

Statistical mechanics of strange metals and black holes

Kansas State University
April 25, 2022

Subir Sachdev



Talk online: sachdev.physics.harvard.edu



INSTITUTE FOR
ADVANCED STUDY

PHYSICS



HARVARD

Foundations

by

Boltzmann

Statistical interpretation of entropy (1870)

$$S = k_B \log W$$

Density of quantum states $D(E) = \exp(S(E)/k_B)$



Ludwig Boltzmann

20 February 1844 - September 5, 1906

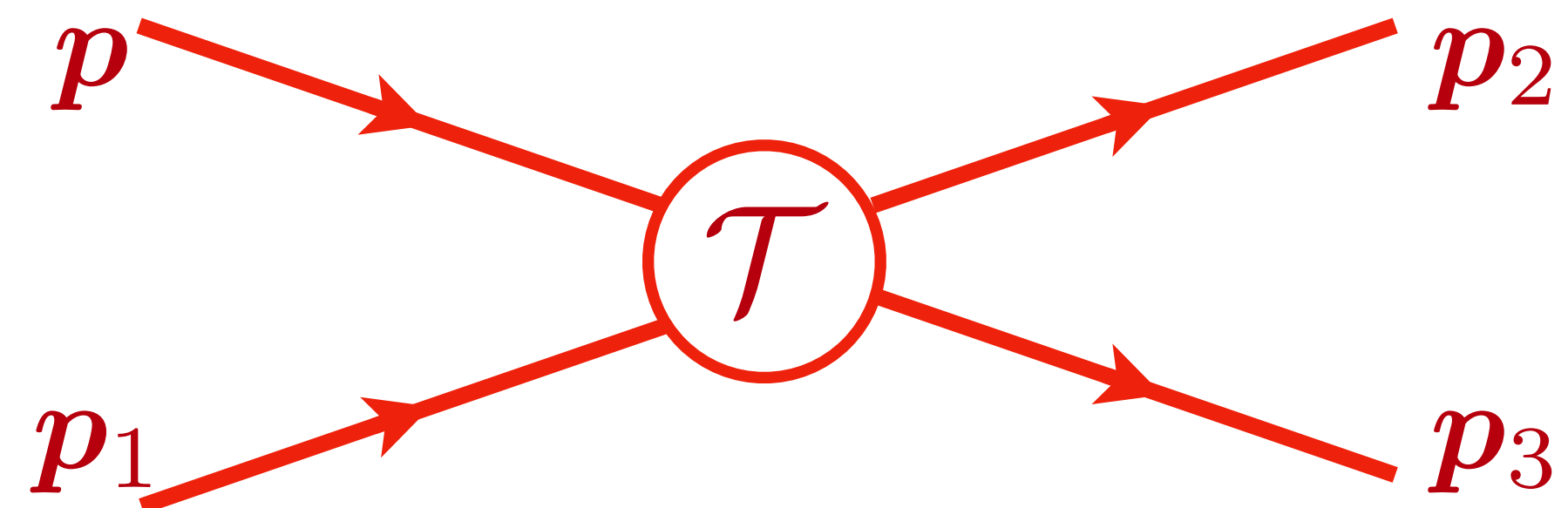
Vienna, Austria

Boltzmann equation (1872)

Dilute classical gas

Molecular chaos: successive collisions are statistically independent

$$\frac{\partial f_{\mathbf{p}}}{\partial t} + \frac{\partial \varepsilon_{\mathbf{p}}}{\partial \mathbf{p}} \cdot \nabla_{\mathbf{r}} f_{\mathbf{p}} + \mathbf{F} \cdot \nabla_{\mathbf{p}} f_{\mathbf{p}} =$$
$$- 2\pi \int_{\mathbf{p}_{1,2,3}} |\mathcal{T}|^2 \delta(\varepsilon_{\mathbf{p}} + \varepsilon_{\mathbf{p}_1} - \varepsilon_{\mathbf{p}_2} - \varepsilon_{\mathbf{p}_3}) \delta(\mathbf{p} + \mathbf{p}_1 - \mathbf{p}_2 - \mathbf{p}_3)$$
$$\times [f_{\mathbf{p}} f_{\mathbf{p}_1} - f_{\mathbf{p}_2} f_{\mathbf{p}_3}]$$



Ludwig Boltzmann

20 February 1844 - September 5, 1906

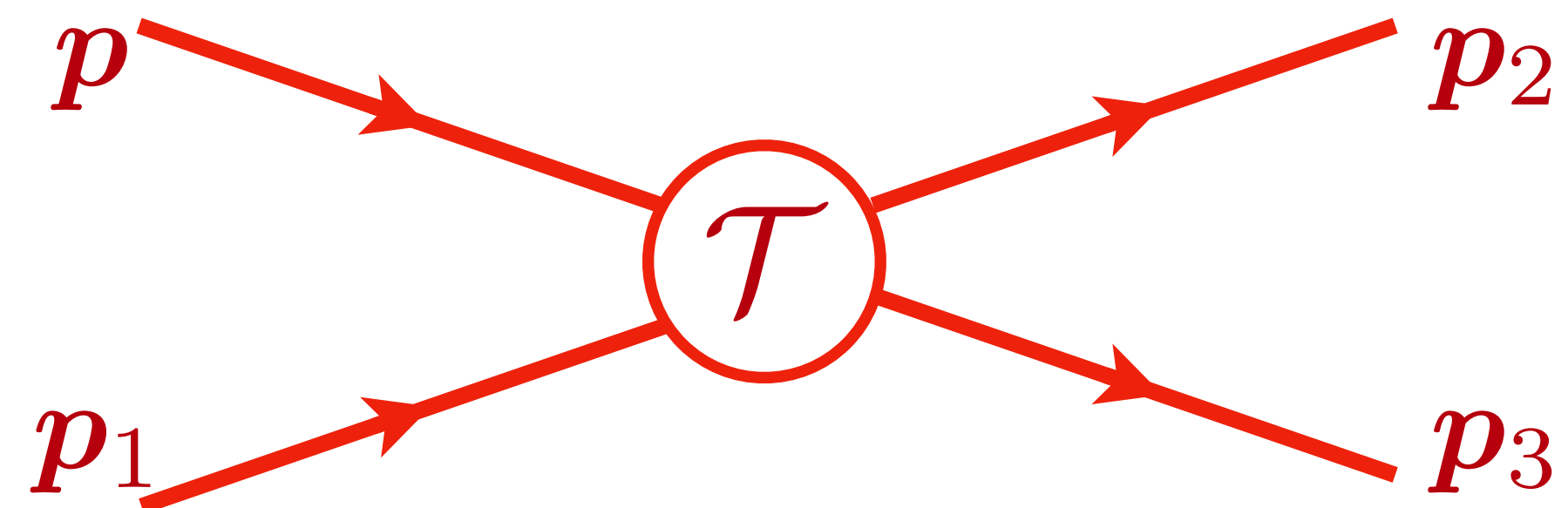
Vienna, Austria

Quantum Boltzmann equation (Landau)

Dense gas of electrons

Neglects quantum interference (entanglement)
between successive collisions

$$\frac{\partial f_{\mathbf{p}}}{\partial t} + \frac{\partial \varepsilon_{\mathbf{p}}}{\partial \mathbf{p}} \cdot \nabla_{\mathbf{r}} f_{\mathbf{p}} + \mathbf{F} \cdot \nabla_{\mathbf{p}} f_{\mathbf{p}} =$$
$$- 2\pi \int_{\mathbf{p}_{1,2,3}} |\mathcal{T}|^2 \delta(\varepsilon_{\mathbf{p}} + \varepsilon_{\mathbf{p}_1} - \varepsilon_{\mathbf{p}_2} - \varepsilon_{\mathbf{p}_3}) \delta(\mathbf{p} + \mathbf{p}_1 - \mathbf{p}_2 - \mathbf{p}_3)$$
$$\times [f_{\mathbf{p}} f_{\mathbf{p}_1} (1 - f_{\mathbf{p}_2}) (1 - f_{\mathbf{p}_3}) - f_{\mathbf{p}_2} f_{\mathbf{p}_3} (1 - f_{\mathbf{p}}) (1 - f_{\mathbf{p}_1})]$$



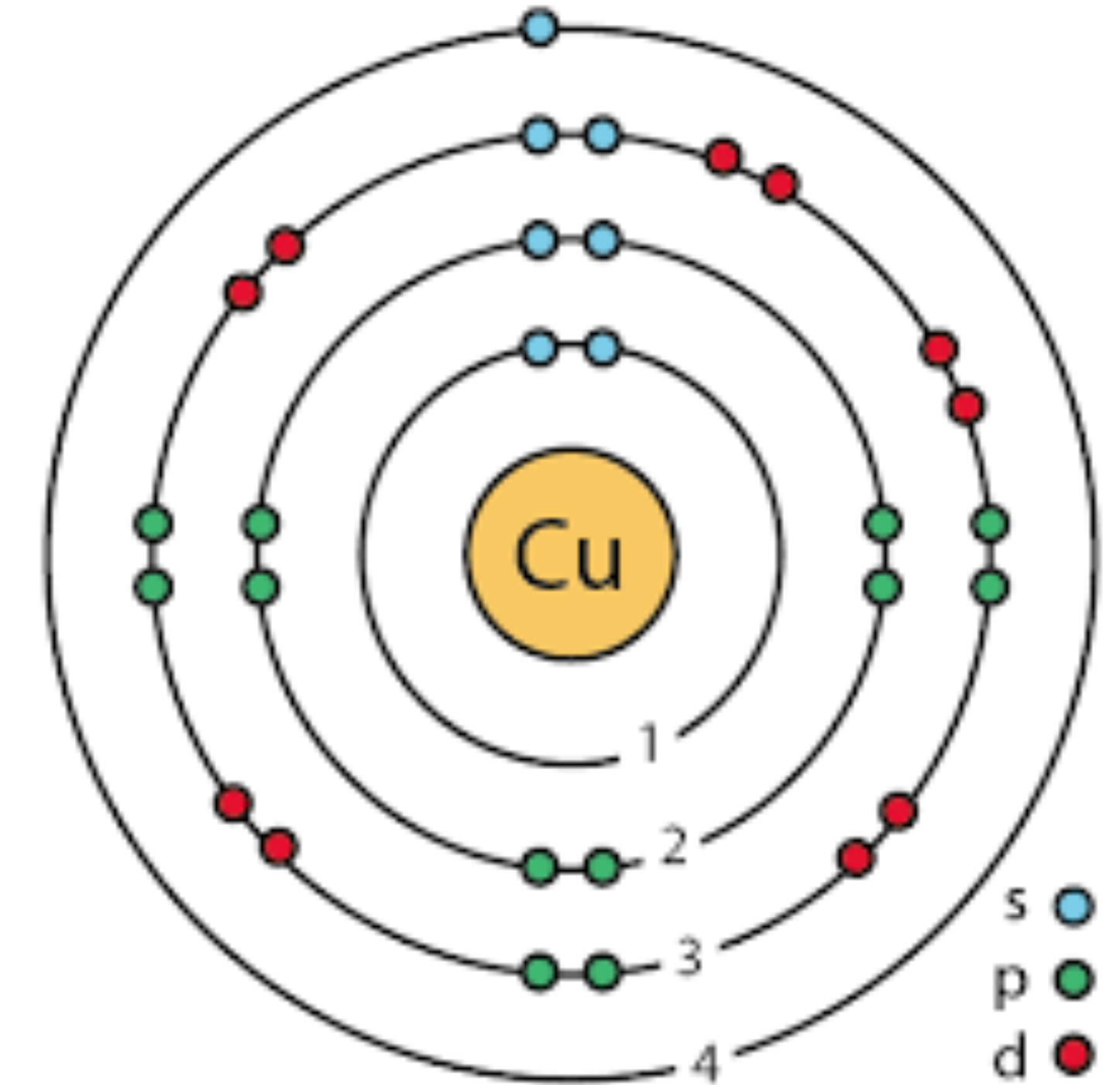
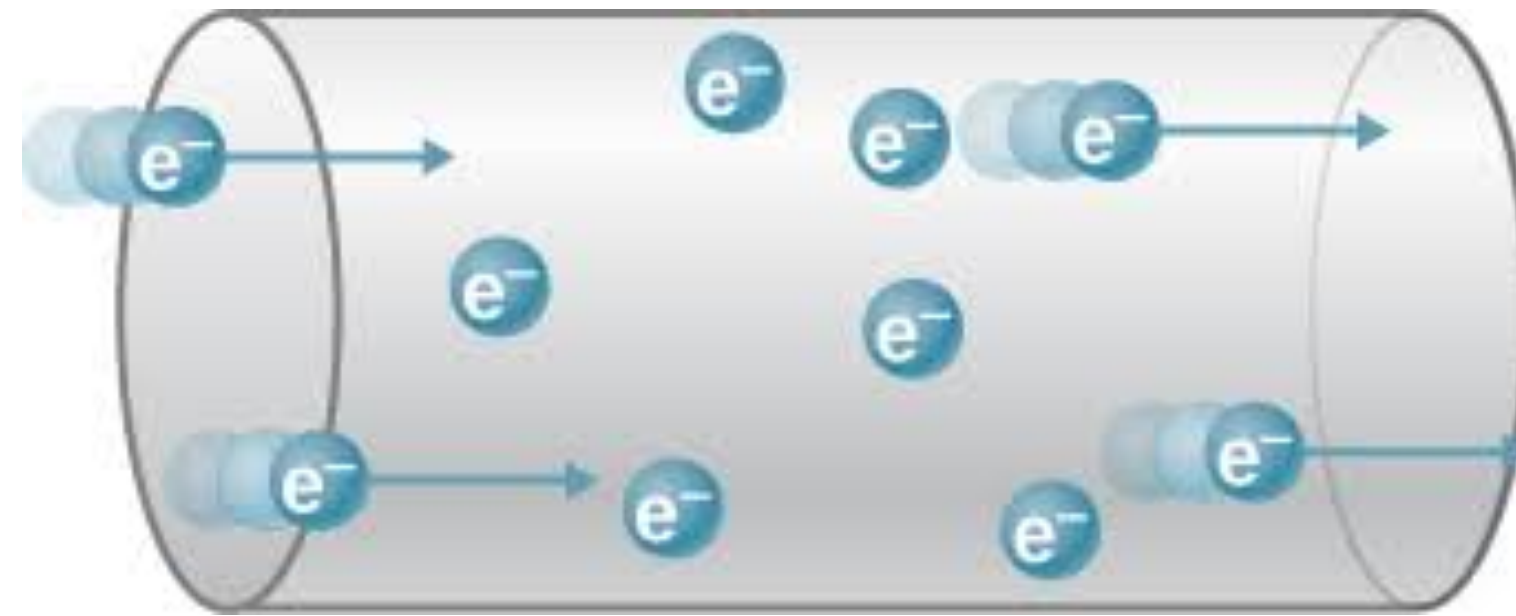
Ludwig Boltzmann

20 February 1844 - September 5, 1906

Vienna, Austria

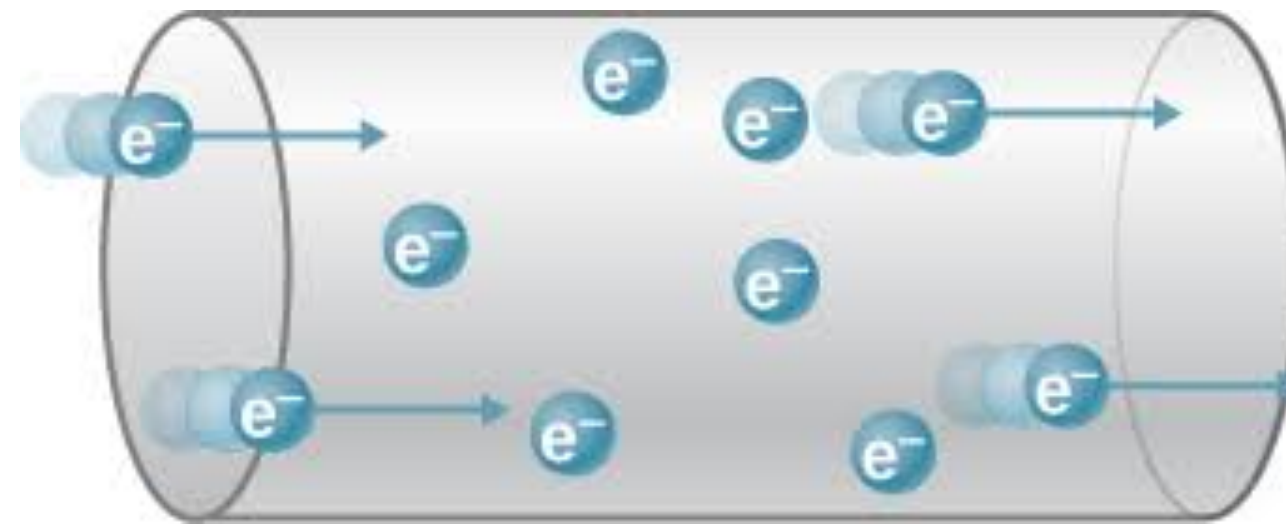
Quantum theory of
electrons:
ordinary metals
and
strange metals

Copper



Each copper atom donates its outermost electron
These electrons move freely throughout the crystal and carry current

Current flow with electrons in Copper

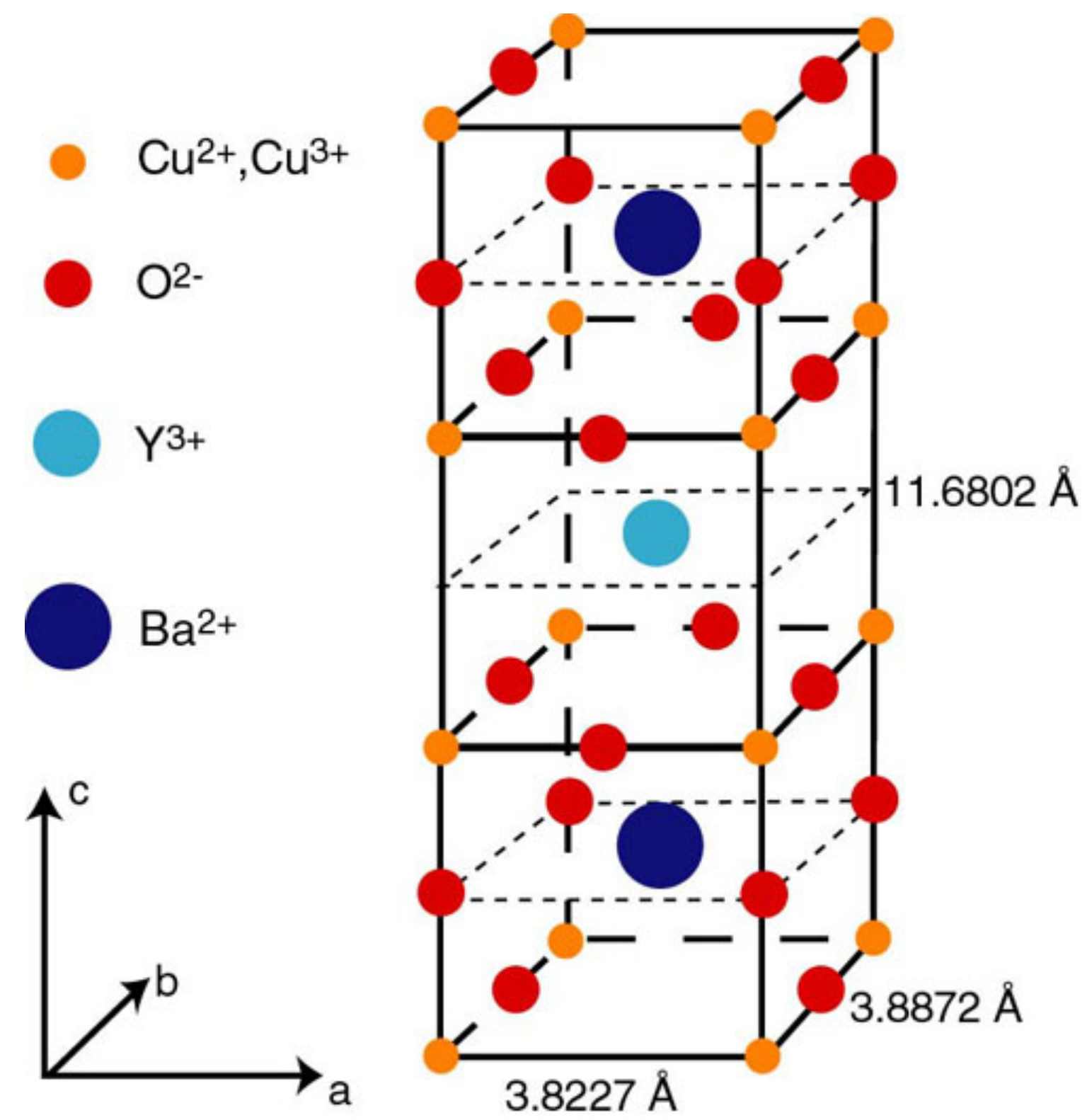
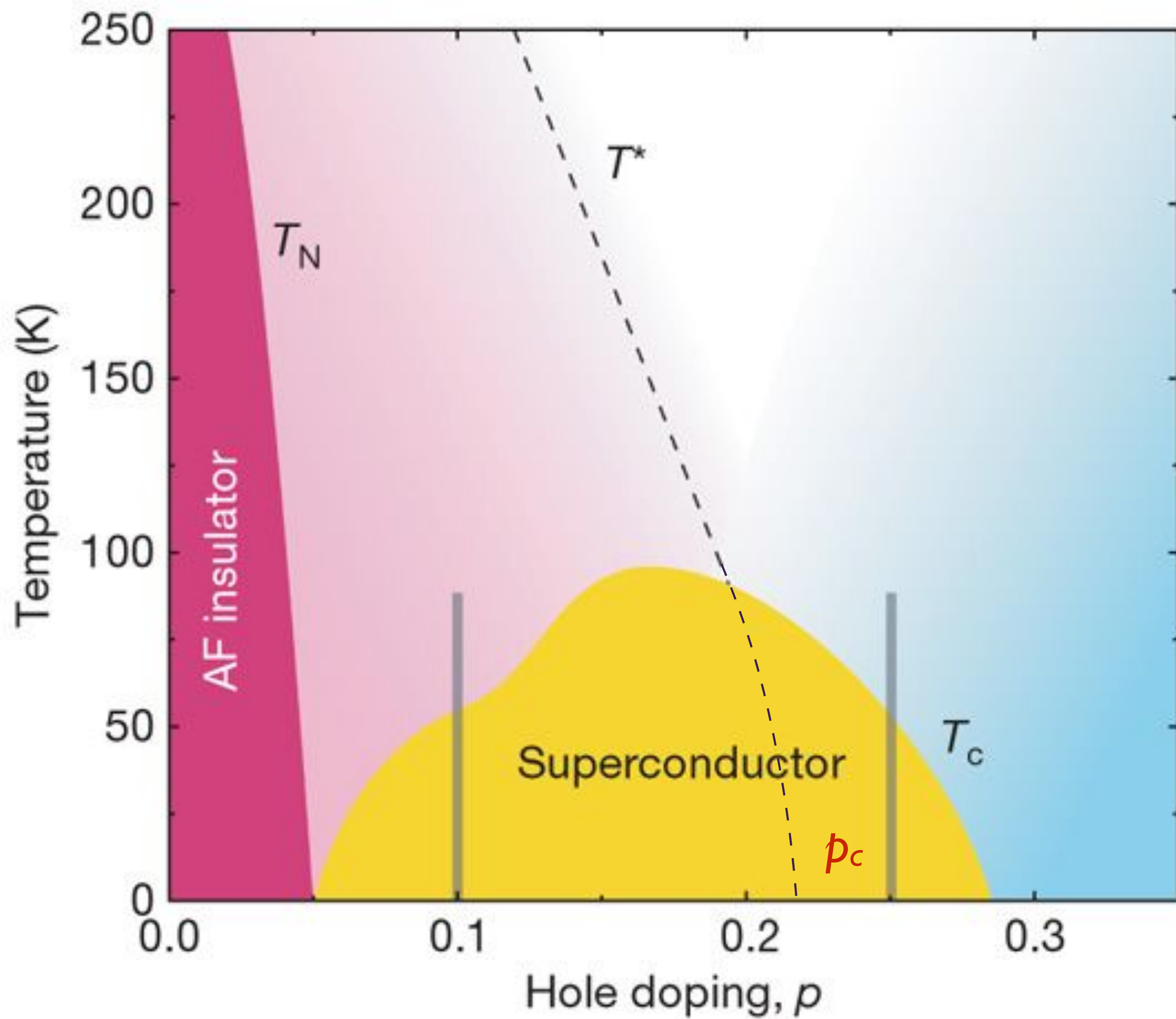


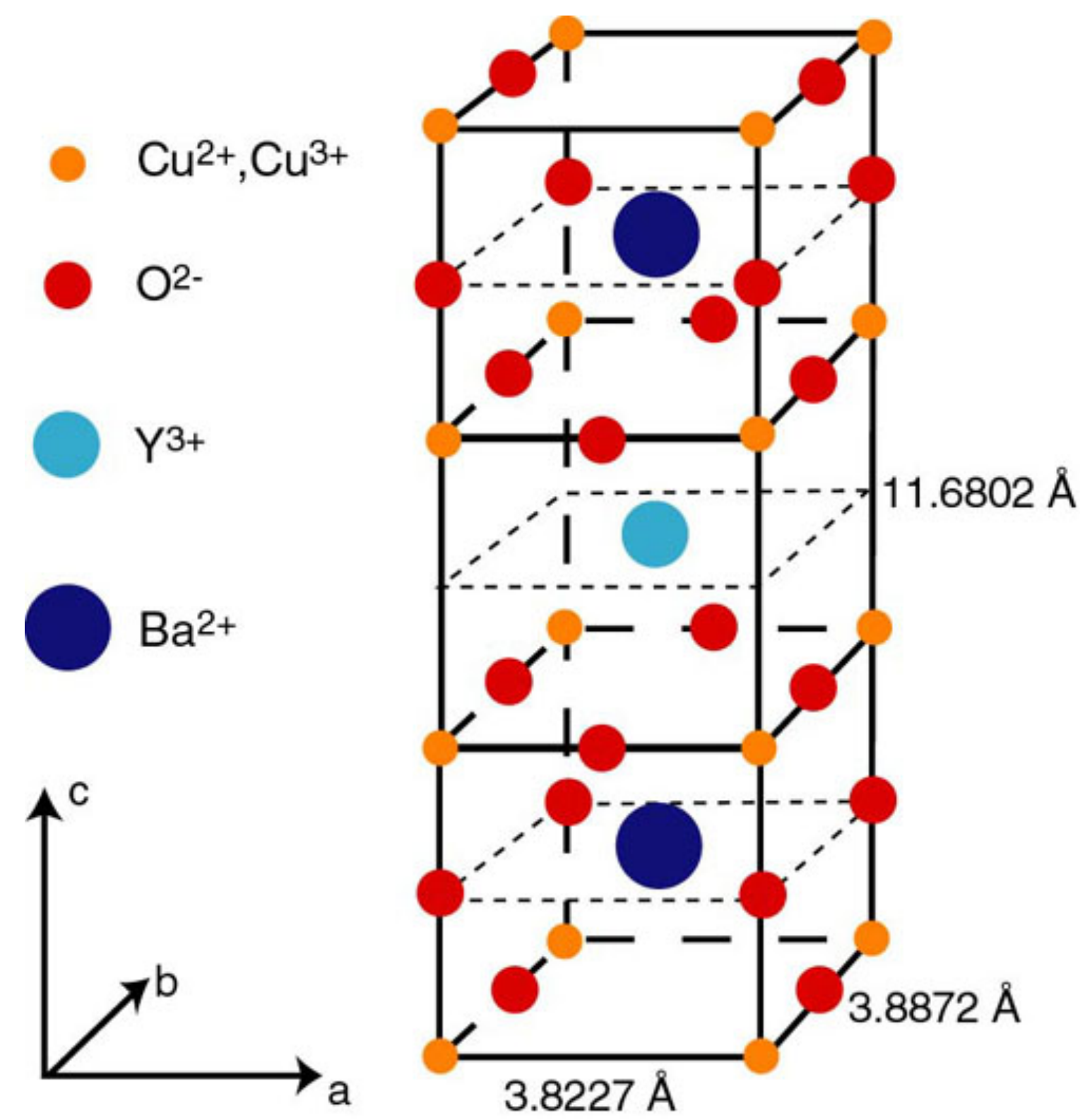
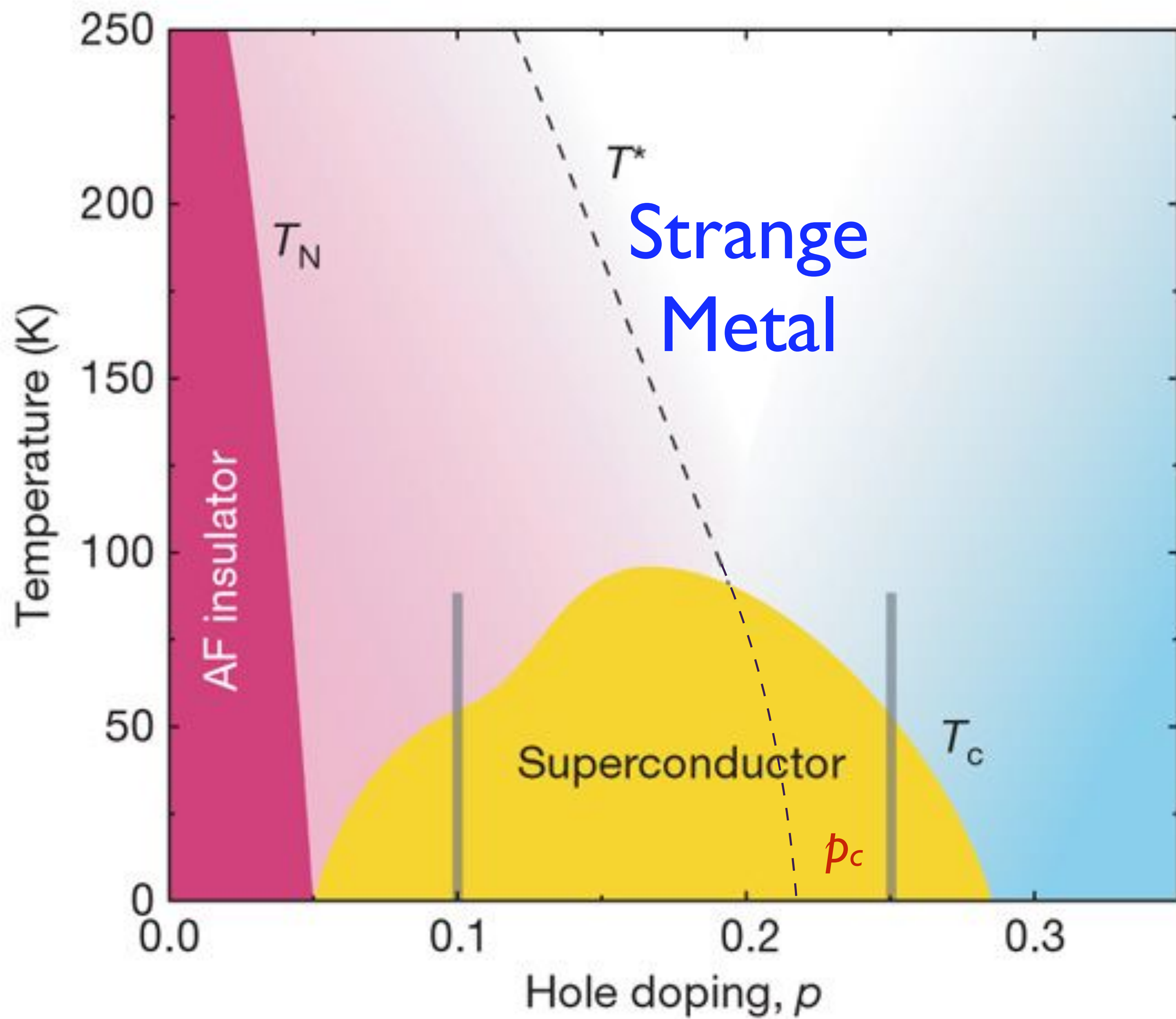
Flow of electrons described by Boltzmann equation \Rightarrow
typical scattering time $\tau \sim 1/T^2$, resistivity $\rho(T) = \rho(0) + AT^2$

The time τ is much longer than a limiting ‘Planckian time’ $\frac{\hbar}{k_B T}$.

