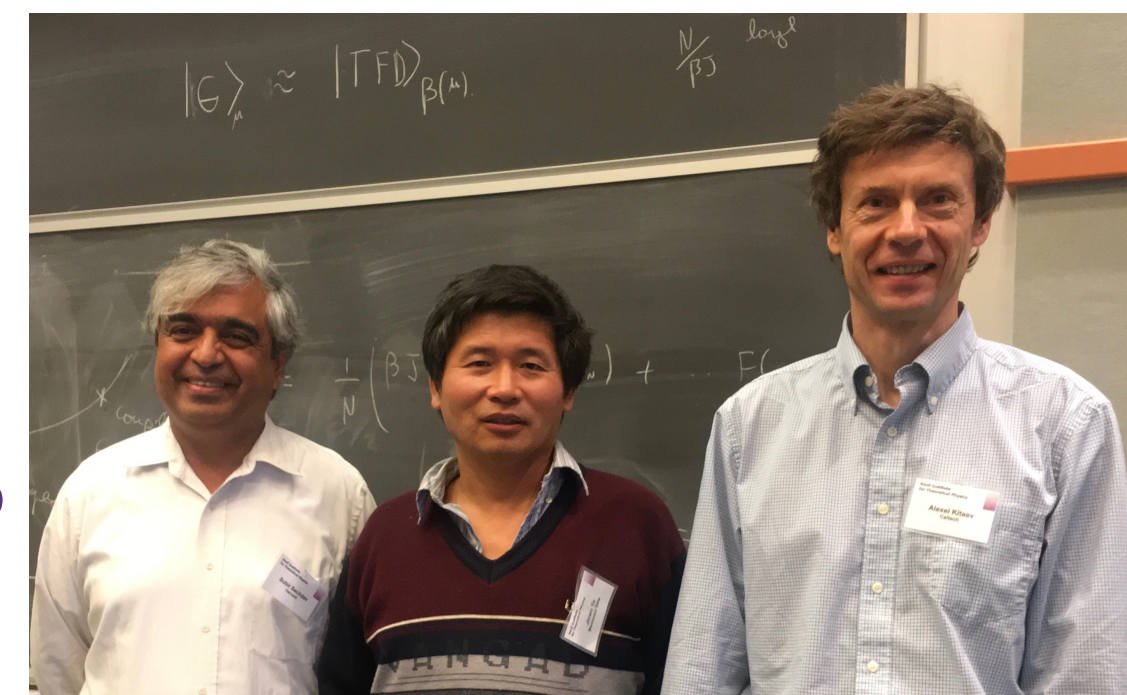


# The SYK model

Sachdev, Ye (1993); Kitaev (2015)



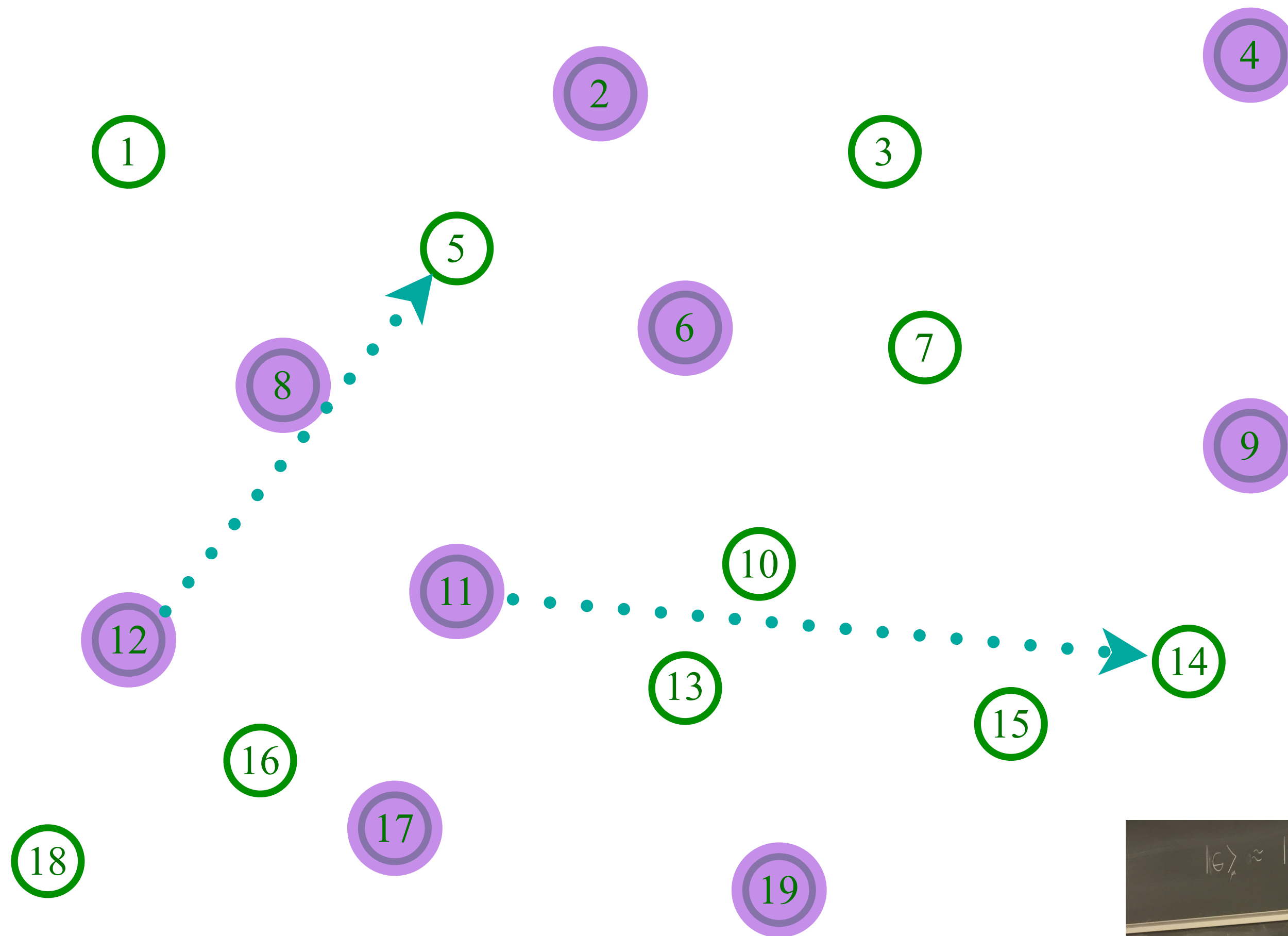
Place electrons randomly on some sites



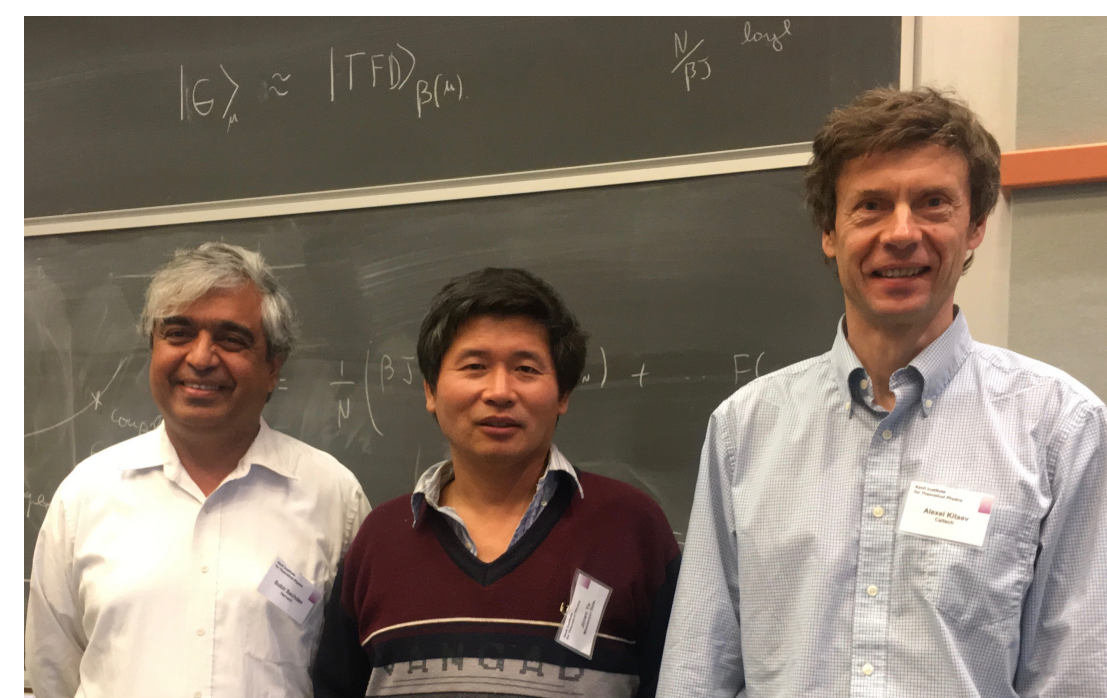
# The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{11,12;5,14}$$



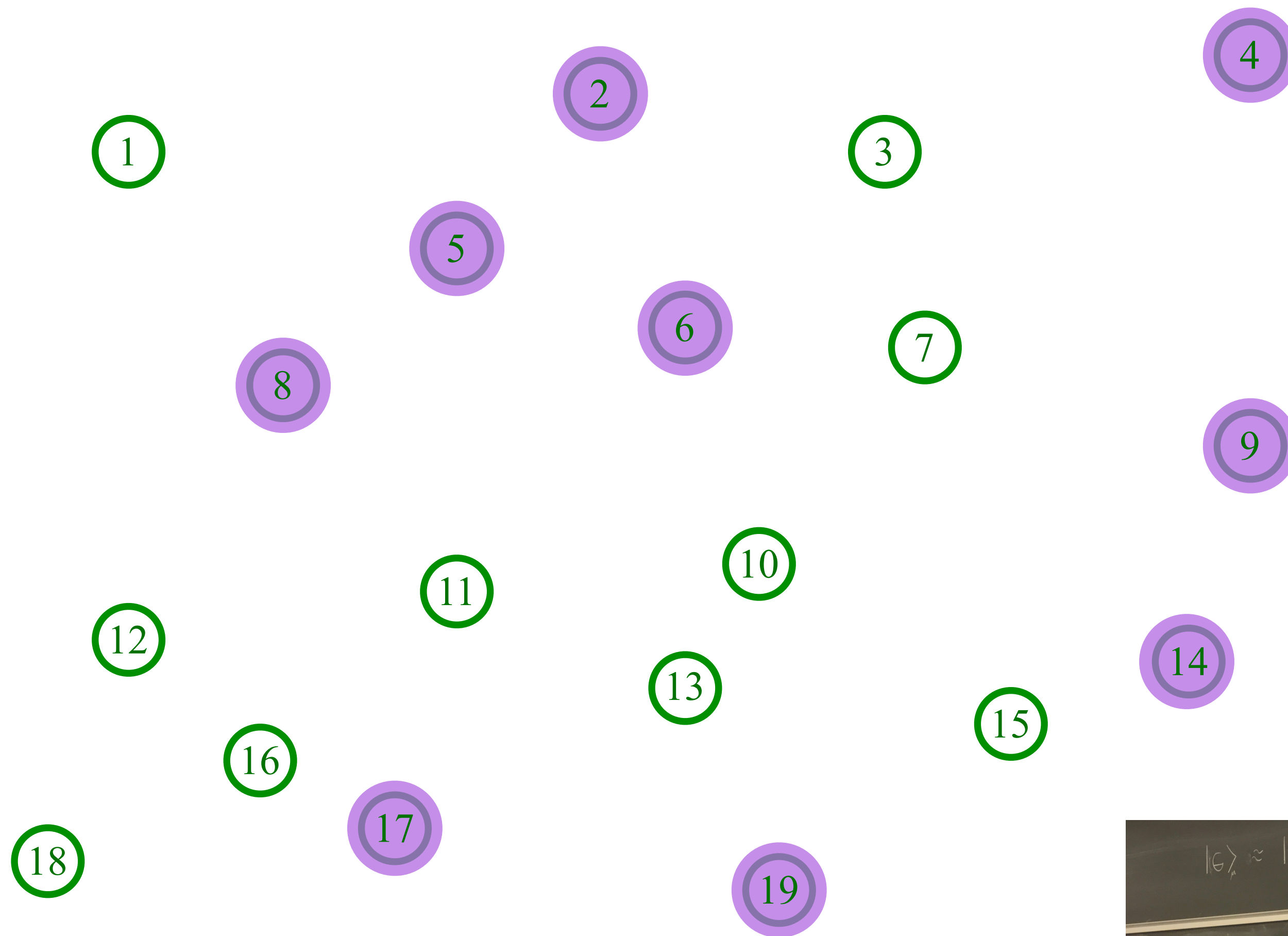
Place electrons randomly on some sites



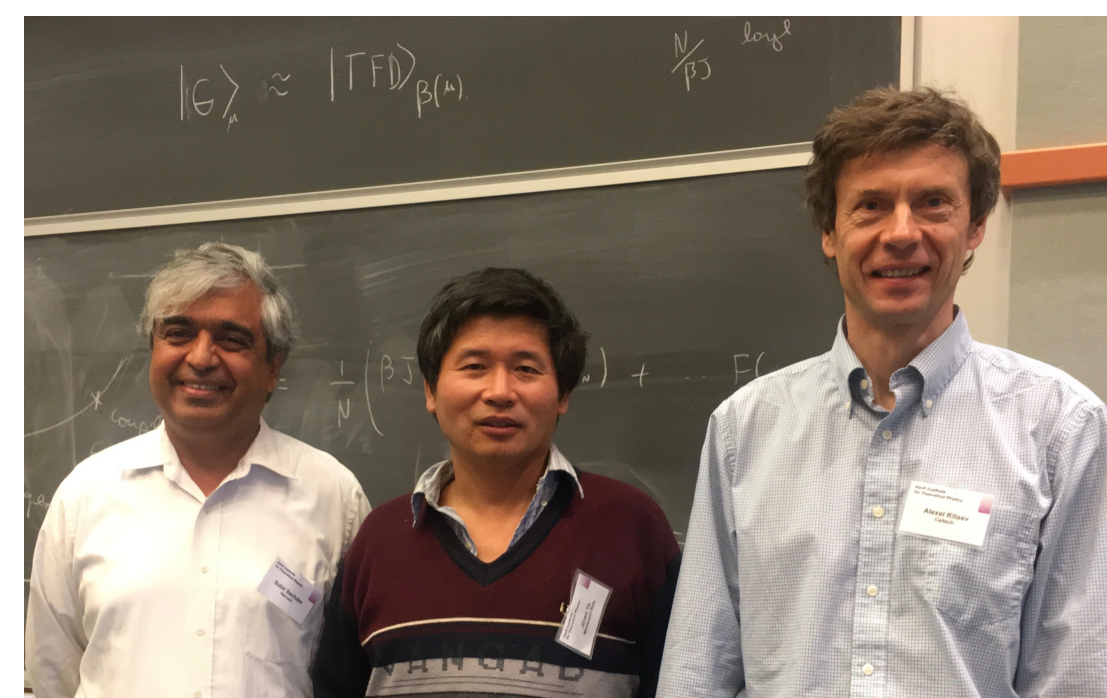
# The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{11,12;5,14}$$



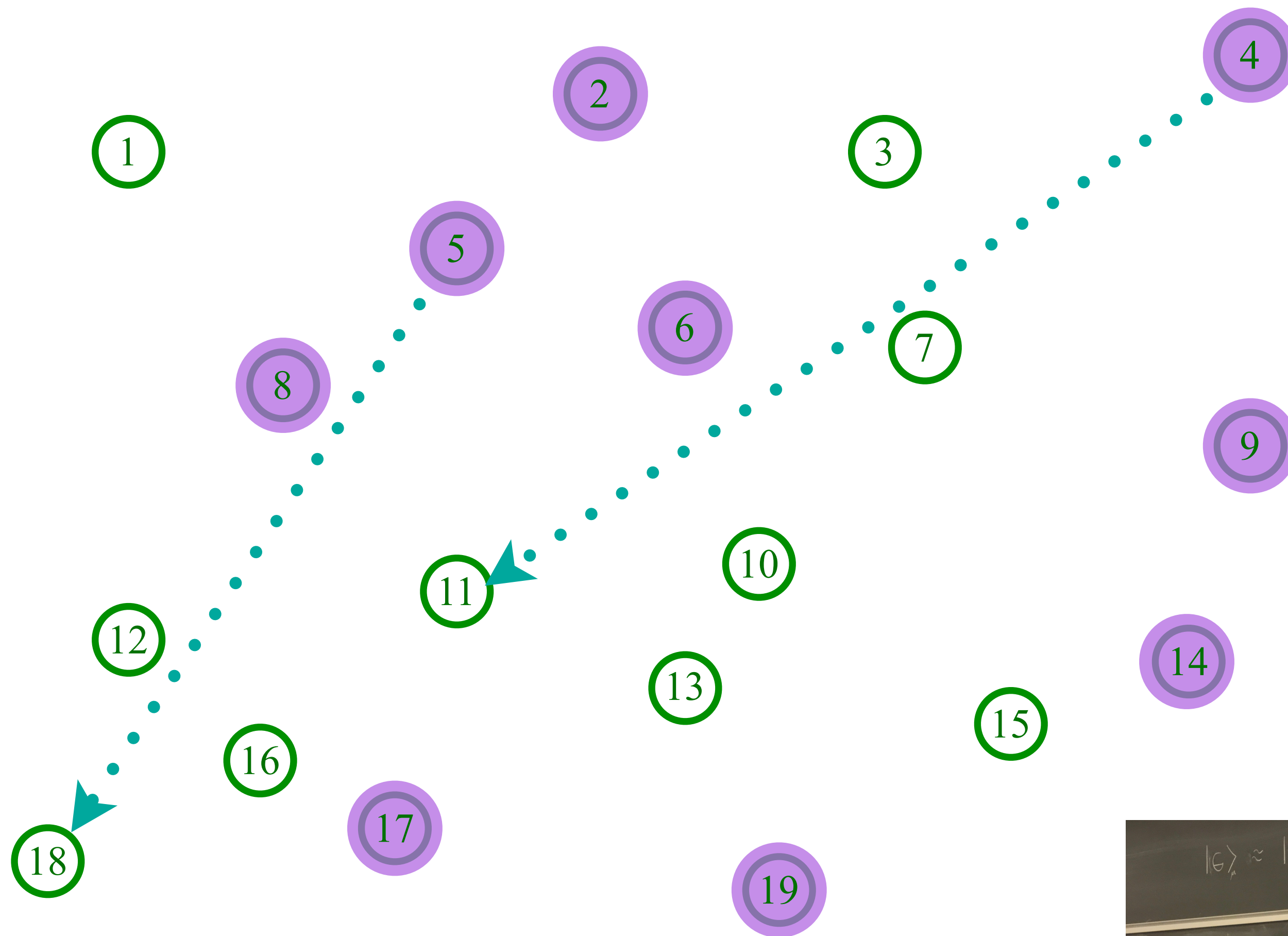
Entangle electrons pairwise randomly



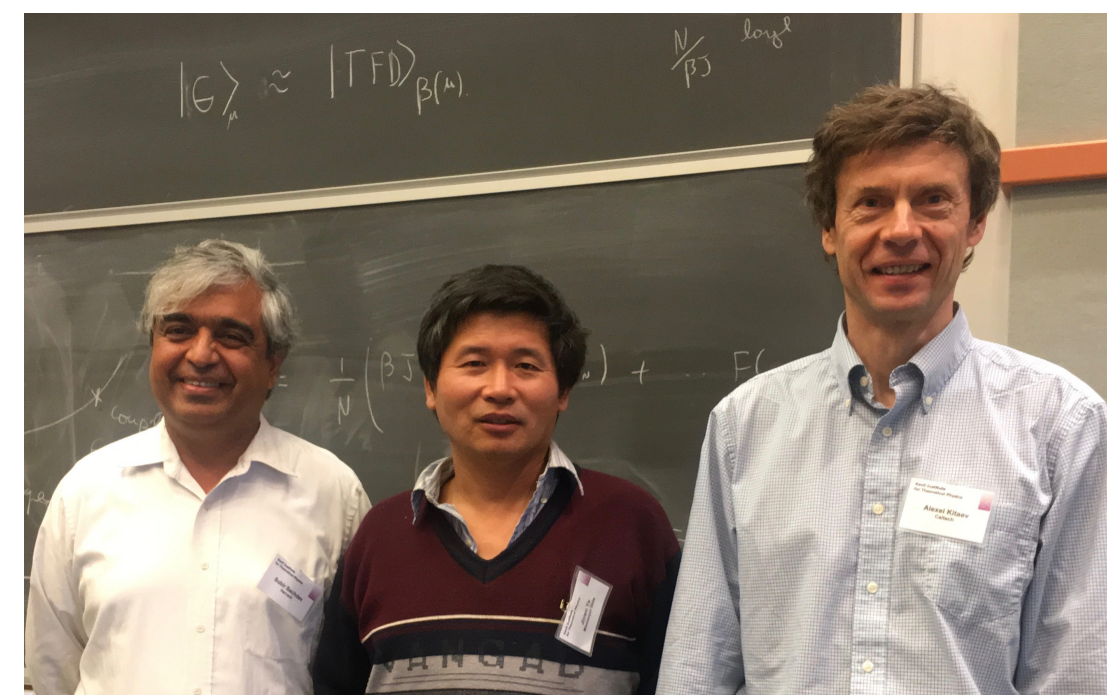
# The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{4,5;11,18}$$



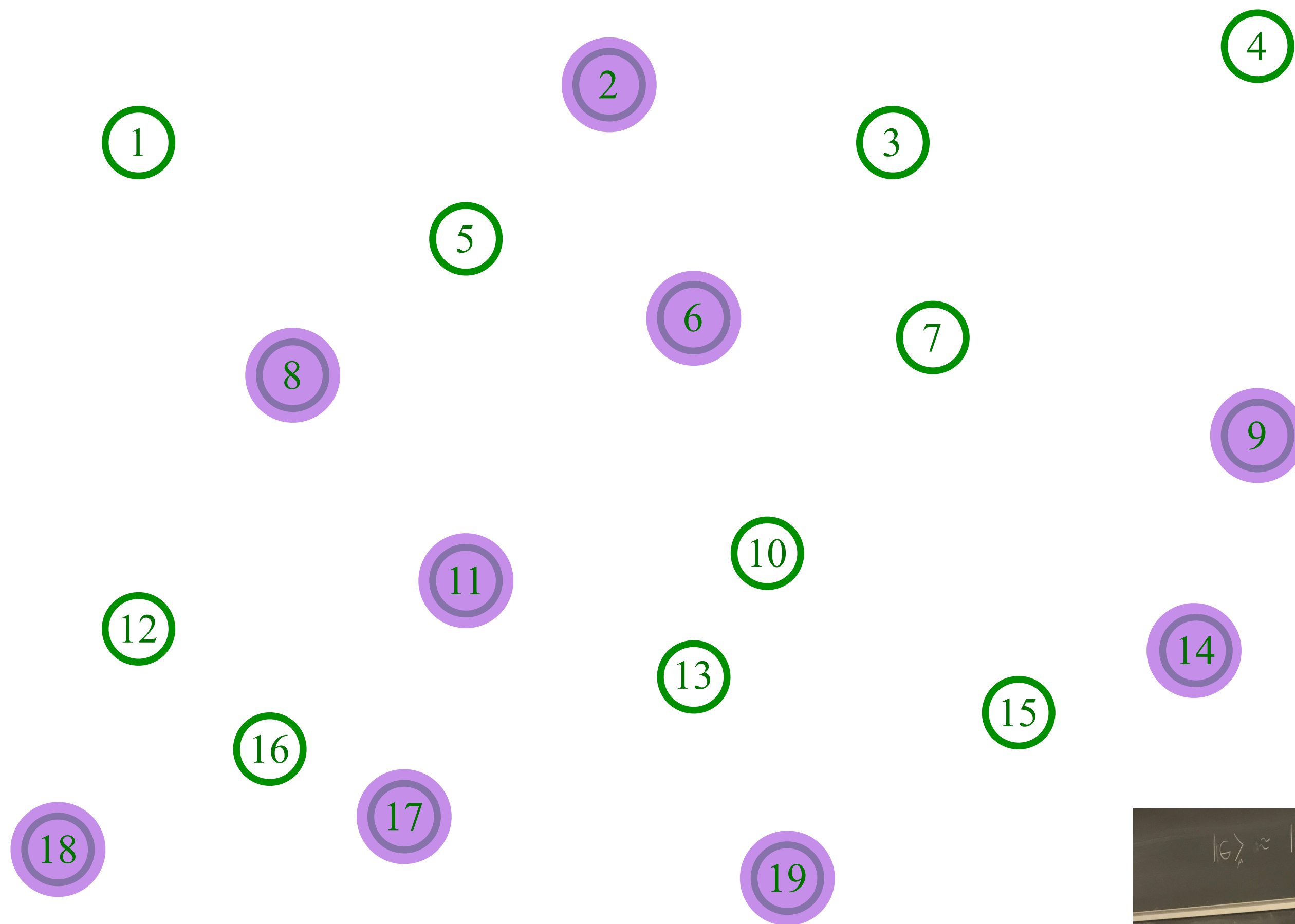
Entangle electrons pairwise randomly



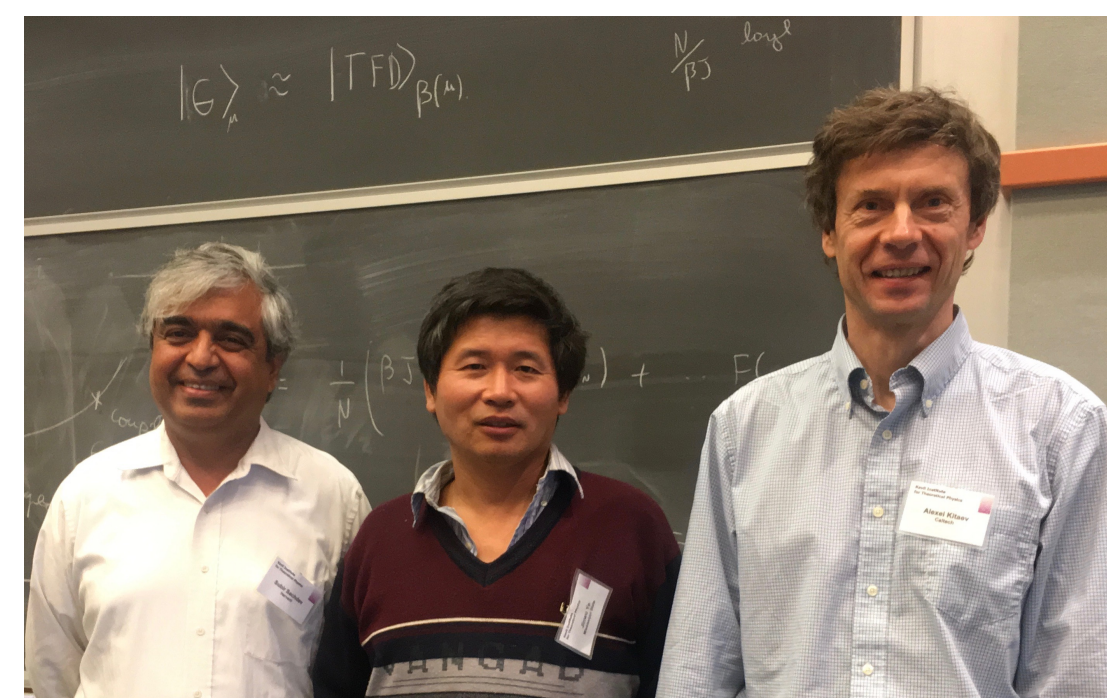
# The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{4,5;11,18}$$



Entangle electrons pairwise randomly

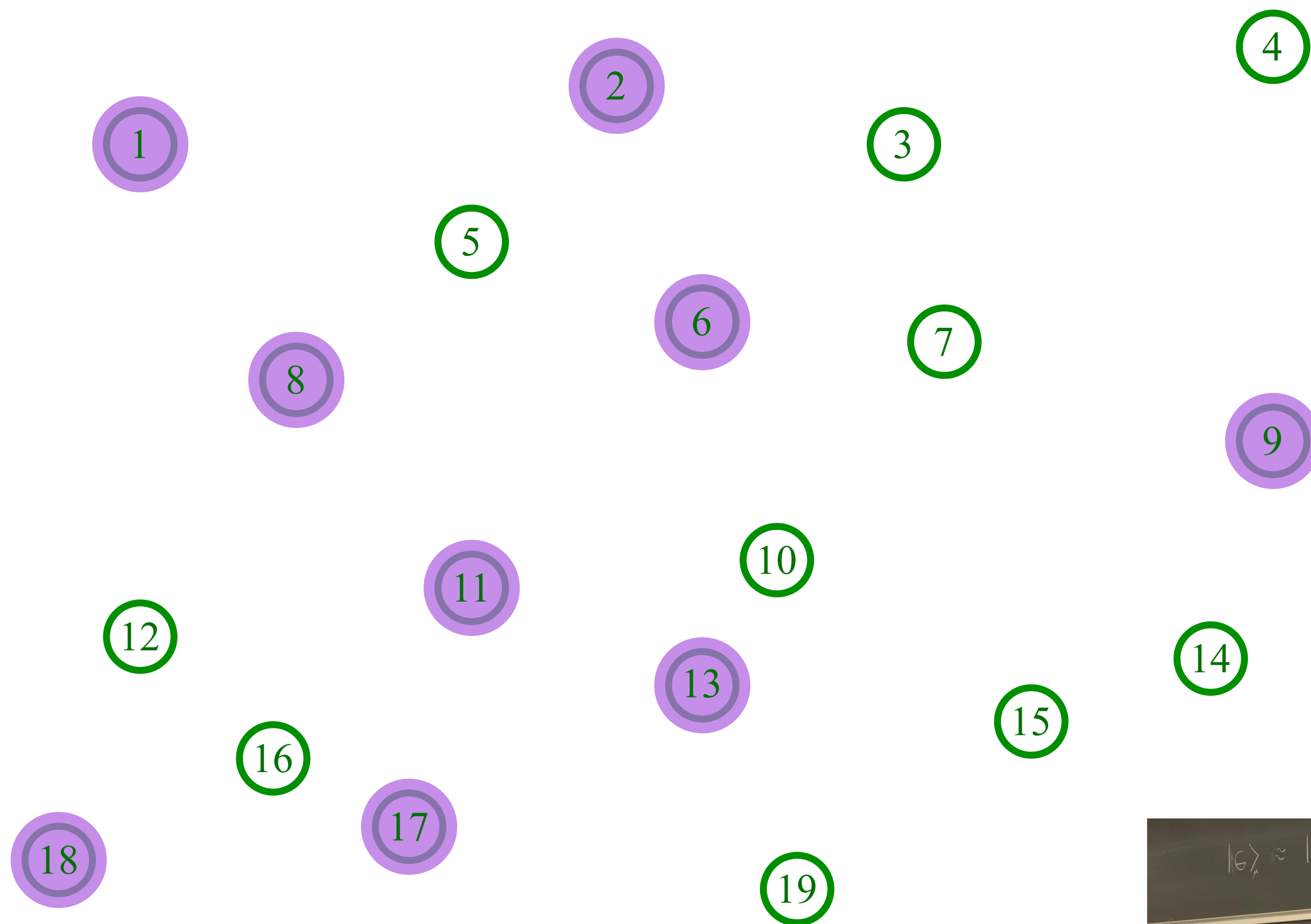




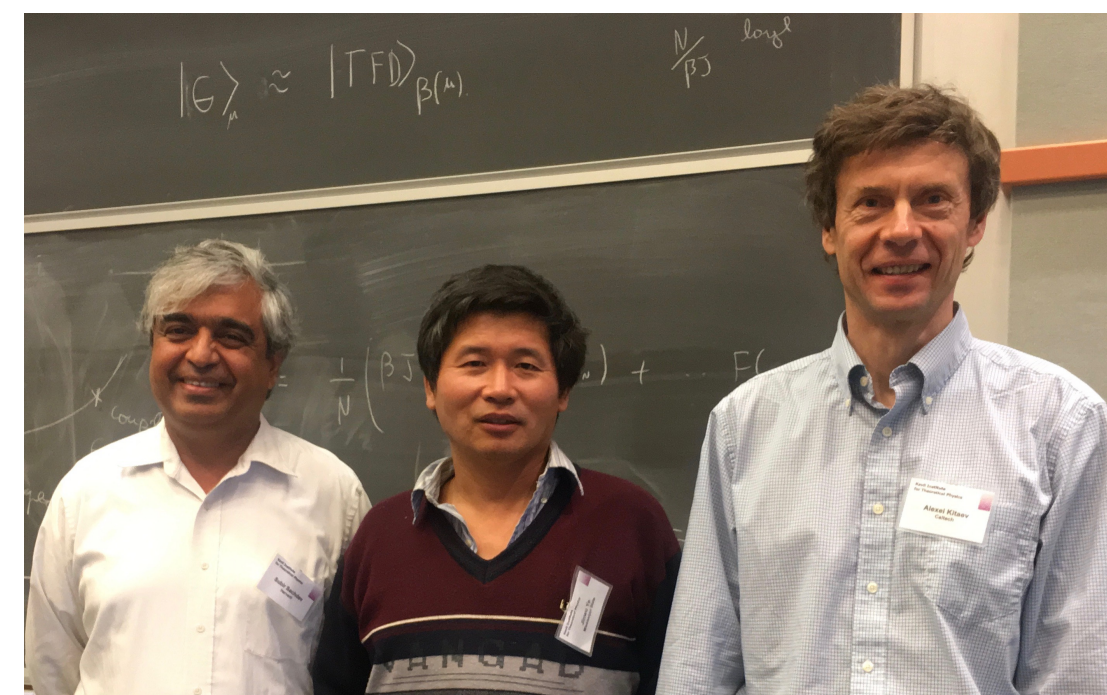
# The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{14,19;1,13}$$



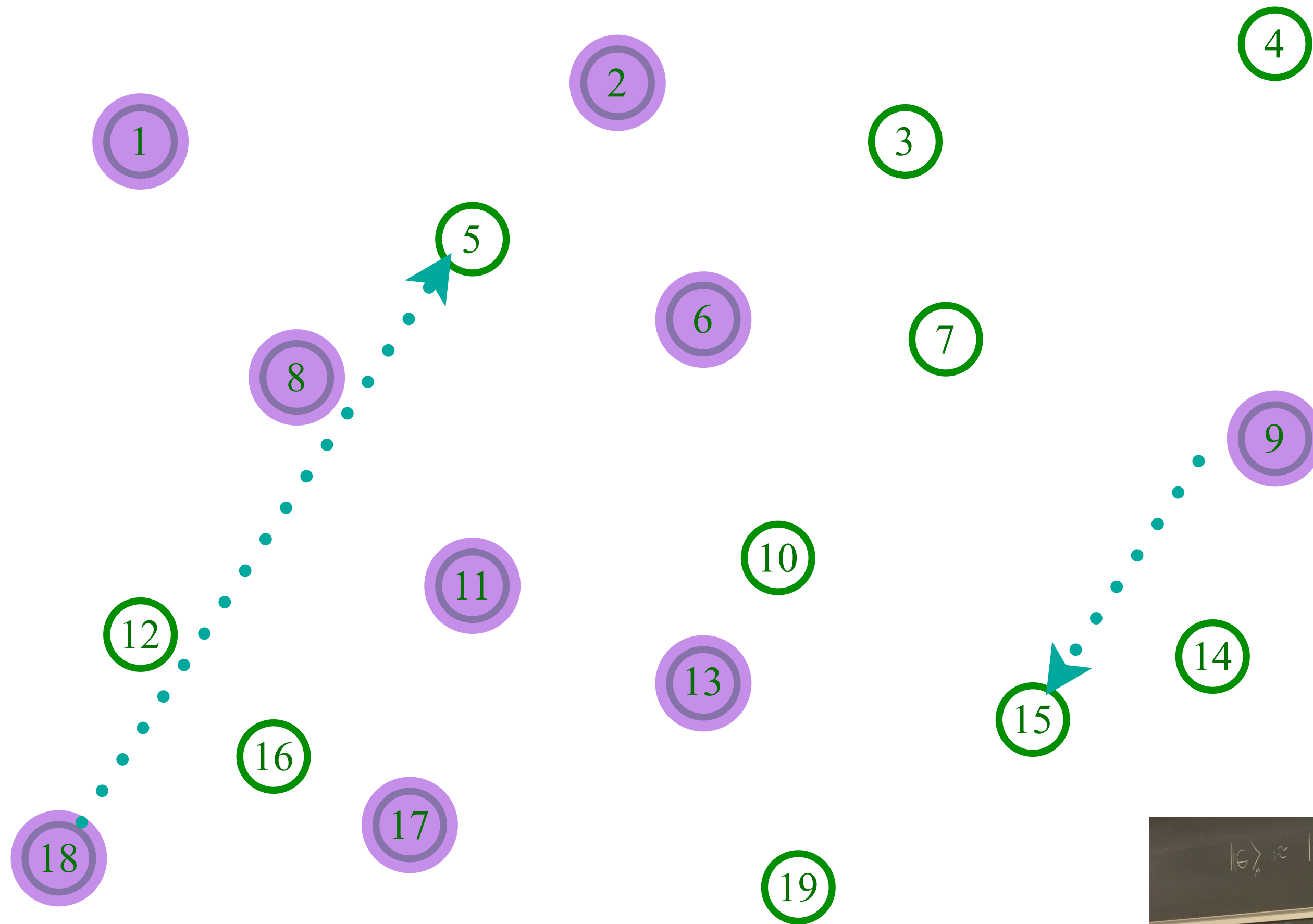
Entangle electrons pairwise randomly



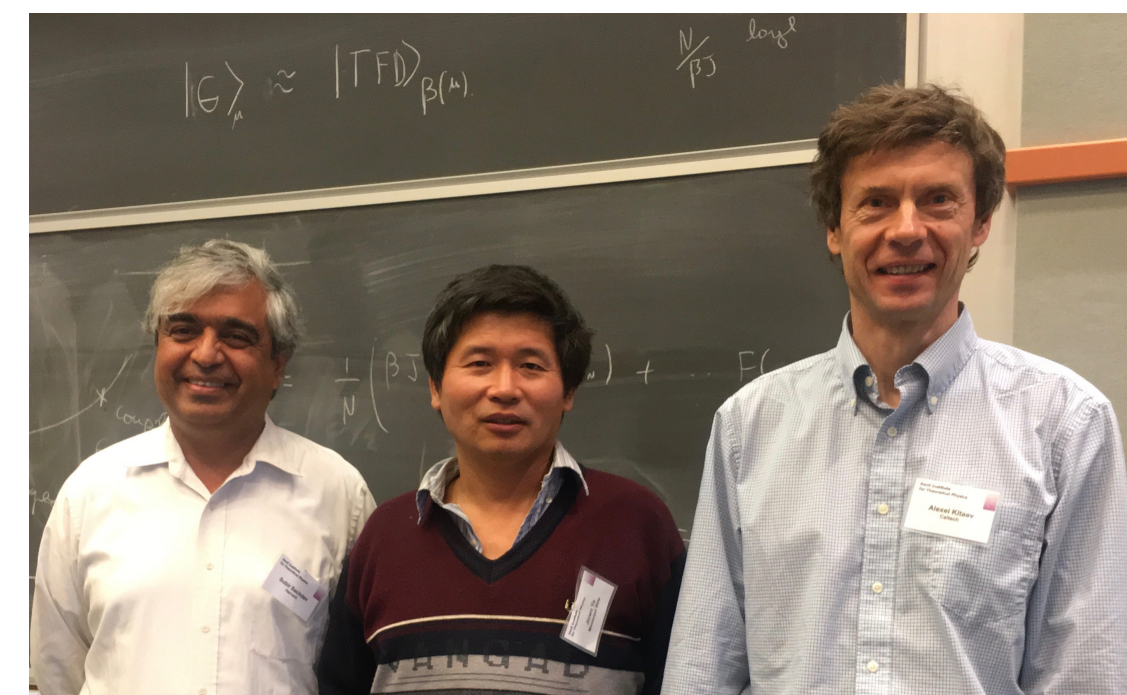
# The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{9,18;5,15}$$