The long scattering time implies that individual electrons are well-defined.

The motion of electrons is ‘ballistic’ or ‘integrable’
up to the long time τ , after which it is chaotic.

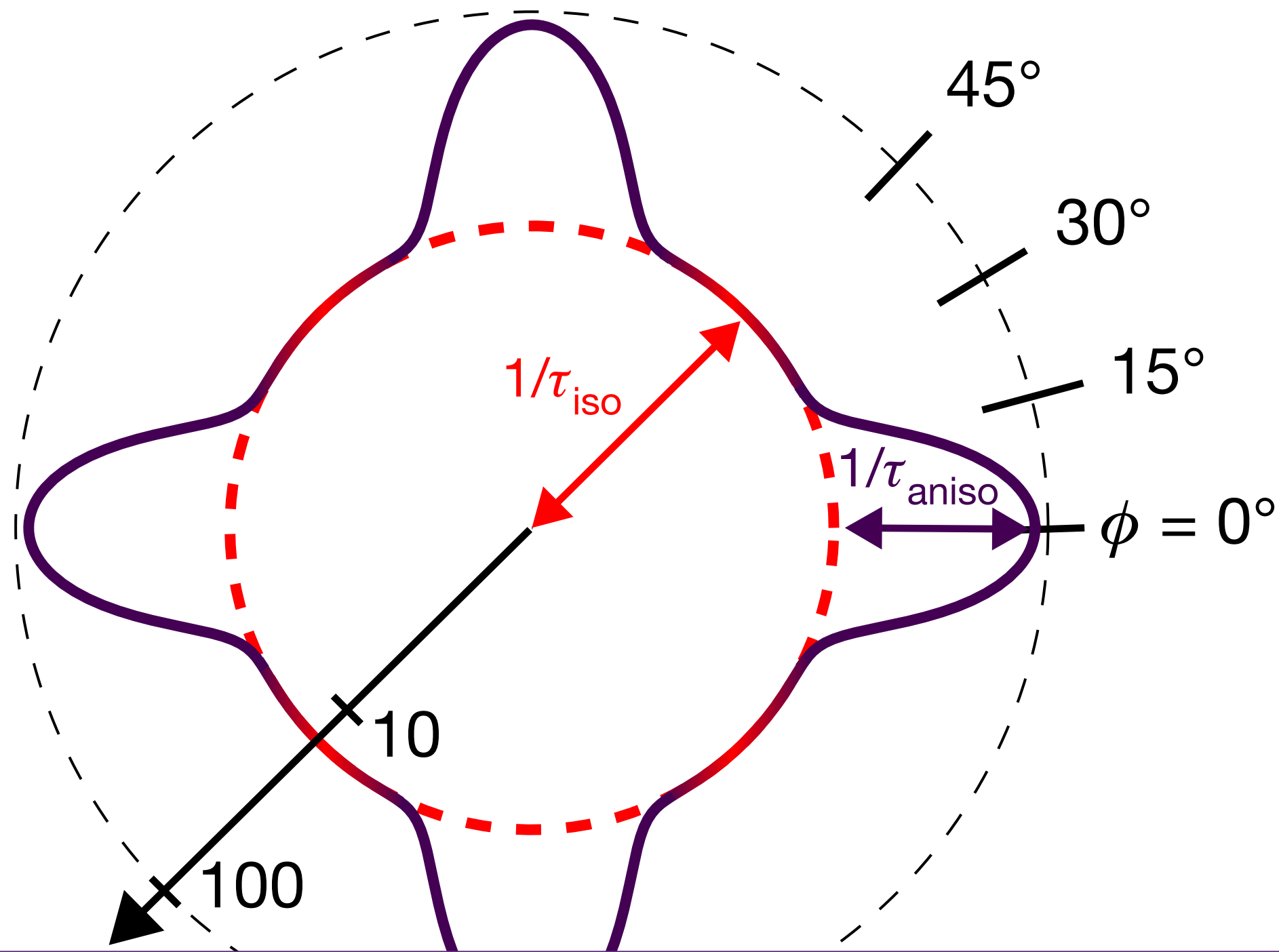




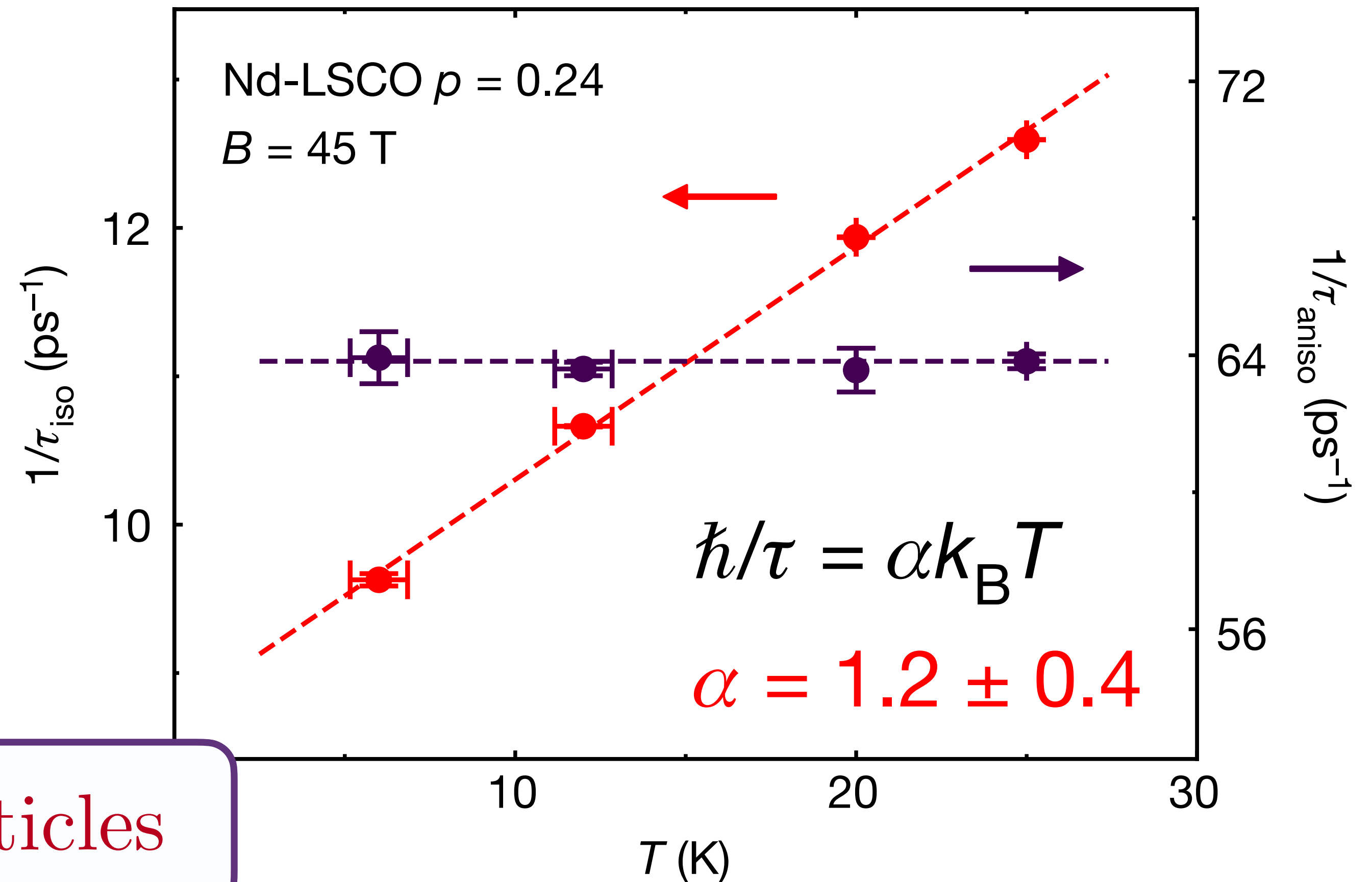
Linear-in temperature resistivity from an isotropic Planckian scattering rate

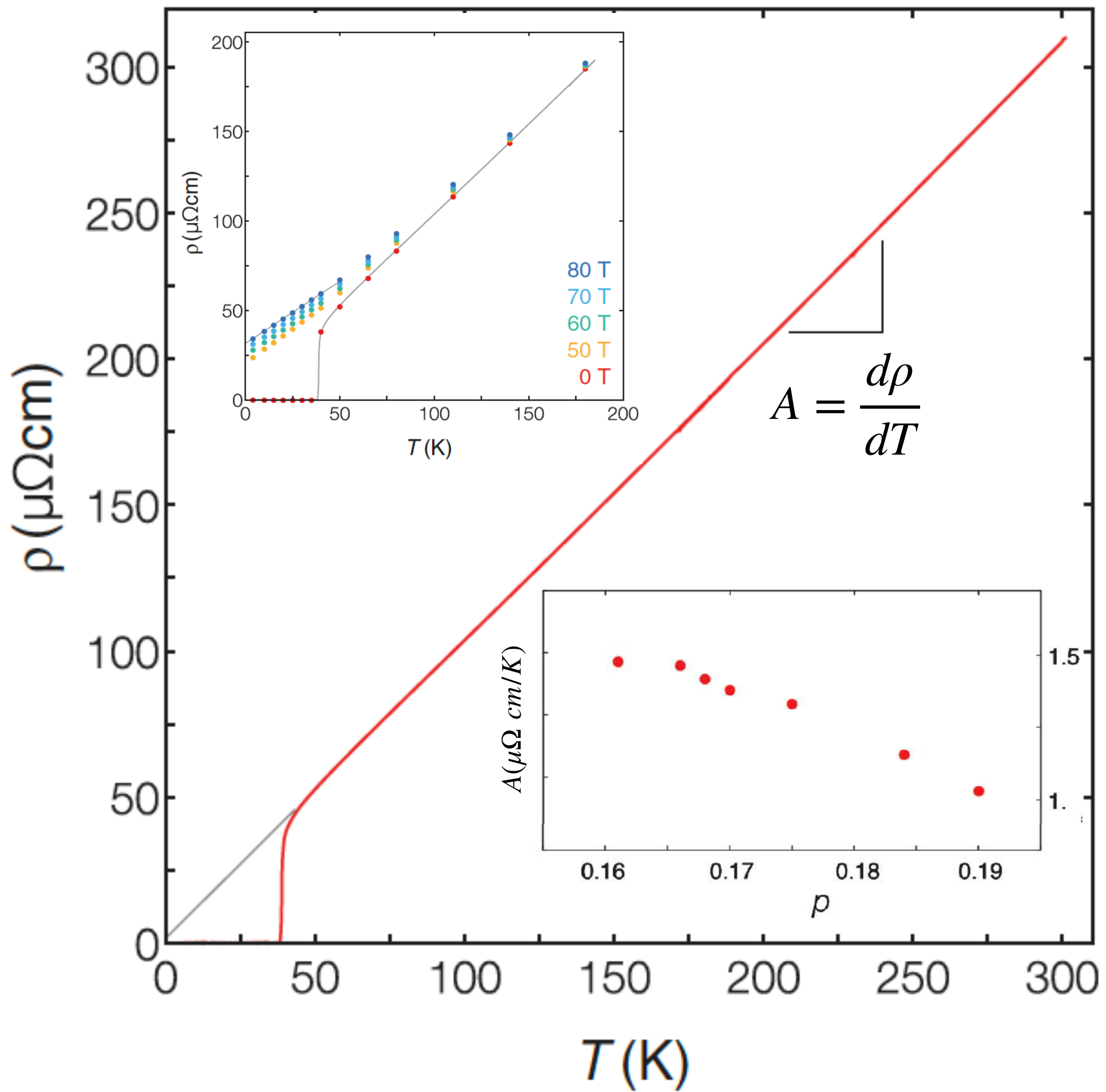
Nature **595**, 667-672 (2021)

G. Grissonnanche, Y. Fang, A. Legros, S. Verret, F. Laliberté, C. Collignon, J. Zhou, D. Graf, P. Goddard, L. Taillefer, B. J. Ramshaw

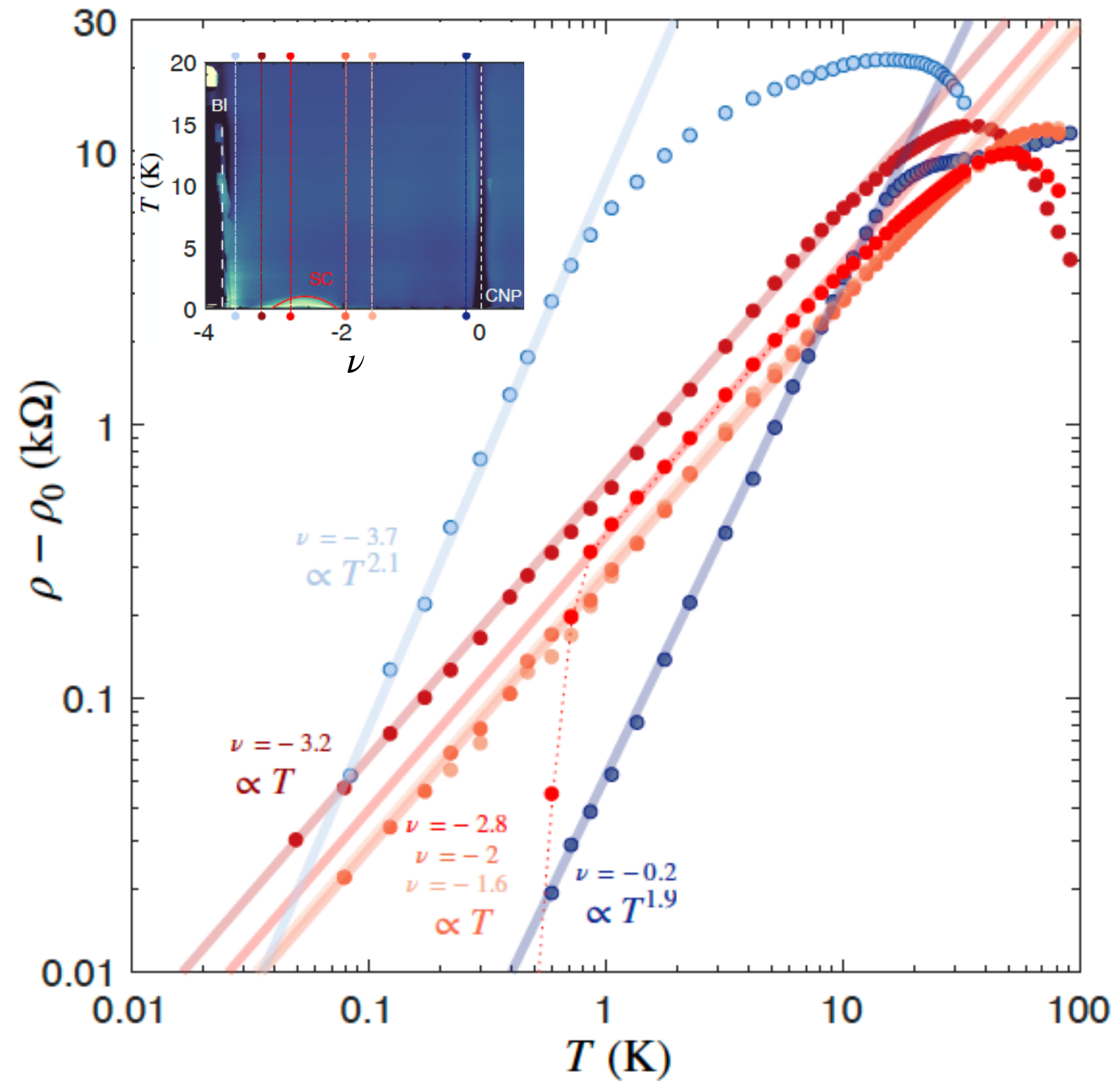


Current flow without quasiparticles





LSCO: Giraldo-Gallo et al. 2018



MATBG: Jaoui et al. 2021

Questions

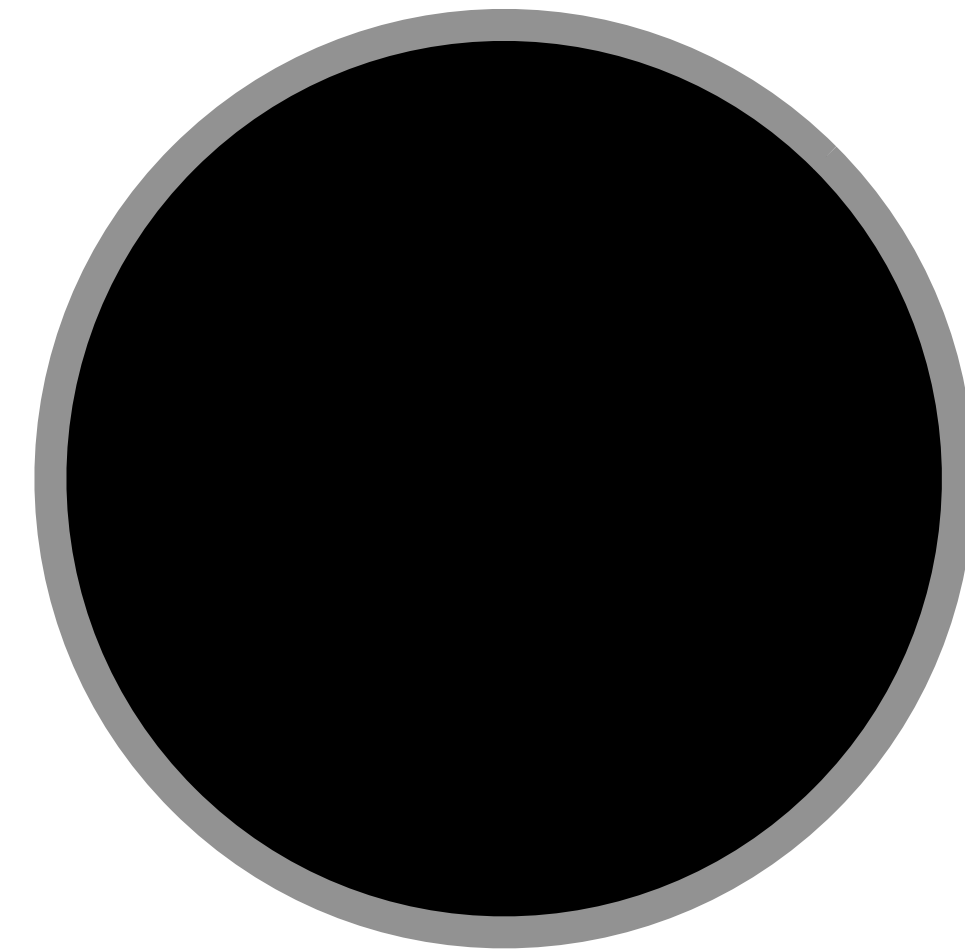
- Needed: A theory for current flow in a ‘strange metal’ with an entangled soup of electrons.
- Needed: theory for collision time in resistivity $\sim \hbar/(k_B T)$.
- Needed: theory for the appearance of superconductivity in such a ‘strange metal’.

**Quantum
black holes
and
holography**

Black Holes

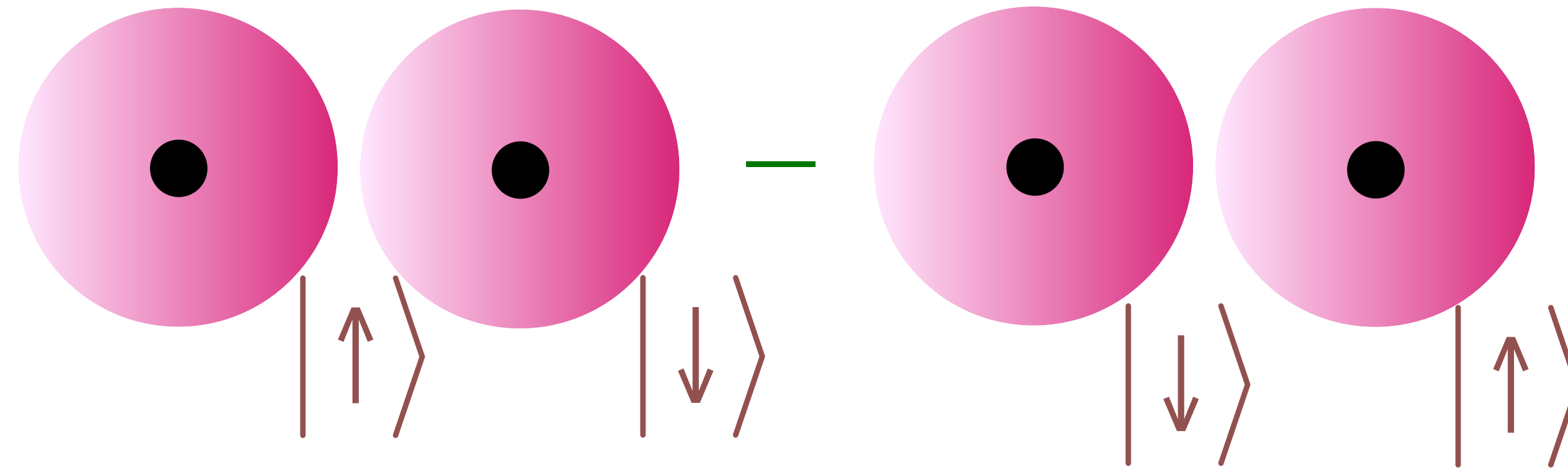
Objects so dense that light is gravitationally bound to them.

Horizon radius $R = \frac{2GM}{c^2}$

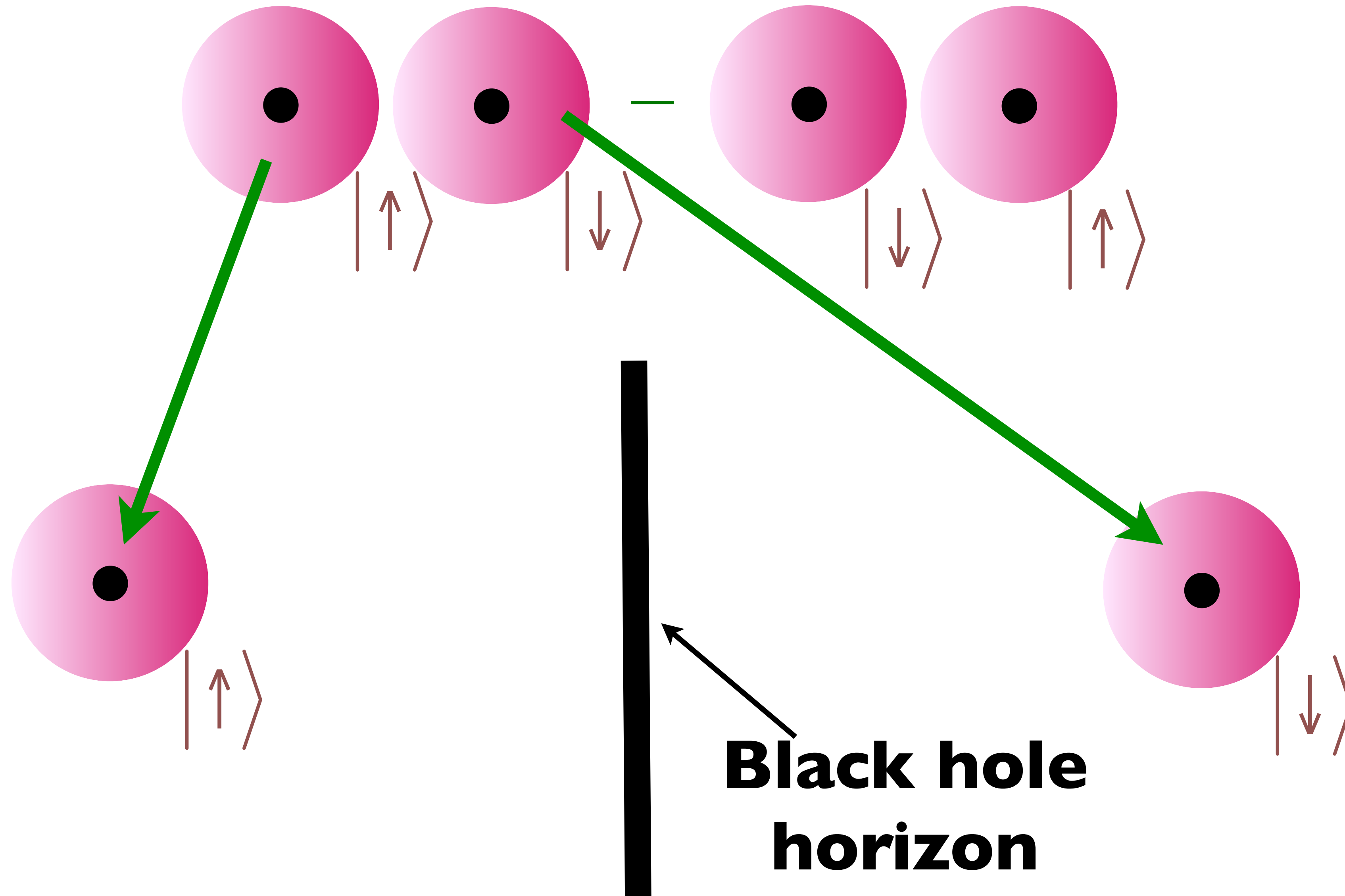


G Newton's constant, c velocity of light, M mass of black hole
For $M = \text{earth's mass}$, $R \approx 9 \text{ mm}$!