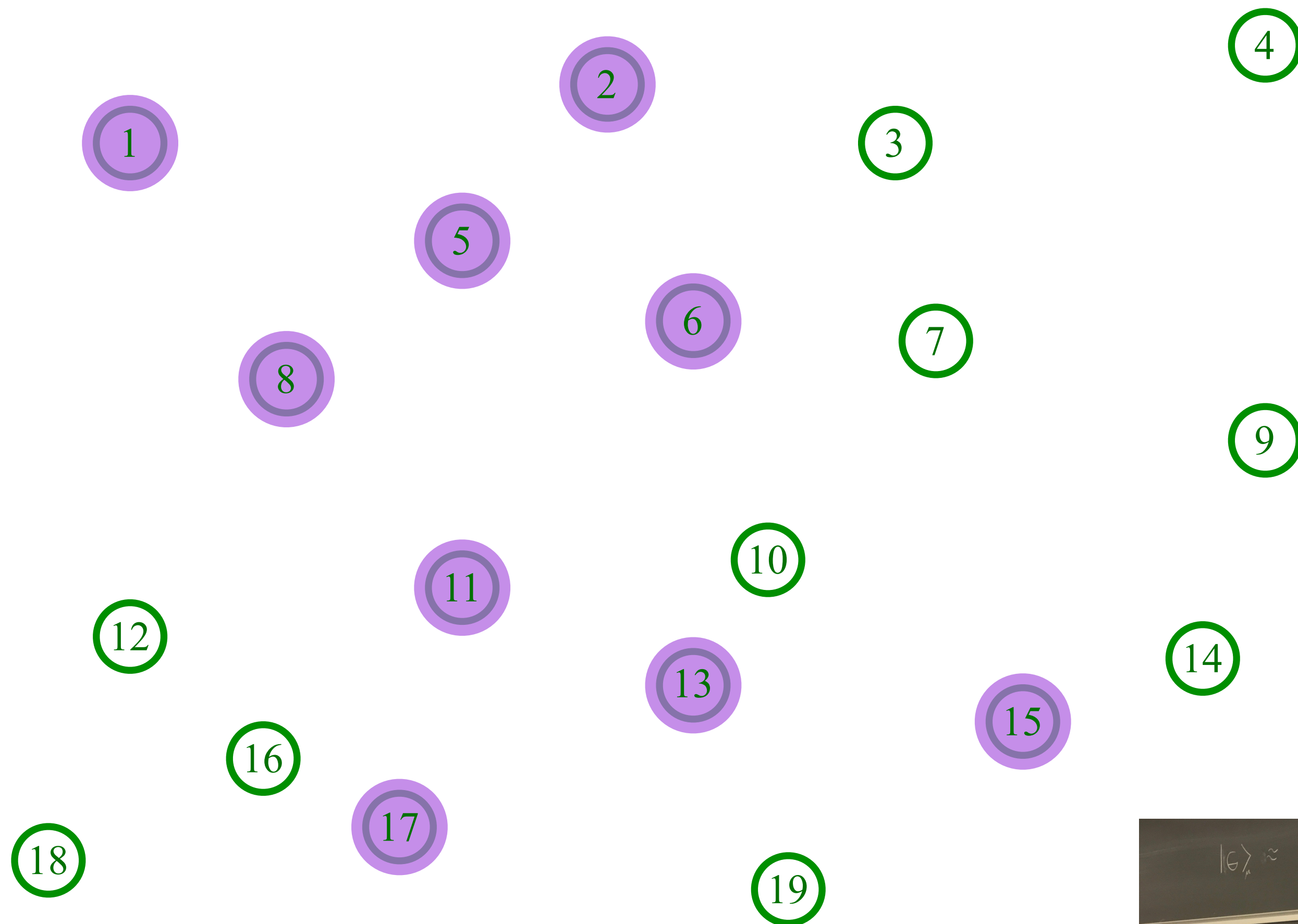
Entangle electrons pairwise randomly



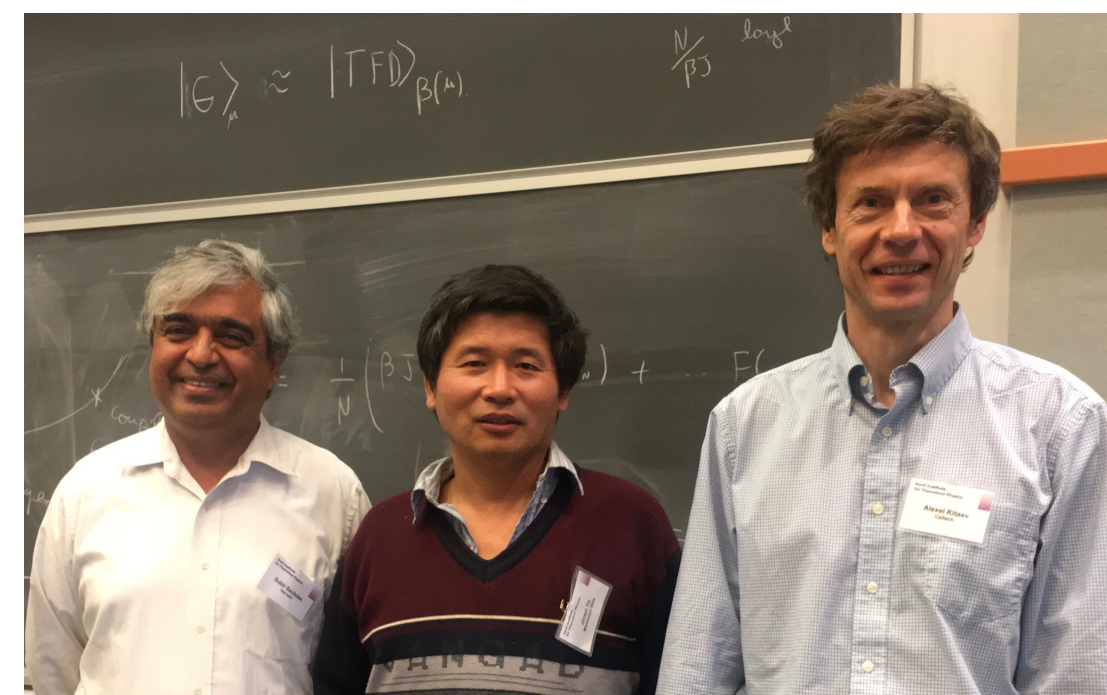
# The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{9,18;5,15}$$



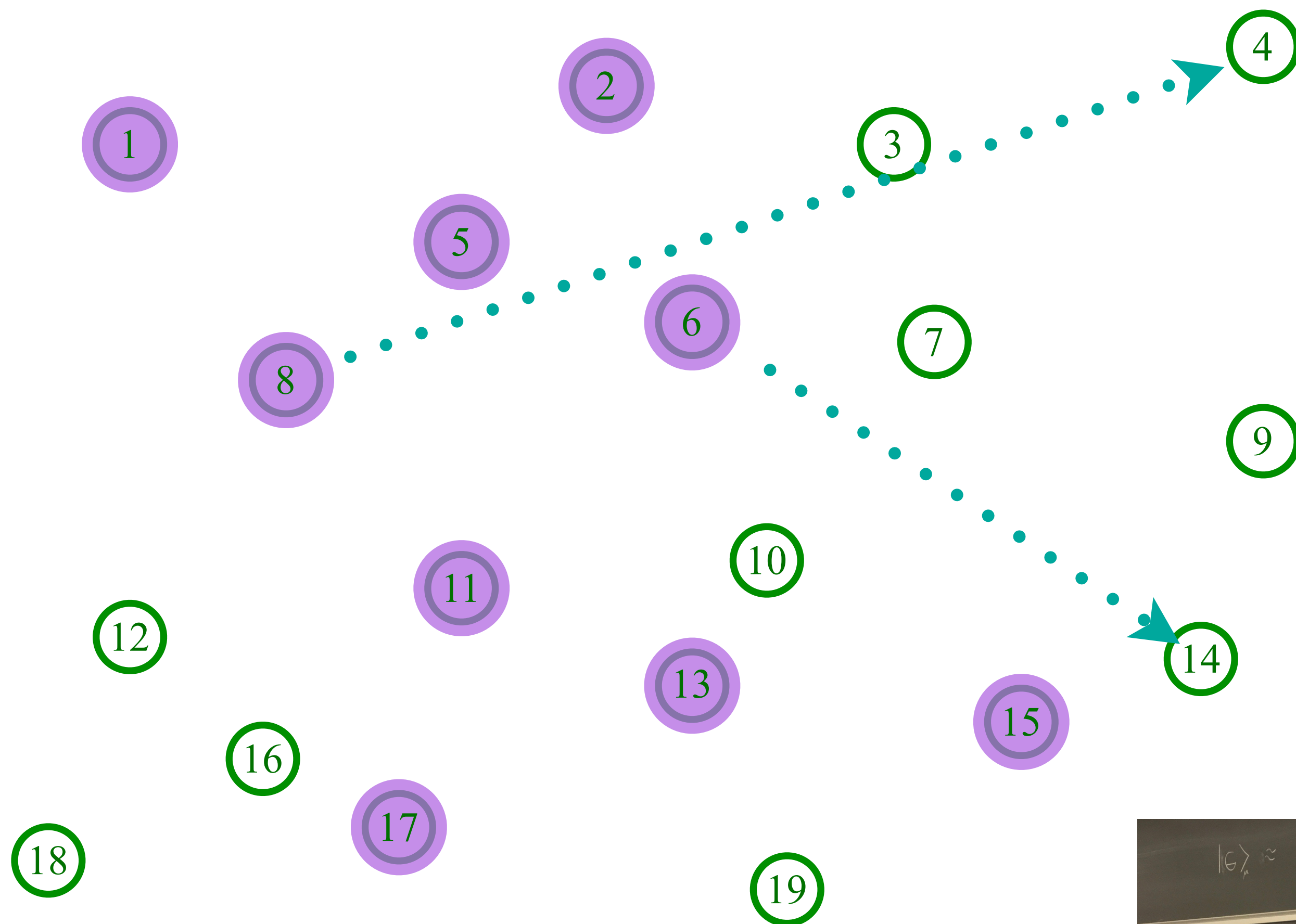
Entangle electrons pairwise randomly



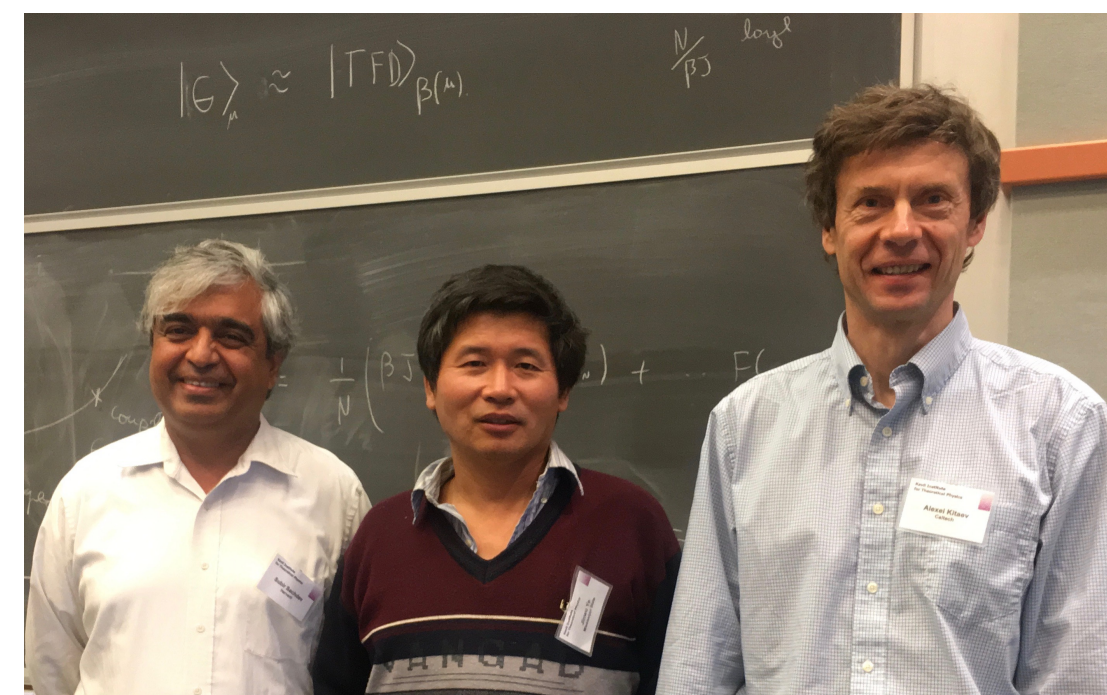
# The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{6,8;4,14}$$



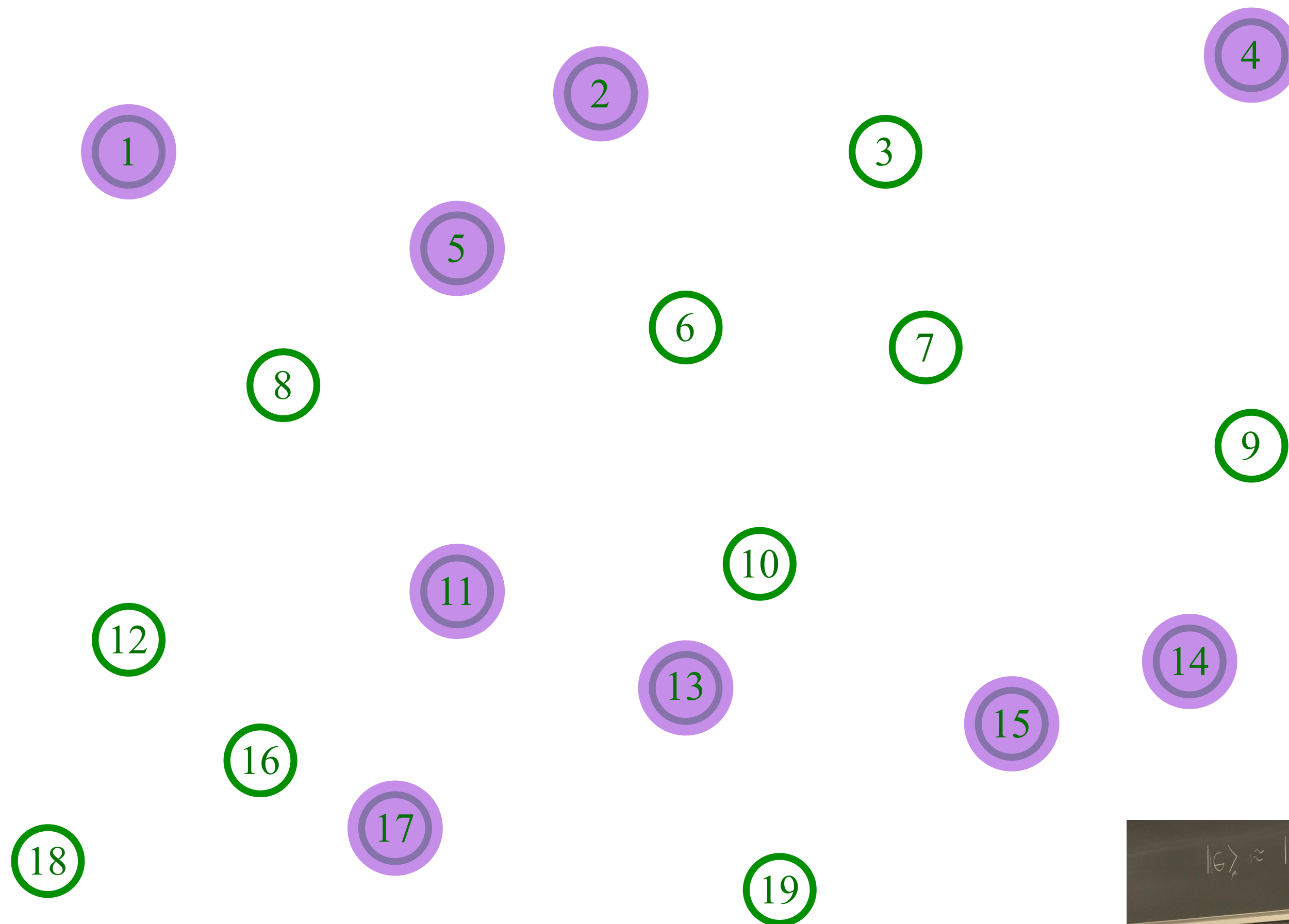
Entangle electrons pairwise randomly



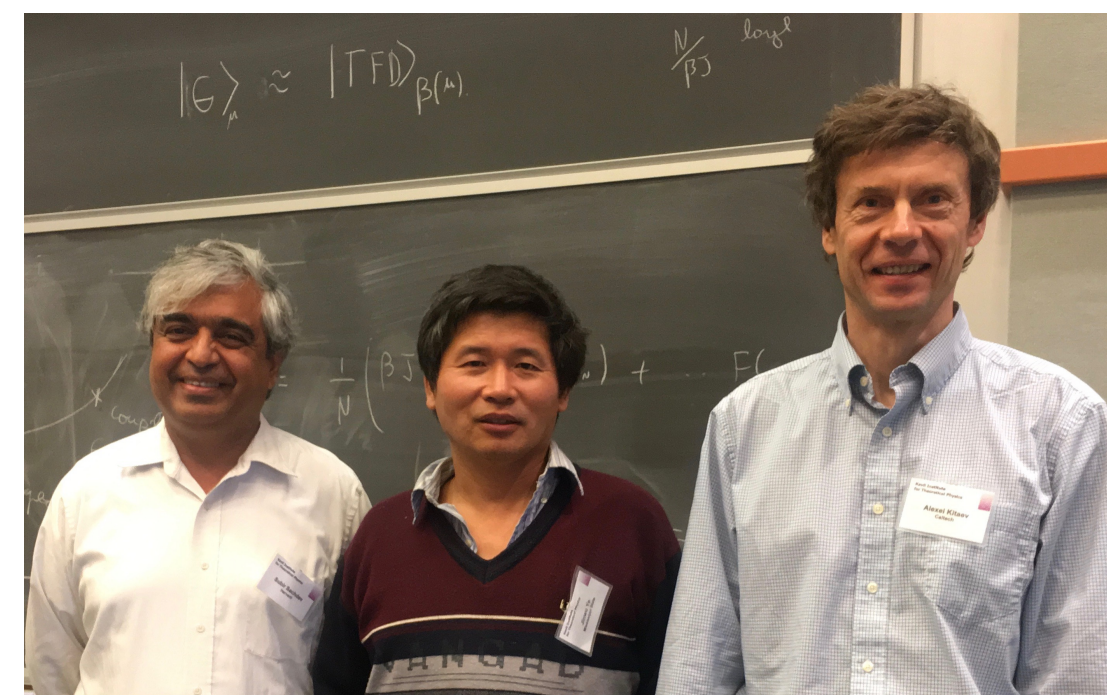
# The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{6,8;4,14}$$



Entangle electrons pairwise randomly



# The SYK model

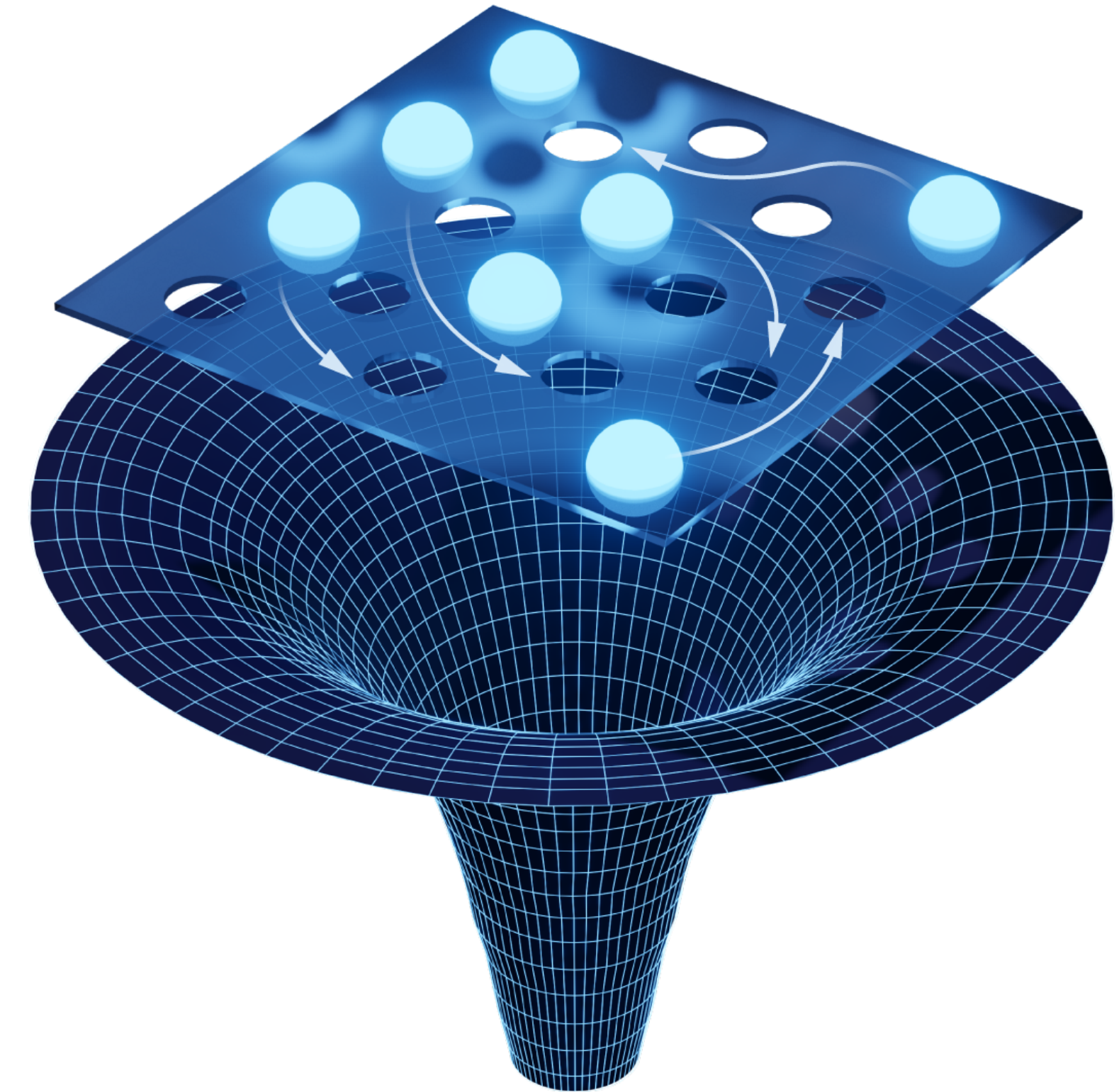
Sachdev, Ye (1993); Kitaev (2015)

Solvable models of multi-particle quantum entanglement with mobile fermions.

Yields a metal whose excitations are not particle-like

i.e. no bosons, fermions, anyons....

Current is carried by an “entangled quantum soup”



# The SYK model

At  $T > 0$ , solutions are fully characterized by a universal, frequency-dependent, ‘Planckian’, relaxation rate,

$$\frac{1}{\tau} \sim \frac{k_B T}{\hbar} .$$

S. Sachdev and J. Ye, PRL **70**, 3339 (1993)

A. Georges and O. Parcollet PRB **59**, 5341 (1999)

A. Georges, O. Parcollet, and S. Sachdev (**GPS**), PRB **63**, 134406 (2001)

arXiv:2503.15646

# Planckian dissipation, anomalous high temperature THz non-linear response and energy relaxation in the strange metal state of the cuprate superconductors

Dipanjan Chaudhuri<sup>#,1</sup> David Barbalas<sup>#,1</sup> Fahad Mahmood,<sup>1,2,3</sup> Jiahao Liang,<sup>1</sup> Ralph Romero III,<sup>1</sup> Anaëlle Legros,<sup>1</sup> Xi He,<sup>4</sup> H el ene Raffy,<sup>5</sup> Ivan Bo zovi c,<sup>4,6</sup> and N.P. Armitage<sup>1,7</sup>

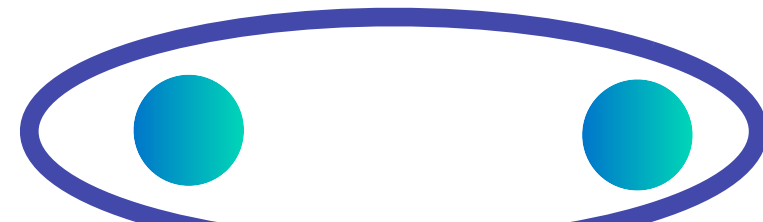
...the momentum relaxation rate is linear in  $T$  and close to its “Planckian” form ( $\Gamma_M \approx 2k_B T/\hbar$ ). We find (the energy relaxation rate)  $\Gamma_E$  to be 10-40 times smaller than the momentum relaxation. This shows that the scattering that causes momentum loss (and  $T$ -linear) resistivity do not remove appreciable energy from the electrons.