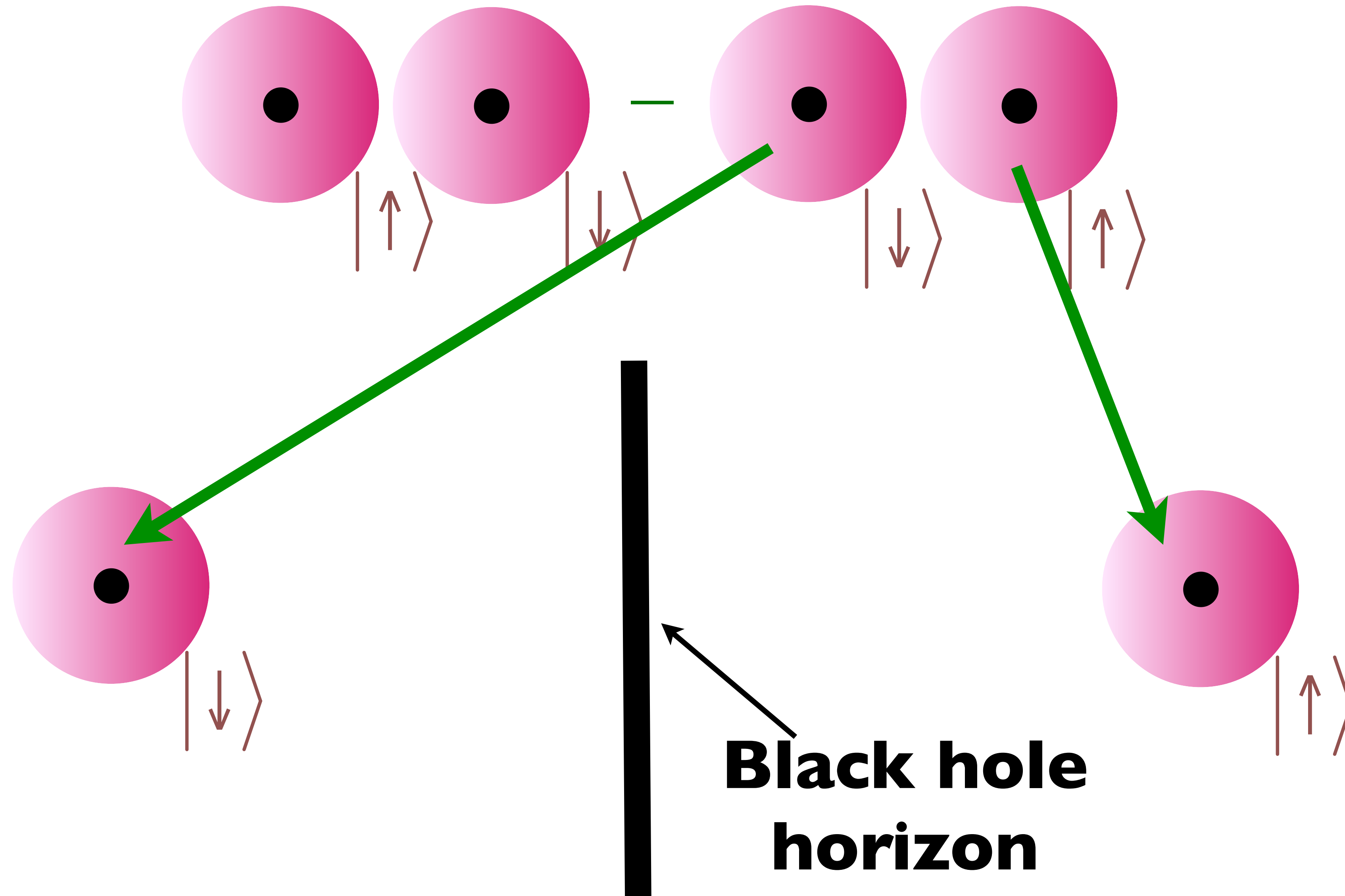
Quantum Entanglement across a black hole horizon



Quantum Entanglement across a black hole horizon

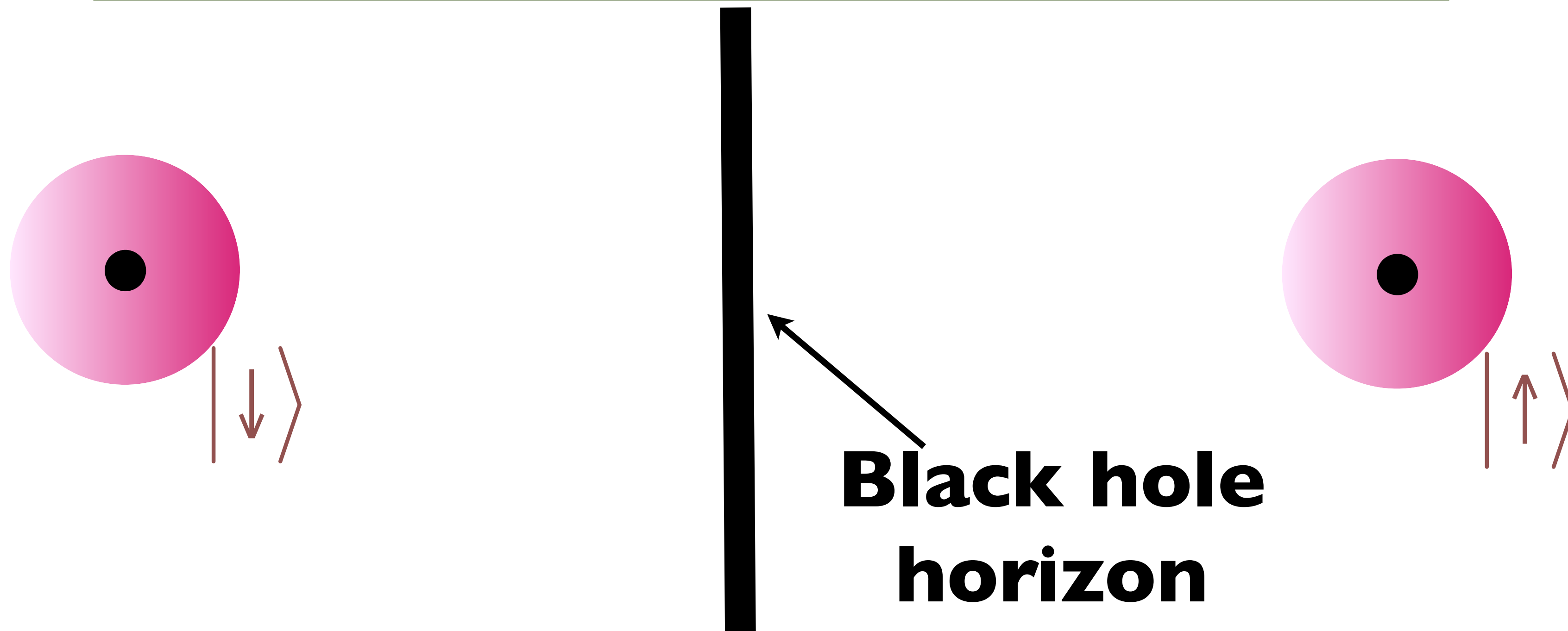


Quantum Entanglement across a black hole horizon



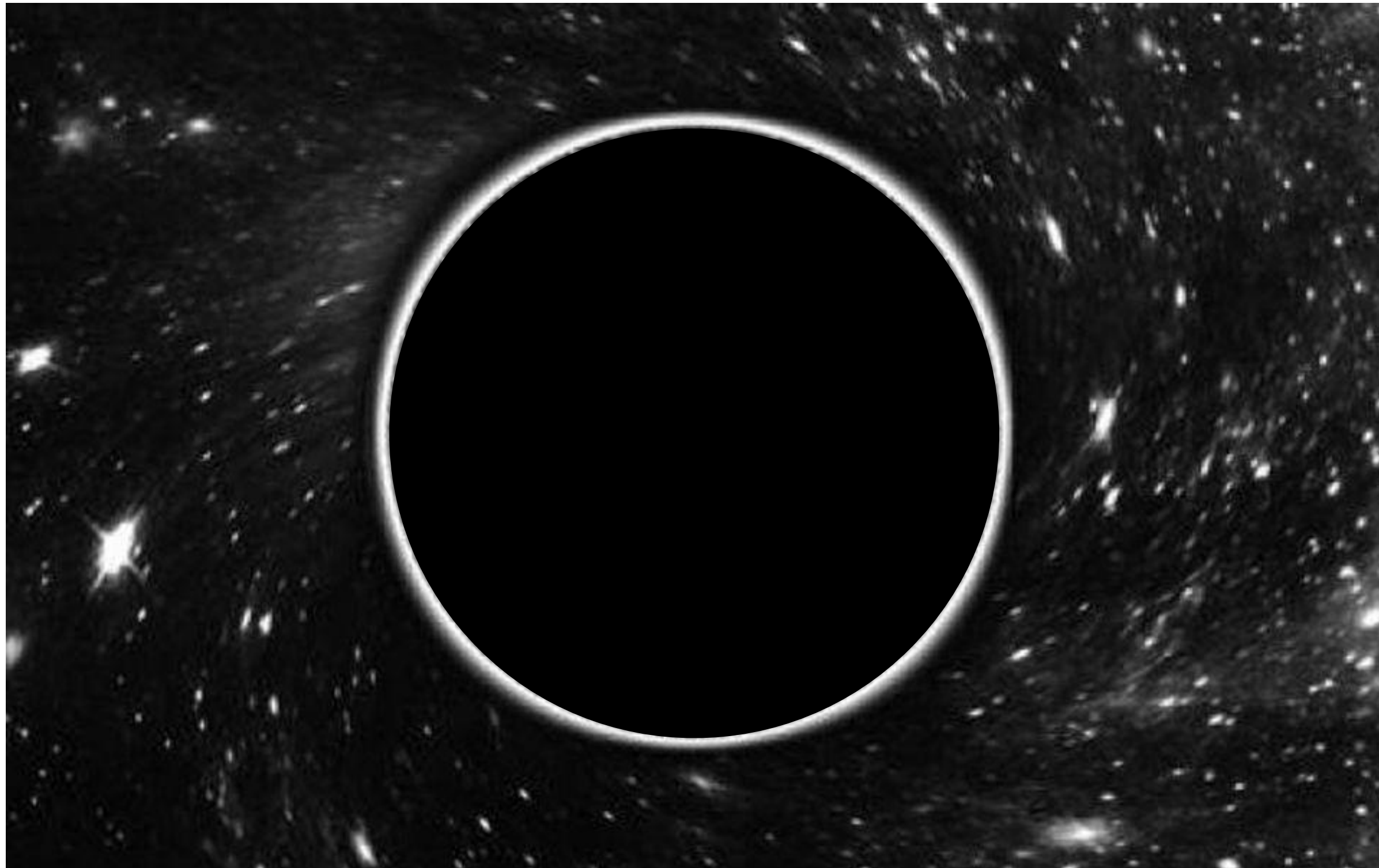
Quantum Entanglement across a black hole horizon

Hawking (1975) used other arguments to show that black hole horizons have a temperature
(The entanglement reasoning: to an outside observer, the state of the electron inside the black hole cannot be known, and so the outside electron is in a random state.)



Quantum Black holes

- Black holes have an entropy and a temperature,
 $T_H = \hbar c^3 / (8\pi G M k_B)$.
- The entropy is proportional to their surface area.
 $S = A k_B c^3 / (4G\hbar)$.



J. D. Bekenstein, PRD **7**, 2333 (1973)
S. W. Hawking, Nature **248**, 30 (1974)

Quantum Black holes

Bohr-Sommerfeld semiclassical quantum theory
of a black hole in d spatial dimensions

$$\mathcal{Z} = \int \mathcal{D}g_{\mu\nu} \mathcal{D}a_{\mu} \exp \left(-\frac{1}{\hbar} \int d^d x \int_0^{\hbar/(k_B T)} d\tau \sqrt{g} \mathcal{L}_d[g_{\mu\nu}, a_{\mu}] \right)$$

$g_{\mu\nu} \Rightarrow$ spacetime metric, $g = \det(g_{\mu\nu})$

$a_{\mu} \Rightarrow$ Electromagnetic gauge field

$\mathcal{L}_d \Rightarrow$ *Classical* Einstein-Maxwell action

Quantum Black holes

Bohr-Sommerfeld semiclassical quantum theory of a black hole in d spatial dimensions

$$\mathcal{Z} = \int \mathcal{D}g_{\mu\nu} \mathcal{D}a_{\mu} \exp \left(-\frac{1}{\hbar} \int d^d x \int_0^{\hbar/(k_B T)} d\tau \sqrt{g} \mathcal{L}_d[g_{\mu\nu}, a_{\mu}] \right)$$

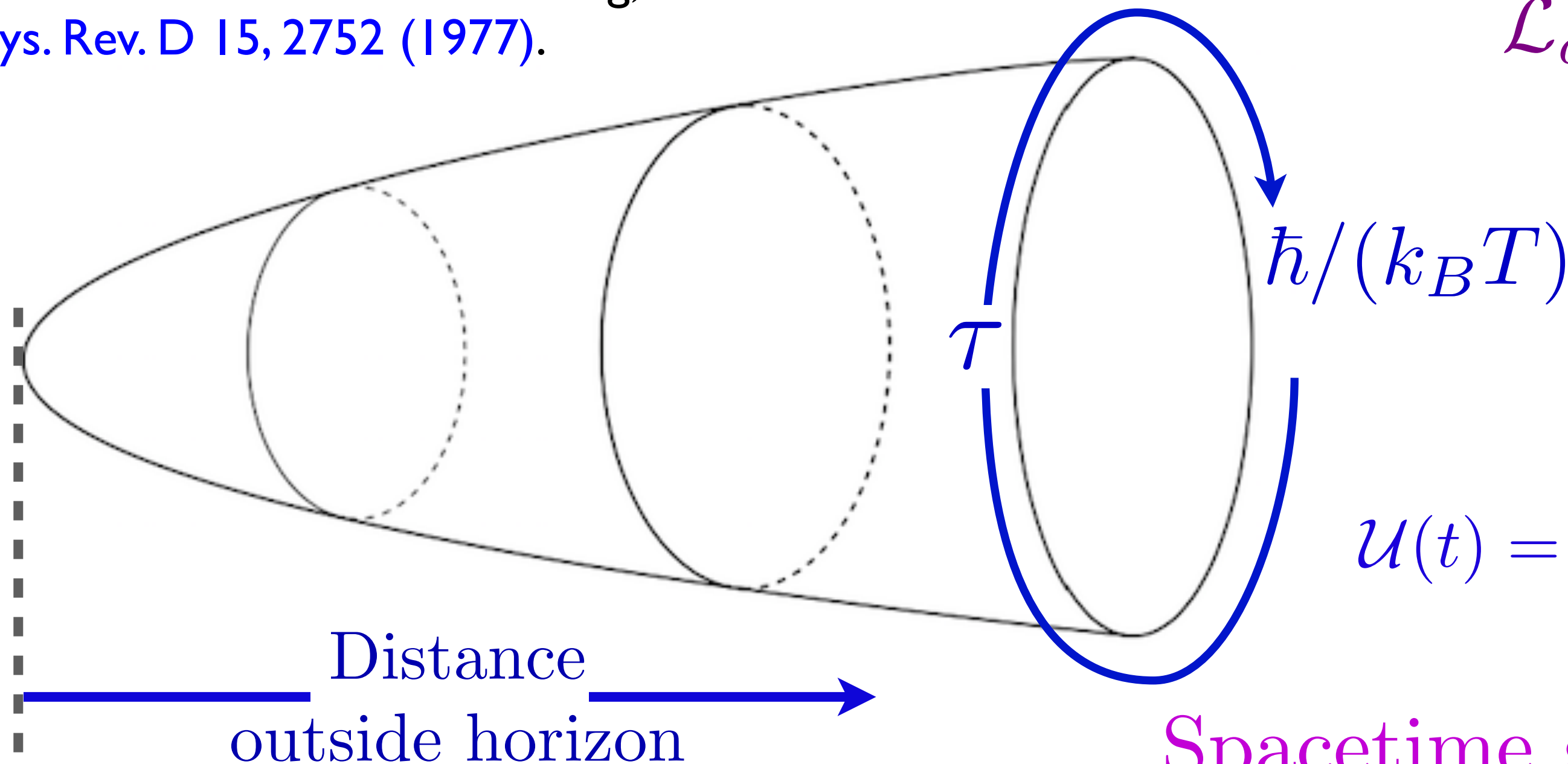
$g_{\mu\nu} \Rightarrow$ spacetime metric, $g = \det(g_{\mu\nu})$

$a_{\mu} \Rightarrow$ Electromagnetic gauge field

$\mathcal{L}_d \Rightarrow$ *Classical* Einstein-Maxwell action

Evaluate path integral at black hole saddle point

G.W. Gibbons and S.W. Hawking, *Phys. Rev. D* 15, 2752 (1977).

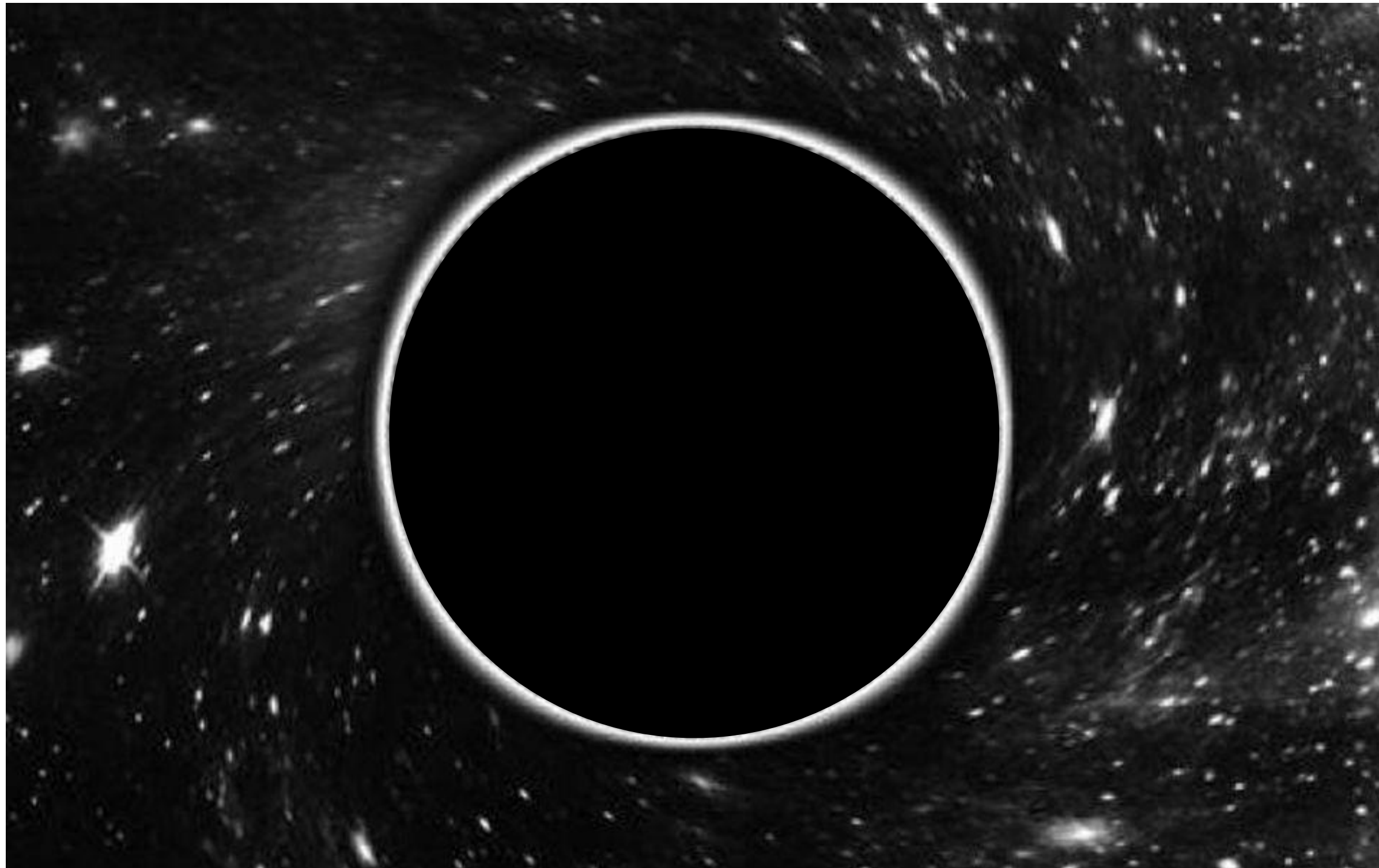


$$\mathcal{U}(t) = \exp(-i\mathcal{H}t/\hbar) \Leftrightarrow \mathcal{Z} = \text{Tr} \exp(-\mathcal{H}/(k_B T))$$

Spacetime geometry of a black hole in imaginary time τ

Quantum Black holes

- Black holes have an entropy and a temperature, $T_H = \hbar c^3 / (8\pi G M k_B)$.
- The entropy is proportional to their surface area. $S = A k_B c^3 / (4G\hbar)$.



J. D. Bekenstein, PRD **7**, 2333 (1973)
S.W. Hawking, Nature **248**, 30 (1974)

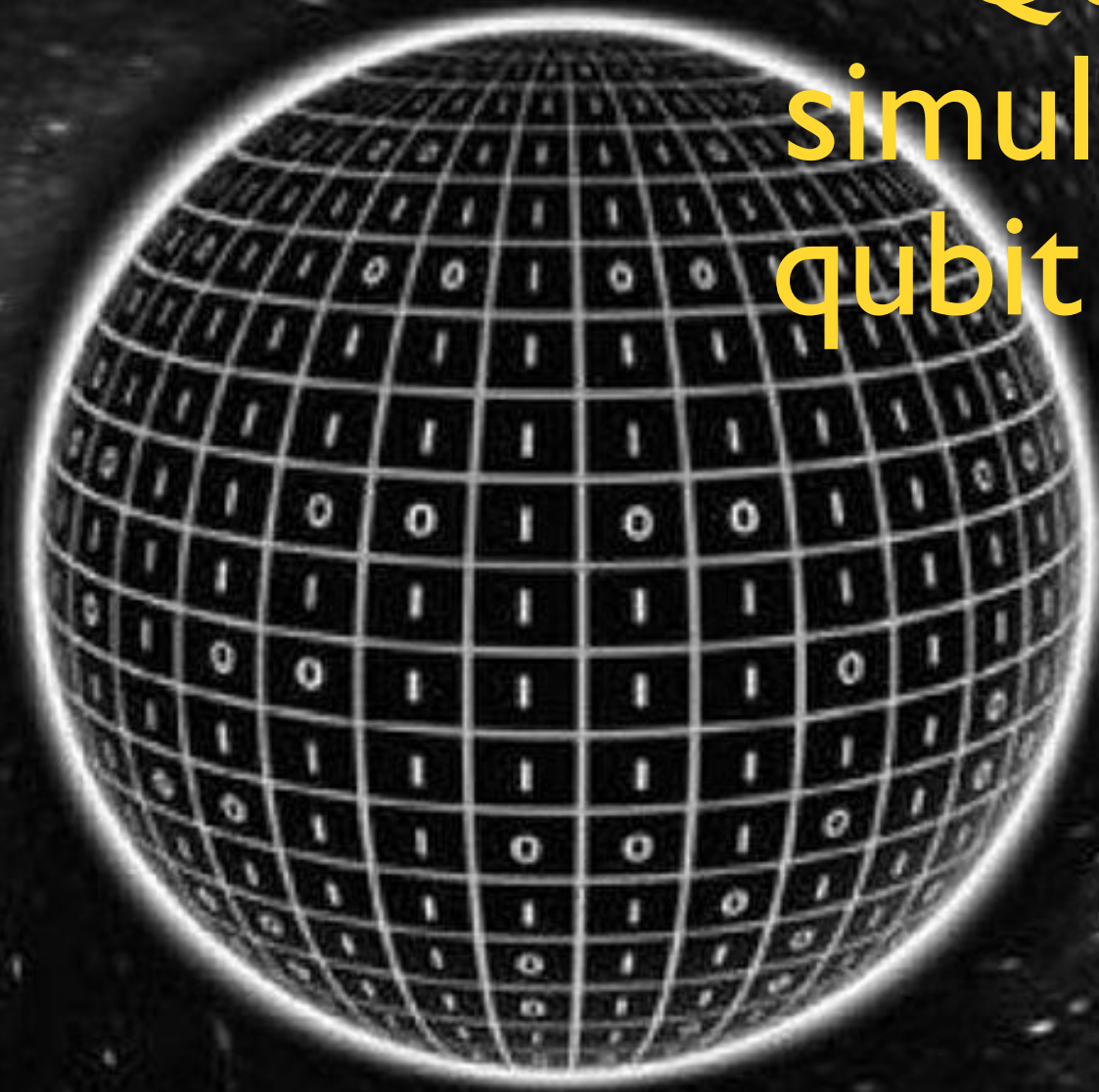
Remarkable features:

- Entropy is finite.
- Entropy is not proportional to volume

Quantum Black holes

- Black holes have an entropy and a temperature, $T_H = \hbar c^3 / (8\pi G M k_B)$.
- The entropy is proportional to their surface area. $S = A k_B c^3 / (4G\hbar)$.

Quantum
simulation by a
qubit hologram



J. D. Bekenstein, PRD **7**, 2333 (1973)
S.W. Hawking, Nature **248**, 30 (1974)

Remarkable features:

- Entropy is finite.
- Entropy is not proportional to volume

Quantum Black holes

- Black holes have an entropy and a temperature, $T_H = \hbar c^3 / (8\pi G M k_B)$.
- The entropy is proportional to their surface area. $S = A k_B c^3 / (4G\hbar)$.
- They relax to thermal equilibrium in a time $\sim 8\pi G M / c^3$

Quantum
simulation by a
qubit hologram



J. D. Bekenstein, PRD **7**, 2333 (1973)

S.W. Hawking, Nature **248**, 30 (1974)

C.V. Vishveshwara, Nature **227**, 936 (1970)

Remarkable features:

- Entropy is finite.
- Entropy is not proportional to volume

Quantum Black holes

- Black holes have an entropy and a temperature, $T_H = \hbar c^3 / (8\pi G M k_B)$.
- The entropy is proportional to their surface area. $S = A k_B c^3 / (4G\hbar)$.
- They relax to thermal equilibrium in a time $\sim 8\pi G M / c^3 = \hbar / (k_B T_H)$ which is Planckian!

Quantum
simulation by a
qubit hologram



J. D. Bekenstein, PRD **7**, 2333 (1973)

S.W. Hawking, Nature **248**, 30 (1974)

C.V. Vishveshwara, Nature **227**, 936 (1970)

Remarkable features:

- Entropy is finite.
- Entropy is not proportional to volume

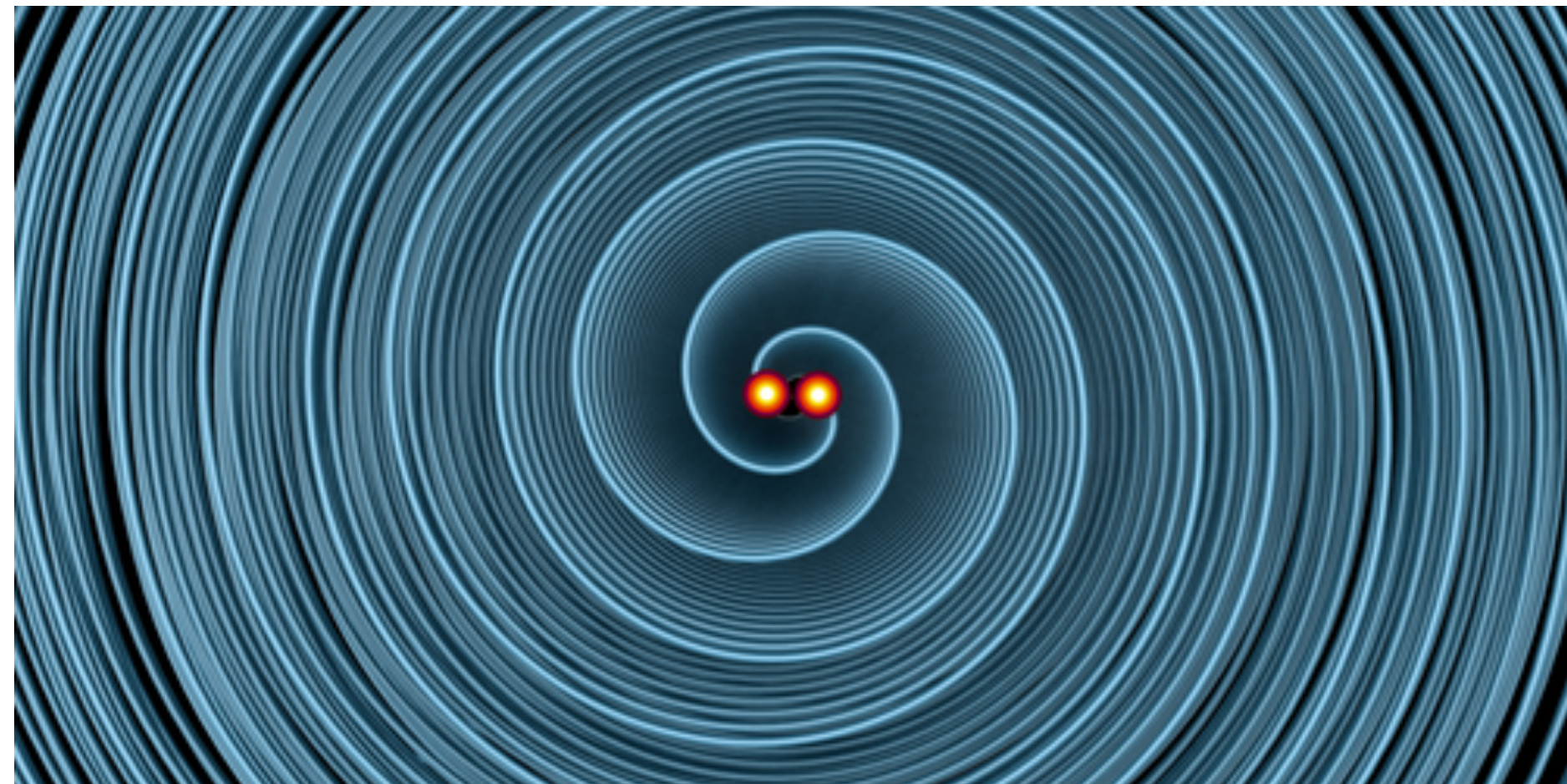
Black Holes Obey Information-Emission Limits

Limits

April 22, 2021 • *Physics* 14, s47 –Christopher Crockett

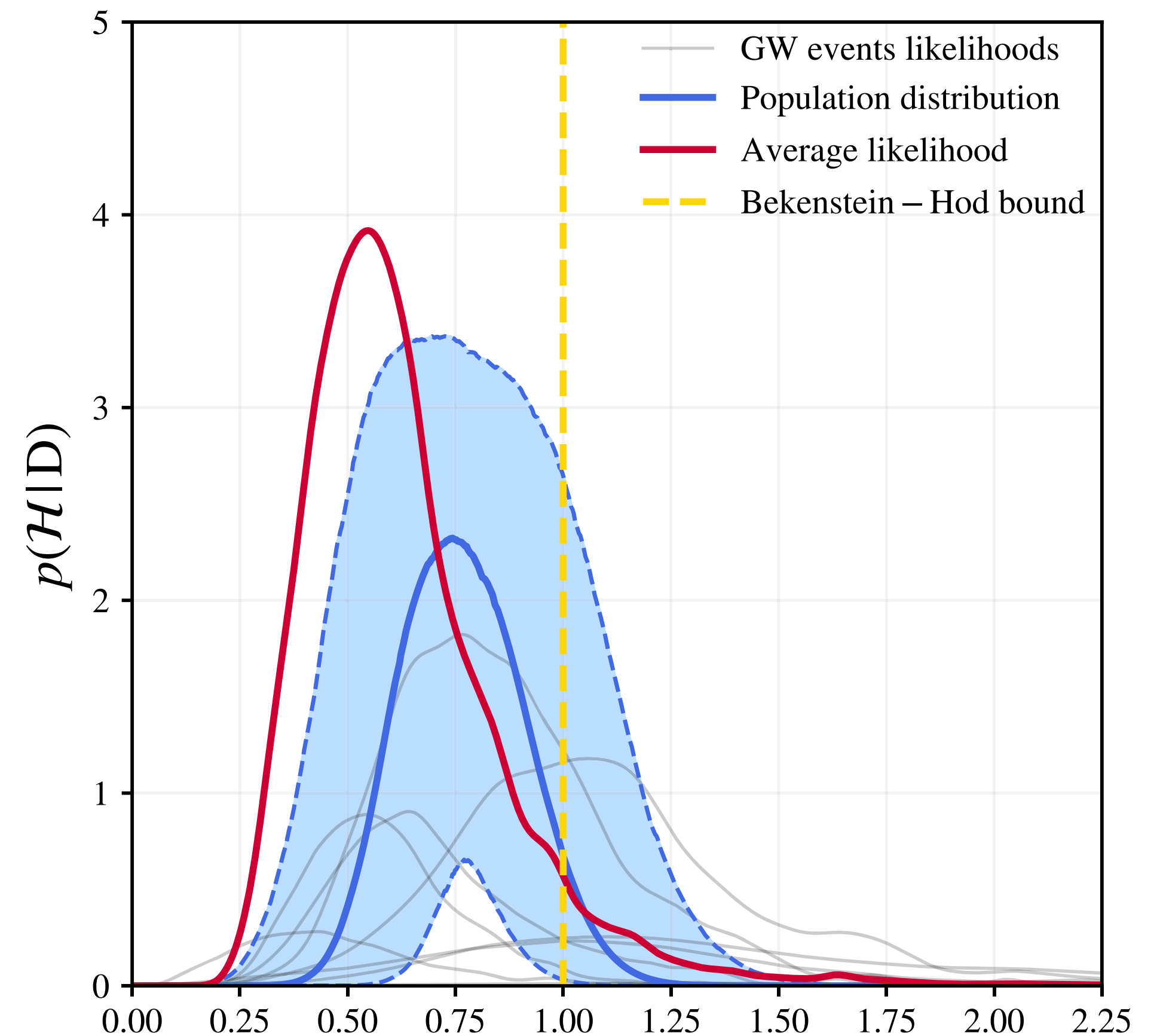
G. Carullo, D. Laghi, J. Veitch, W. Del Pozzo, *Phys. Rev. Lett.* **126**, 161102 (2021)

An analysis of the gravitational waves emitted from black hole mergers confirms that black holes are the fastest known information dissipaters.