Many fermion entanglement II:

The SYK model  
and black holes

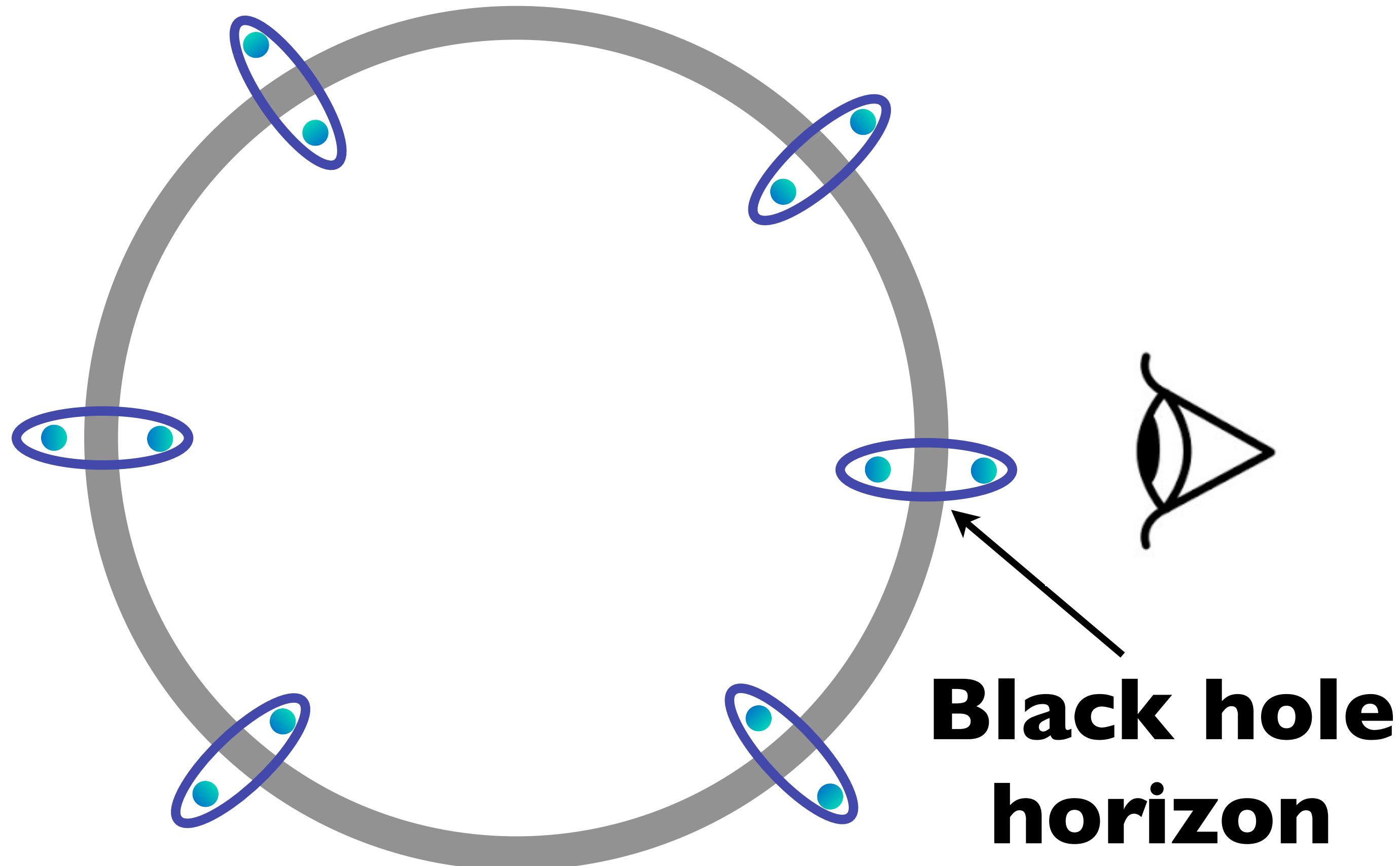
# Quantum Entanglement across a black hole horizon

Quantum entanglement  
on the surface



A diagram showing two blue dots representing particles inside a blue oval, which is itself inside a larger blue oval. This represents an entangled pair of particles.

$$= |\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle$$



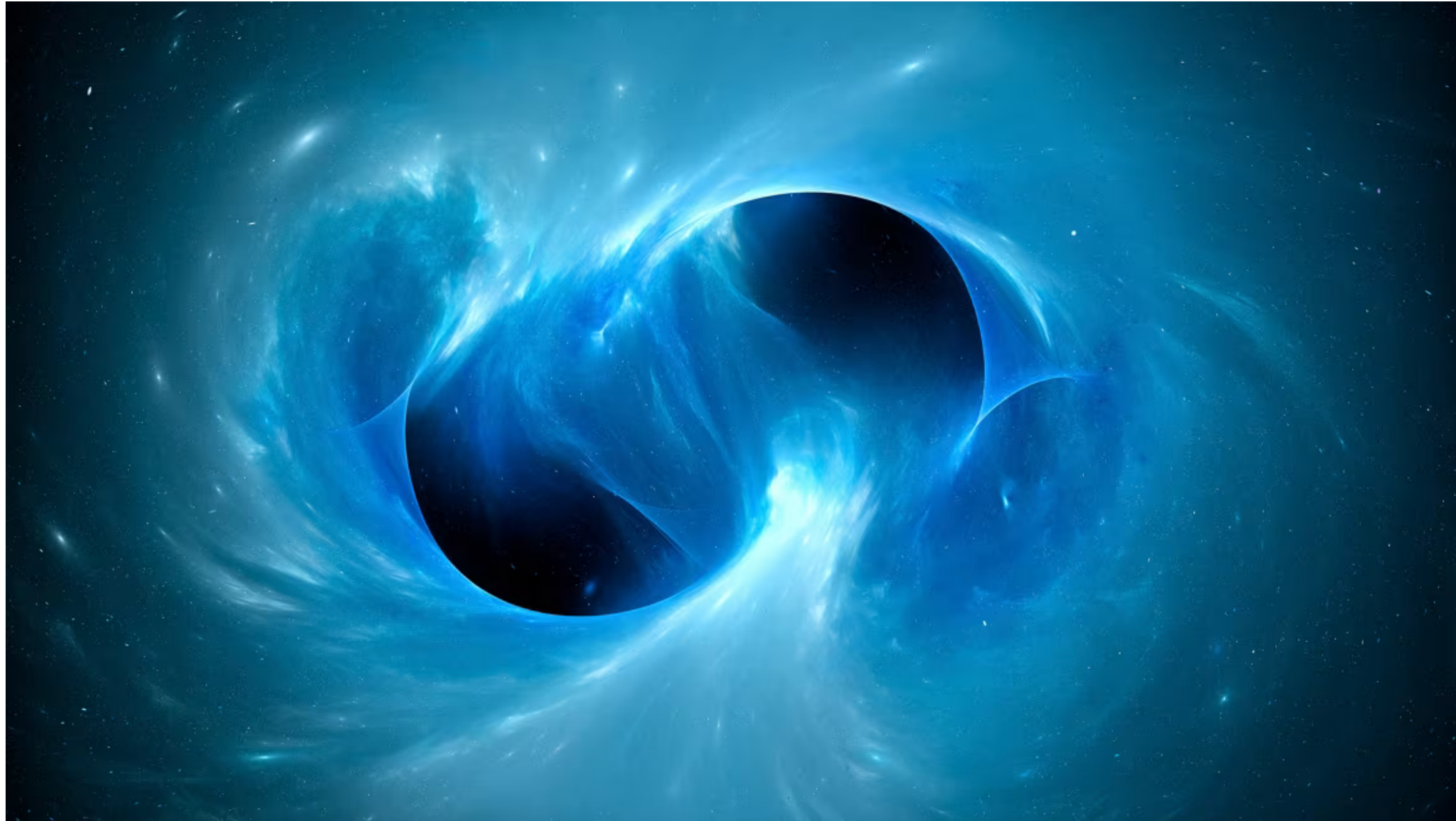
By computations *outside*  
the black hole,  
Hawking obtained  
the black hole entropy

$$S = \frac{Ac^3}{4G\hbar}$$

where  $A$  is area of the  
black hole horizon.

All other systems have  
entropy proportional to  
their volume.

# Quantum Entanglement across a black hole horizon



Sakkmesterke/Science Photo Library RF/Getty Images

$$\tau_{\text{ring-down}} \sim \frac{\hbar}{k_B T}$$

Planckian dynamics of  
quasi-normal modes!

C.V. Vishveshwara  
Nature **227**, 936 (1970)

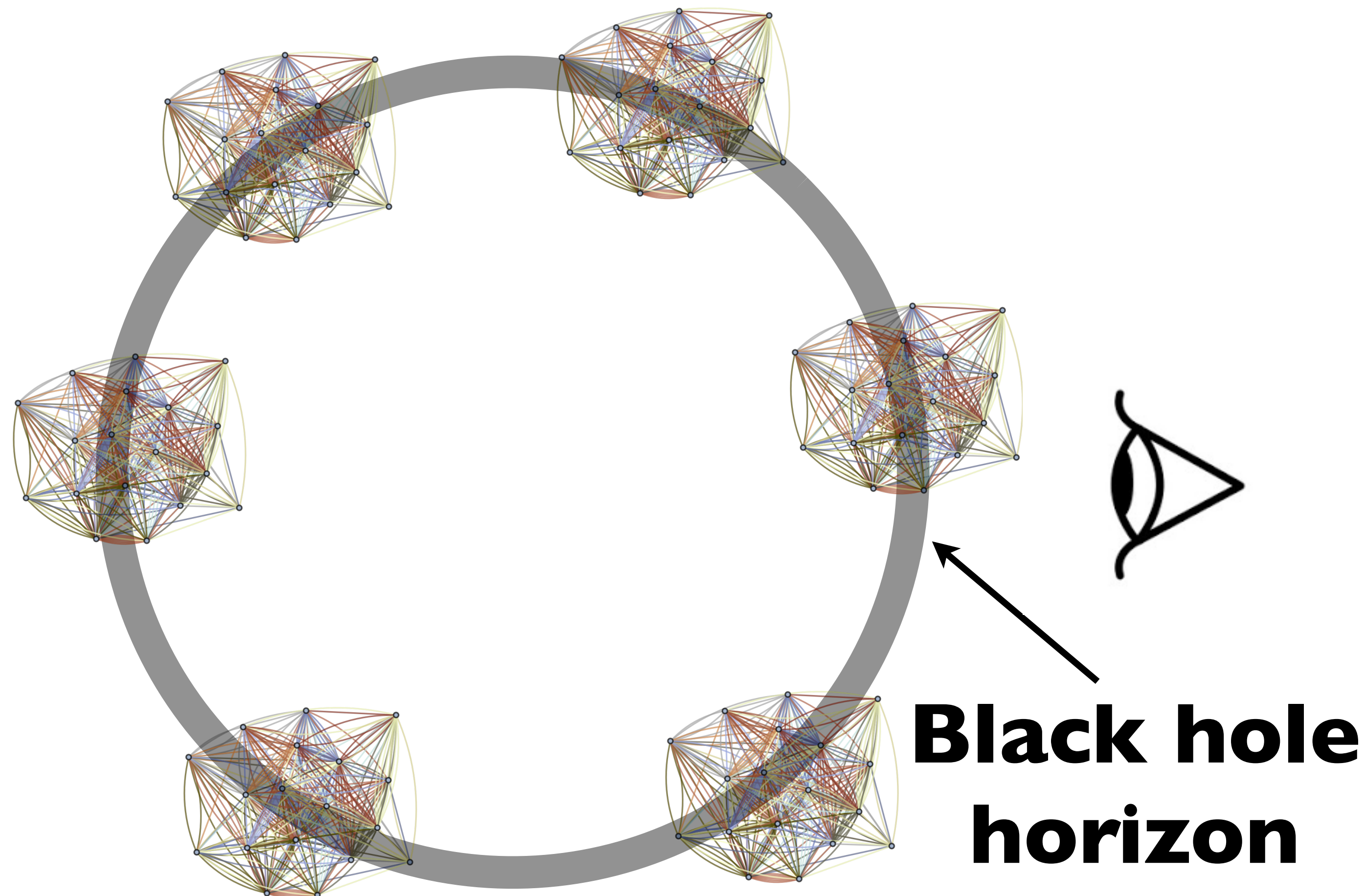
$T$  is the Hawking  
temperature of  
the black hole

# Quantum Entanglement across a black hole horizon

## Quantum entanglement on the surface

S. Sachdev, PRL **105**, 151602 (2010)

## Holographic Metals and the Fractionalized Fermi Liquid



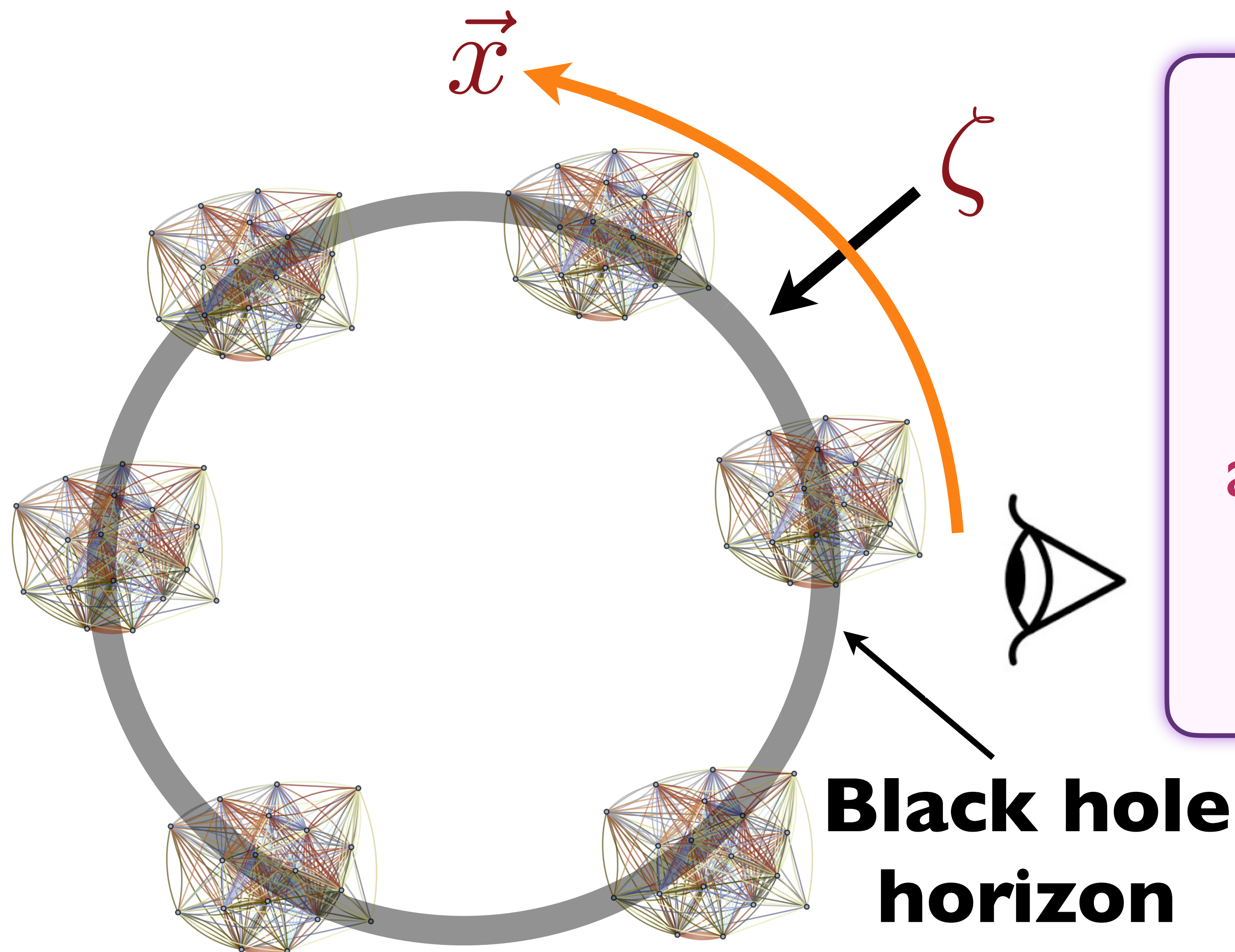
Subir Sachdev

“... This correspondence implies that certain mean-field gapless spin liquids are states of matter at nonzero density realizing the near-horizon,  $AdS_2 \times R_2$  physics of Reissner- Nordström black holes.”

cf. “fuzzballs” of Samir Mathur



Maxwell's electromagnetism  
and Einstein's general relativity  
allow black hole solutions with a net charge

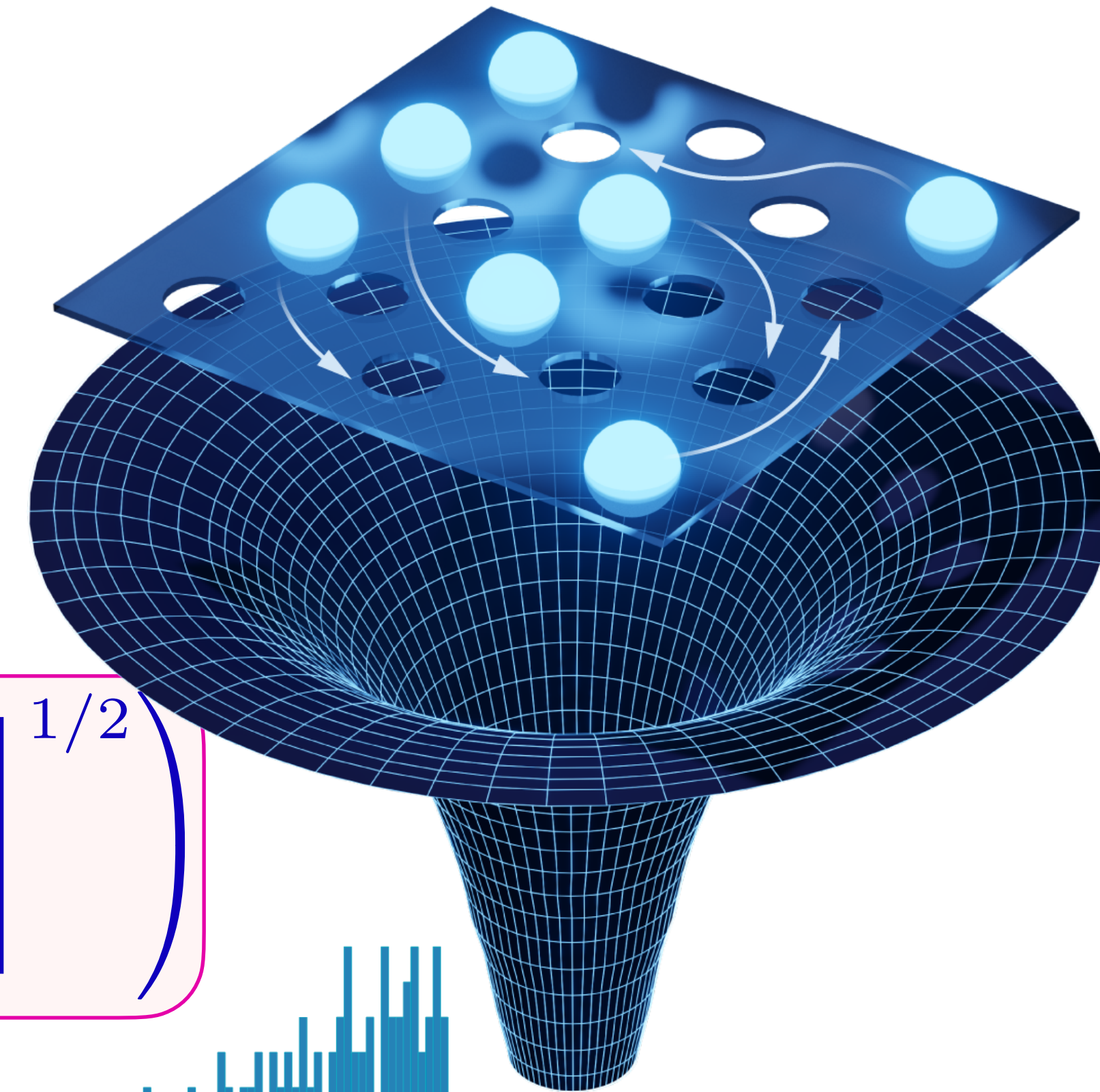


The quantum versions of  
Maxwell's and Einstein's  
equations in  
 $\zeta$  space and time are  
also the equations describing  
electron entanglement  
in the SYK model!