Gravity wave observations of 8 different black holes show a relaxation time

$$\tau \sim \frac{\hbar}{k_B T}$$



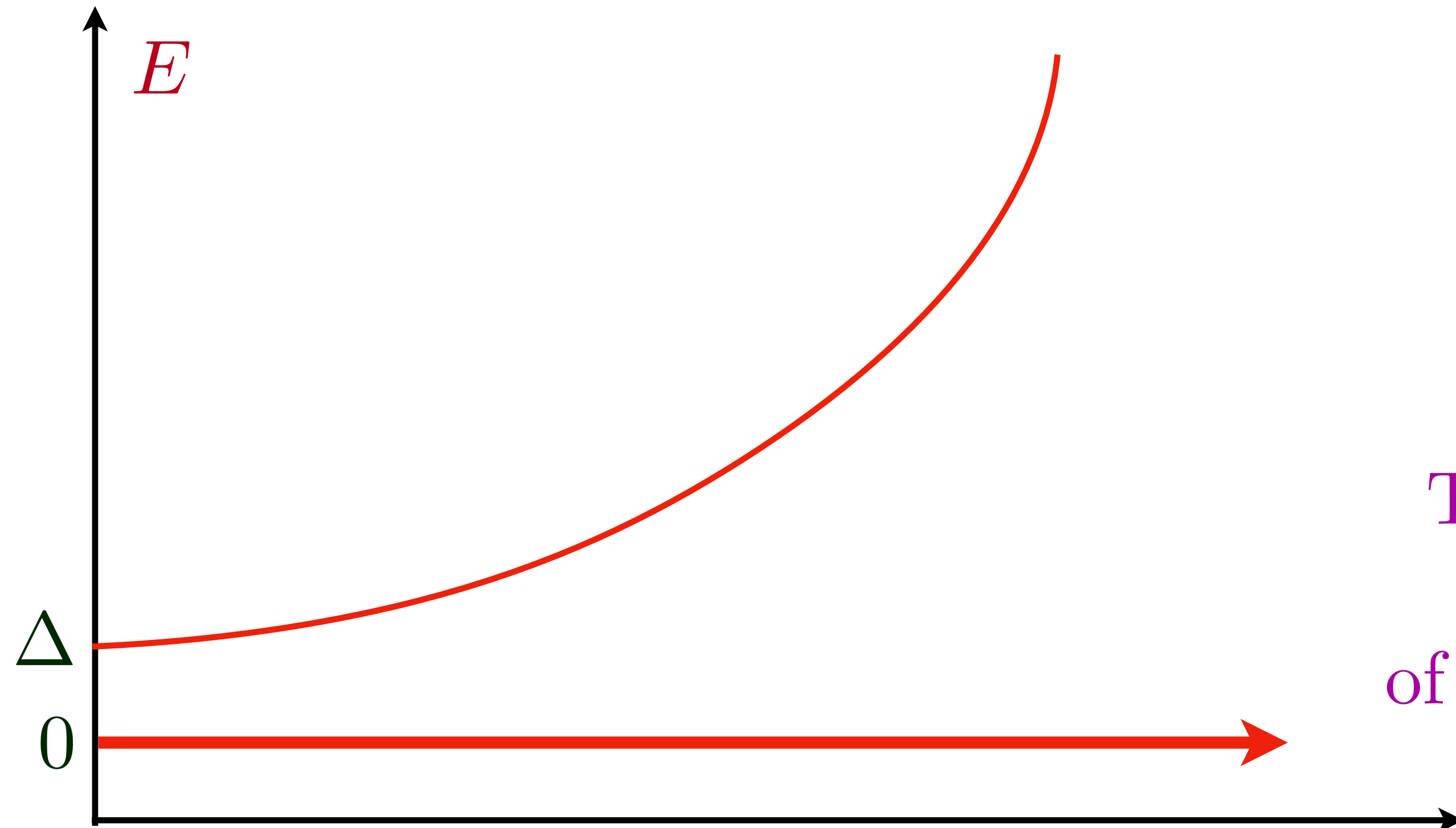
$$\mathcal{H} = \frac{1}{\pi} \frac{\hbar/\tau}{k_B T}$$

Questions

- Can Hawking's Bohr-Sommerfeld theory of black hole entropy be interpreted in terms of a $D(E)$ of a Schrödinger-Heisenberg quantum system?

Questions

- Can Hawking's Bohr-Sommerfeld theory of black hole entropy be interpreted in terms of a $D(E)$ of a Schrödinger-Heisenberg quantum system?



$$D(E) = \sum_i \delta(E - E_i)$$
$$= \exp(S/k_B) \delta(E) + \dots$$

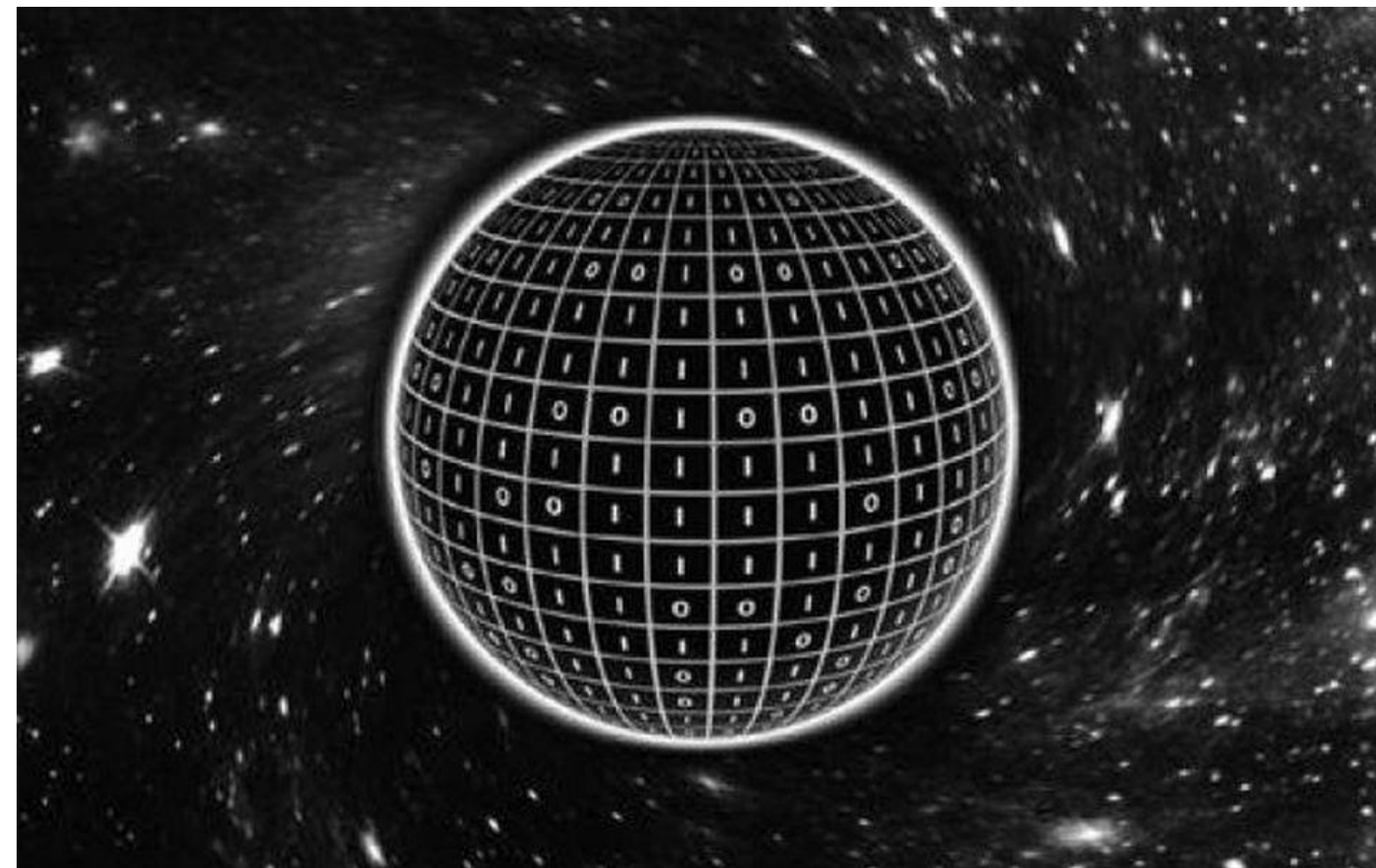
Black holes in string theory realize the entropy as an exact, exponentially large, degeneracy of the ground state.

This is not the generic behavior of the semiclassical path integral of Einstein gravity, as we will see ...

Questions

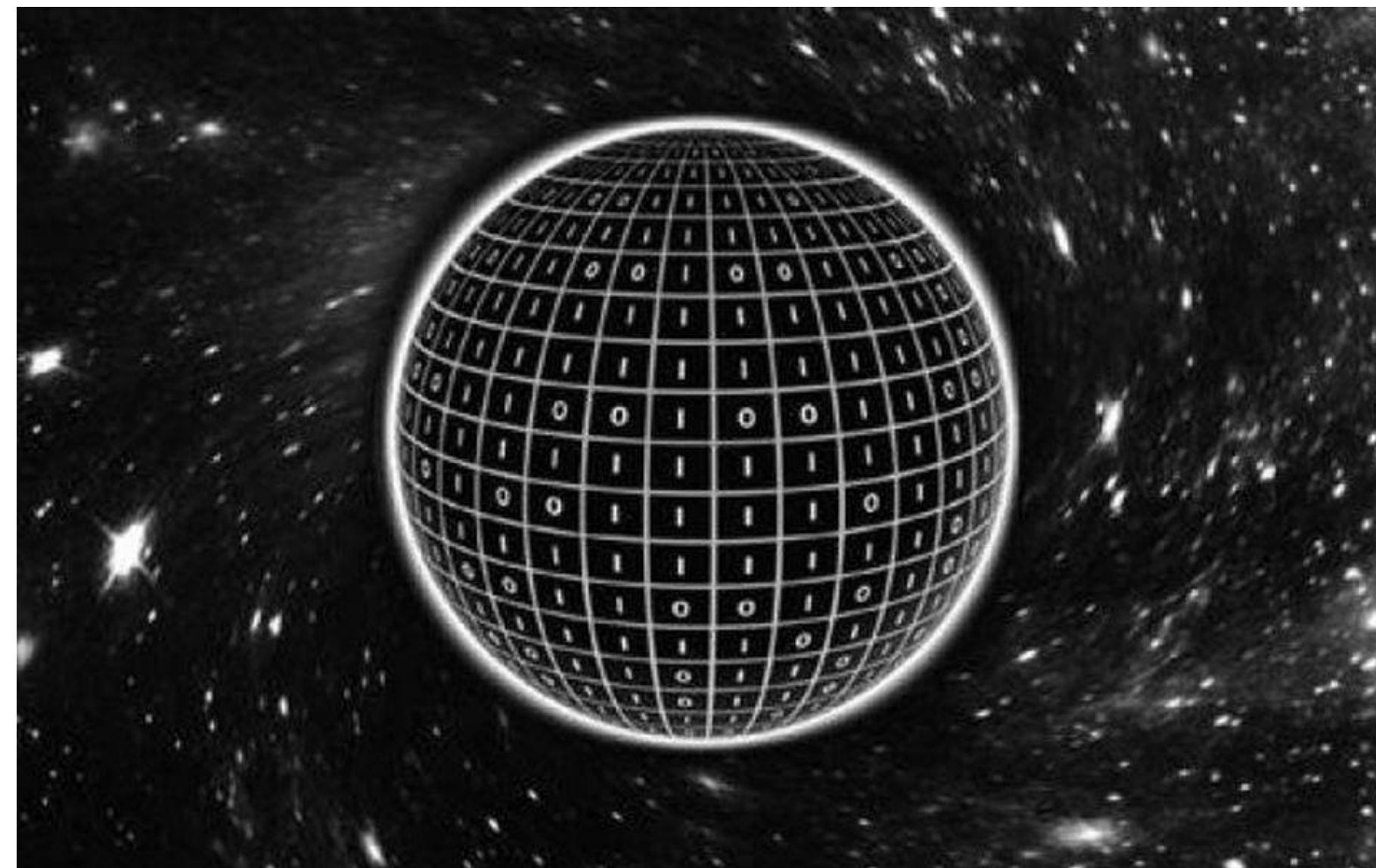
- Can Hawking's Bohr-Sommerfeld theory of black hole entropy be interpreted in terms of a $D(E)$ of a Schrödinger-Heisenberg quantum system?
- Can black hole entropy be understood 'holographically', as that of a unitary quantum system in one lower spatial dimension with a finite number of states?

G. 'tHooft (1993); L. Susskind (1993); Maldacena (1998)



Questions

- Can Hawking's Bohr-Sommerfeld theory of black hole entropy be interpreted in terms of a $D(E)$ of a Schrödinger-Heisenberg quantum system?
- Can black hole entropy be understood 'holographically', as that of a unitary quantum system in one lower spatial dimension with a finite number of states?
- The unitary quantum system cannot have particle-like excitations if it is to reproduce the rapid Planckian dynamics at the rate $k_B T / \hbar$.



Questions

- Can Hawking's Bohr-Sommerfeld theory of black hole entropy be interpreted in terms of a $D(E)$ of a Schrödinger-Heisenberg quantum system?
- Can black hole entropy be understood 'holographically', as that of a unitary quantum system in one lower spatial dimension with a finite number of states?
- The unitary quantum system cannot have particle-like excitations if it is to reproduce the rapid Planckian dynamics at the rate $k_B T/\hbar$.
- Can we compute the evolution of the entropy as the black hole evaporates? Is it that of an evaporating unitary quantum system?

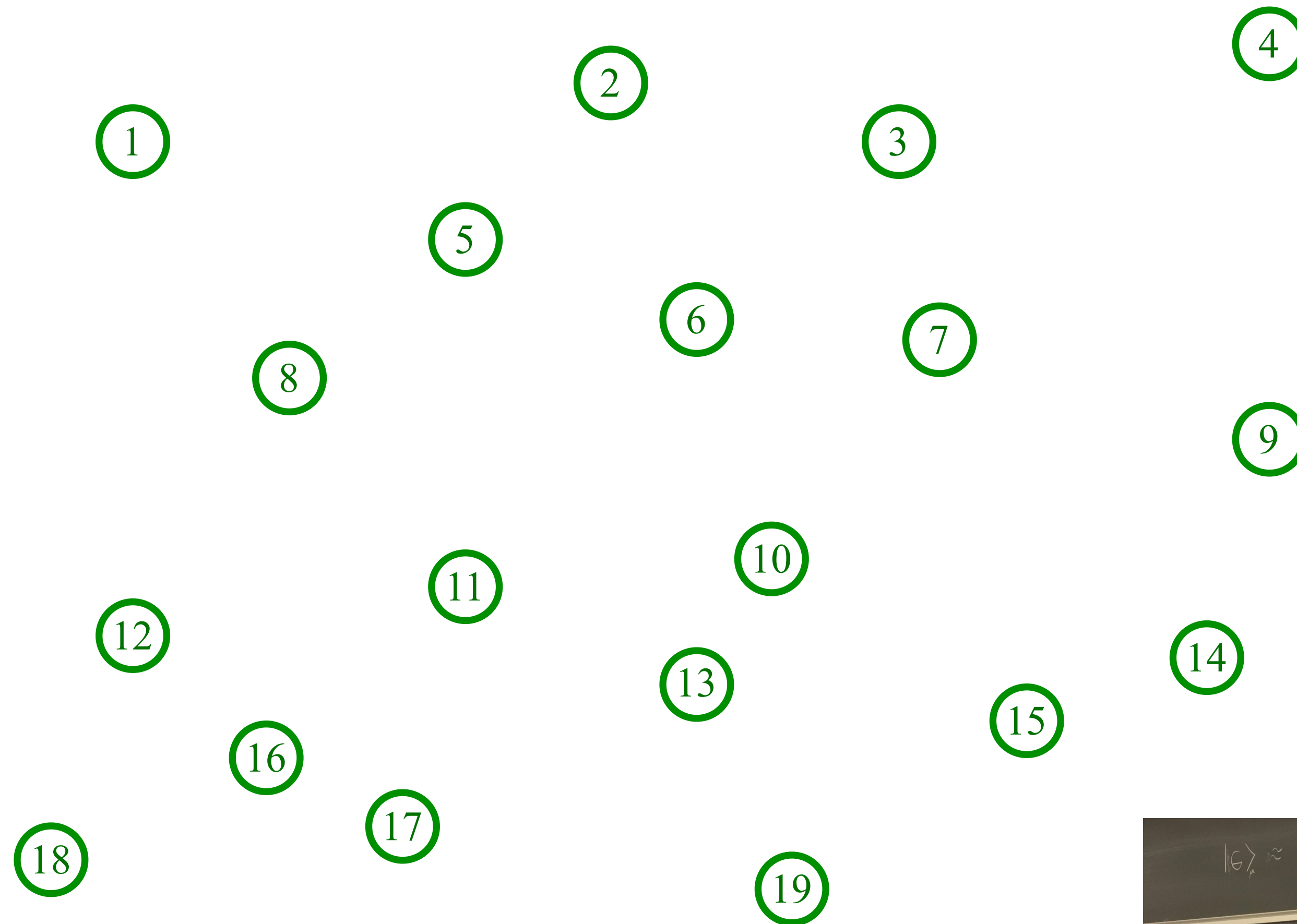
Sachdev-Ye-Kitaev Model

A solvable model of multi-particle entanglement which accounts for quantum interference between successive collisions:

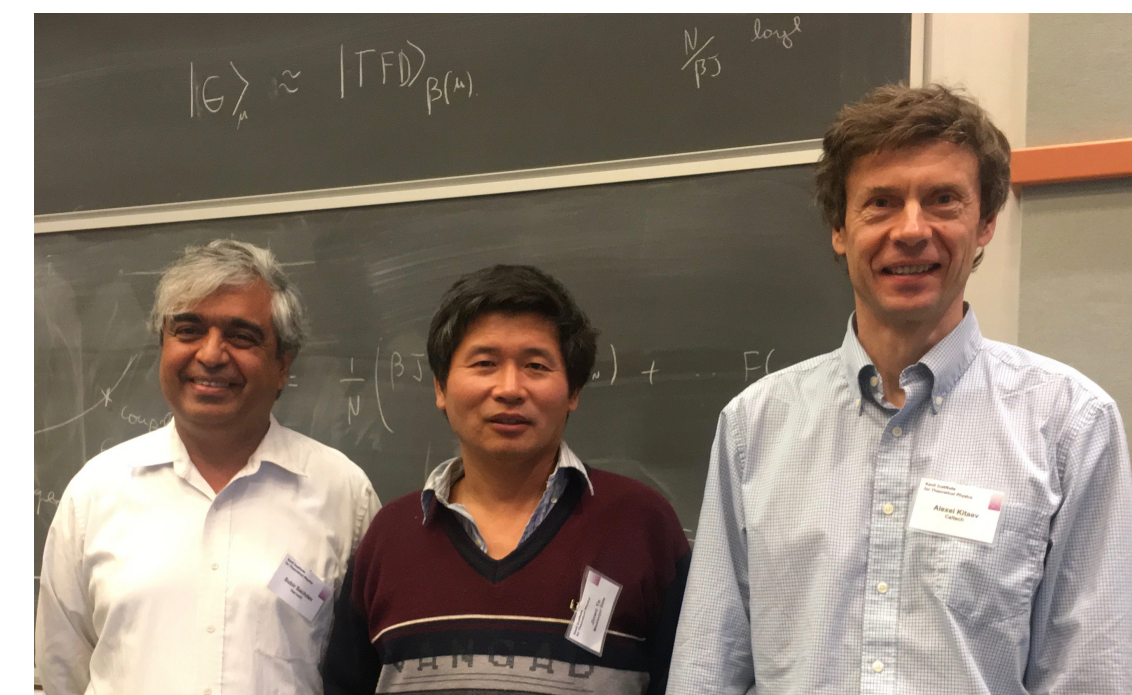
leading to a metal with no particle-like excitations

The SYK model

Sachdev, Ye (1993); Kitaev (2015)

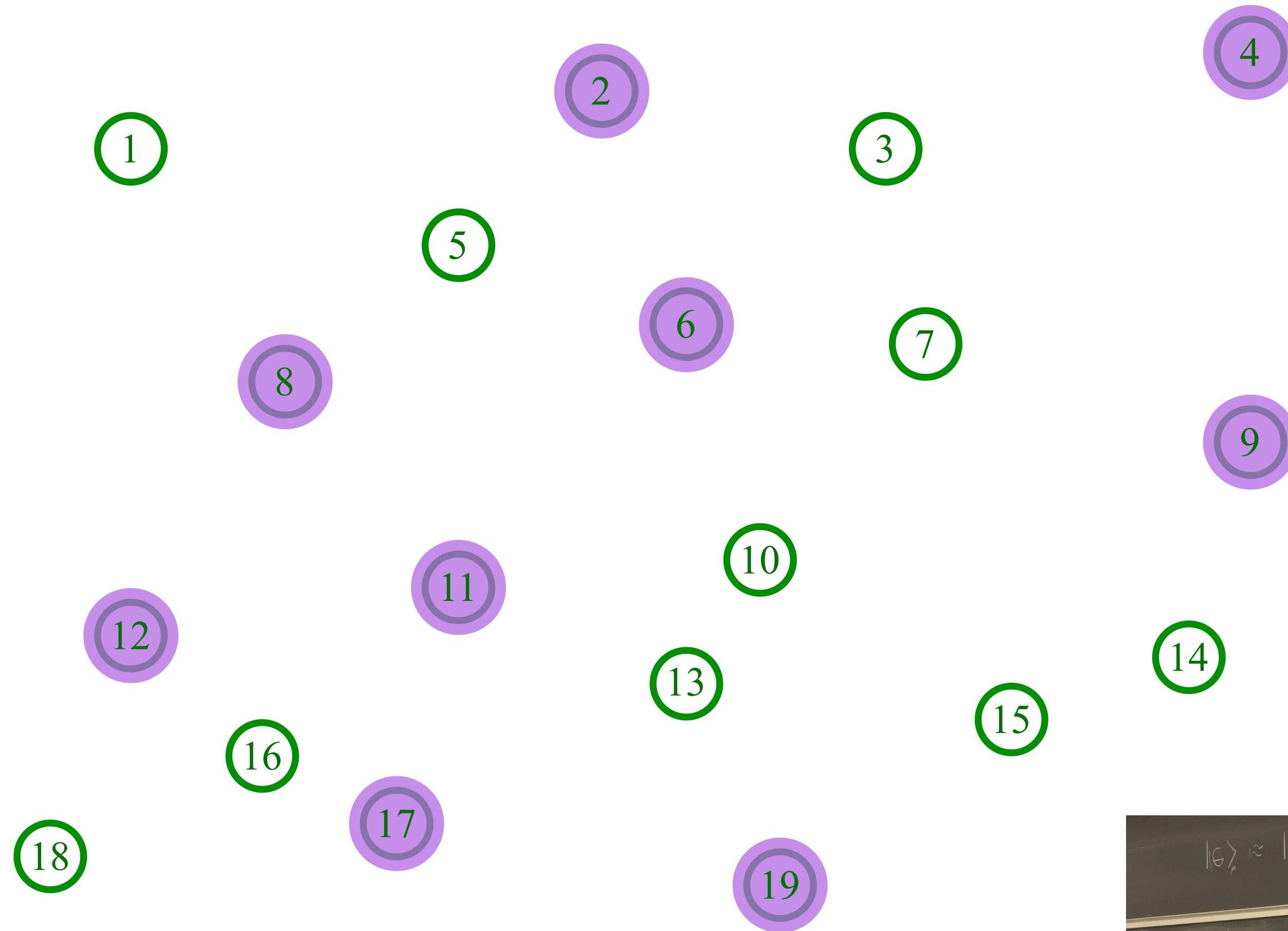


Pick a set of random positions

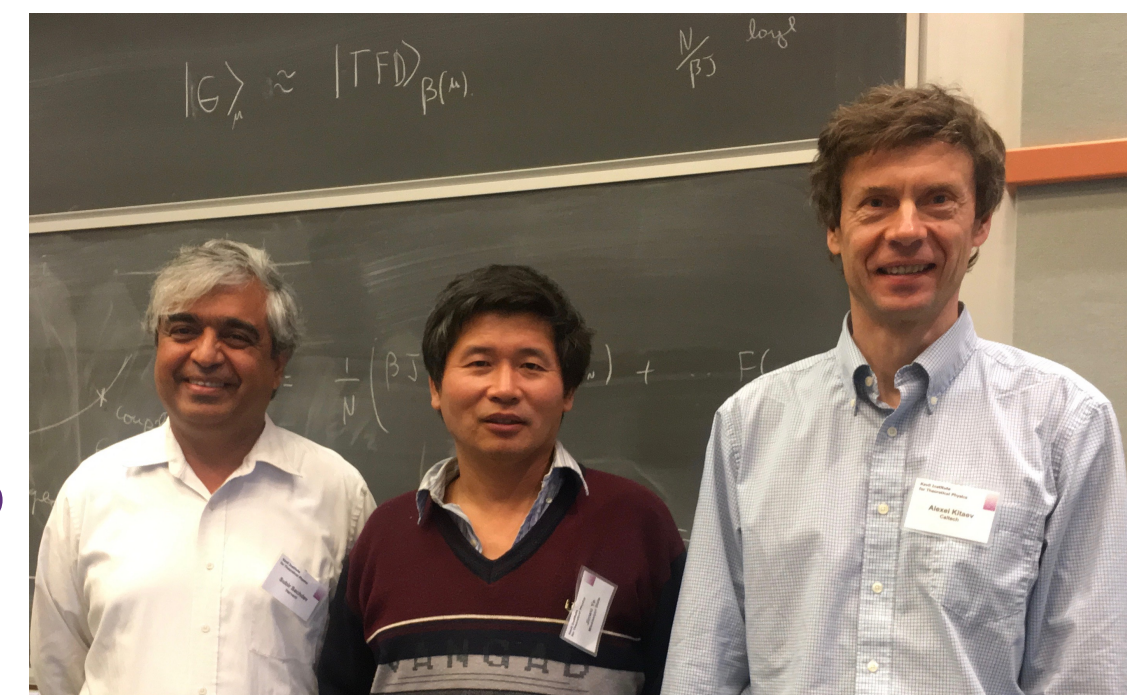


The SYK model

Sachdev, Ye (1993); Kitaev (2015)



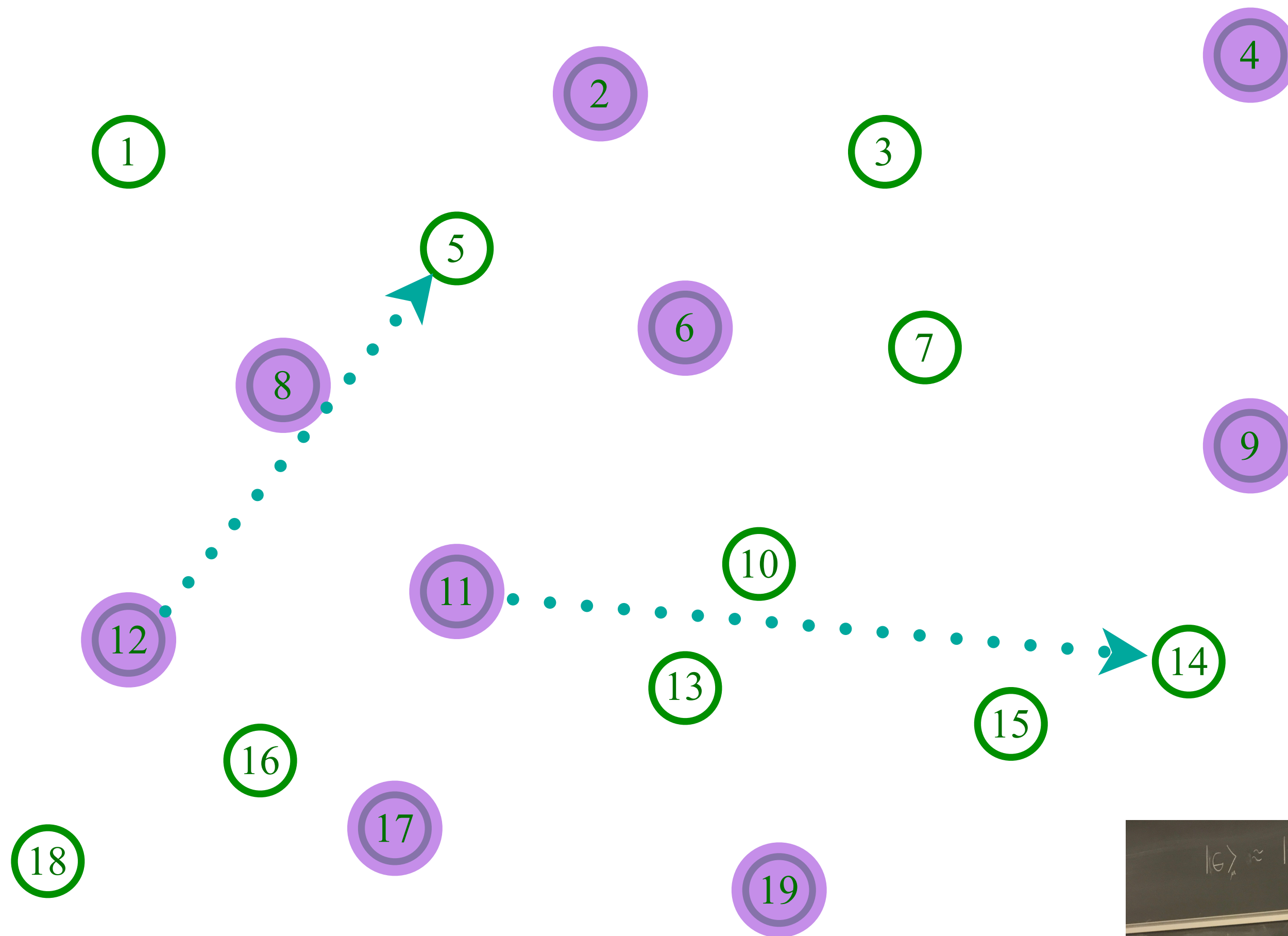
Place electrons randomly on some sites



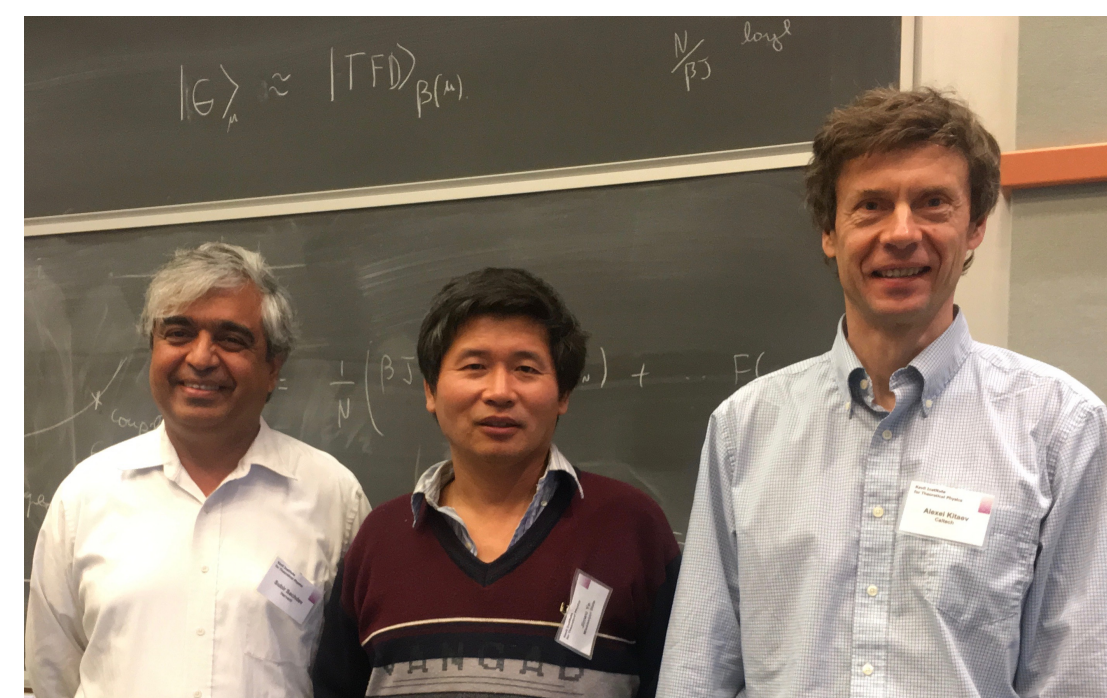
The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{11,12;5,14}$$



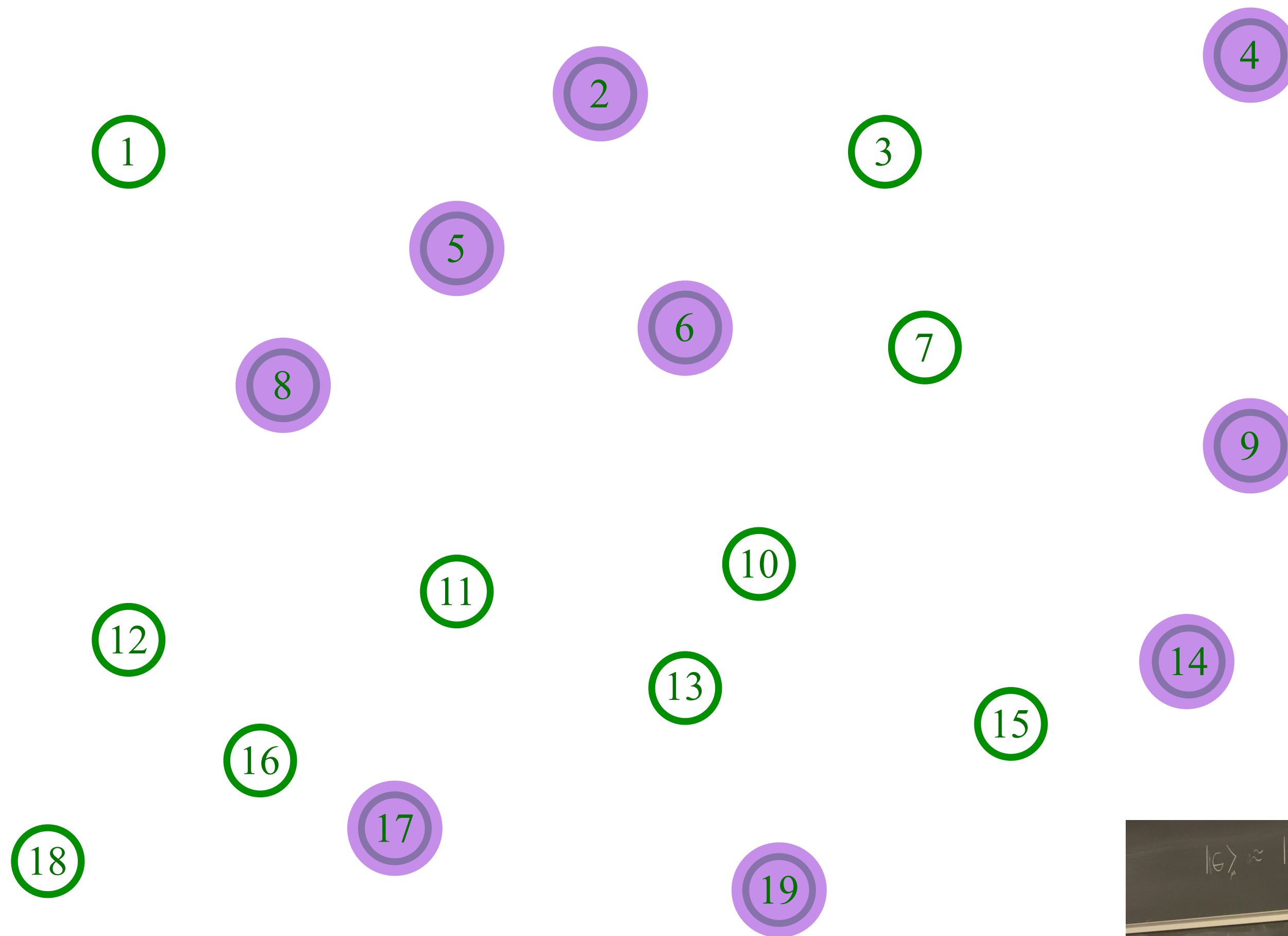
Place electrons randomly on some sites



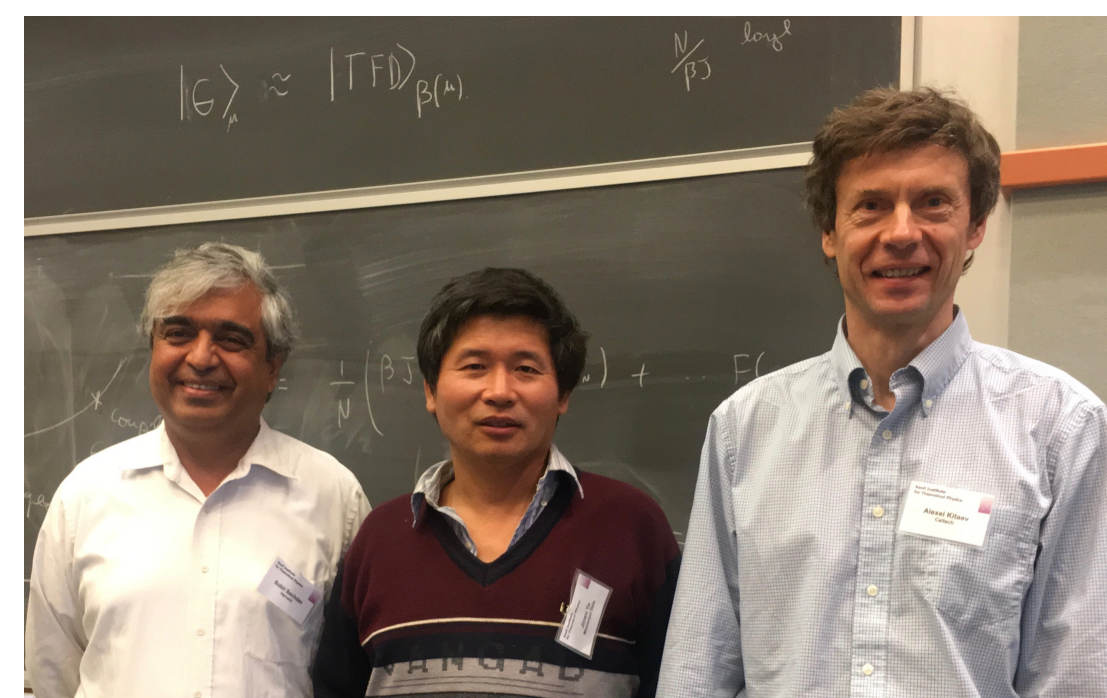
The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{11,12;5,14}$$



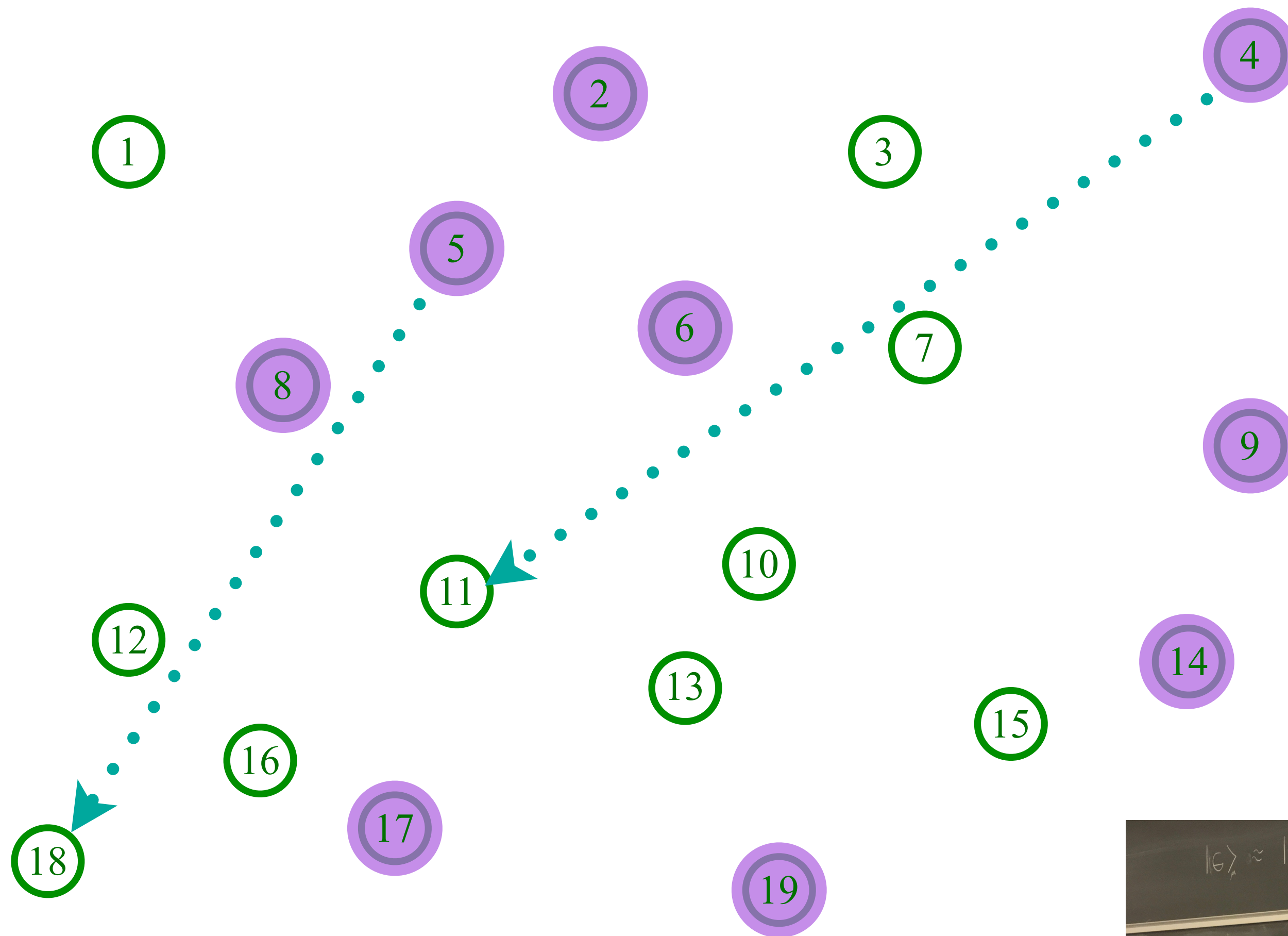
Entangle electrons pairwise randomly



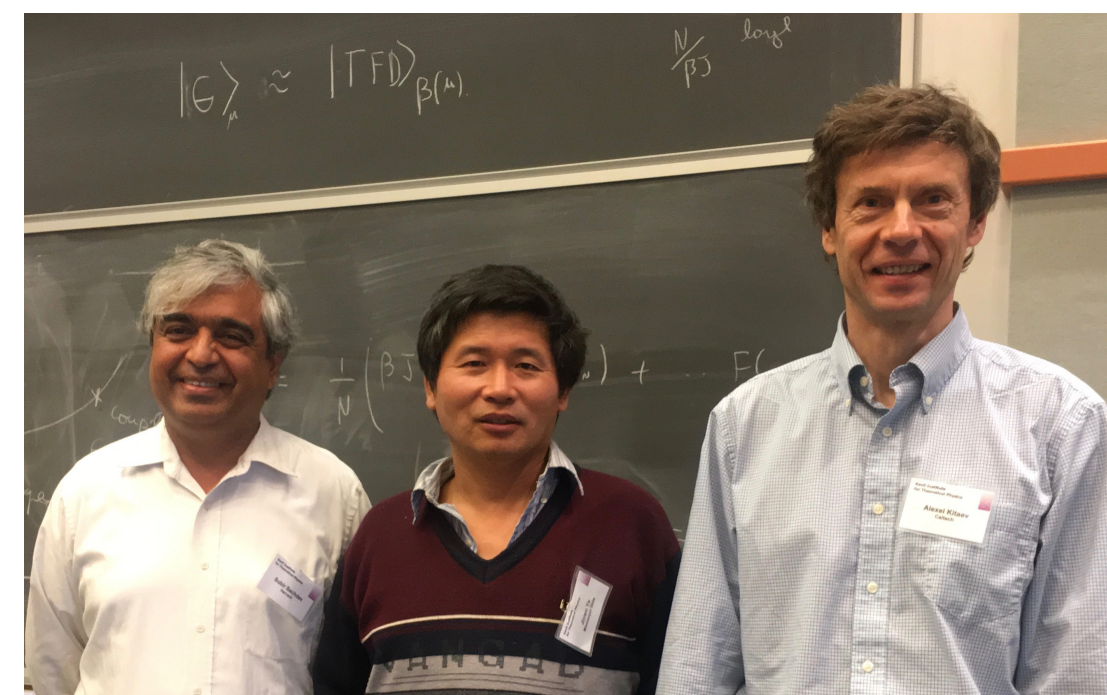
The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{4,5;11,18}$$



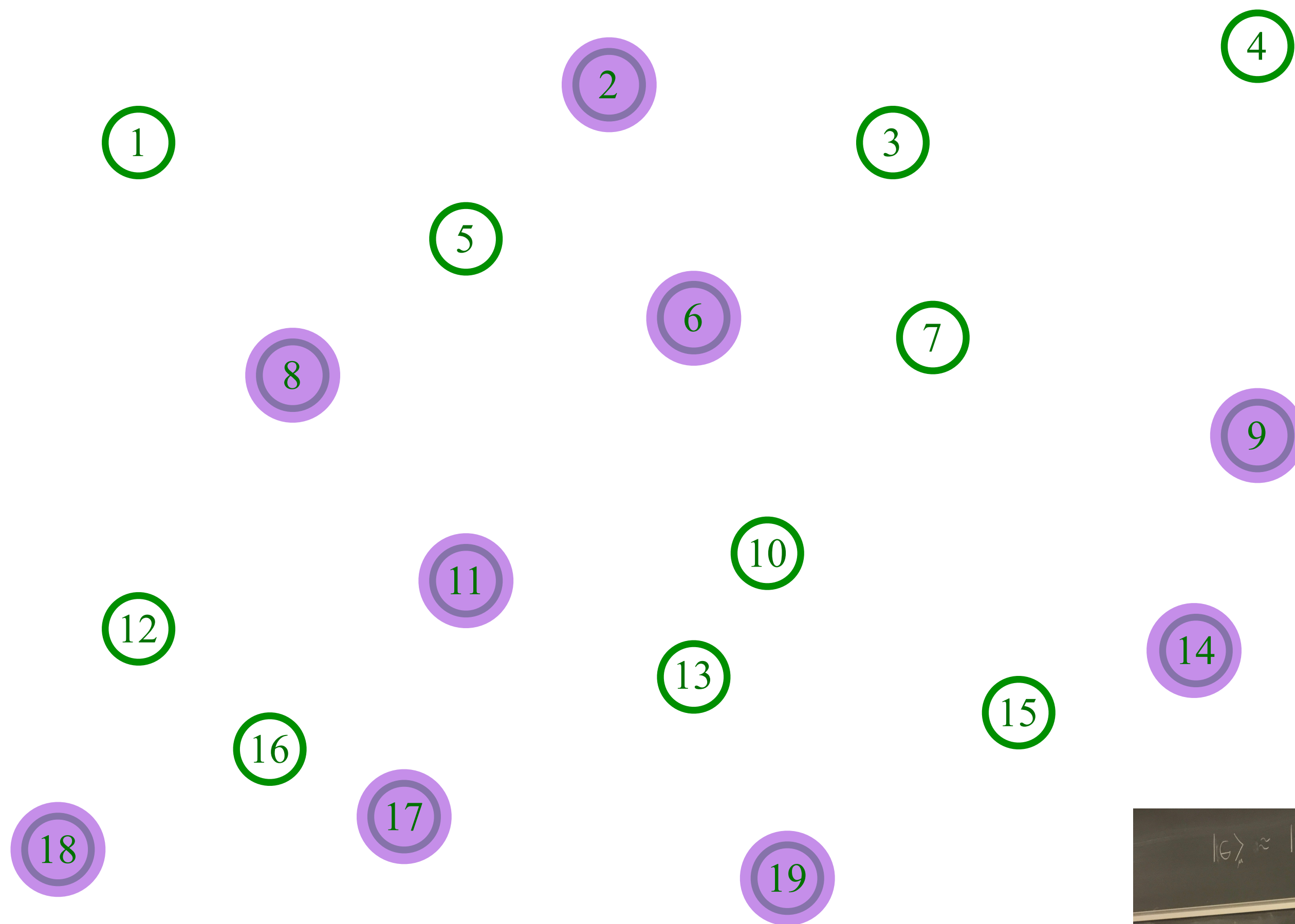
Entangle electrons pairwise randomly



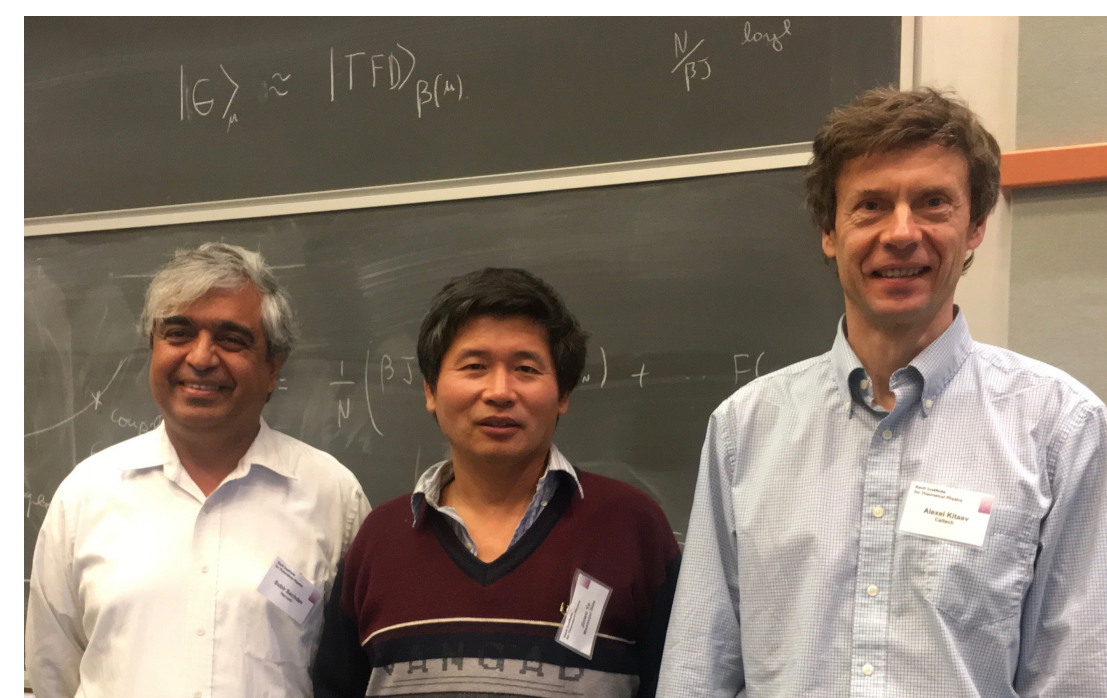
The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{4,5;11,18}$$



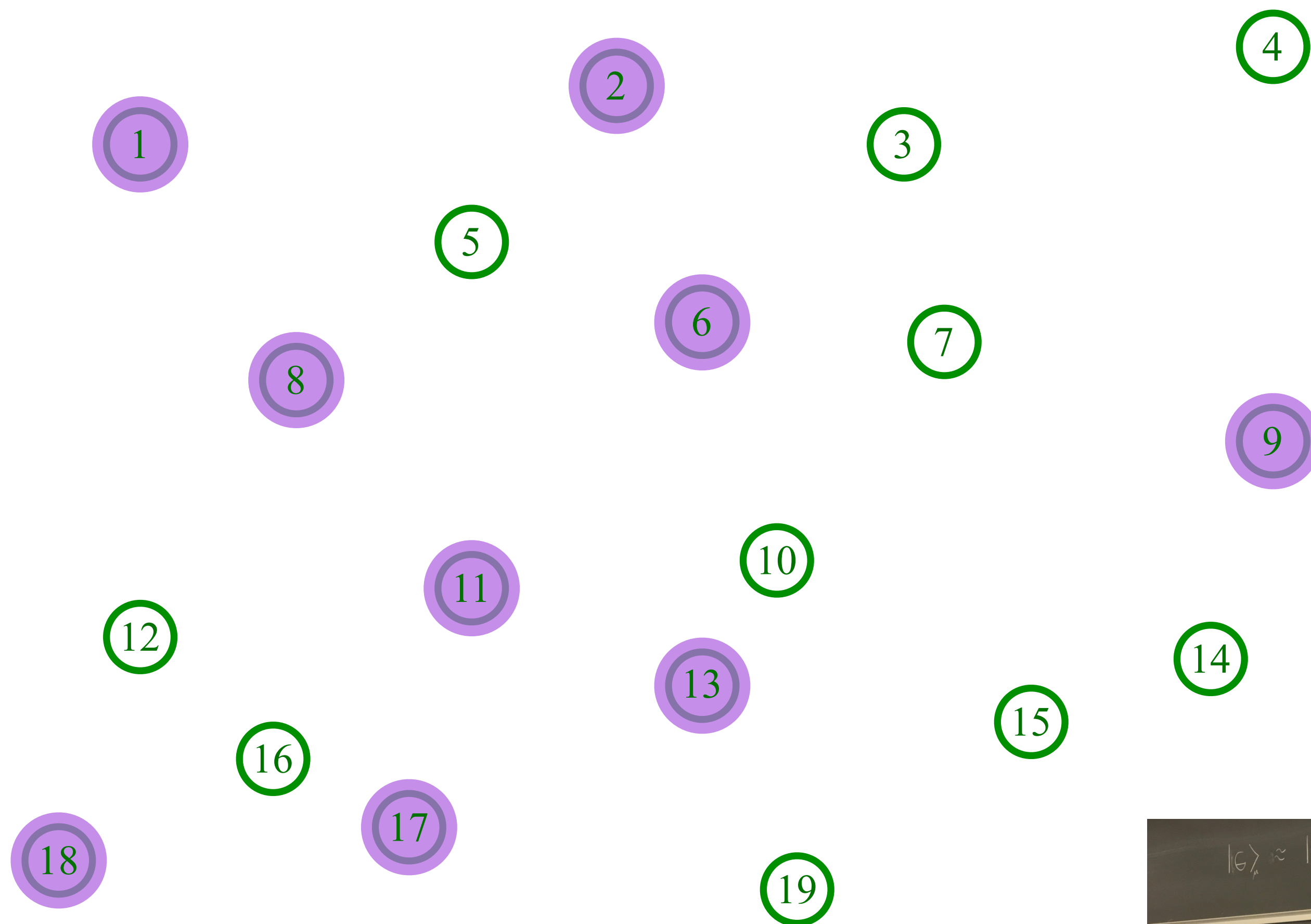
Entangle electrons pairwise randomly



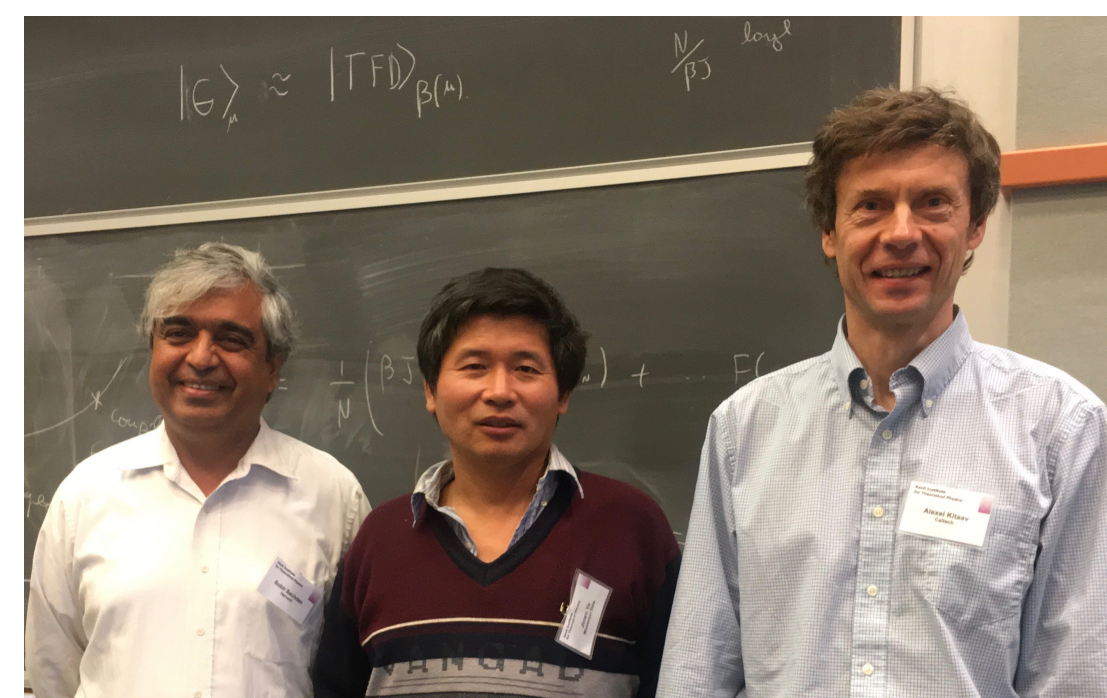
The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{14,19;1,13}$$