# D(E) of charged black holes from the SYK model

- For generic charged black holes in 3+1 dimensions with horizon area  $A_0$  at  $T = 0$  and fixed charge  $Q$  ( $A_0 = 2GQ^2/c^4$ ), the density of quantum states at small energy  $E$  is

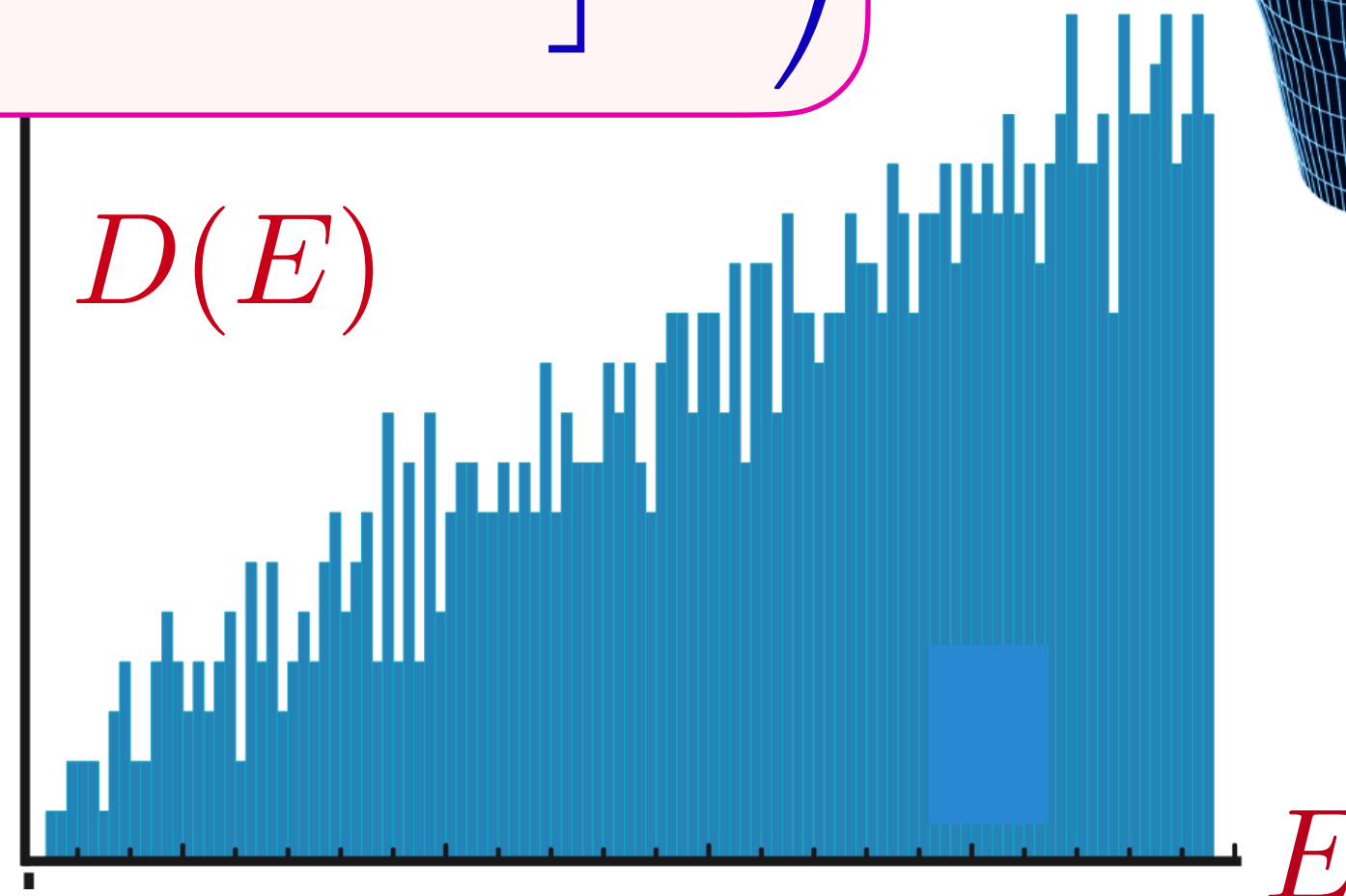
$$D(E) \sim \left( \frac{A_0 c^3}{\hbar G} \right)^{-347/90} \exp \left( \frac{A_0 c^3}{4\hbar G} \right) \sinh \left( \left[ \frac{\sqrt{\pi} A_0^{3/2} c^2}{\hbar^2 G} E \right]^{1/2} \right)$$



Bekenstein-Hawking

Iliesiu, Murthy, Turiaci (2022)

Developments from the SYK model

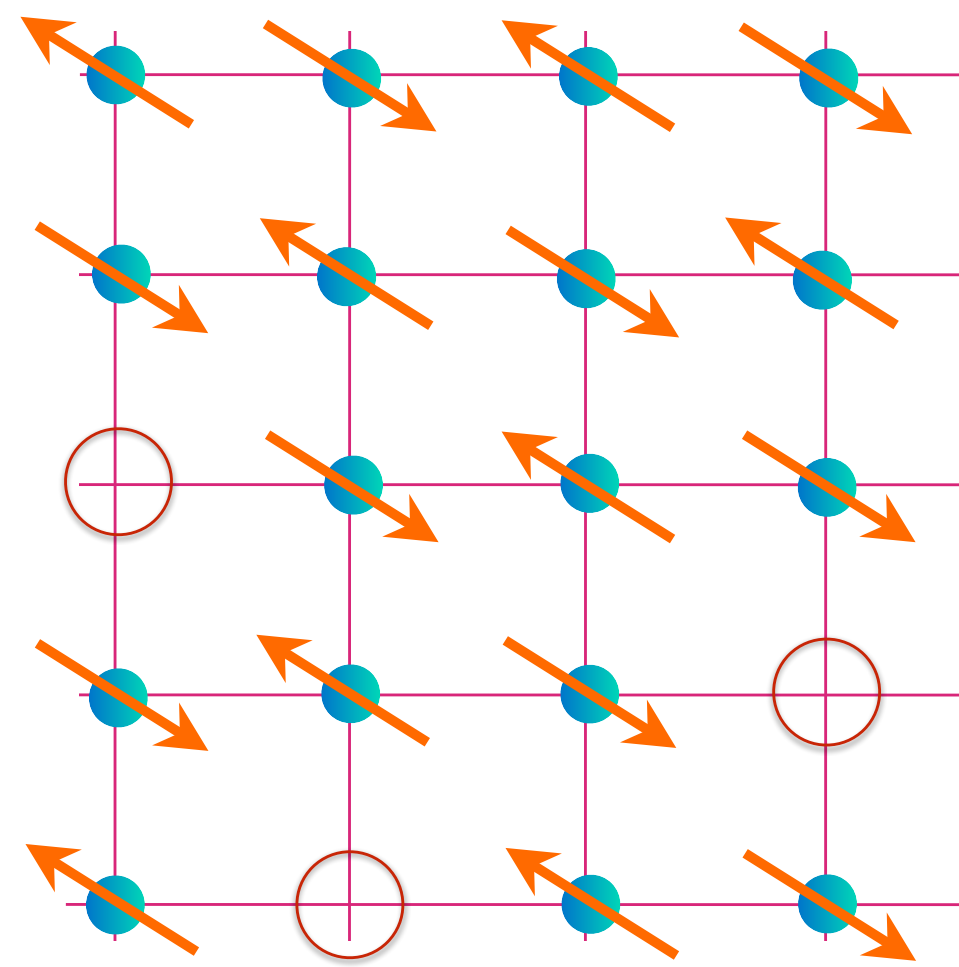


Similar remarks apply to rotating neutral black holes.

Many fermion entanglement I & II:

Theory of the  
strange metal

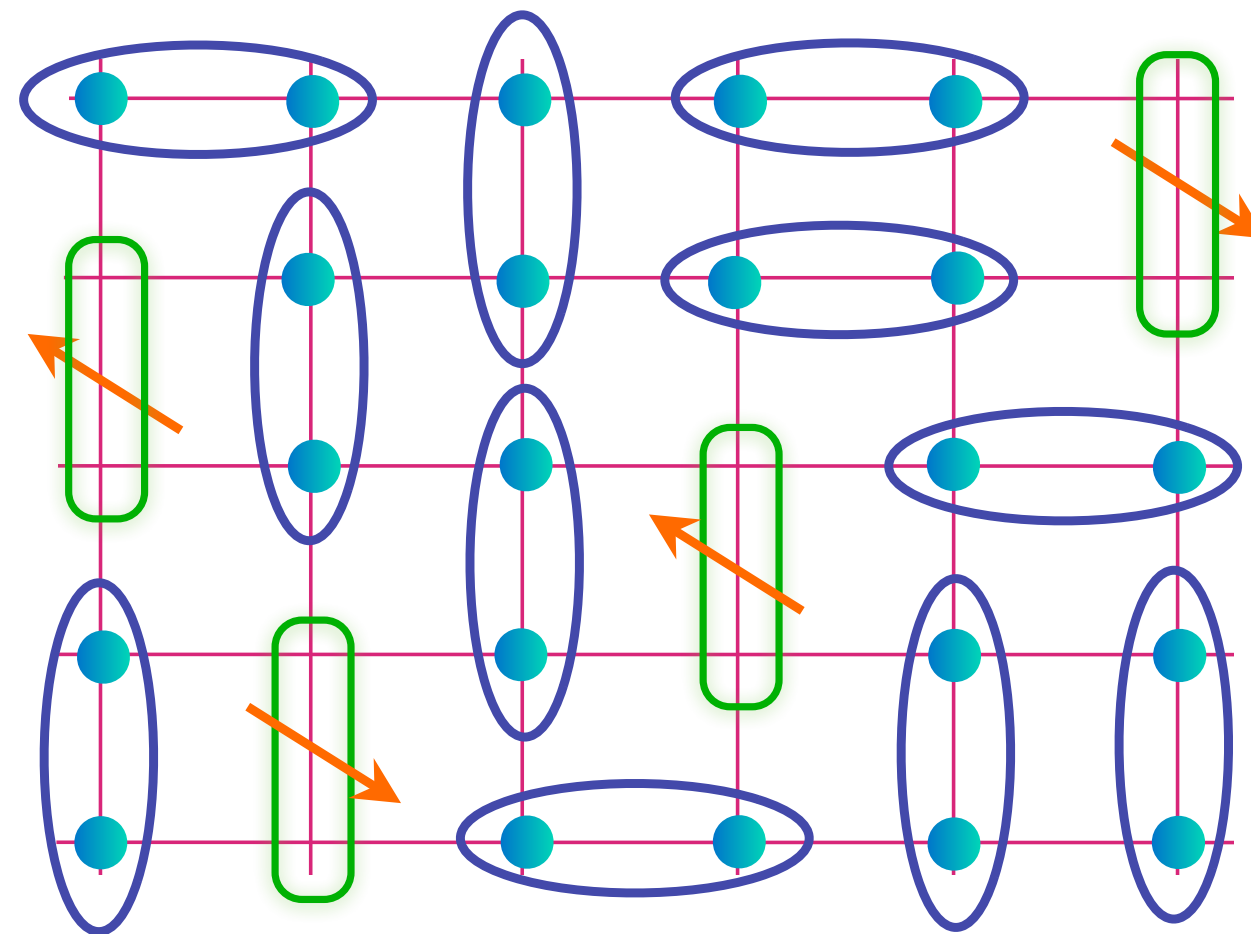
# AF Metal



Carrier density  $p$   
Pocket area  $p/4$

$$\langle (-1)^r \mathbf{S}_r \rangle \neq 0$$

# FL\*



$$\text{Green oval with arrow} = (|\uparrow \circ\rangle + |\circ \uparrow\rangle) / \sqrt{2}$$

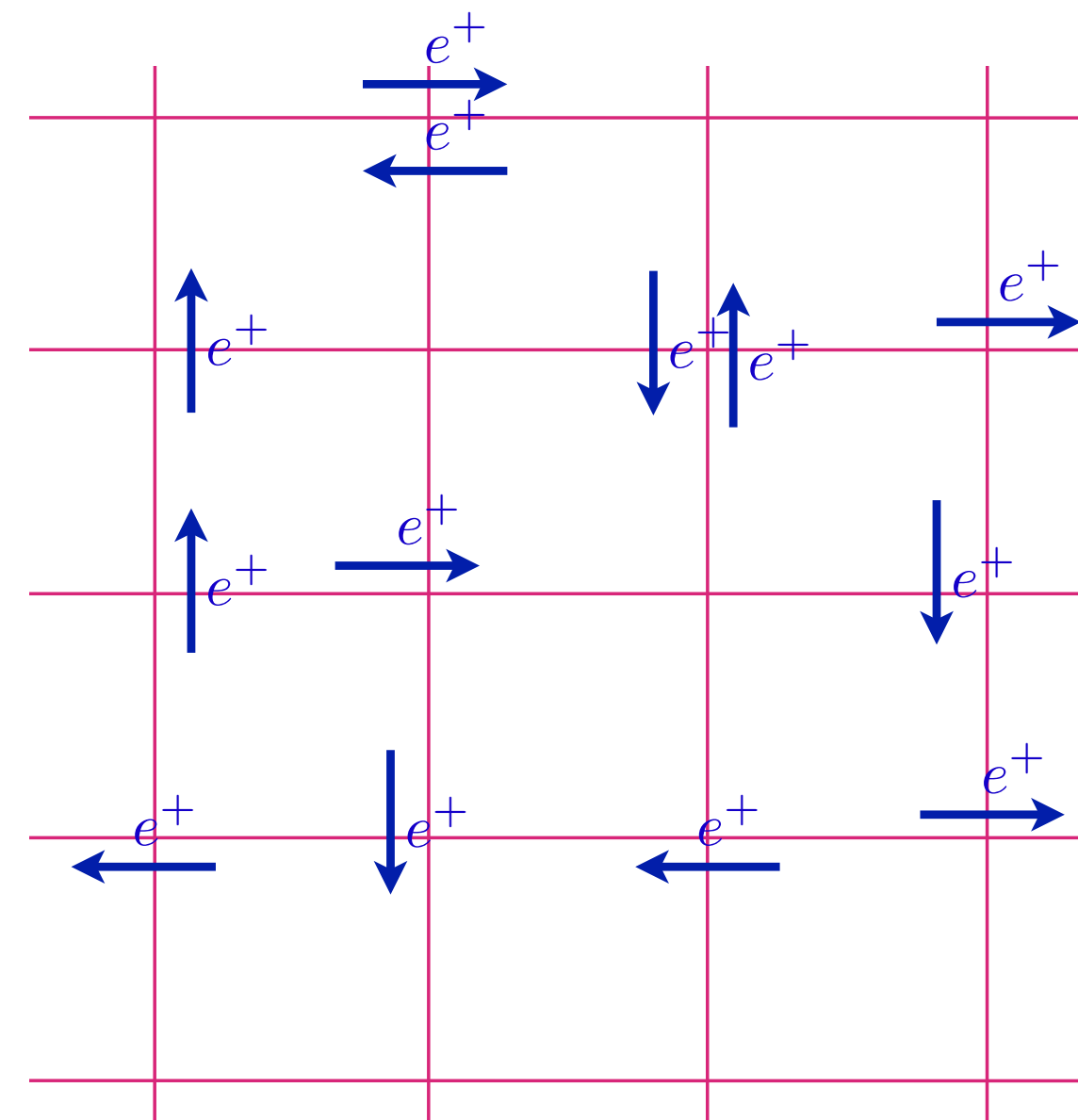
$$\text{Blue oval} = (|\uparrow \downarrow\rangle - |\downarrow \uparrow\rangle) / \sqrt{2}$$

Carrier density  $p$   
Pocket area  $p/8$

$$\langle (-1)^r \mathbf{S}_r \rangle = 0$$

$$\langle \Phi \rangle \neq 0$$

# FL



Carrier density  $1 + p$   
Fermi area  $(1 + p)/2$

$$\langle \Phi \rangle = 0$$

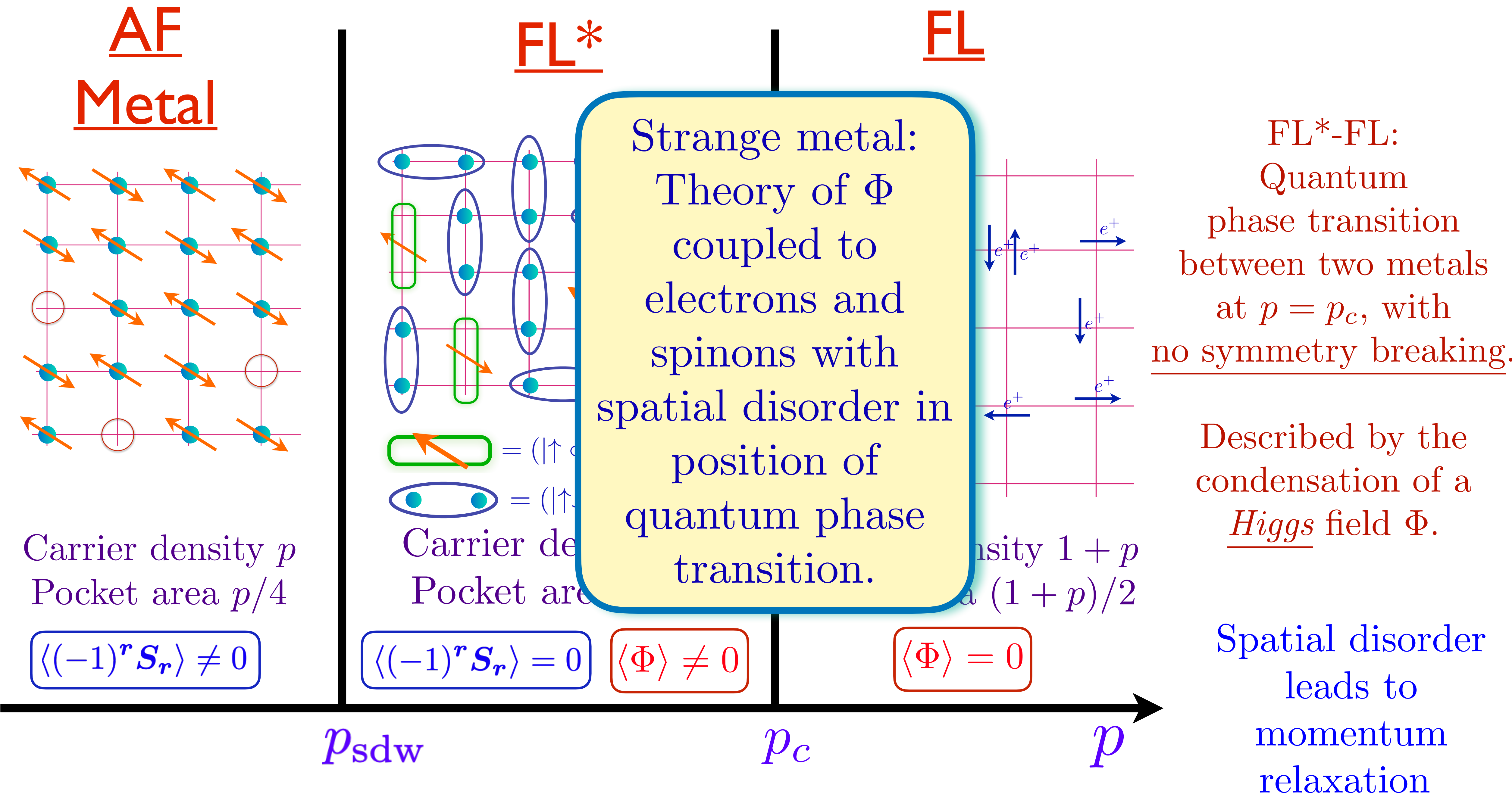
FL\*-FL:  
Quantum  
phase transition  
between two metals  
at  $p = p_c$ , with  
no symmetry breaking.

Described by the  
condensation of a  
Higgs field  $\Phi$ .

$p_{sdw}$

$p_c$

$p$



S. Sachdev, M.A. Metlitski and M. Punk, Journal of Physics Condensed Matter **24**, 294205 (2012)

Ya-Hui Zhang and S. S., PRR **2**, 023172 (2020)

# Yukawa-Sachdev-Ye-Kitaev model

$$\mathcal{H} = -\mu \sum_i c_i^\dagger c_i + \sum_\ell \frac{1}{2} (\pi_\ell^2 + \omega_0^2 \Phi_\ell^2) + \frac{1}{N} \sum_{ij\ell} g_{ij\ell} c_i^\dagger c_j \Phi_\ell$$

with  $g_{ij\ell}$  independent random numbers with zero mean.

W. Fu, D. Gaiotto, J. Maldacena, and S. Sachdev, PRD **95**, 026009 (2017)

J. Murugan, D. Stanford, and E. Witten, JHEP 08, 146 (2017)

A. A. Patel and S. Sachdev, PRB **98**, 125134 (2018)

E. Marcus and S. Vandoren, JHEP 01, 166 (2018)

Yuxuan Wang, PRL **124**, 017002 (2020)

I. Esterlis and J. Schmalian, PRB **100**, 115132 (2019)

Yuxuan Wang and A. V. Chubukov, PRR **2**, 033084 (2020)

E. E. Aldape, T. Cookmeyer, A. A. Patel, and E. Altman, PRB **105**, 235111 (2022)

Jaewon Kim, E. Altman, and Xiangyu Cao, PRB **103**, 081113 (2021)

W. Wang, A. Davis, G. Pan, Yuxuan Wang, and Zi Yang Meng, PRB **103**, 195108 (2021)

I. Esterlis, H. Guo, A. A. Patel, and S. Sachdev, PRB **103**, 235129 (2021).

# Yukawa-Sachdev-Ye-Kitaev model

$$\mathcal{H} = -\mu \sum_i c_i^\dagger c_i + \sum_\ell \frac{1}{2} (\pi_\ell^2 + \omega_0^2 \Phi_\ell^2) + \frac{1}{N} \sum_{ij\ell} g_{ij\ell} c_i^\dagger c_j \Phi_\ell$$

with  $g_{ij\ell}$  independent random numbers with zero mean.

W. Fu, D. Gaiotto, J. Maldacena, and S. Sachdev, PRD **95**, 026009 (2017)

J. Murugan, D. Stanford, and E. Witten, JHEP 08, 146 (2017)

A. A. Patel and S. Sachdev, PRB **98**, 125134 (2018)

E. Marcus and S. Vandoren, JHEP 01, 166 (2018)

Yuxuan Wang, PRL **124**, 017002 (2020)

I. Esterlis and J. Schmalian, PRB **100**, 115132 (2019)

Yuxuan Wang and A. V. Chubukov, PRR **2**, 033084 (2020)

E. E. Aldape, T. Cookmeyer, A. A. Patel, and E. Altman, PRB **105**, 235111 (2022)

Jaewon Kim, E. Altman, and Xiangyu Cao, PRB **103**, 081113 (2021)

W. Wang, A. Davis, G. Pan, Yuxuan Wang, and Zi Yang Meng, PRB **103**, 195108 (2021)

I. Esterlis, H. Guo, A. A. Patel, and S. Sachdev, PRB **103**, 235129 (2021).

# Yukawa-Sachdev-Ye-Kitaev model

$$\mathcal{H} = -\mu \sum_i c_i^\dagger c_i + \sum_\ell \frac{1}{2} (\pi_\ell^2 + \omega_0^2 \Phi_\ell^2) + \frac{1}{N} \sum_{ij\ell} g_{ij\ell} c_i^\dagger c_j \Phi_\ell$$

with  $g_{ij\ell}$  independent random numbers with zero mean.