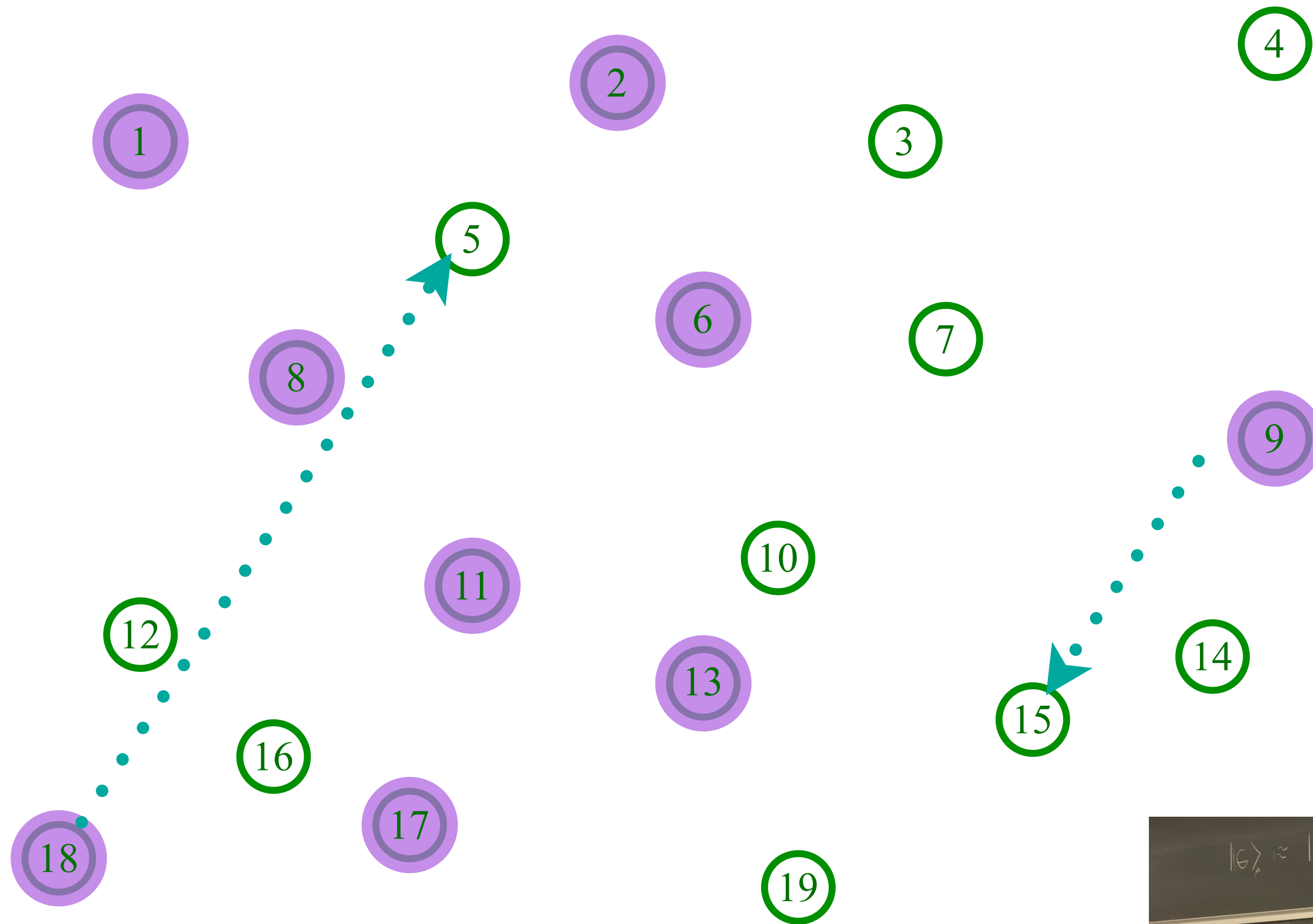
Entangle electrons pairwise randomly



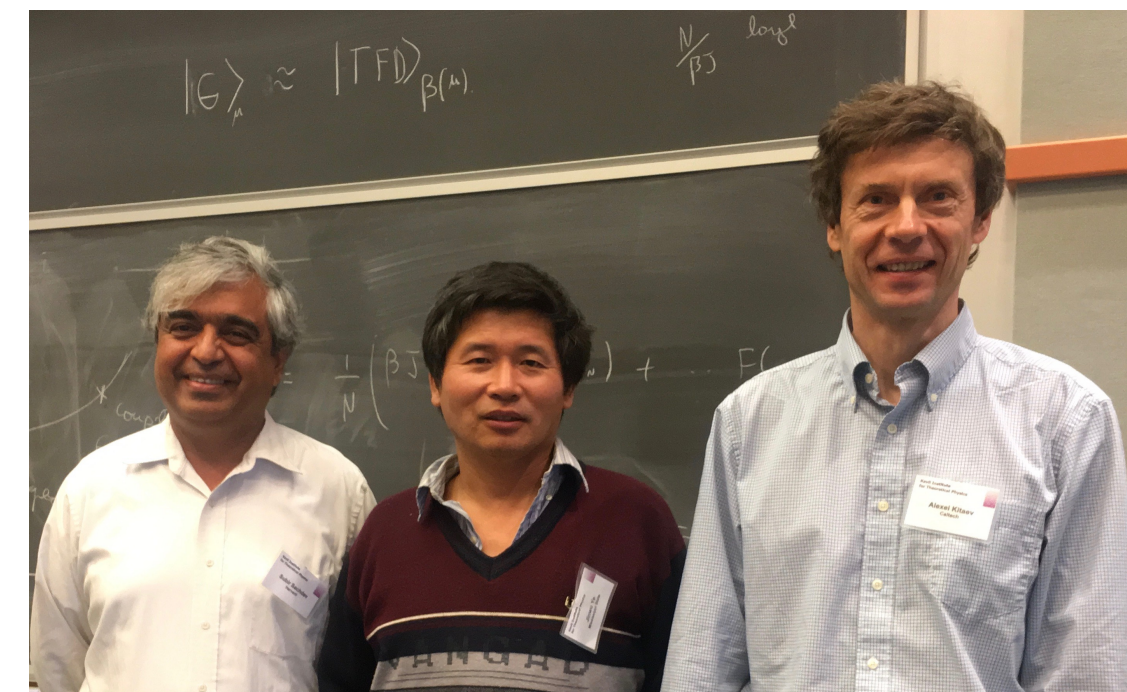
The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{9,18;5,15}$$



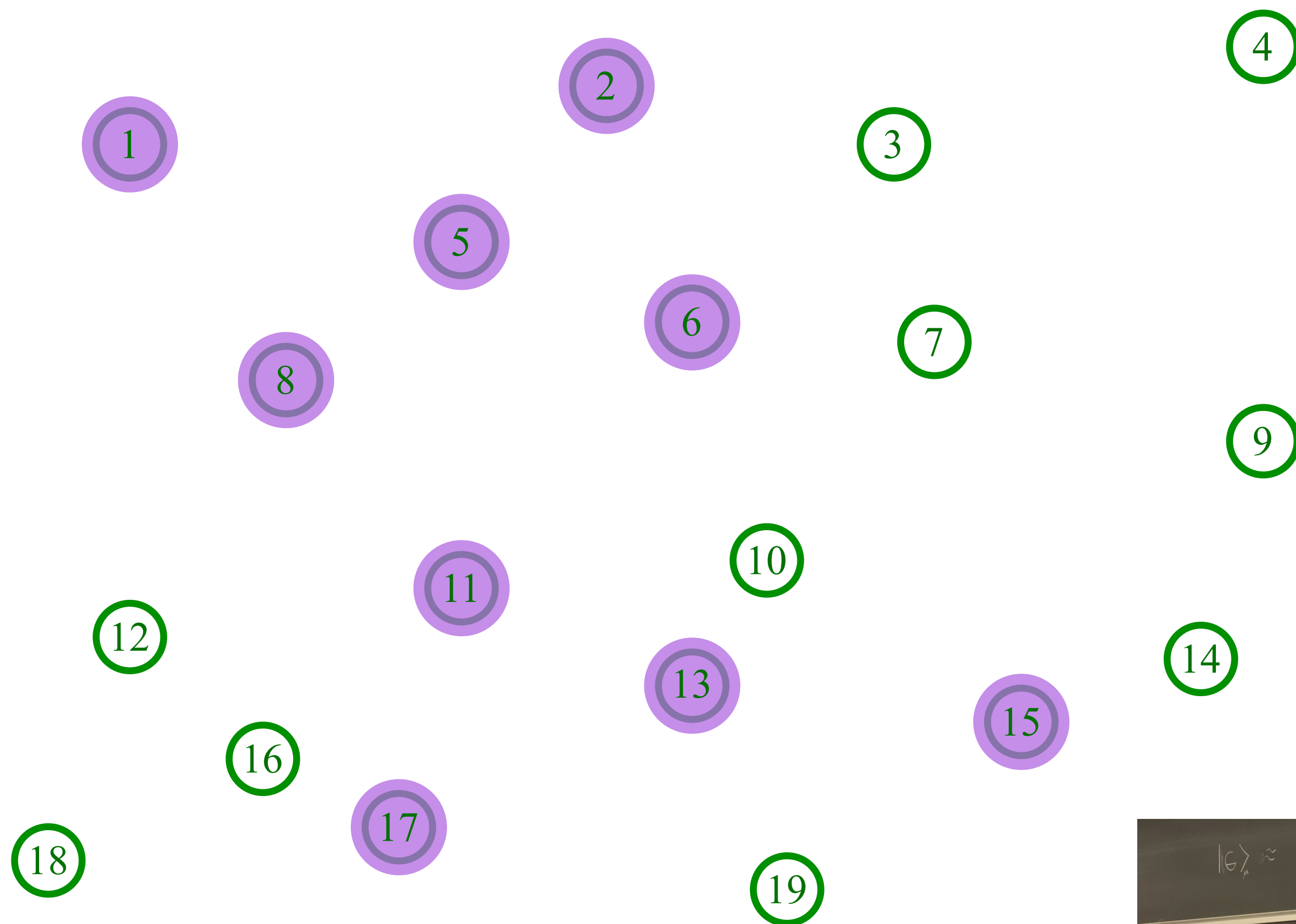
Entangle electrons pairwise randomly



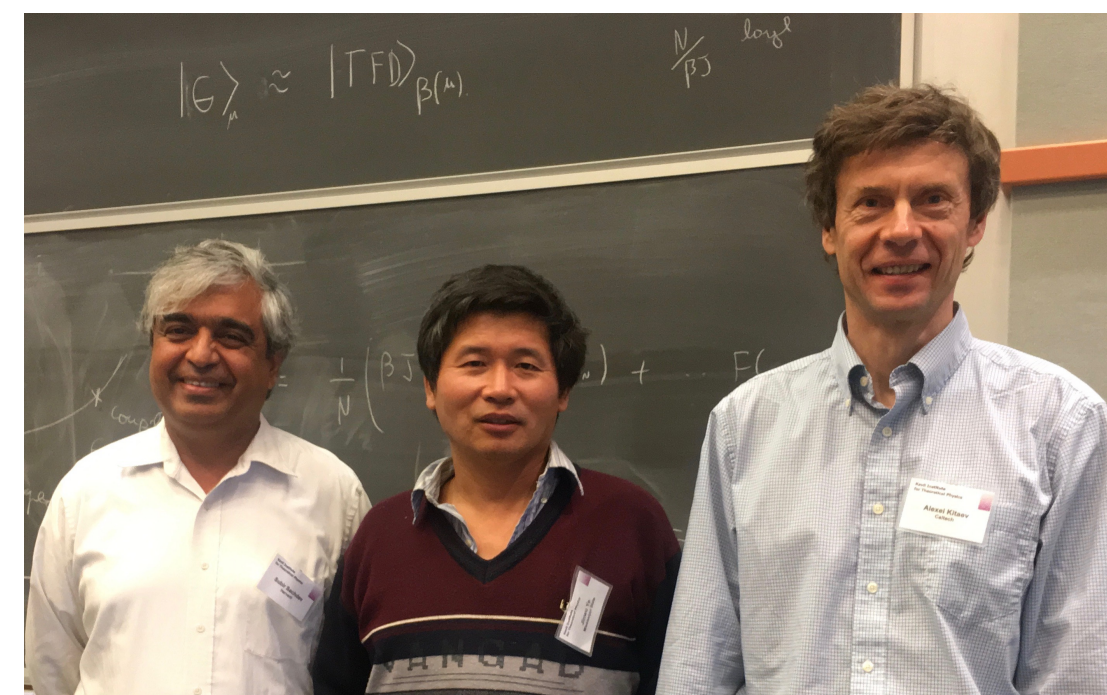
The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{9,18;5,15}$$



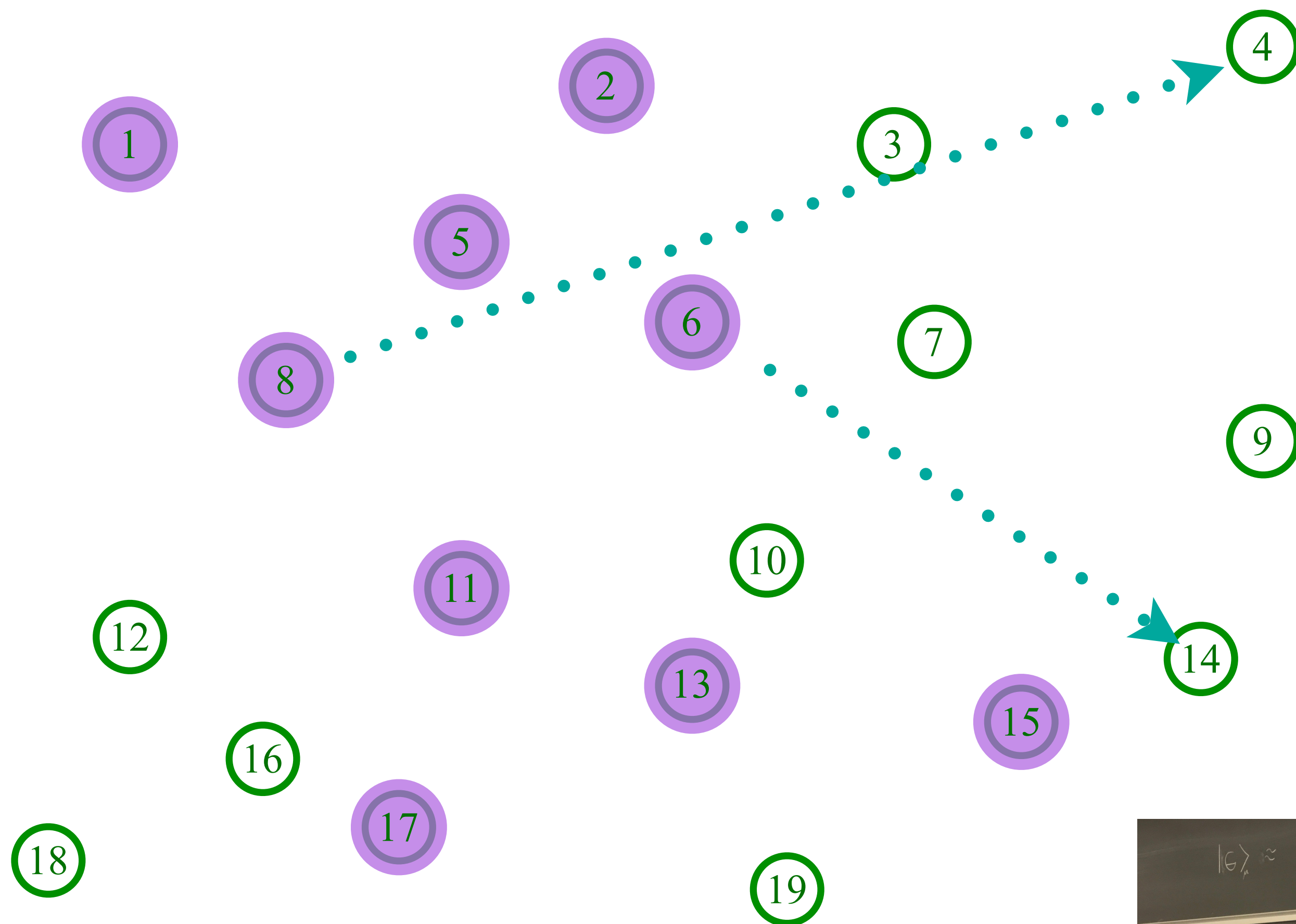
Entangle electrons pairwise randomly



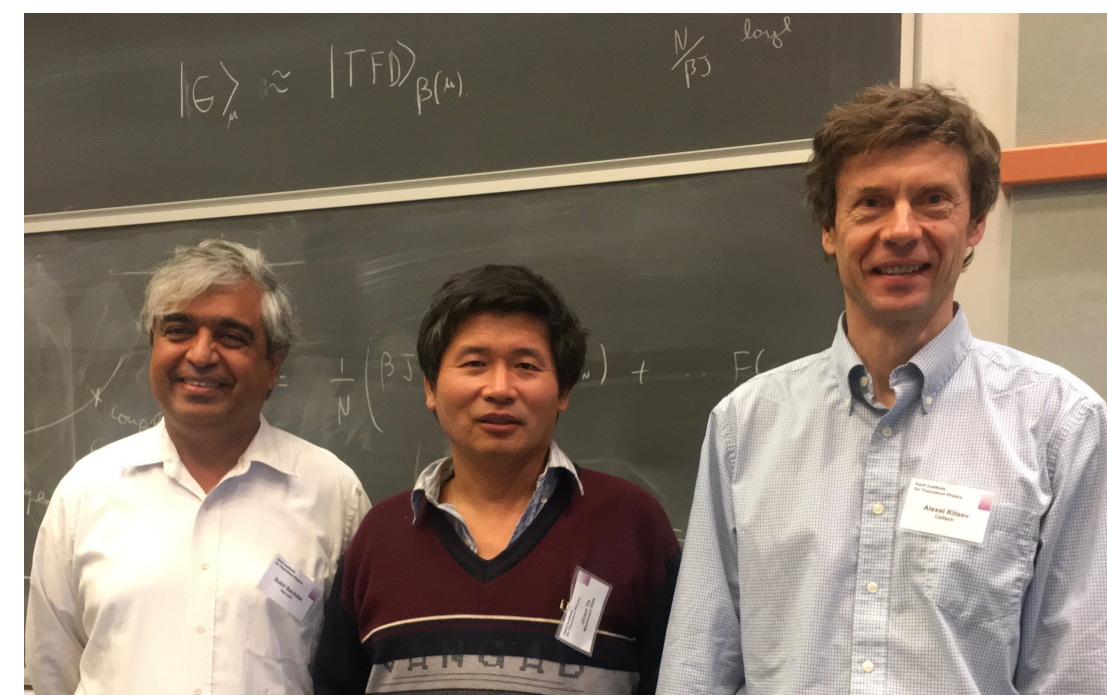
The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{6,8;4,14}$$



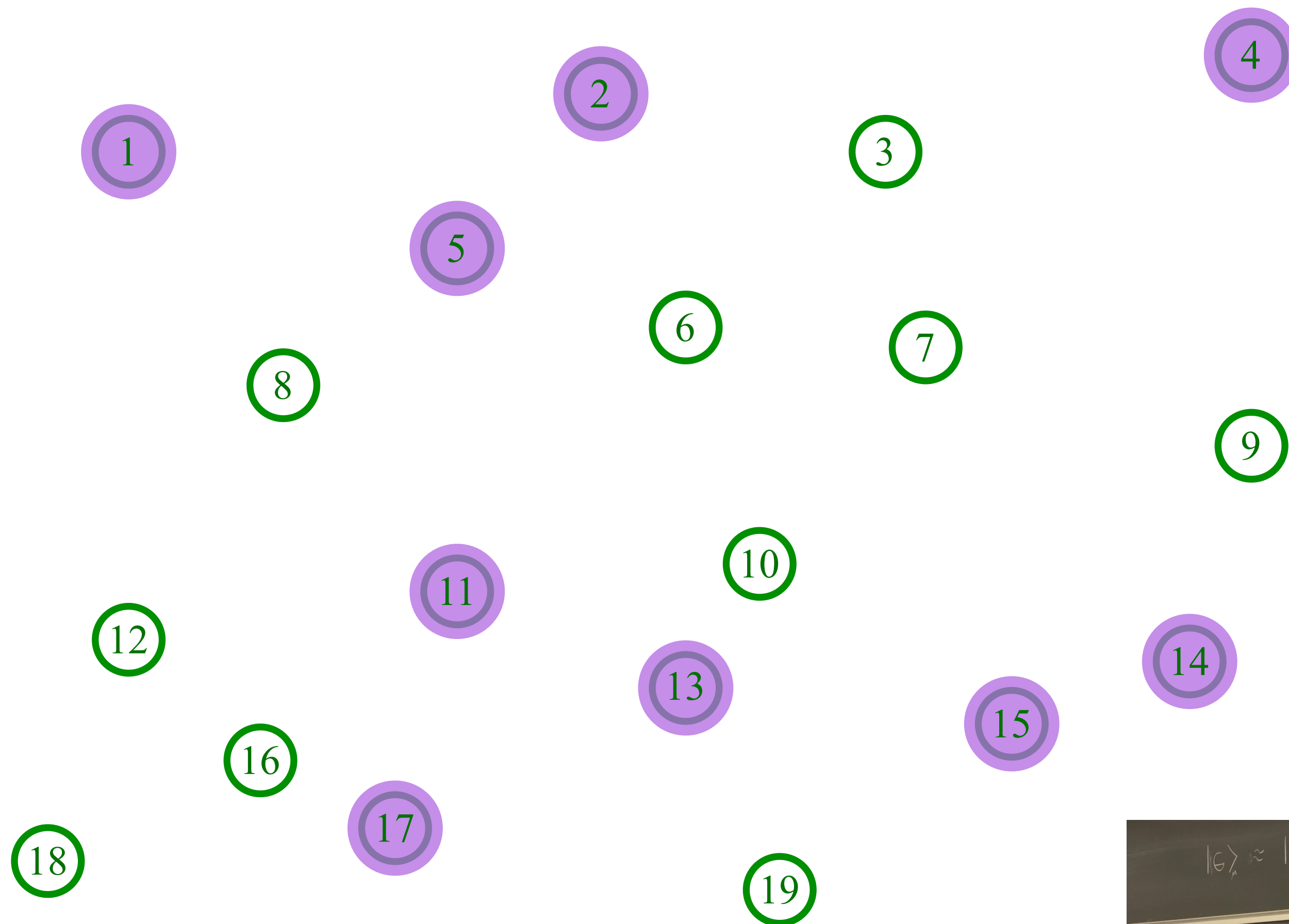
Entangle electrons pairwise randomly



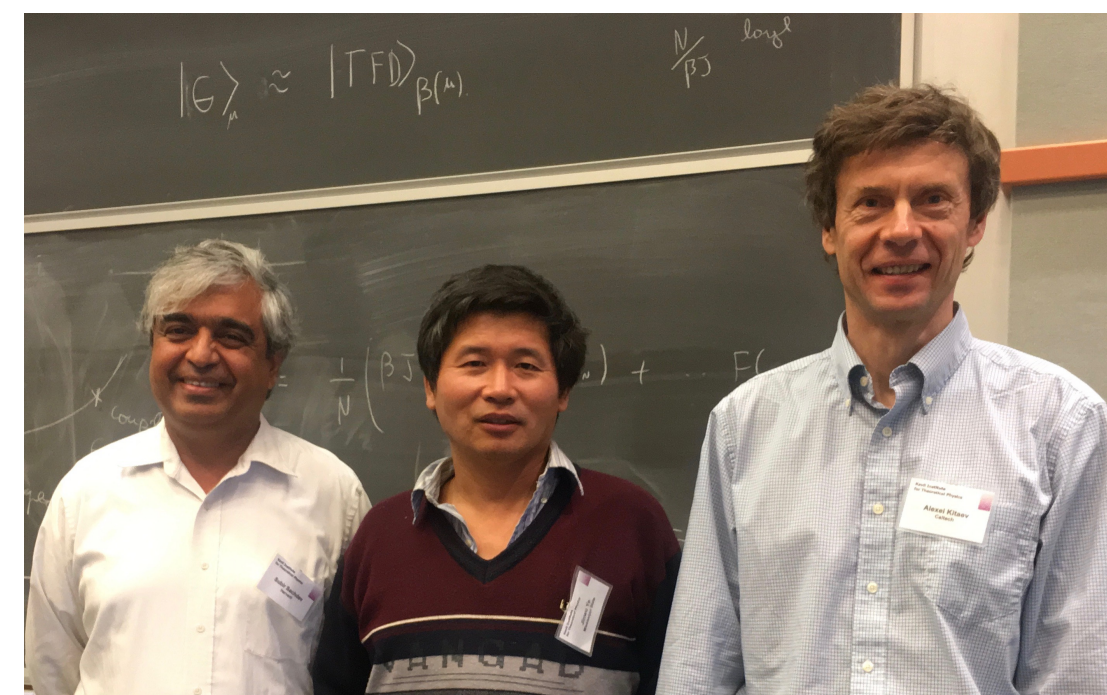
The SYK model

Sachdev, Ye (1993); Kitaev (2015)

$$U_{6,8;4,14}$$



Entangle electrons pairwise randomly



The Sachdev-Ye-Kitaev (SYK) model

(See also: the “2-Body Random Ensemble” in nuclear physics; did not obtain the large N limit;
T.A. Brody, J. Flores, J.B. French, P.A. Mello, A. Pandey, and S.S.M. Wong, Rev. Mod. Phys. **53**, 385 (1981))

$$H = \frac{1}{(2N)^{3/2}} \sum_{\alpha, \beta, \gamma, \delta=1}^N U_{\alpha\beta;\gamma\delta} c_{\alpha}^{\dagger} c_{\beta}^{\dagger} c_{\gamma} c_{\delta} - \mu \sum_{\alpha} c_{\alpha}^{\dagger} c_{\alpha}$$

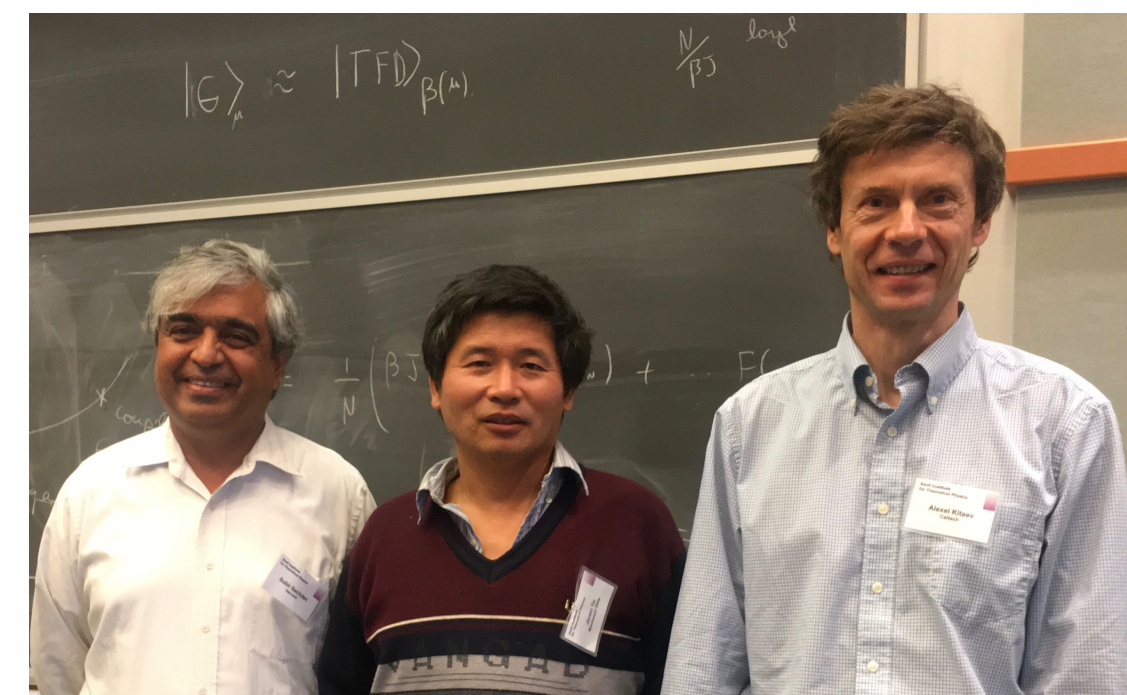
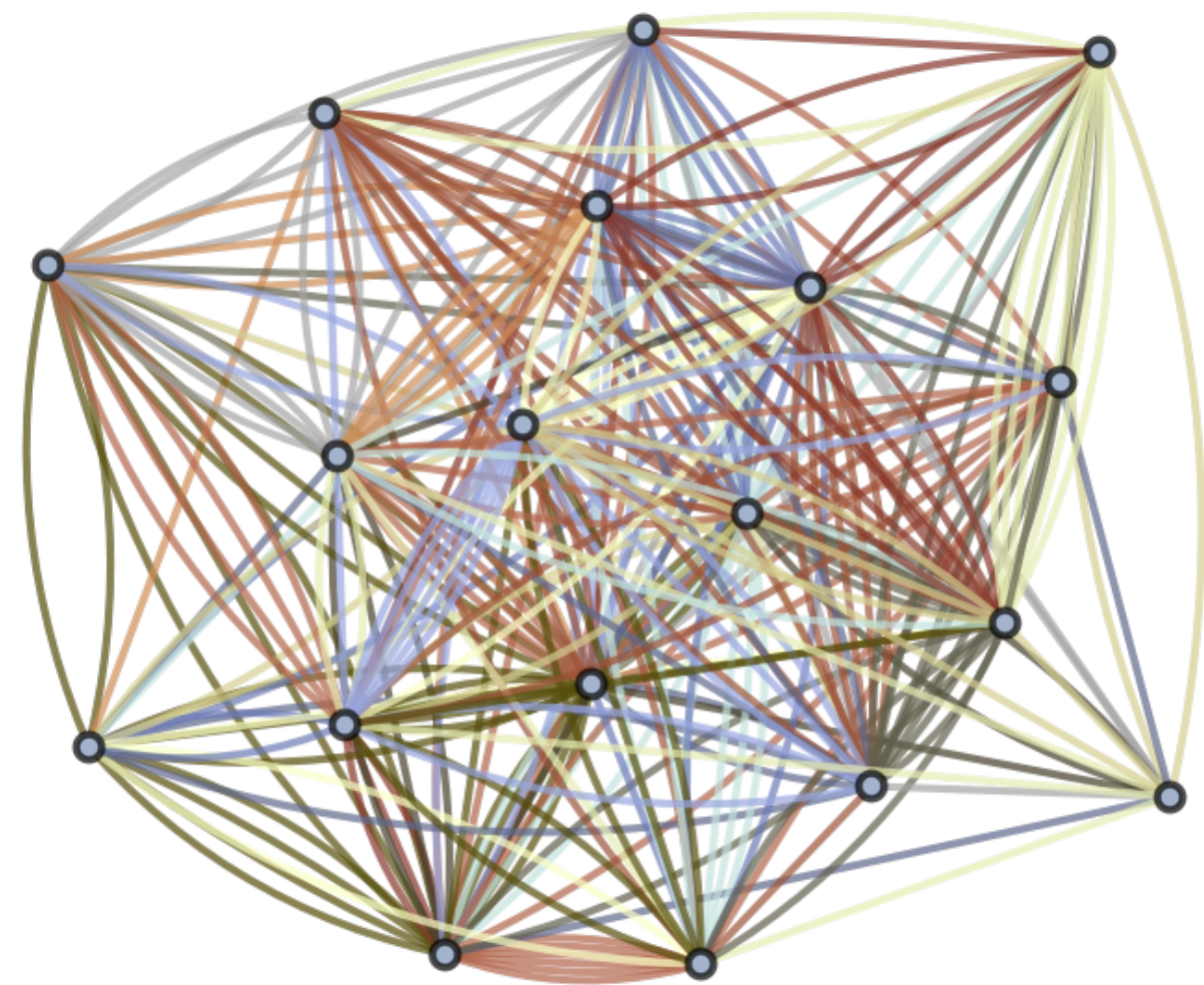
$$c_{\alpha} c_{\beta} + c_{\beta} c_{\alpha} = 0 \quad , \quad c_{\alpha} c_{\beta}^{\dagger} + c_{\beta}^{\dagger} c_{\alpha} = \delta_{\alpha\beta}$$

$$Q = \frac{1}{N} \sum_{\alpha} c_{\alpha}^{\dagger} c_{\alpha}$$

$U_{\alpha\beta;\gamma\delta}$ are independent random variables with $\overline{U_{\alpha\beta;\gamma\delta}} = 0$ and $\overline{|U_{\alpha\beta;\gamma\delta}|^2} = U^2$
 $N \rightarrow \infty$ yields critical strange metal.

S. Sachdev and J. Ye, PRL **70**, 3339 (1993)

A. Kitaev, unpublished; S. Sachdev, PRX **5**, 041025 (2015)



The SYK model

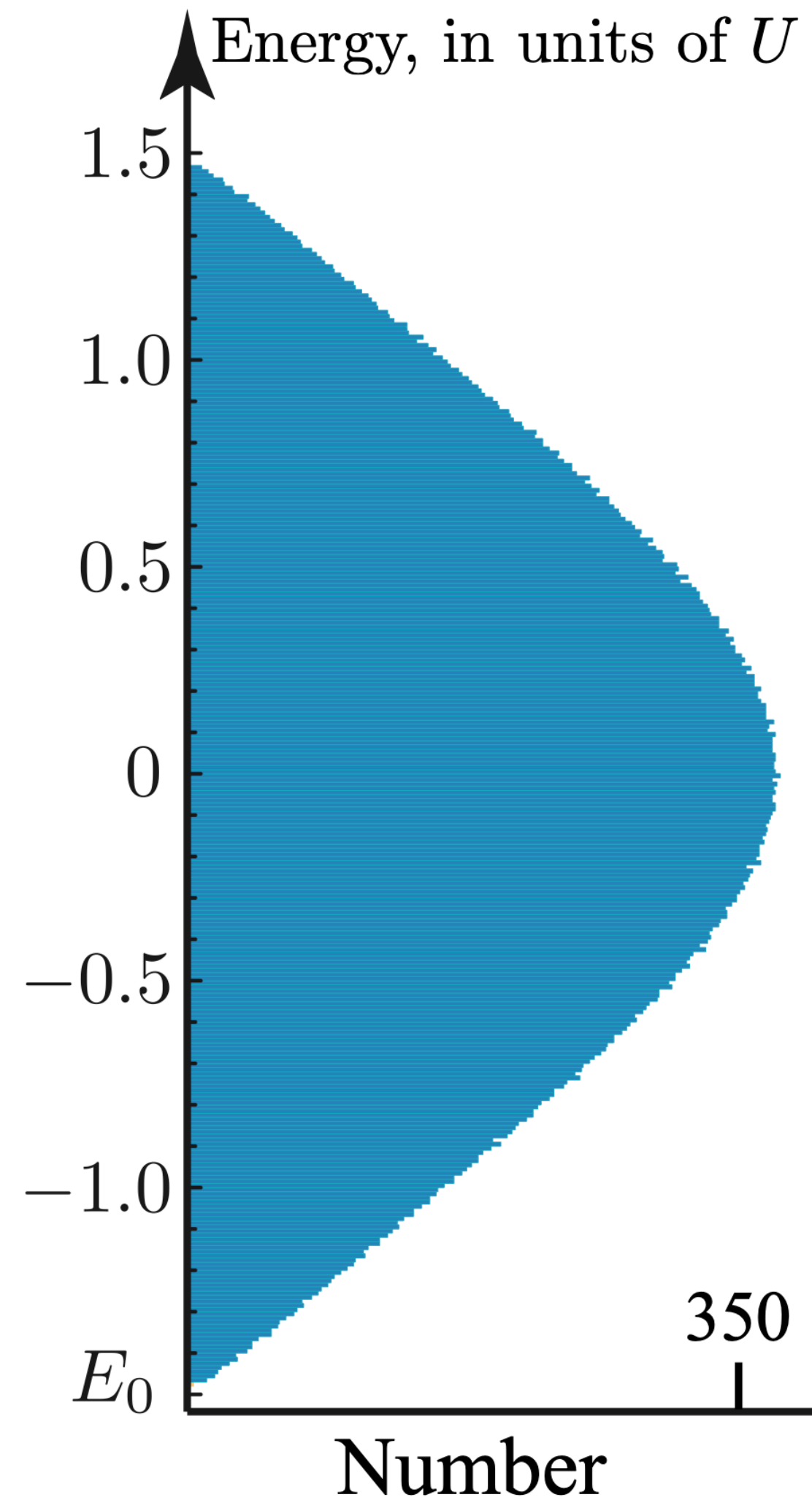
- Planckian time dynamics with a relaxation time $\sim \hbar/(k_B T)$ when $k_B T \ll U$.

The SYK model

- Planckian time dynamics with a relaxation time $\sim \hbar/(k_B T)$ when $k_B T \ll U$.
- There is an extensive entropy as $T \rightarrow 0$ ($\lim_{T \rightarrow 0} \lim_{N \rightarrow \infty} S/N \neq 0$); however, the ground state is *not* extensively degenerate.

The SYK model

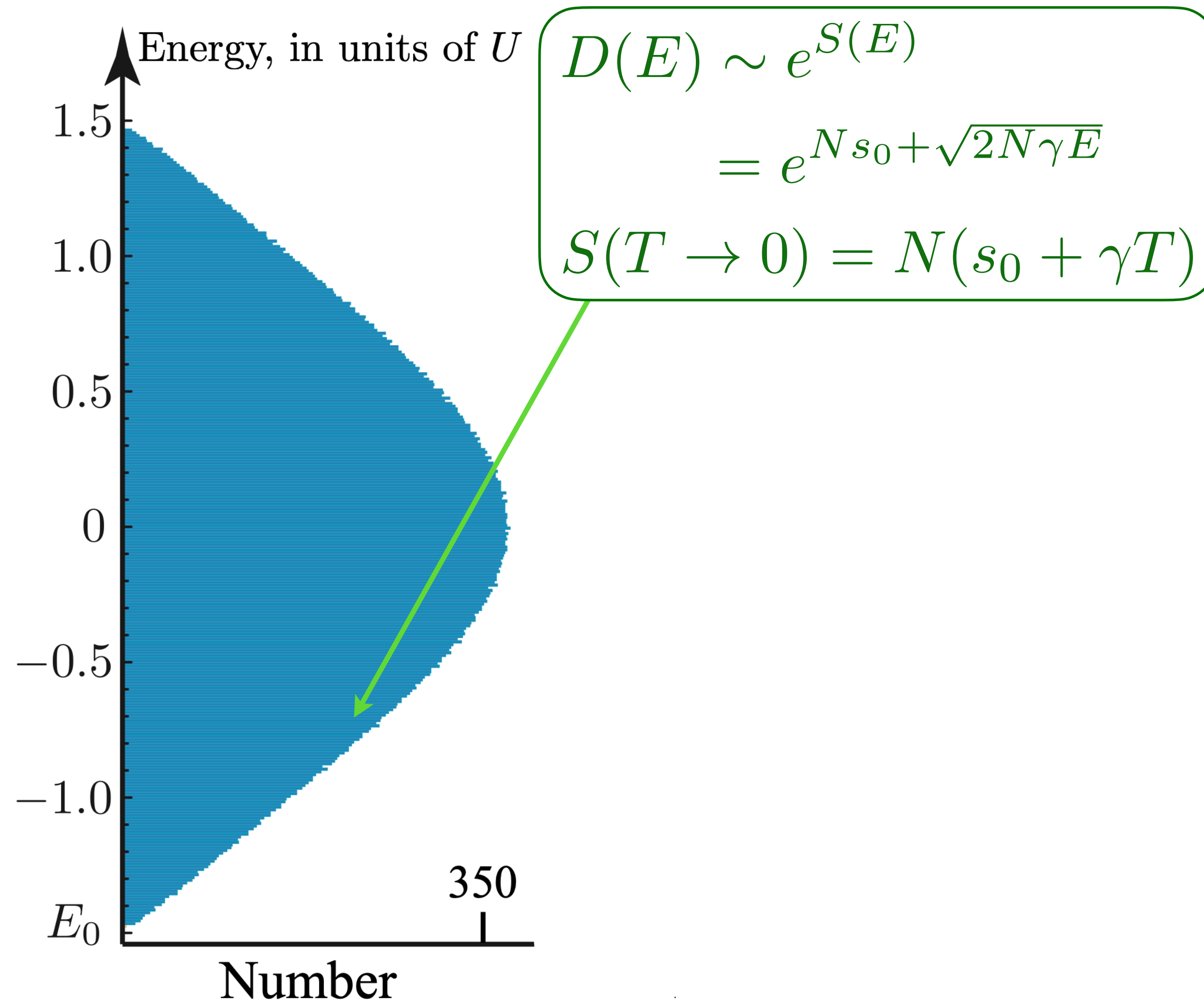
$$D(E) = \sum_i \delta(E - E_i); \quad E_0 + E_i \Rightarrow \text{Many body eigenvalue}$$



Many-body density of states

The SYK model

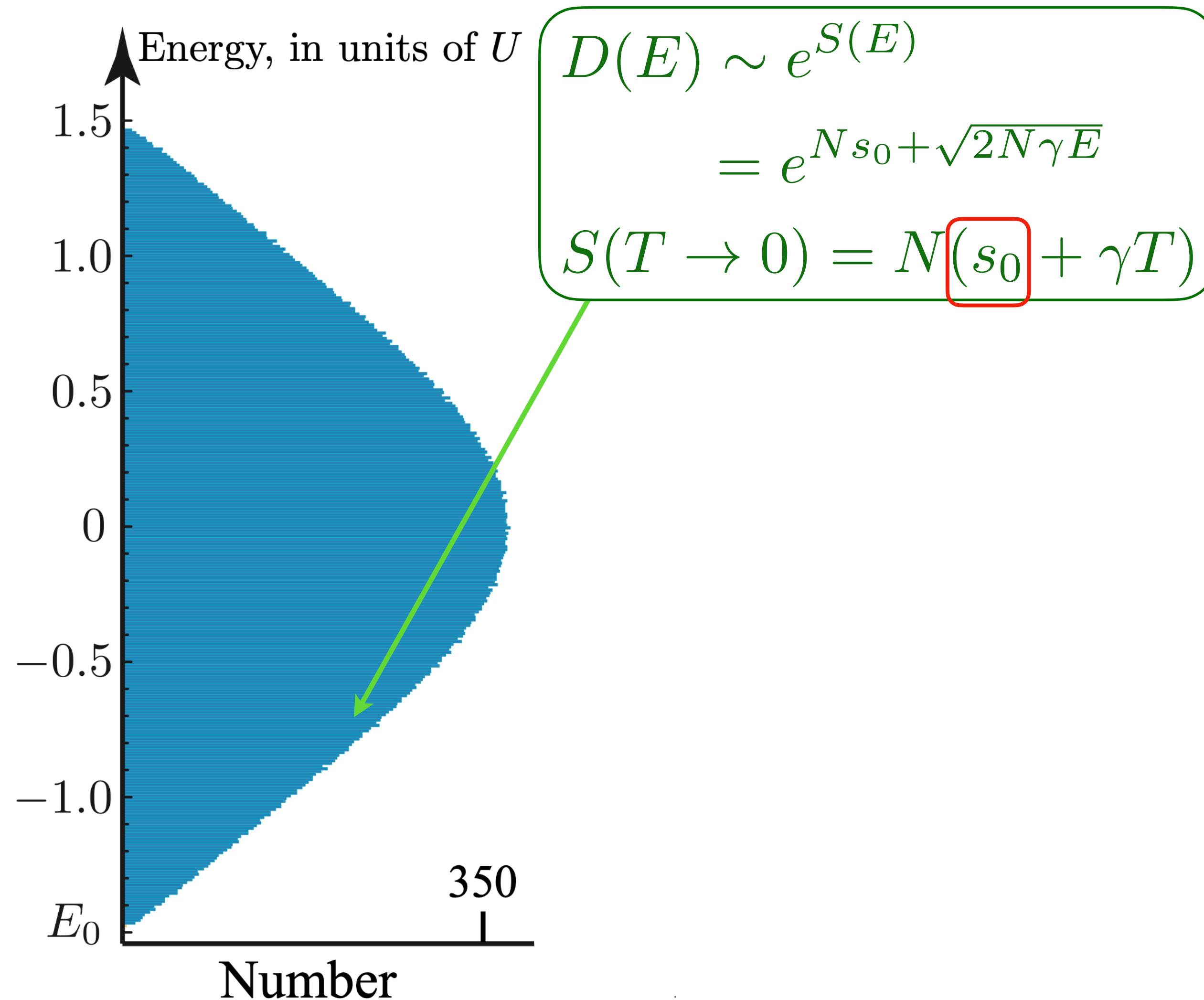
$$D(E) = \sum_i \delta(E - E_i); \quad E_0 + E_i \Rightarrow \text{Many body eigenvalue}$$



Many-body density of states

The SYK model

$$D(E) = \sum_i \delta(E - E_i); \quad E_0 + E_i \Rightarrow \text{Many body eigenvalue}$$



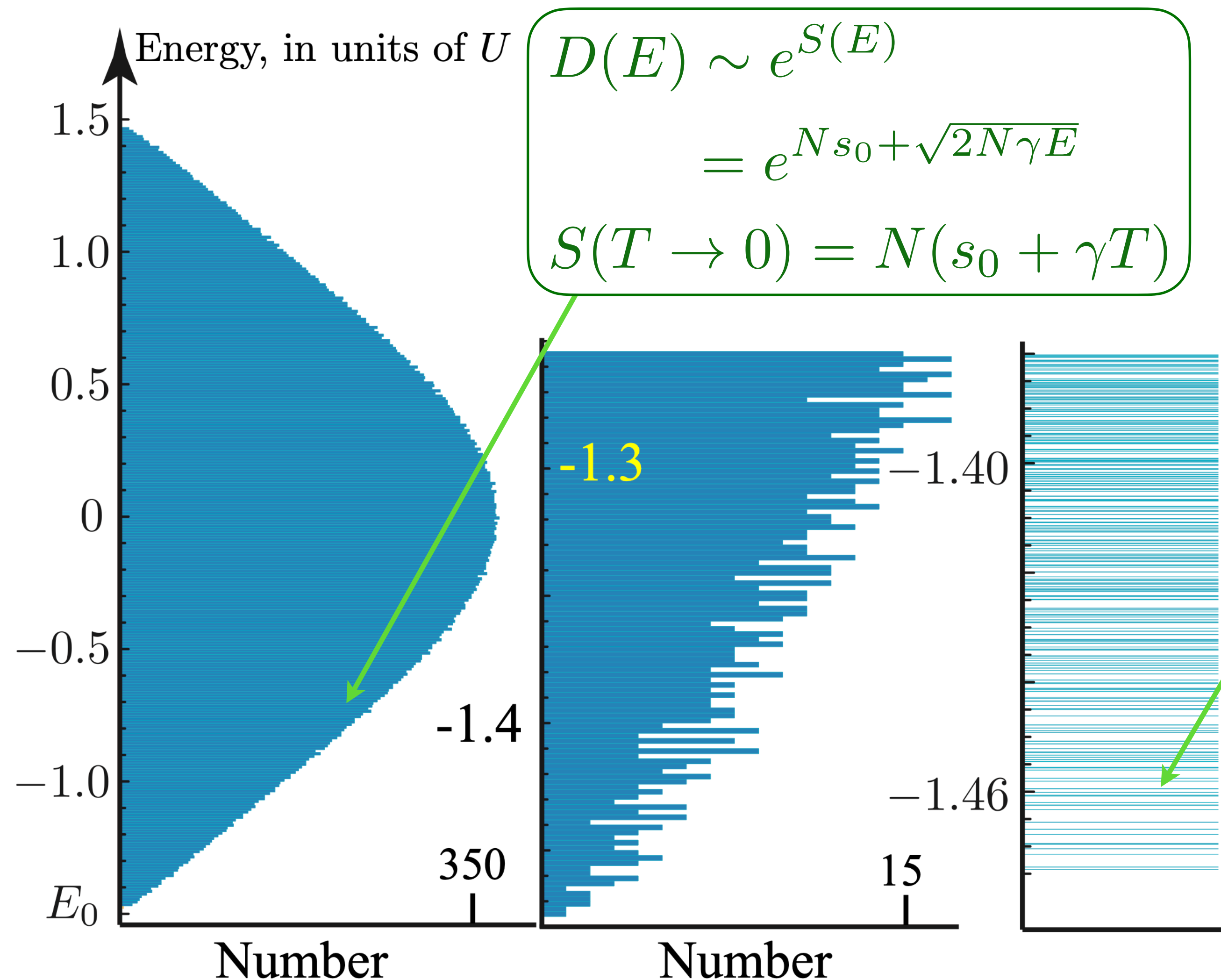
$$s_0 = 0.464848 \dots$$

A. Georges, O. Parcollet, and
S. Sachdev,
PRB **63**, 134406 (2001)

Many-body density of states

The SYK model

$$D(E) = \sum_i \delta(E - E_i); \quad E_0 + E_i \Rightarrow \text{Many body eigenvalue}$$



$$D(E) \sim e^{S(E)}$$

$$= e^{N s_0 + \sqrt{2N\gamma E}}$$

$$S(T \rightarrow 0) = N(s_0 + \gamma T)$$

$$D(E) \sim 2 e^{N s_0} \sqrt{2N\gamma E}$$

No particle-like decomposition:
wavefunctions change chaotically
from one state to the next.

$$s_0 = 0.464848 \dots$$

A. Georges, O. Parcollet, and S. Sachdev,
PRB **63**, 134406 (2001)

The SYK model

- Planckian time dynamics with a relaxation time $\sim \hbar/(k_B T)$ when $k_B T \ll U$.
- There is an extensive entropy as $T \rightarrow 0$ ($\lim_{T \rightarrow 0} \lim_{N \rightarrow \infty} S/N \neq 0$); however, the ground state is *not* extensively degenerate.

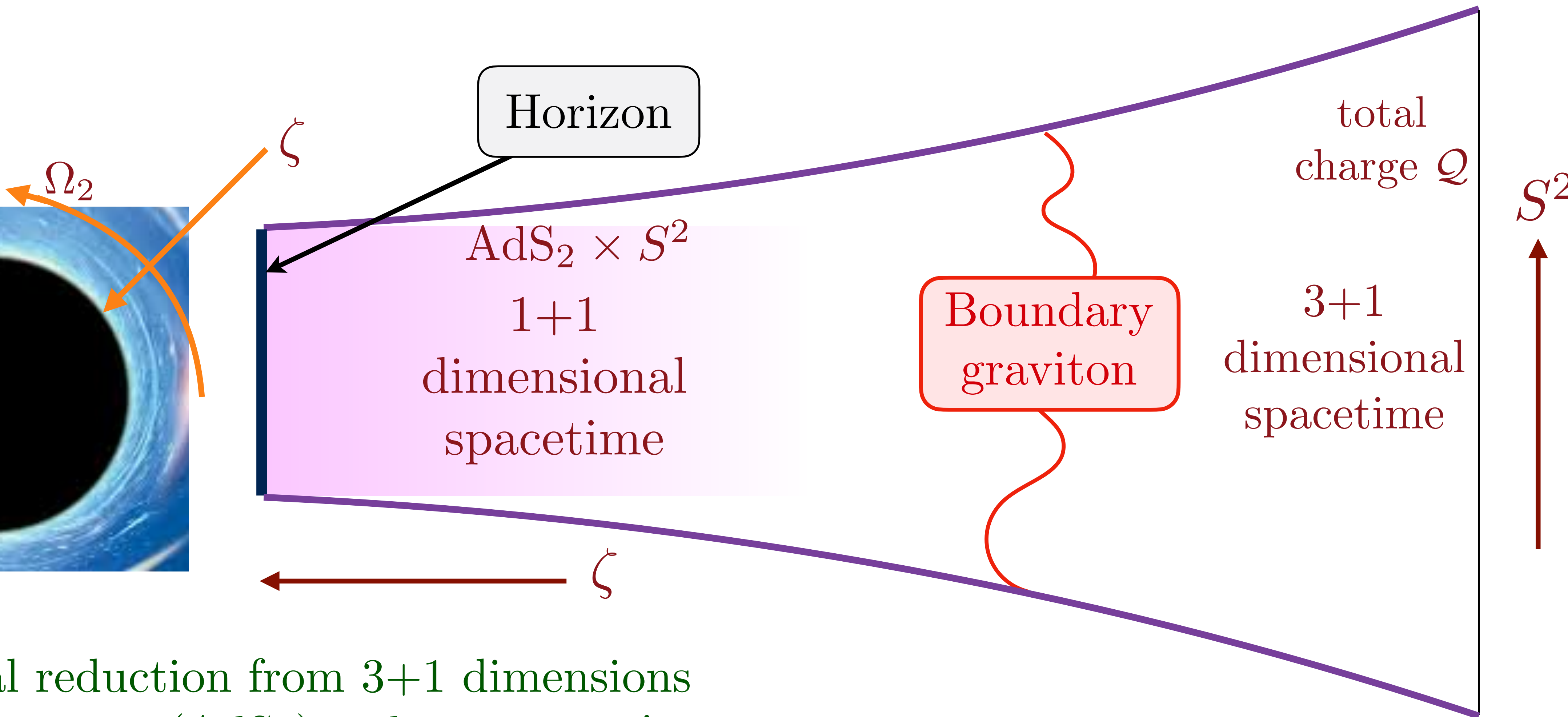
The SYK model

- Planckian time dynamics with a relaxation time $\sim \hbar/(k_B T)$ when $k_B T \ll U$.
- There is an extensive entropy as $T \rightarrow 0$ ($\lim_{T \rightarrow 0} \lim_{N \rightarrow \infty} S/N \neq 0$); however, the ground state is *not* extensively degenerate.
- The $D(E)$ is determined by a time-reparameterization $\tau \rightarrow f(\tau)$ mode (similar to the graviton being fluctuations of the spacetime metric), and a phase mode $\phi(\tau)$:

$$\mathcal{Z}_{SYK} = e^{N s_0} \int \mathcal{D}f \mathcal{D}\phi \exp \left(-\frac{1}{\hbar} \int_0^{\hbar/(k_B T)} d\tau \mathcal{L}_{SYK}[f, \phi] \right)$$

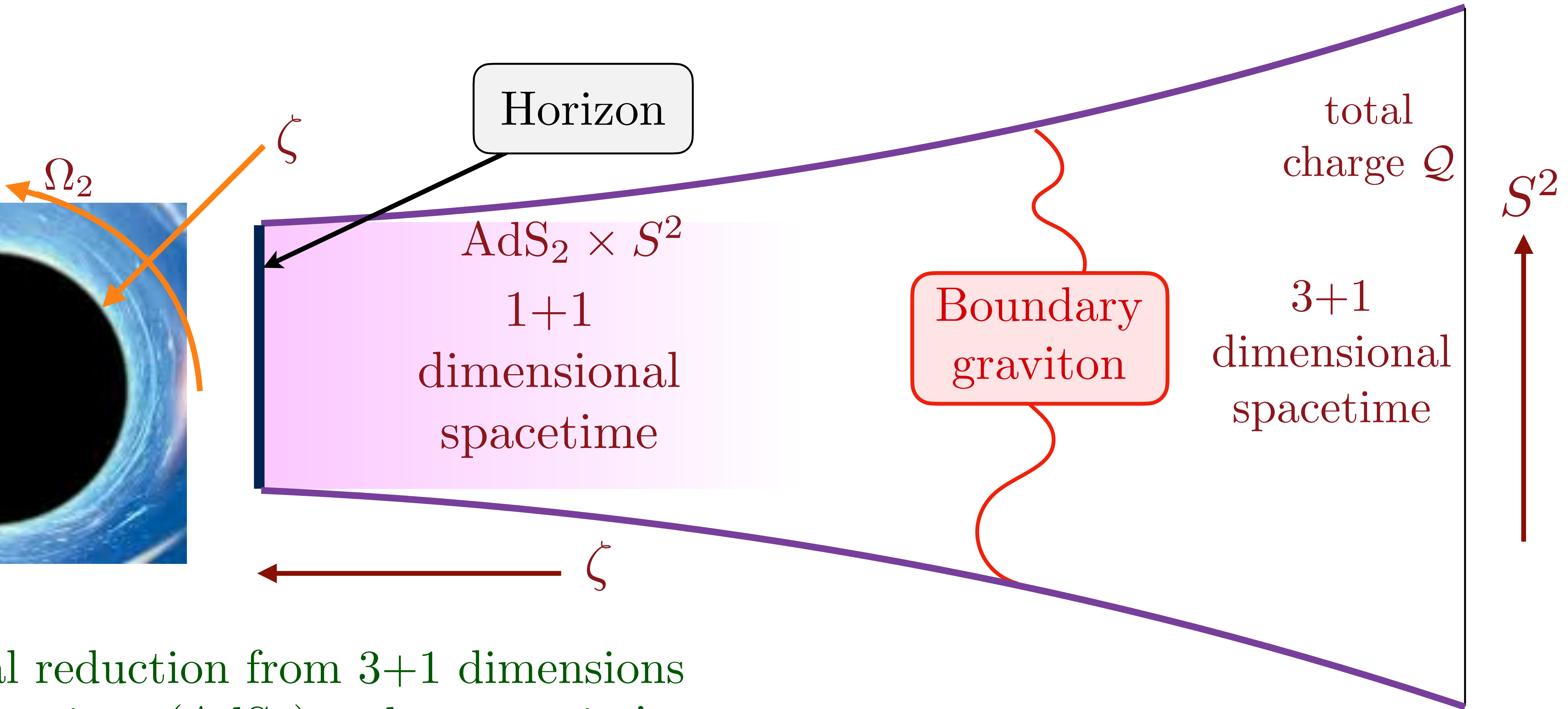
From the
SYK model
to
charged black holes

Reissner-Nordstrom black hole of Einstein-Maxwell theory



Dimensional reduction from 3+1 dimensions to 1+1 dimensions (AdS₂) at low energies!