Properties very similar to the SYK model,  
including Planckian dynamics:

$$\frac{1}{\tau(\omega)} = \frac{k_B T}{\hbar}.$$

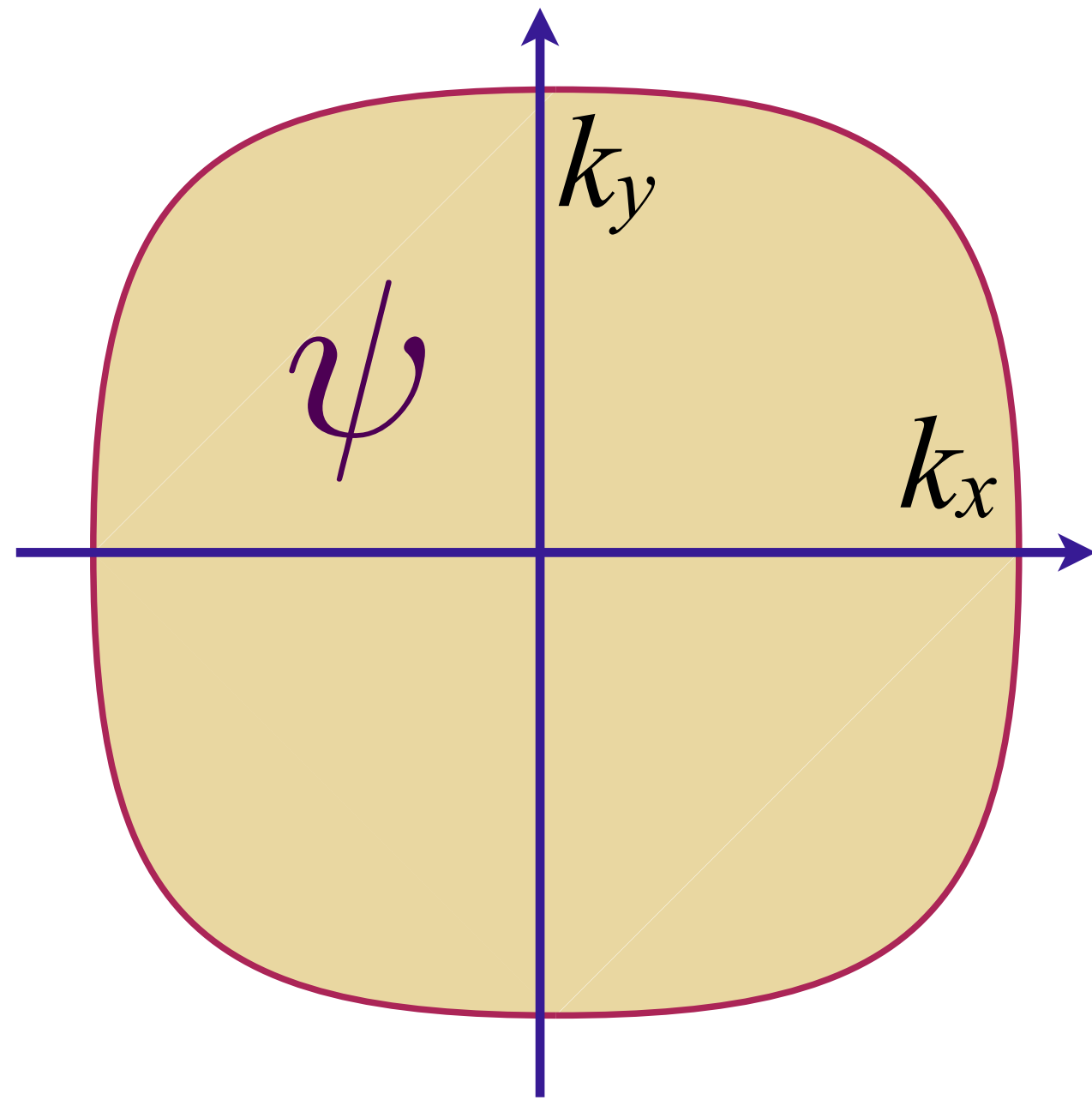
# 2D-YSYK model: Fermi surface + Higgs boson with interaction disorder

$$\mathcal{L} = c_{\mathbf{k}\alpha}^\dagger \left( \frac{\partial}{\partial \tau} + \varepsilon(\mathbf{k}) \right) c_{\mathbf{k}\alpha} + f_{1\mathbf{k}\alpha}^\dagger \left( \frac{\partial}{\partial \tau} + \tilde{\varepsilon}(\mathbf{k}) \right) f_{1\mathbf{k}\alpha}$$

$$+ [\nabla \Phi(\mathbf{r})]^2 + s [\Phi(\mathbf{r})]^2 + u [\Phi(\mathbf{r})]^4$$

$$+ [g + g'(\mathbf{r})] c_\alpha^\dagger(\mathbf{r}) f_{1\alpha}(\mathbf{r}) \Phi(\mathbf{r}) + \text{H.c.}$$

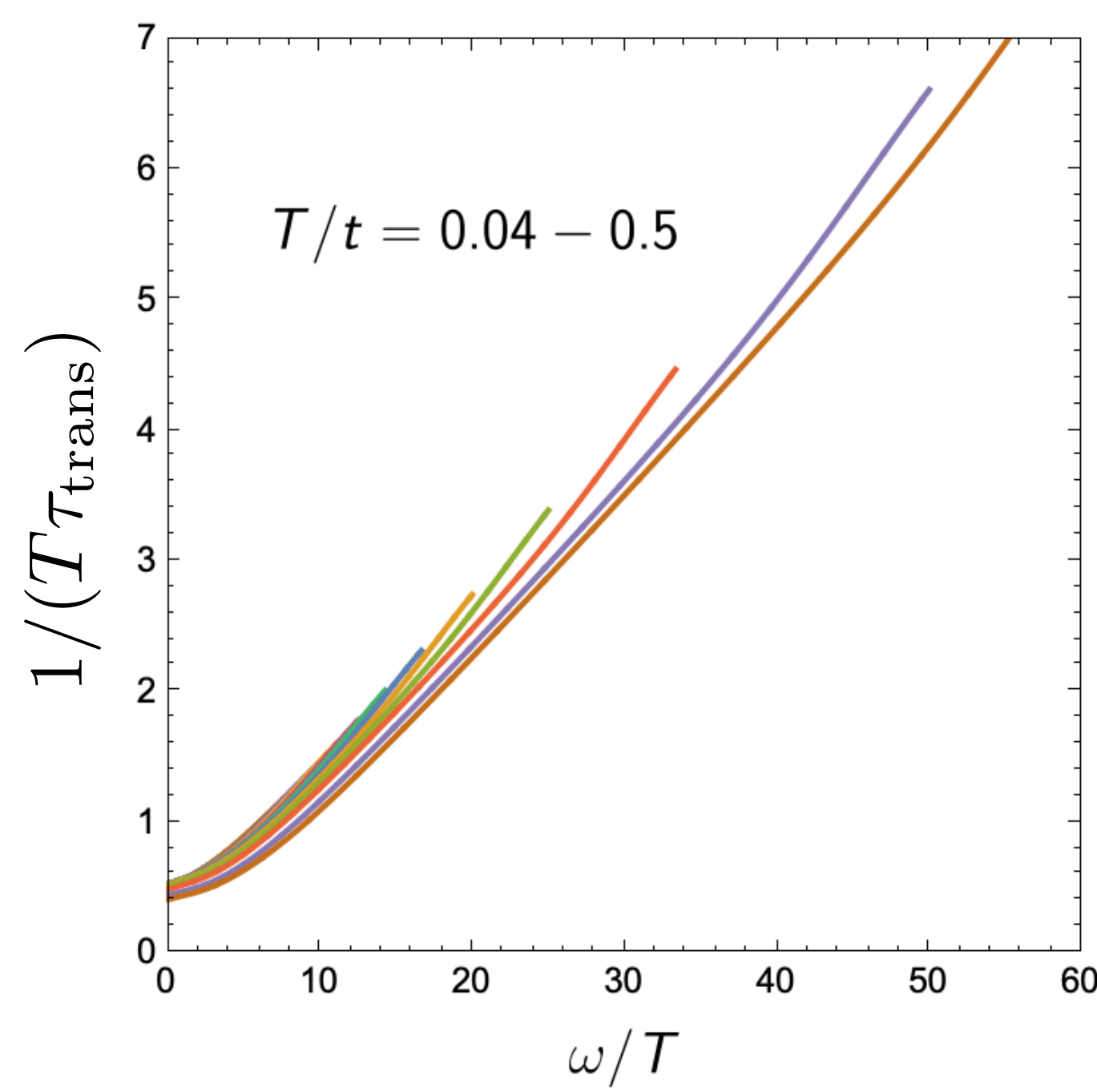
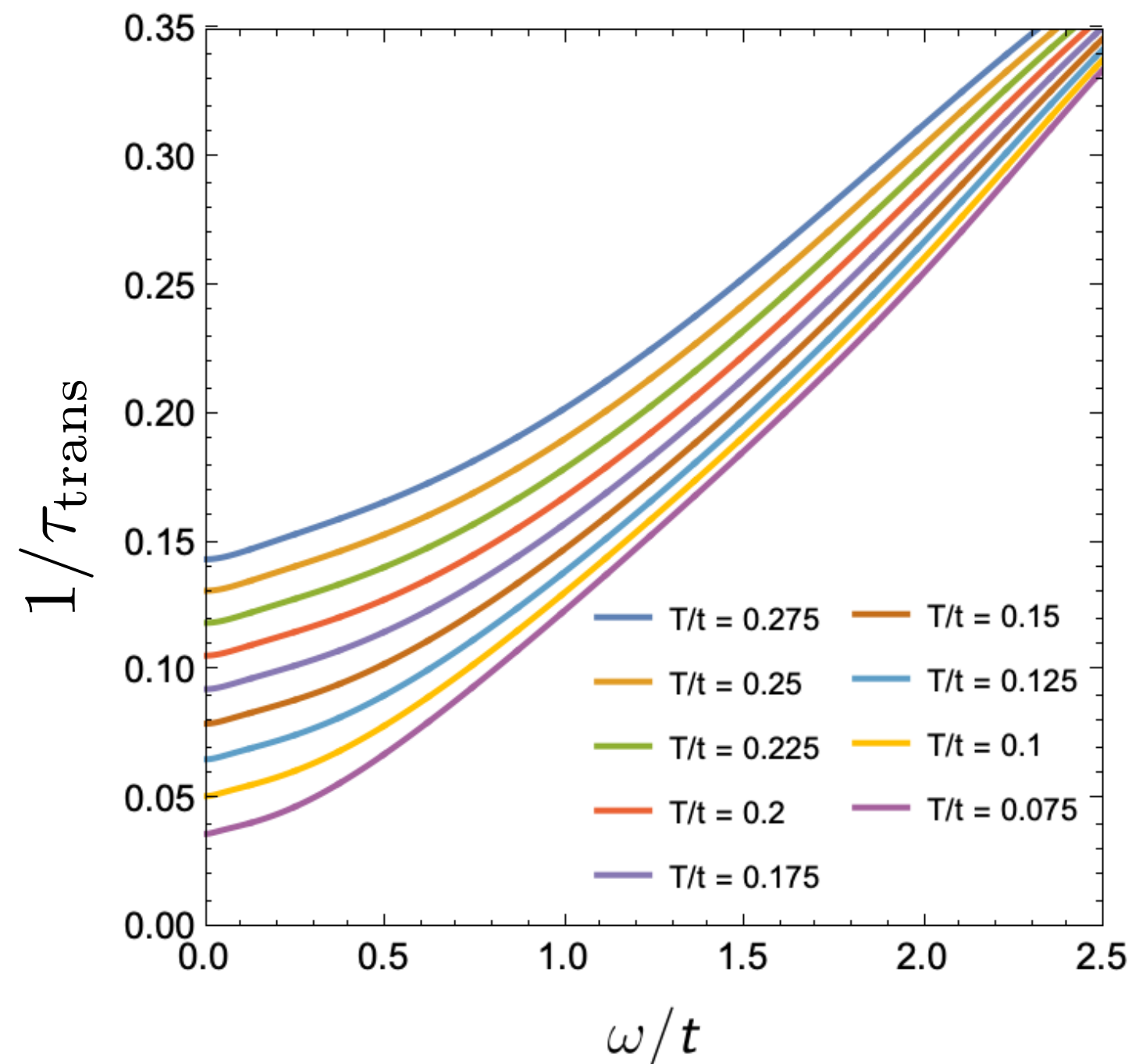
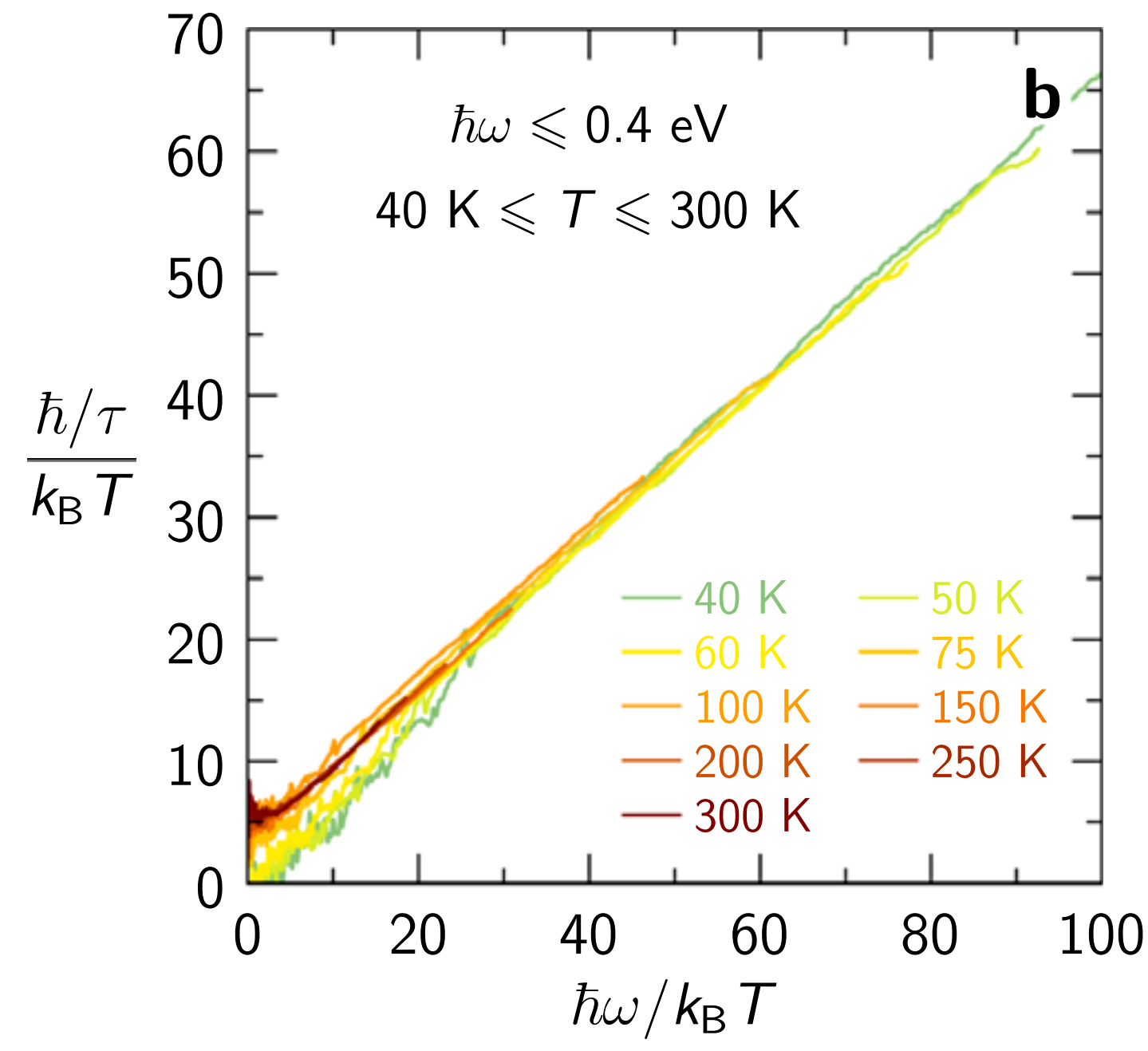
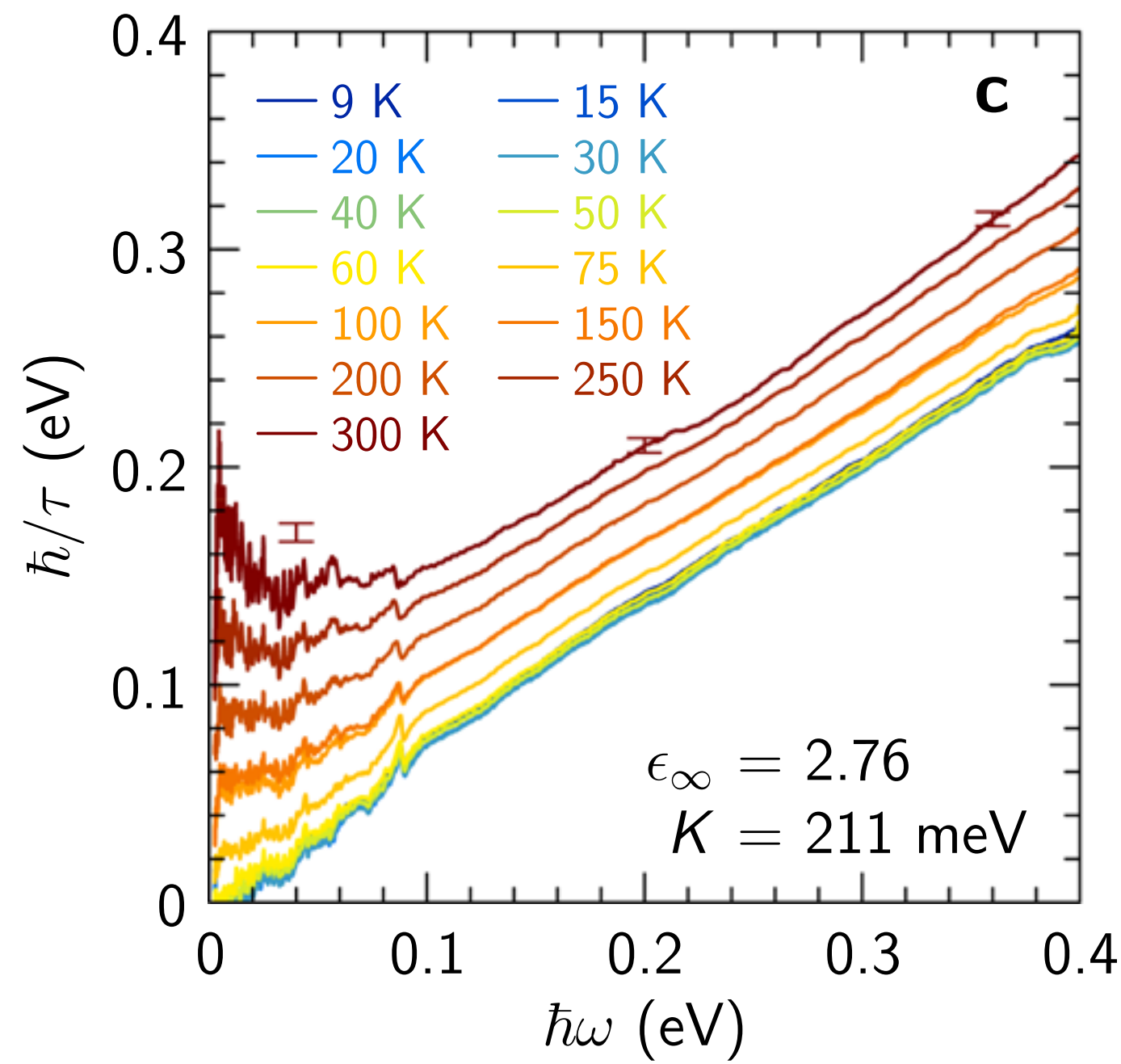
$$+ v(\mathbf{r}) c_\alpha^\dagger(\mathbf{r}) c_\alpha(\mathbf{r})$$



$\Phi^2$  “mass” disorder  $s \rightarrow s + \delta s(\mathbf{r})$  is strongly relevant;  
rescale  $\Phi$  to move disorder to the Yukawa coupling.