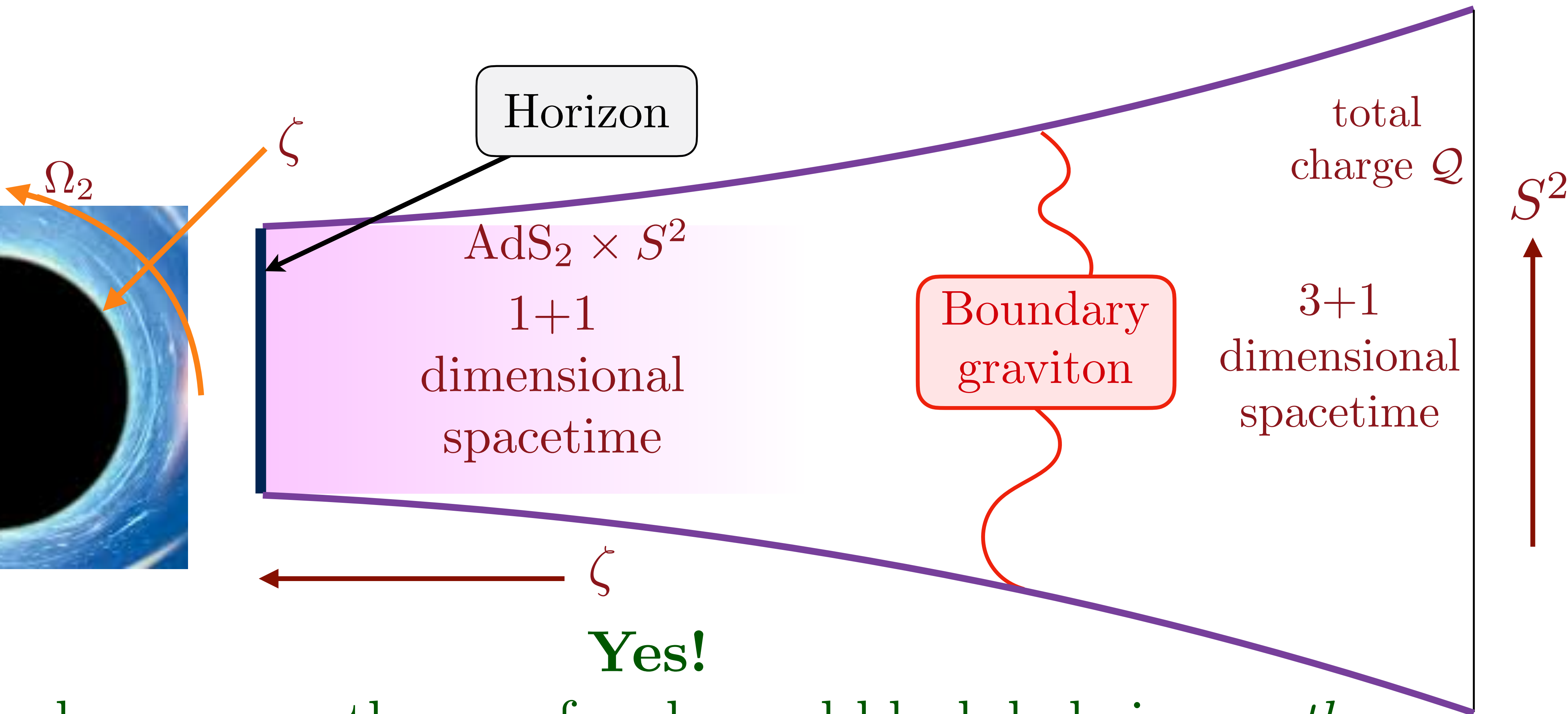
Reissner-Nordstrom black hole of Einstein-Maxwell theory



Dimensional reduction from 3+1 dimensions to 1+1 dimensions (AdS_2) at low energies!

Is there a mapping to a quantum system with Planckian dynamics in 0+1 dimensions?

Reissner-Nordstrom black hole of Einstein-Maxwell theory



The low energy theory of a charged black hole is *exactly* the low energy theory of time reparameterizations of the SYK model.

Quantum theory of charged black holes

The near-horizon 1+1 dimensional theory of a charged black hole

$$\mathcal{Z}_Q = \int \mathcal{D}g_{\mu\nu} \mathcal{D}a_\mu \exp \left(-\frac{1}{\hbar} \int d\zeta \int_0^{\hbar/(k_B T)} d\tau \sqrt{g} \mathcal{L}_1[g_{\mu\nu}, a_\mu] \right)$$

Quantum theory of charged black holes

The near-horizon 1+1 dimensional theory of a charged black hole

$$\mathcal{Z}_Q = \int \mathcal{D}g_{\mu\nu} \mathcal{D}a_\mu \exp \left(-\frac{1}{\hbar} \int d\zeta \int_0^{\hbar/(k_B T)} d\tau \sqrt{g} \mathcal{L}_1[g_{\mu\nu}, a_\mu] \right)$$



$$\mathcal{Z}_{SYK} = e^{N s_0} \int \mathcal{D}f \mathcal{D}\phi \exp \left(-\frac{1}{\hbar} \int_0^{\hbar/(k_B T)} d\tau \mathcal{L}_{SYK}[f, \phi] \right)$$

after relating the boundary component of $g_{\mu\nu}$ to f ,
and the boundary value of a_τ to ϕ .

Quantum theory of charged black holes

The near-horizon 1+1 dimensional theory of a charged black hole

$$\mathcal{Z}_Q = \int \mathcal{D}g_{\mu\nu} \mathcal{D}a_\mu \exp \left(-\frac{1}{\hbar} \int d\zeta \int_0^{\hbar/(k_B T)} d\tau \sqrt{g} \mathcal{L}_1[g_{\mu\nu}, a_\mu] \right)$$



$$\mathcal{Z}_{SYK} = e^{N s_0} \int \mathcal{D}f \mathcal{D}\phi \exp \left(-\frac{1}{\hbar} \int_0^{\hbar/(k_B T)} d\tau \mathcal{L}_{SYK}[f, \phi] \right)$$

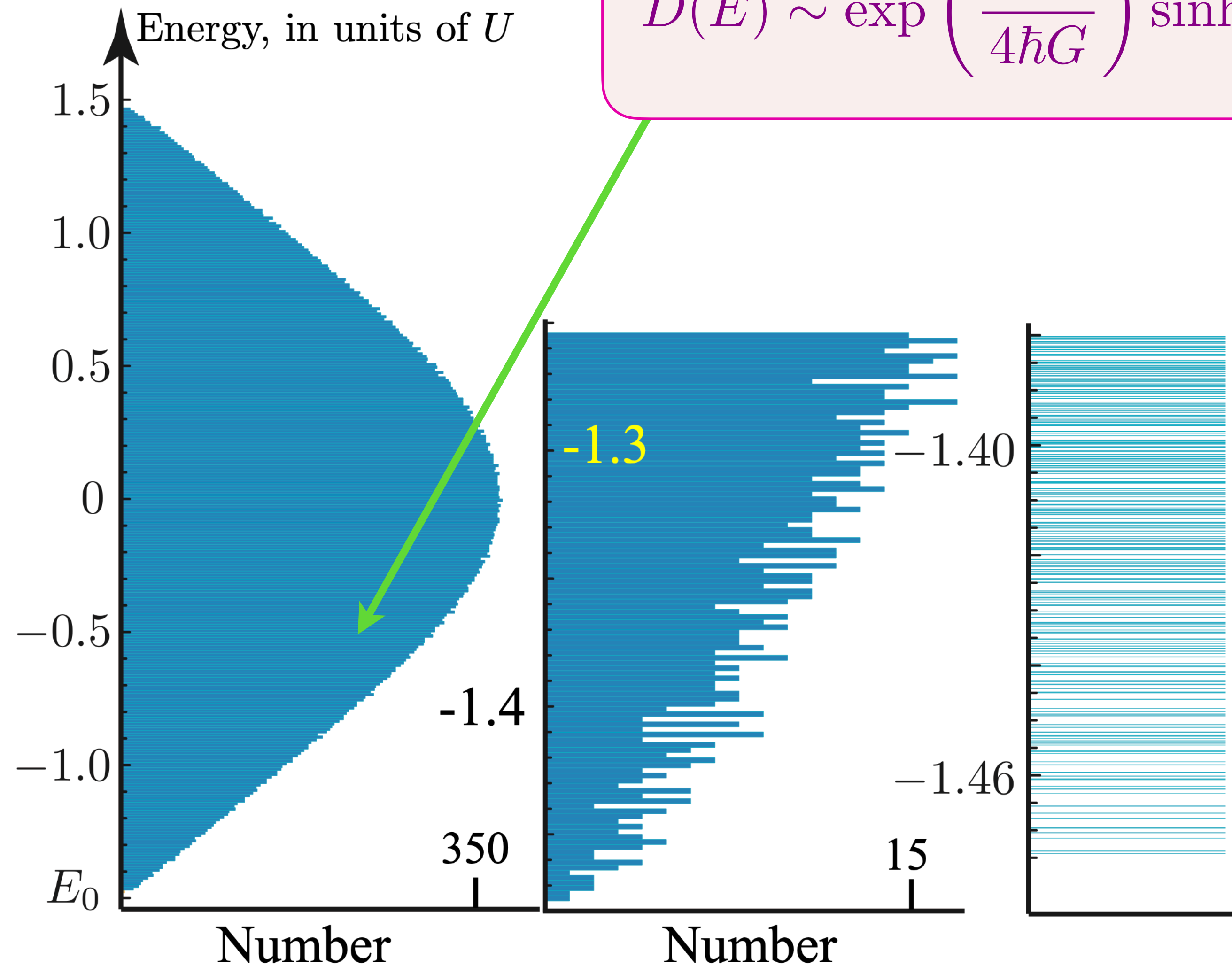
after relating the boundary component of $g_{\mu\nu}$ to f ,
and the boundary value of a_τ to ϕ .

$$\frac{S(T)}{k_B} = \frac{1}{\hbar G} \left(\frac{A_0 c^3}{4} + \frac{\sqrt{\pi} A_0^{3/2} c^2 k_B T}{2 \hbar} \right) - \frac{3}{2} \ln \left(\frac{\sqrt{c^5 / \hbar G}}{k_B T / \hbar} \right) + \dots$$

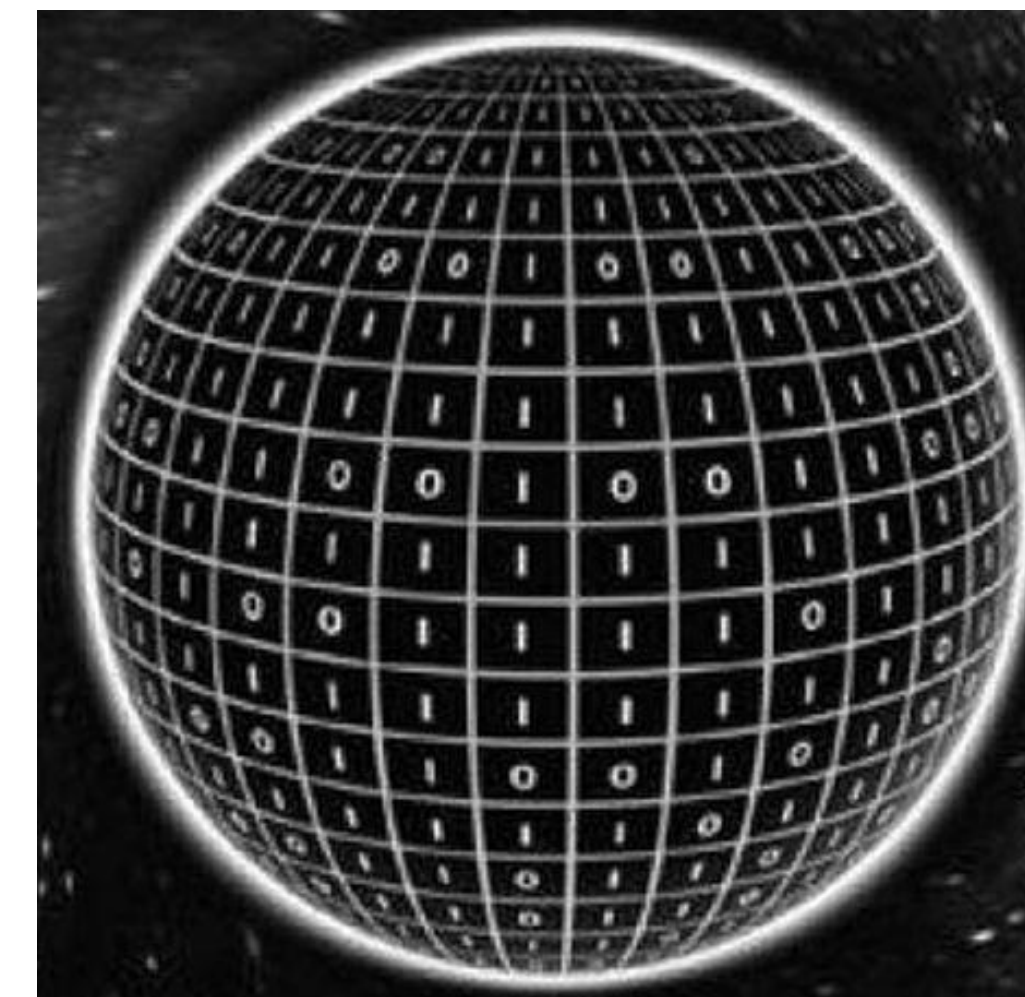
where A_0 is the area of the black hole horizon at $T = 0$.

Quantum theory of charged black holes

$$D(E) \sim \exp\left(\frac{A_0 c^3}{4\hbar G}\right) \sinh\left(\left[\frac{\sqrt{\pi} A_0^{3/2} c^2}{\hbar^2 G} E\right]^{1/2}\right)$$

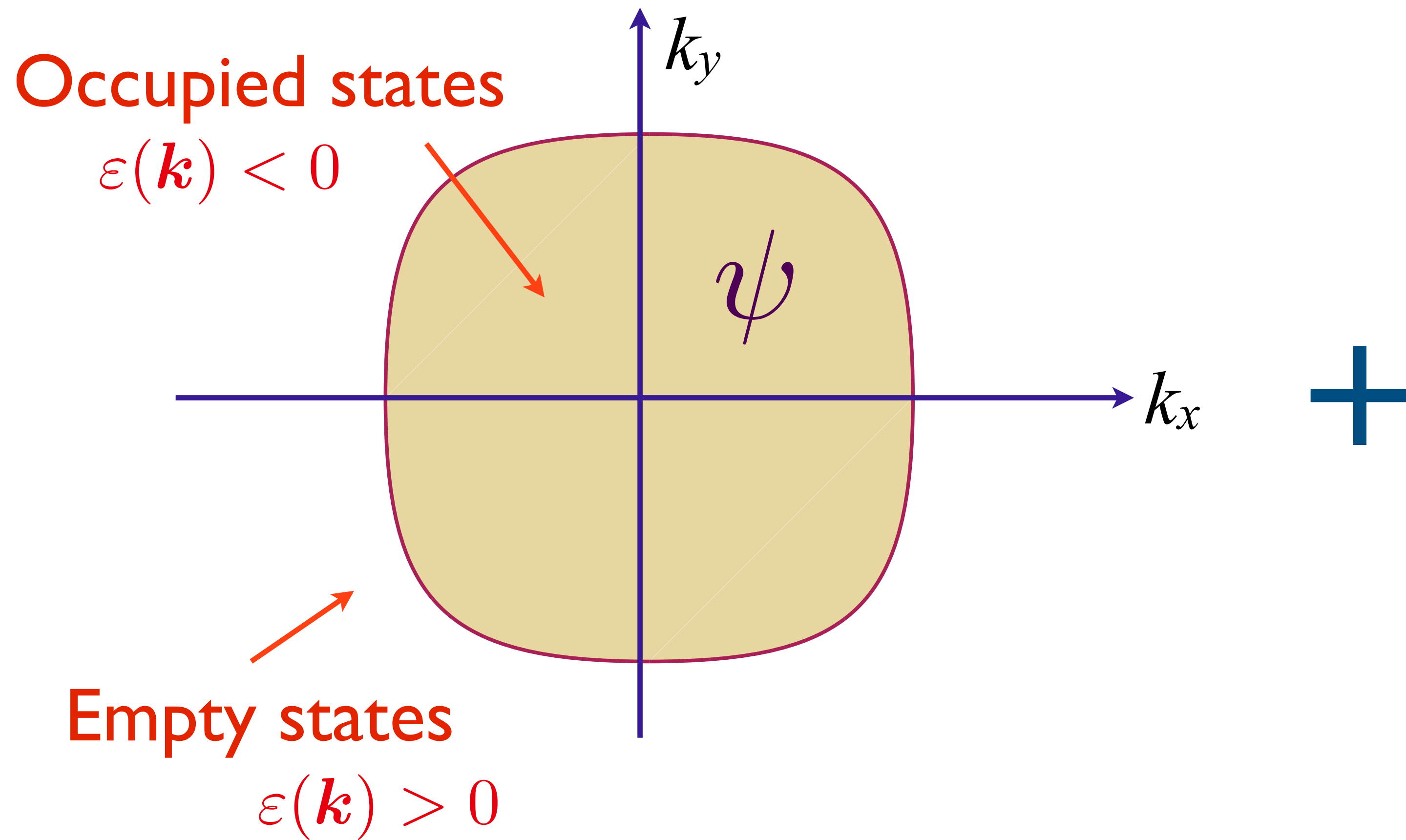


Same lower energy coarse-grained density of states in a model of interacting (fermionic) qubits with a discrete spectrum!



From the
SYK model
to
linear-T resistivity

Fermi surface coupled to a critical boson

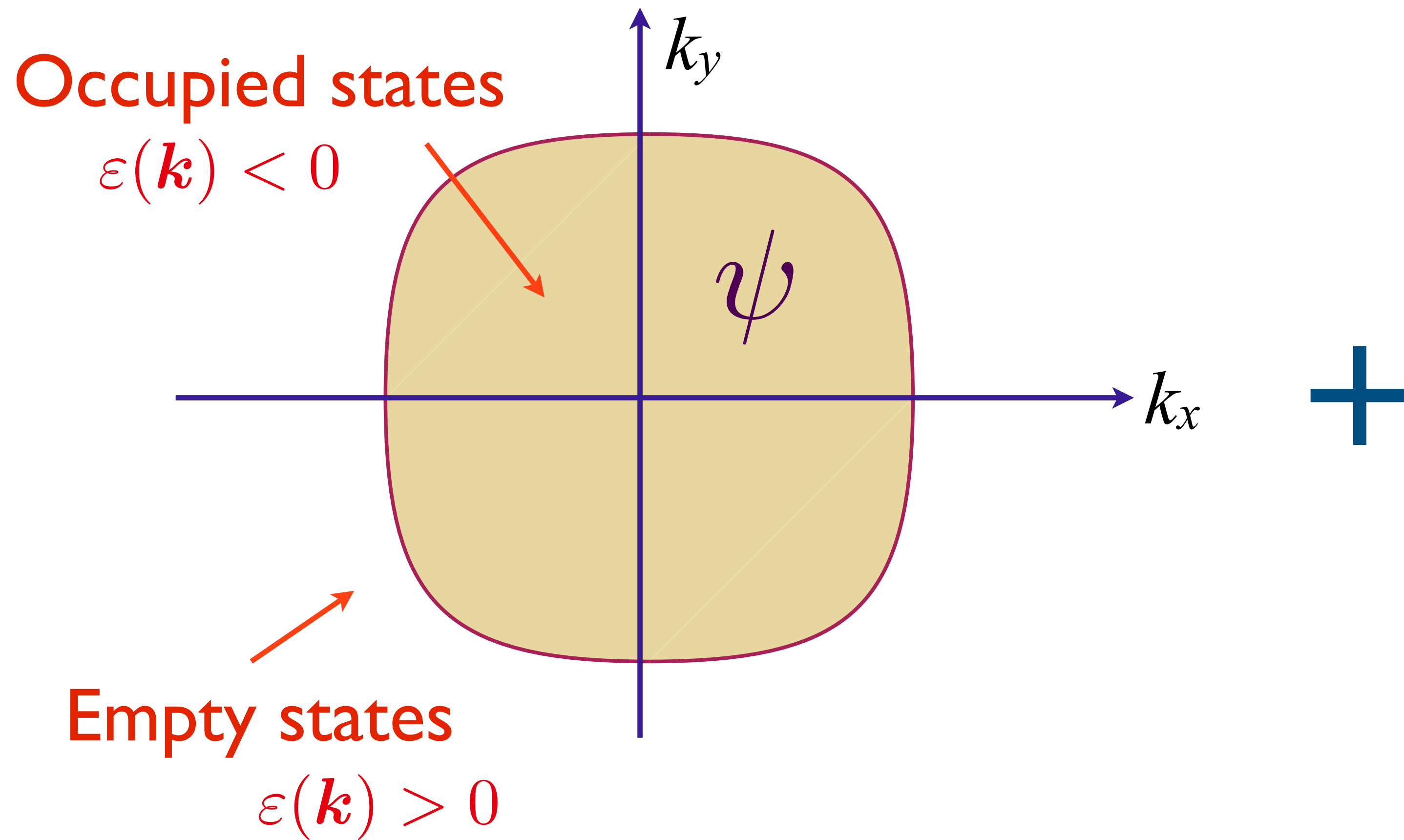


a critical boson

ϕ

- Nematic order
- Ferromagnetic order
- Transverse component of abelian or non-abelian gauge field

Fermi surface coupled to a critical boson



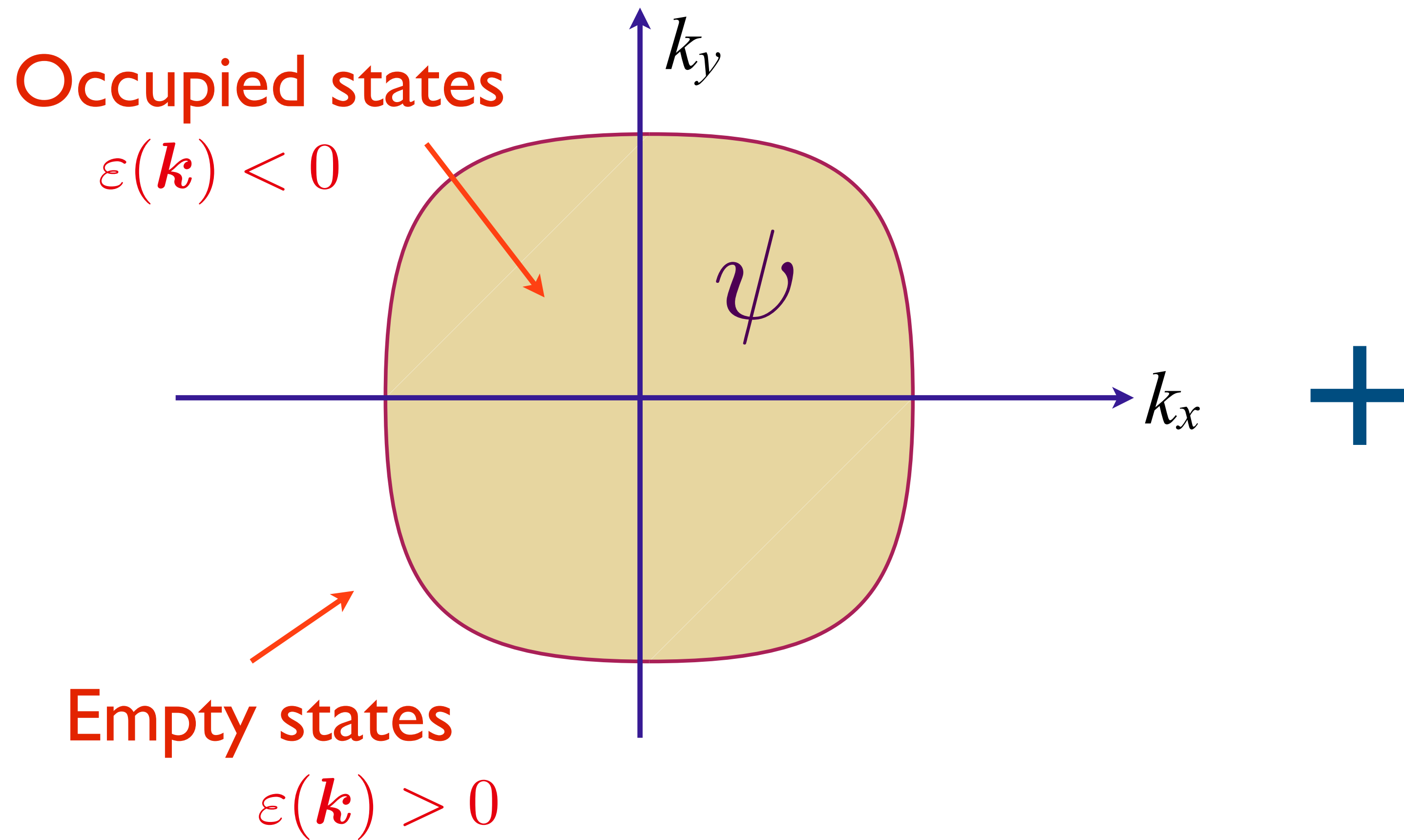
a critical boson

ϕ

- Nematic order
- Ferromagnetic order
- Transverse component of abelian or non-abelian gauge field

“Yukawa” coupling: $g \int d^2 r d\tau \psi^\dagger(r, \tau) \psi(r, \tau) \phi(r, \tau)$

Fermi surface coupled to a critical boson



a critical boson

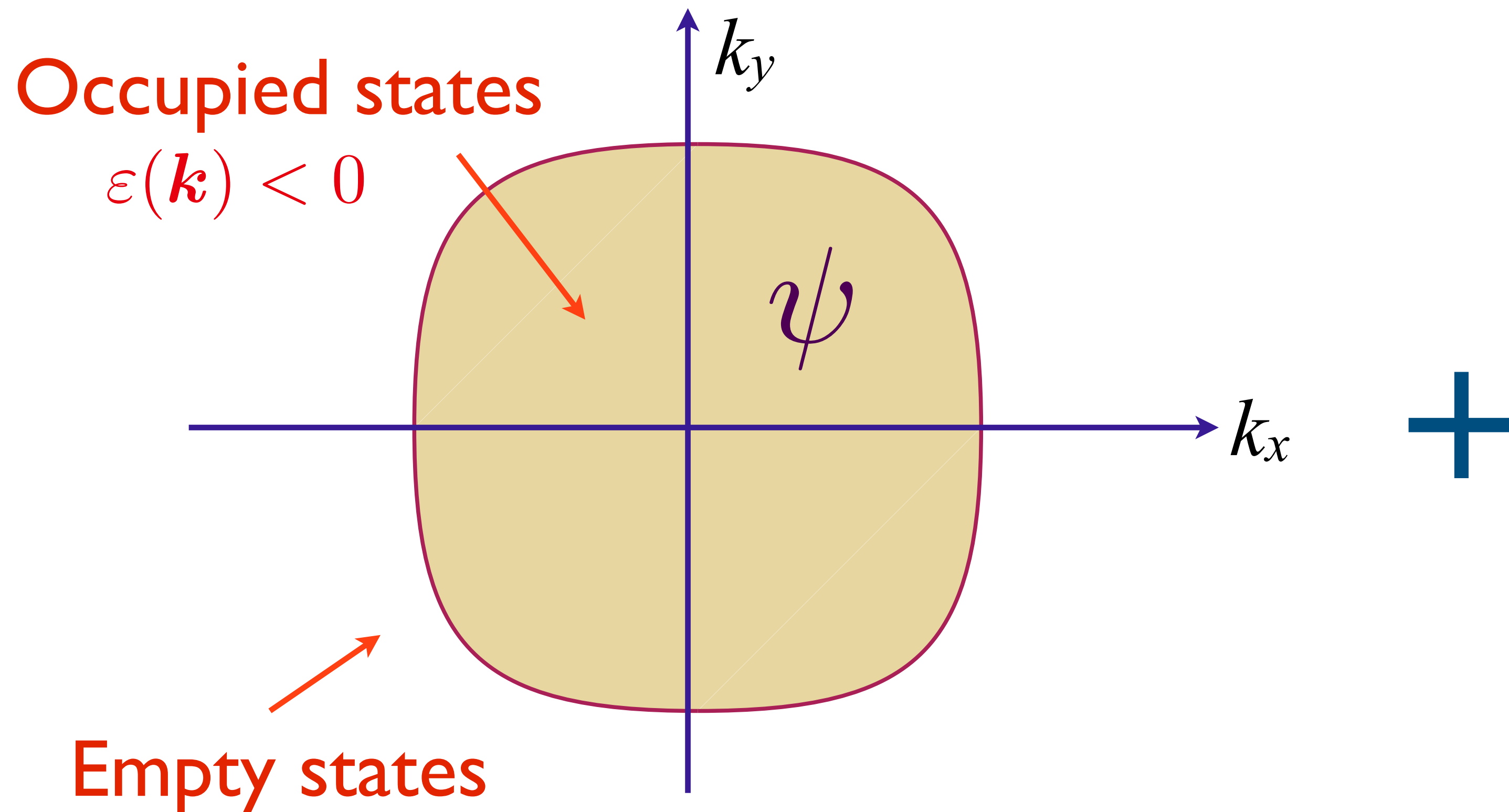
ϕ

- Nematic order
- Ferromagnetic order
- Transverse component of abelian or non-abelian gauge field

“Yukawa” coupling: $\frac{g_{ijl}}{N} \int d^2r d\tau \psi_i^\dagger(r, \tau) \psi_j(r, \tau) \phi_l(r, \tau)$

Random couplings in flavor space leads to large N theory of a strange metal, with zero resistivity

Fermi surface coupled to a critical boson



a critical boson

ϕ

- Nematic order
- Ferromagnetic order
- Transverse component of abelian or non-abelian gauge field

$$\int d^2r d\tau \left[\frac{g_{ijl}}{N} + \frac{g'_{ijl}(r)}{N} \right] \psi_i^\dagger(r, \tau) \psi_j(r, \tau) \phi_l(r, \tau)$$

Random couplings in flavor *and* position space leads to large N theory of a strange metal, with linear- T resistivity

Summary

- SYK: a solvable model without particle-like excitations, exhibiting thermalization and many-body chaos in a time of order $\hbar/(k_B T)$, independent of microscopic energy scales.

Summary

- SYK: a solvable model without particle-like excitations, exhibiting thermalization and many-body chaos in a time of order $\hbar/(k_B T)$, independent of microscopic energy scales.
- Low energy theory of time reparameterizations is the theory of the boundary graviton in 1+1 dimensional quantum gravity on AdS_2 .

Summary

- The semiclassical entropy of Einstein gravity is reproduced by a unitary quantum system with a discrete spectrum. Further work along these lines has led to progress on the Page curve describing the time evolution of the entropy of an evaporating black hole.



Summary

- The semiclassical entropy of Einstein gravity is reproduced by a unitary quantum system with a discrete spectrum. Further work along these lines has led to progress on the Page curve describing the time evolution of the entropy of an evaporating black hole.
- Linear- T resistivity arises from spatially random interactions in a two-dimensional quantum-critical metal.