Spatially random Yukawa coupling  $g'(\mathbf{r})$  with  $\overline{g'(\mathbf{r})} = 0$ ,  $\overline{g'(\mathbf{r})g'(\mathbf{r}')} = g'^2 \delta(\mathbf{r} - \mathbf{r}')$

Spatially random potential  $v(\mathbf{r})$  with  $\overline{v(\mathbf{r})} = 0$ ,  $\overline{v(\mathbf{r})v(\mathbf{r}')} = v^2 \delta(\mathbf{r} - \mathbf{r}')$



$$\sigma(\omega) = i \frac{e^2 K / (\hbar d_c)}{\hbar\omega \frac{m^*(\omega)}{m} + i \frac{\hbar}{\tau(\omega)}}$$

From  
optical conductivity  
data of  
Michon et al. (2023)

$$\frac{\hbar}{\tau(\omega)} = k_B T \Phi_\tau \left( \frac{\hbar\omega}{k_B T} \right)$$

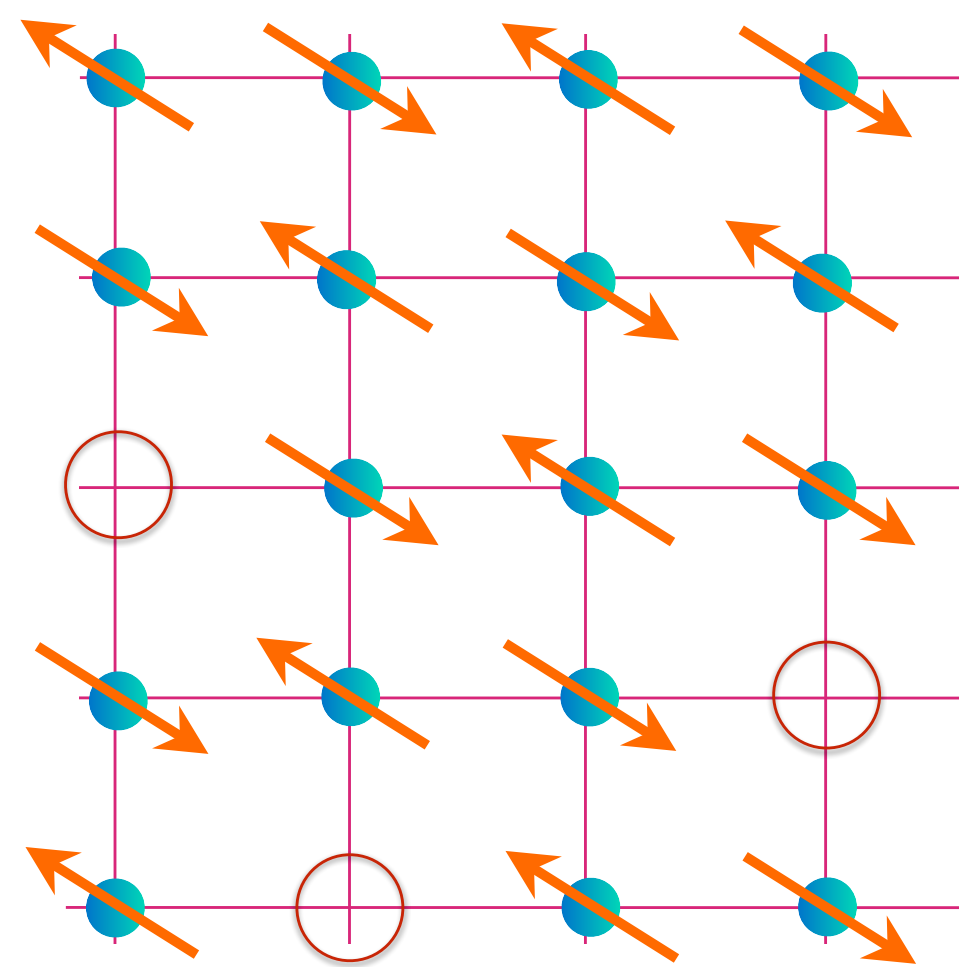
## 2d-YSYK theory

Aavishkar A. Patel, Haoyu Guo, Ilya Esterlis, S. S., *Science* **381**, 790 (2023)

Chenyuan Li, Aavishkar A. Patel, Haoyu Guo, Davide Valentini, Jorg Schmalian, S.S., Ilya Esterlis, *PRL* **133**, 186502 (2024)

Summary

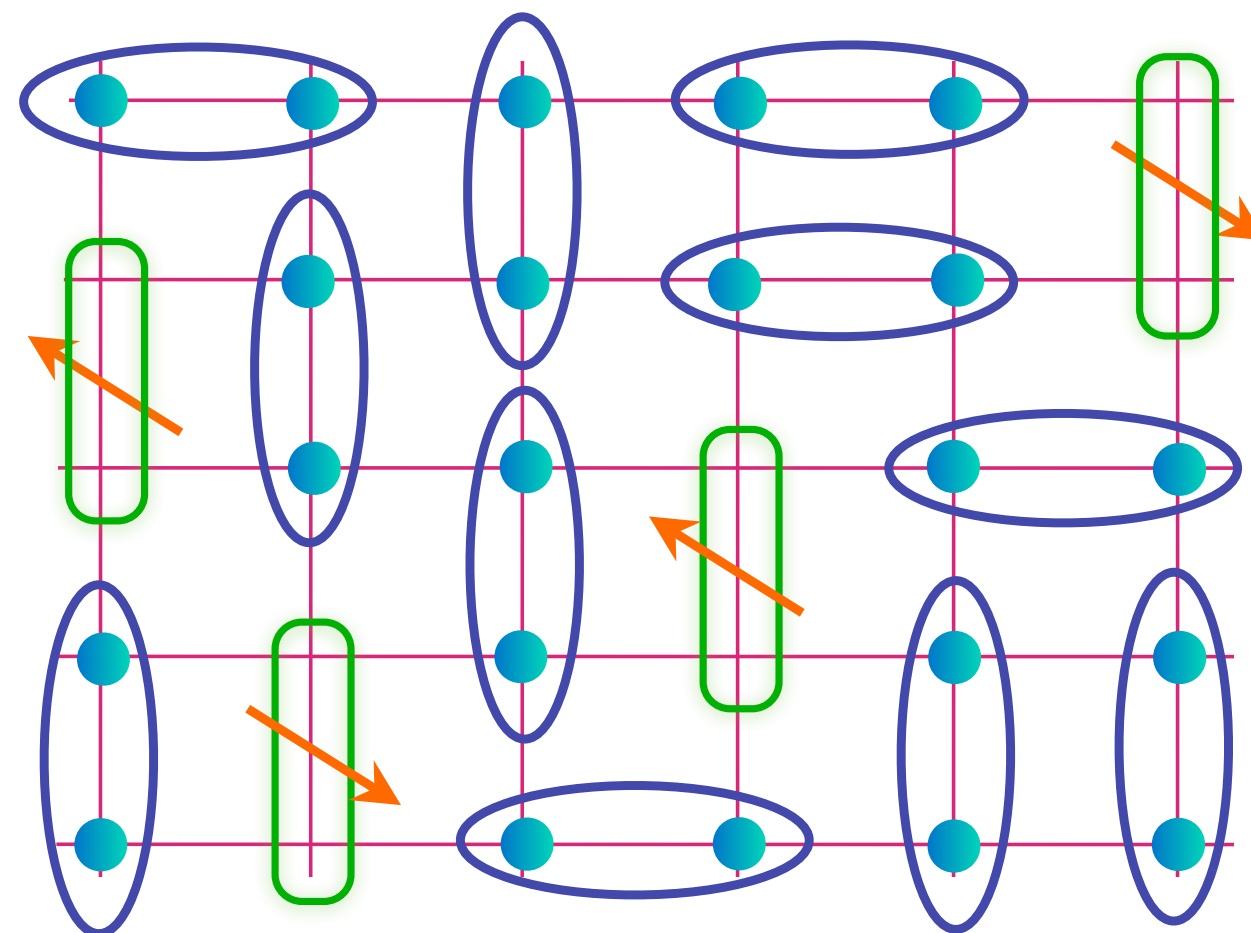
# AF Metal



Carrier density  $p$   
Pocket area  $p/4$

$$\langle (-1)^r \mathbf{S}_r \rangle \neq 0$$

# FL\*



$$\text{Green oval with arrow} = (|\uparrow \circ\rangle + |\circ \uparrow\rangle) / \sqrt{2}$$

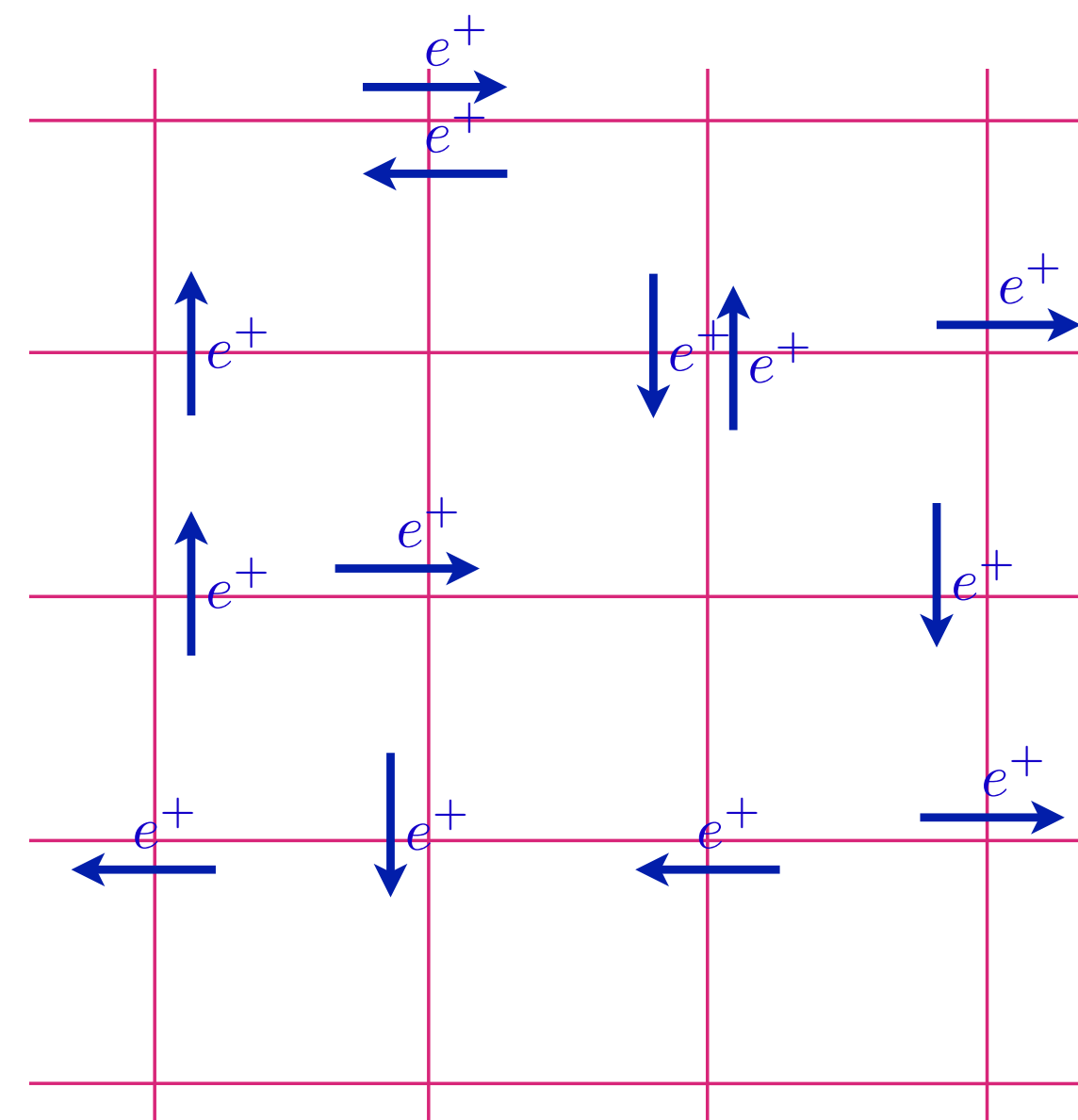
$$\text{Blue oval} = (|\uparrow \downarrow\rangle - |\downarrow \uparrow\rangle) / \sqrt{2}$$

Carrier density  $p$   
Pocket area  $p/8$

$$\langle (-1)^r \mathbf{S}_r \rangle = 0$$

$$\langle \Phi \rangle \neq 0$$

# FL



Carrier density  $1 + p$   
Fermi area  $(1 + p)/2$

$$\langle \Phi \rangle = 0$$

FL\*-FL:  
Quantum  
phase transition  
between two metals  
at  $p = p_c$ , with  
no symmetry breaking.

Described by the  
condensation of a  
Higgs field  $\Phi$ .

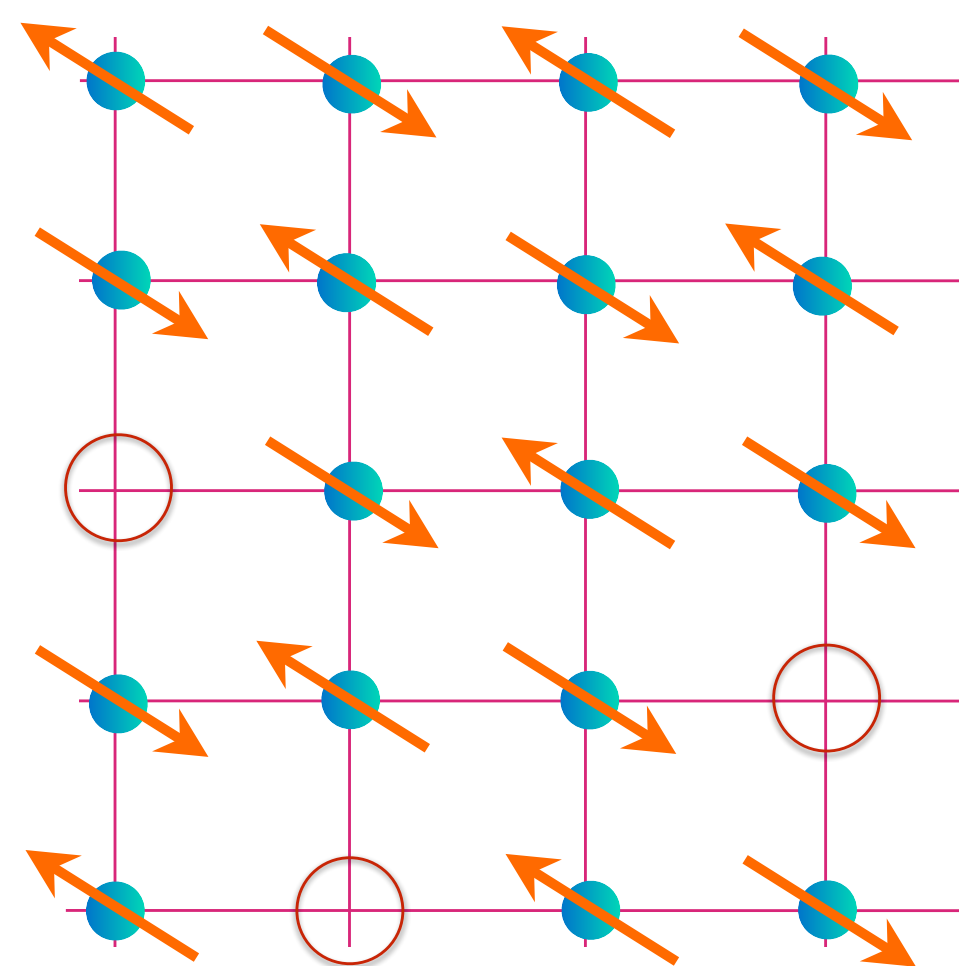
$p_{sdw}$

$p_c$

$p$

**AF**

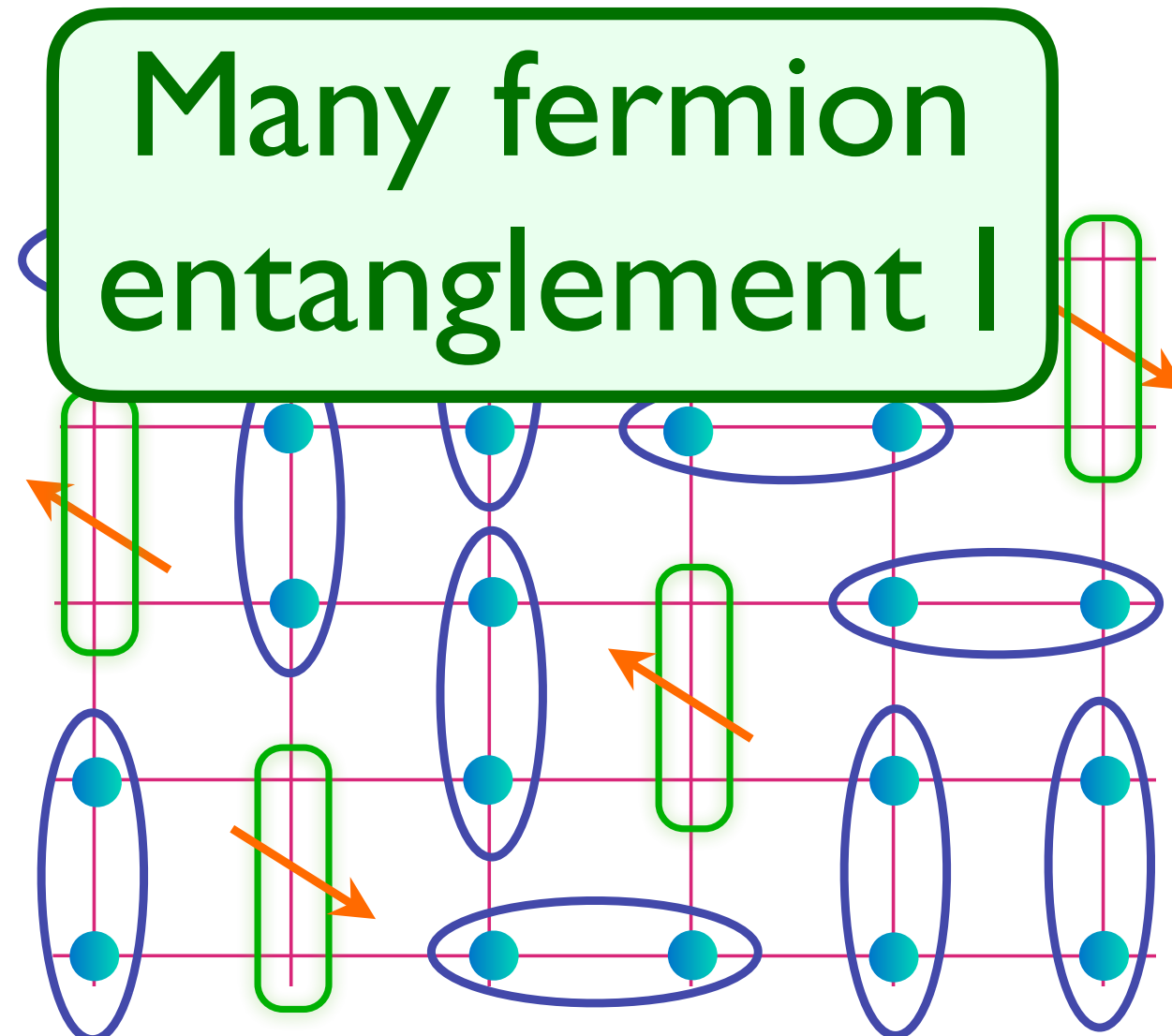
**Metal**



Carrier density  $p$   
 Pocket area  $p/4$

$$\langle (-1)^r \mathbf{S}_r \rangle \neq 0$$

**FL\***



$$\text{Green oval with arrow} = (|\uparrow \circ\rangle + |\circ \uparrow\rangle) / \sqrt{2}$$

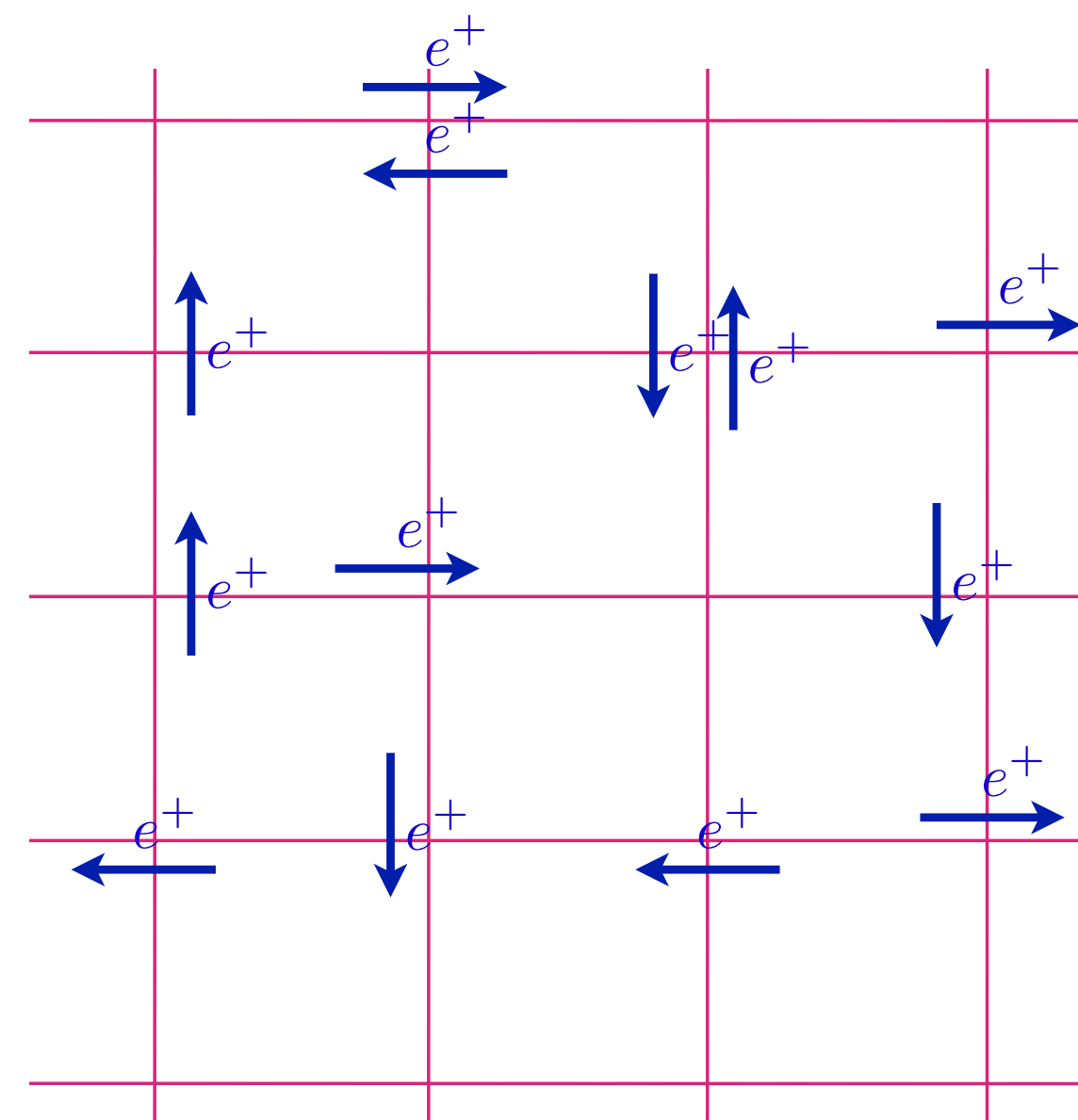
$$\text{Blue oval} = (|\uparrow \downarrow\rangle - |\downarrow \uparrow\rangle) / \sqrt{2}$$

Carrier density  $p$   
 Pocket area  $p/8$

$$\langle (-1)^r \mathbf{S}_r \rangle = 0$$

$$\langle \Phi \rangle \neq 0$$

**FL**



Carrier density  $1 + p$   
 Fermi area  $(1 + p)/2$

$$\langle \Phi \rangle = 0$$

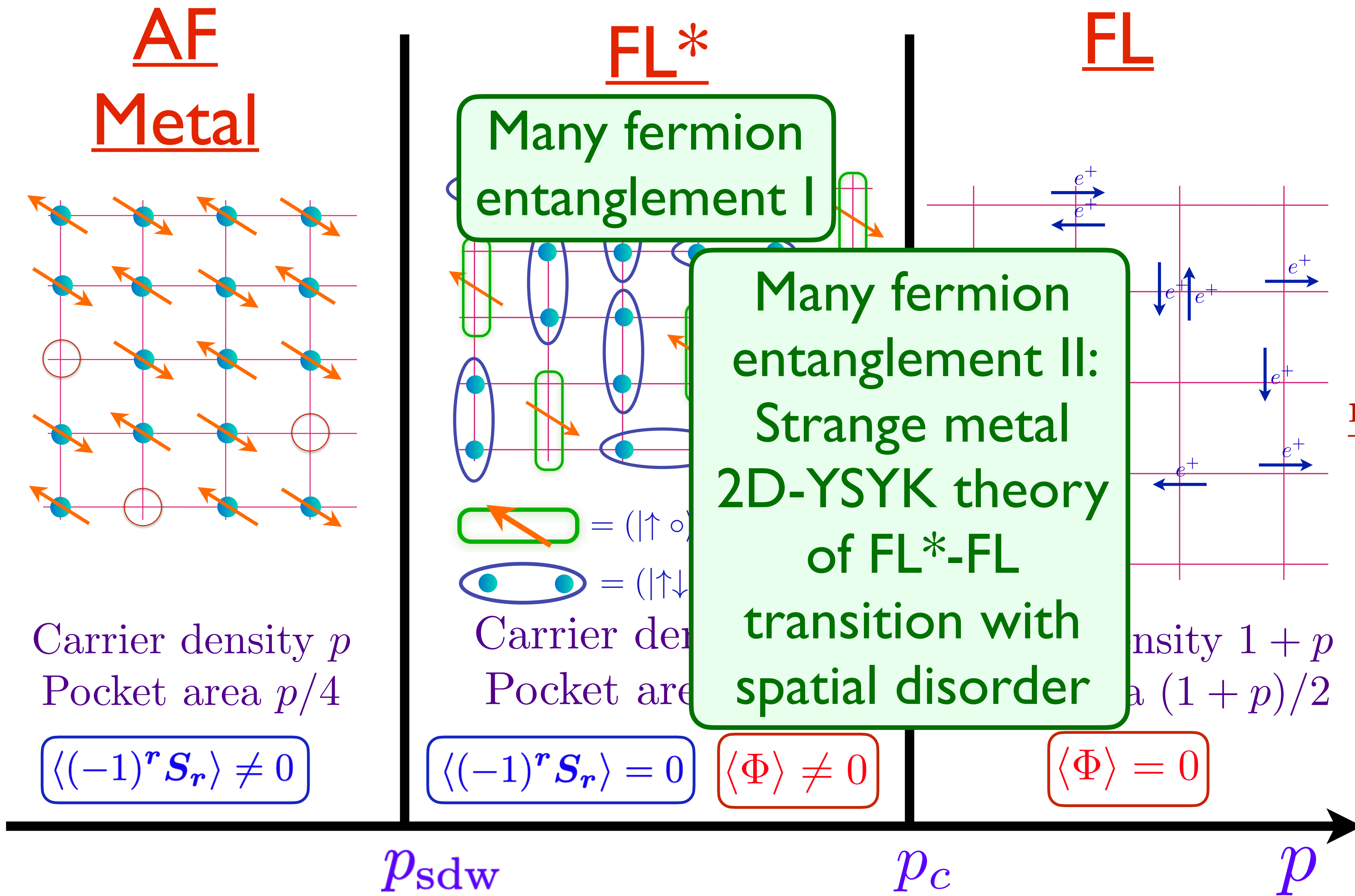
FL\*-FL:  
 Quantum phase transition between two metals at  $p = p_c$ , with no symmetry breaking.

Described by the condensation of a Higgs field  $\Phi$ .

$p_{sdw}$

$p_c$

$p$



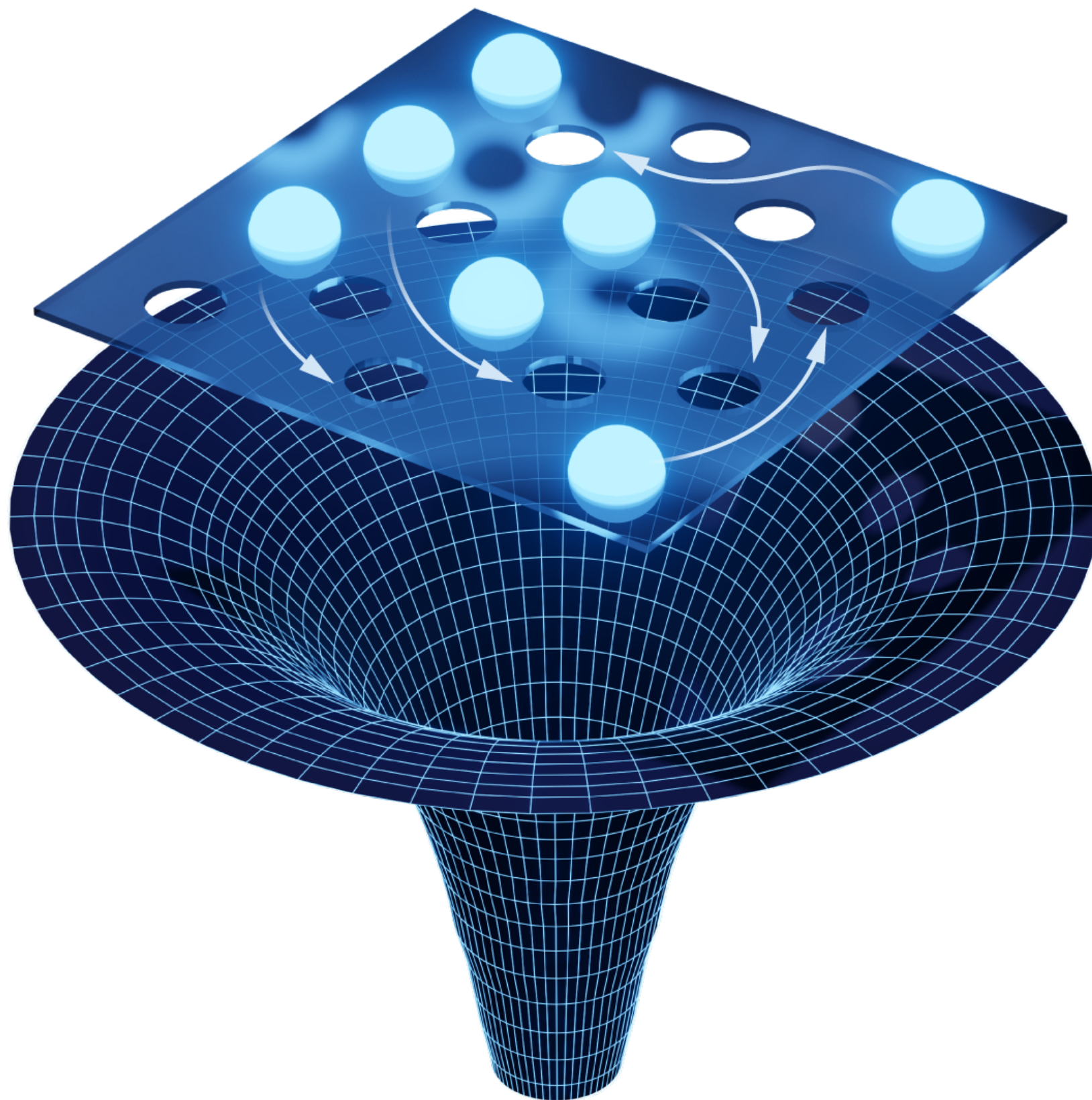
FL\*-FL:  
Quantum phase transition between two metals at  $p = p_c$ , with no symmetry breaking.

Described by the condensation of a Higgs field  $\Phi$ .

# The Sachdev-Ye-Kitaev (SYK) model

The SYK model describes multi-particle quantum entanglement resulting in the loss of identity of the particles

Many fermion entanglement II



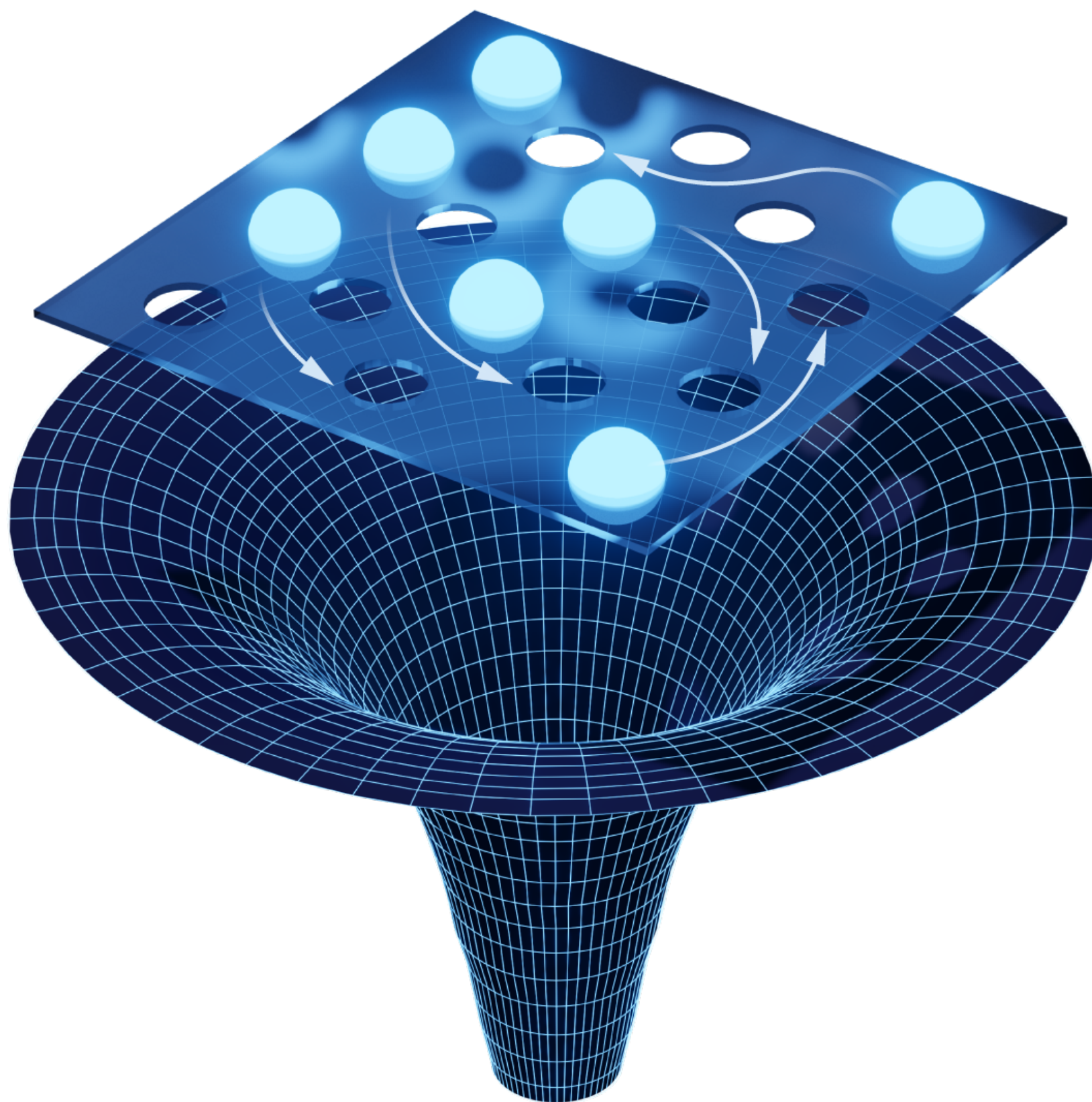
# The Sachdev-Ye-Kitaev (SYK) model

The SYK model describes multi-particle quantum entanglement resulting in the loss of identity of the particles

Many fermion entanglement II

Extending to 2D-YSYK theory of FL\*-FL transition, it helps describe the *strange* electrical properties of YBCO

Patel, Guo, Esterlis, Sachdev (2023)



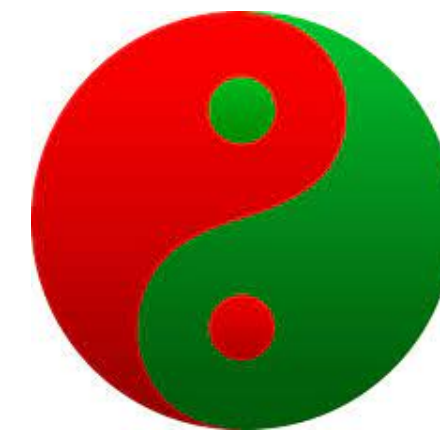
# The Sachdev-Ye-Kitaev (SYK) model

The SYK model describes multi-particle quantum entanglement resulting in the loss of identity of the particles

Many fermion entanglement II

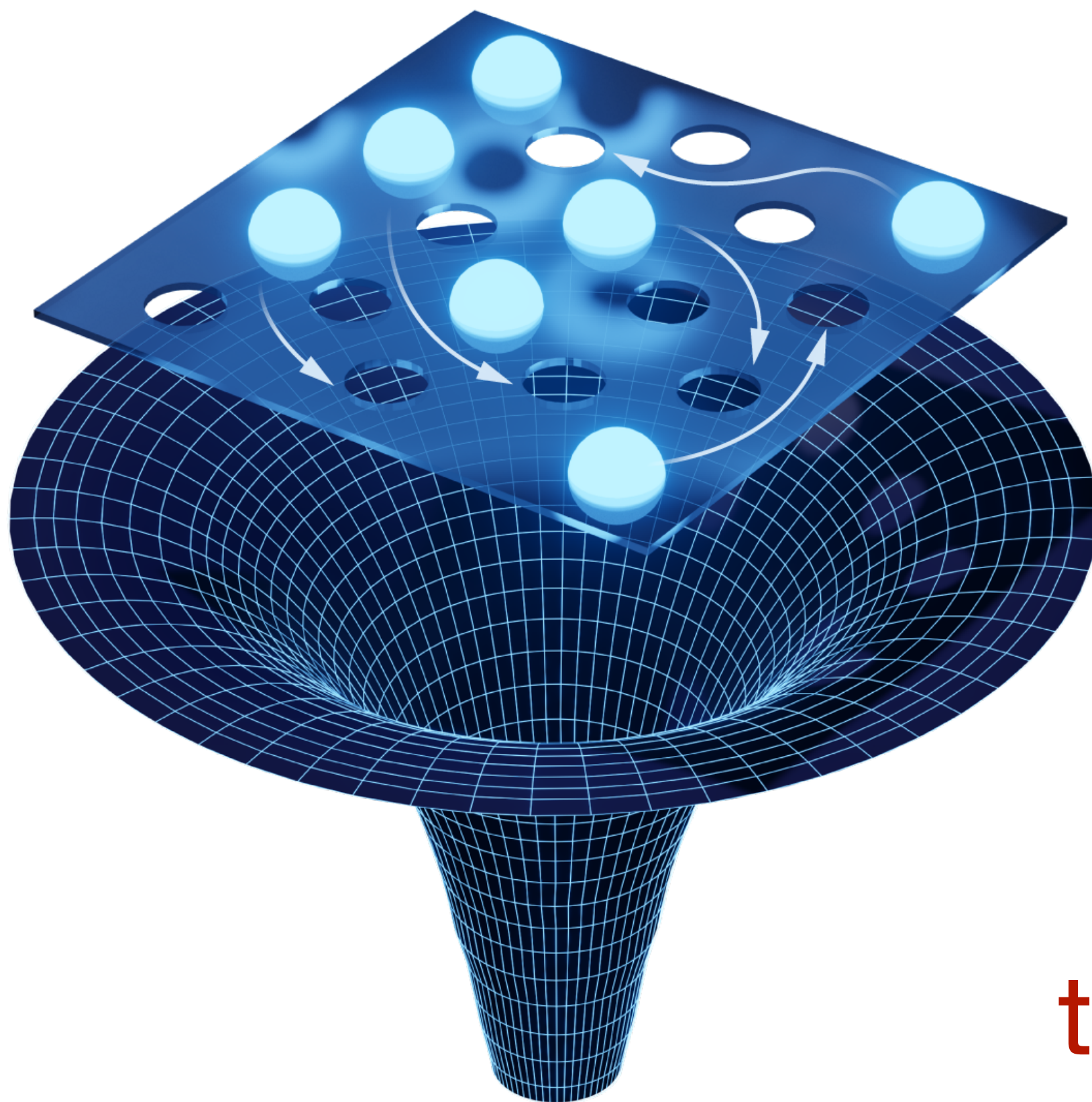
Extending to 2D-YSYK theory of FL\*-FL transition, it helps describe the *strange* electrical properties of YBCO

Patel, Guo, Esterlis, Sachdev (2023)



In a *dual* set of variables it describes the quantum horizon of *charged black holes*

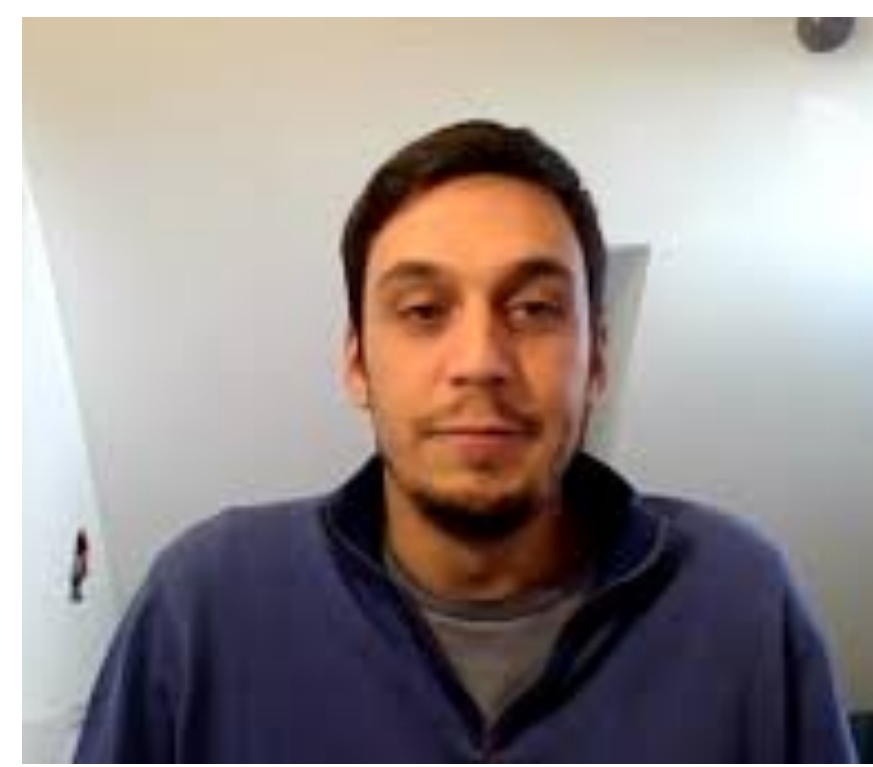
Sachdev (2010), Kitaev (2015), Maldacena Stanford (2015)





Maine Christos  
Caltech

The Institute of  
Mathematical  
Sciences,  
Chennai



Pietro Bonetti  
Stuttgart



Alexander  
Nikolaenko



Aavishkar Patel  
ICTS, Bengaluru



Harshit Pandey



Ravi Shanker



Sayantan Sharma

- *Lectures on insulating and conducting quantum spin liquids*, S. Sachdev, arXiv:2512.23962
- *Fractionalized Fermi liquids and the cuprate phase diagram*, P. M. Bonetti, M. Christos, A. Nikolaenko, A.A. Patel, and S. Sachdev, arXiv:2508.20164
- *Thermal  $SU(2)$  lattice gauge theory of the cuprate pseudogap: reconciling Fermi arcs and hole pockets*, H. Pandey, M. Christos, P. M. Bonetti, R. Shanker, A. Nikolaenko, S. Sharma, and S. Sachdev, arXiv:2507.05336