

The quantum phases of matter

Physics Training and Talent Search
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INSTITUTE FOR
ADVANCED STUDY

PHYSICS



HARVARD

Talk online: sachdev.physics.harvard.edu

1. “Conventional” phases of matter

Metals, insulators, superconductors

2. Emergent gauge fields and topology

Spin liquids with Rydberg atoms

3. Strange metals

SYK model and emergent gravity

1. “Conventional” phases of matter

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Ordinary metals

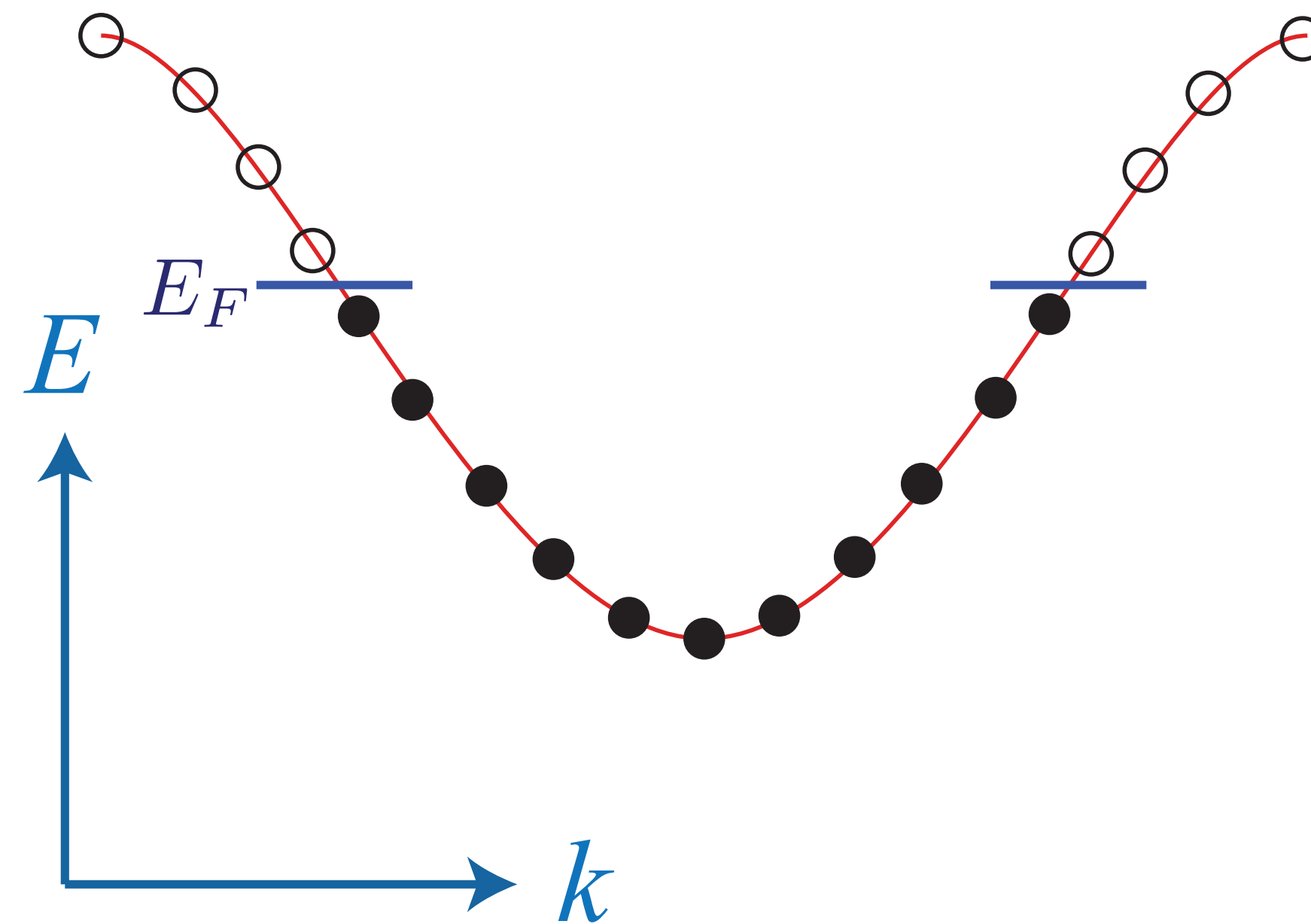


Ordinary metals are shiny, and they conduct heat and electricity efficiently. Each atom donates electrons which are delocalized throughout the entire crystal

Foundations of quantum many body theory:

I. Ground states connected adiabatically to independent electron states

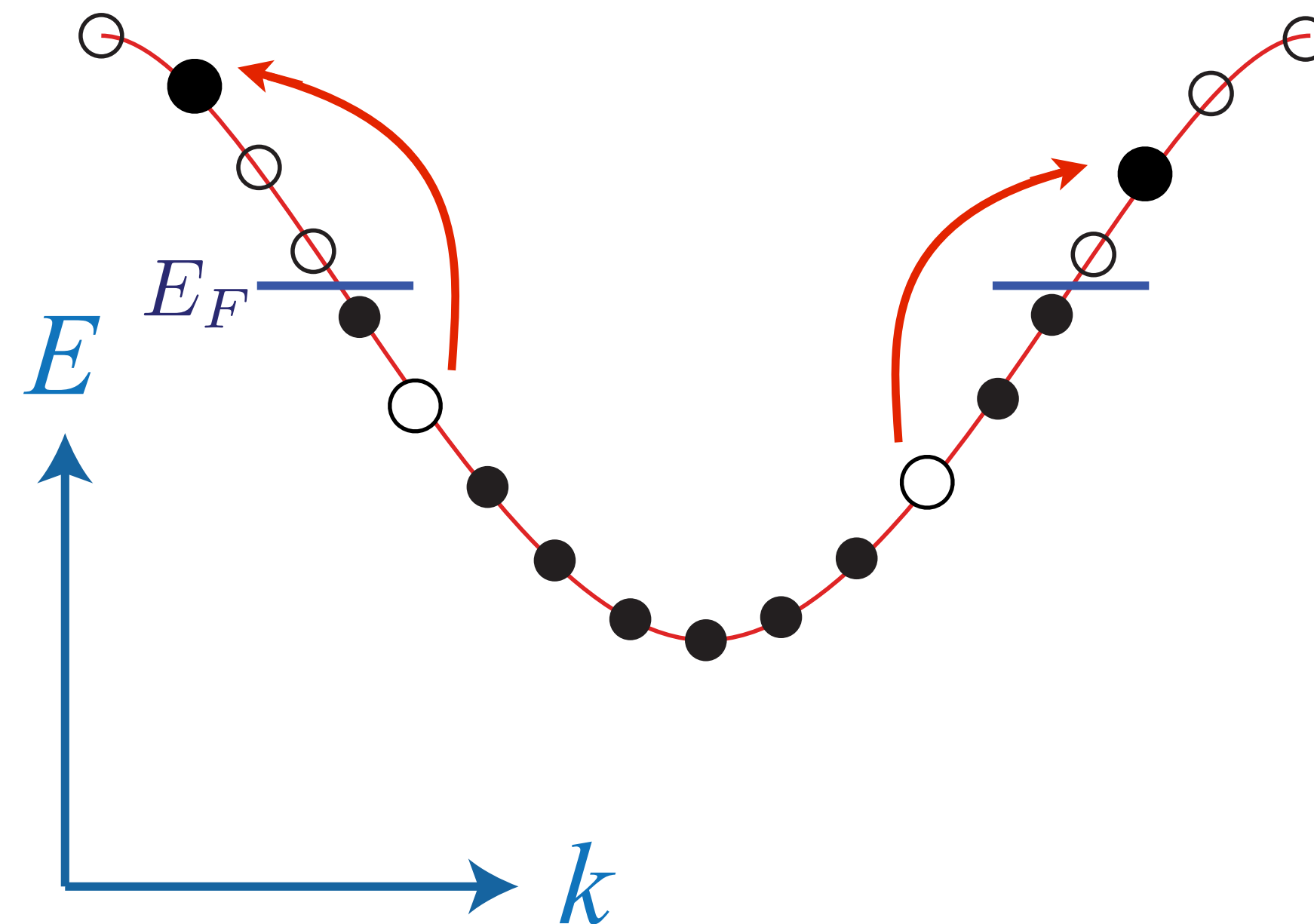
Metals



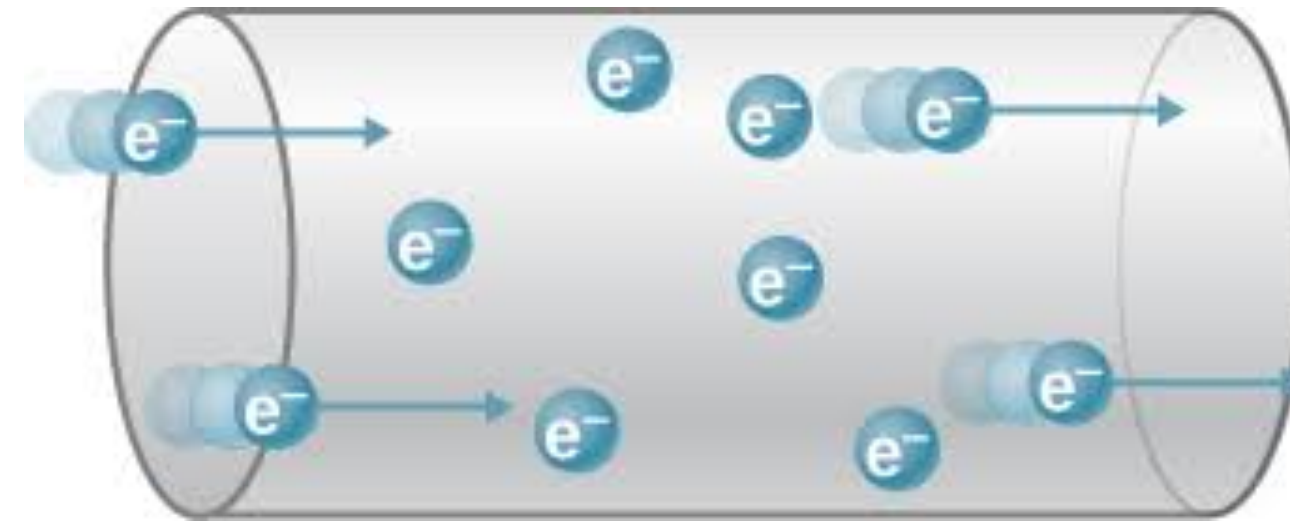
Foundations of quantum many body theory:

1. Ground states connected adiabatically to independent electron states
2. Boltzmann-Landau theory of quasiparticles

Metals



Current flow with quasiparticles

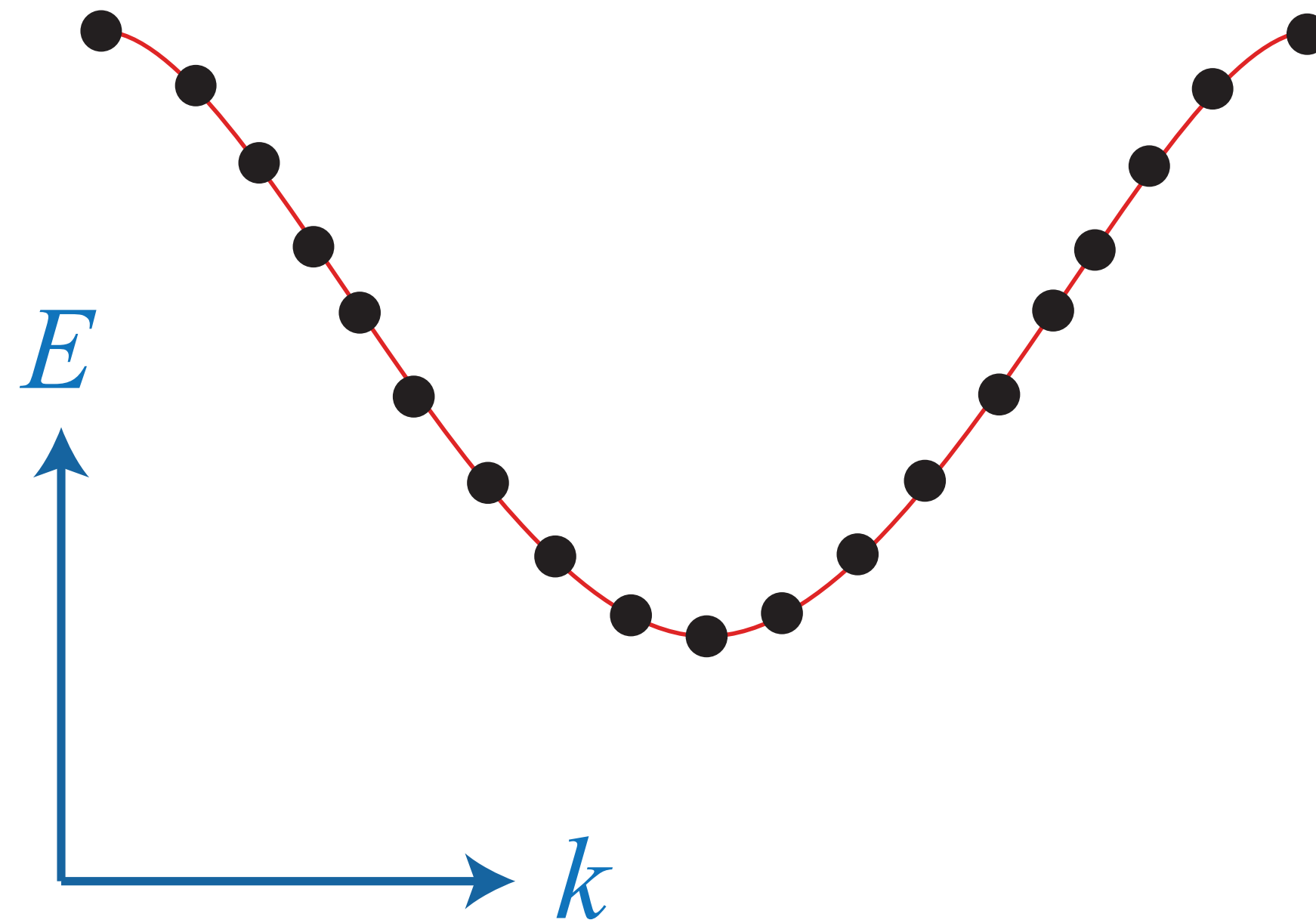


Flowing quasiparticles scatter off each other in a typical scattering time τ

This time is much longer than a limiting
'Planckian time' $\frac{\hbar}{k_B T}$.

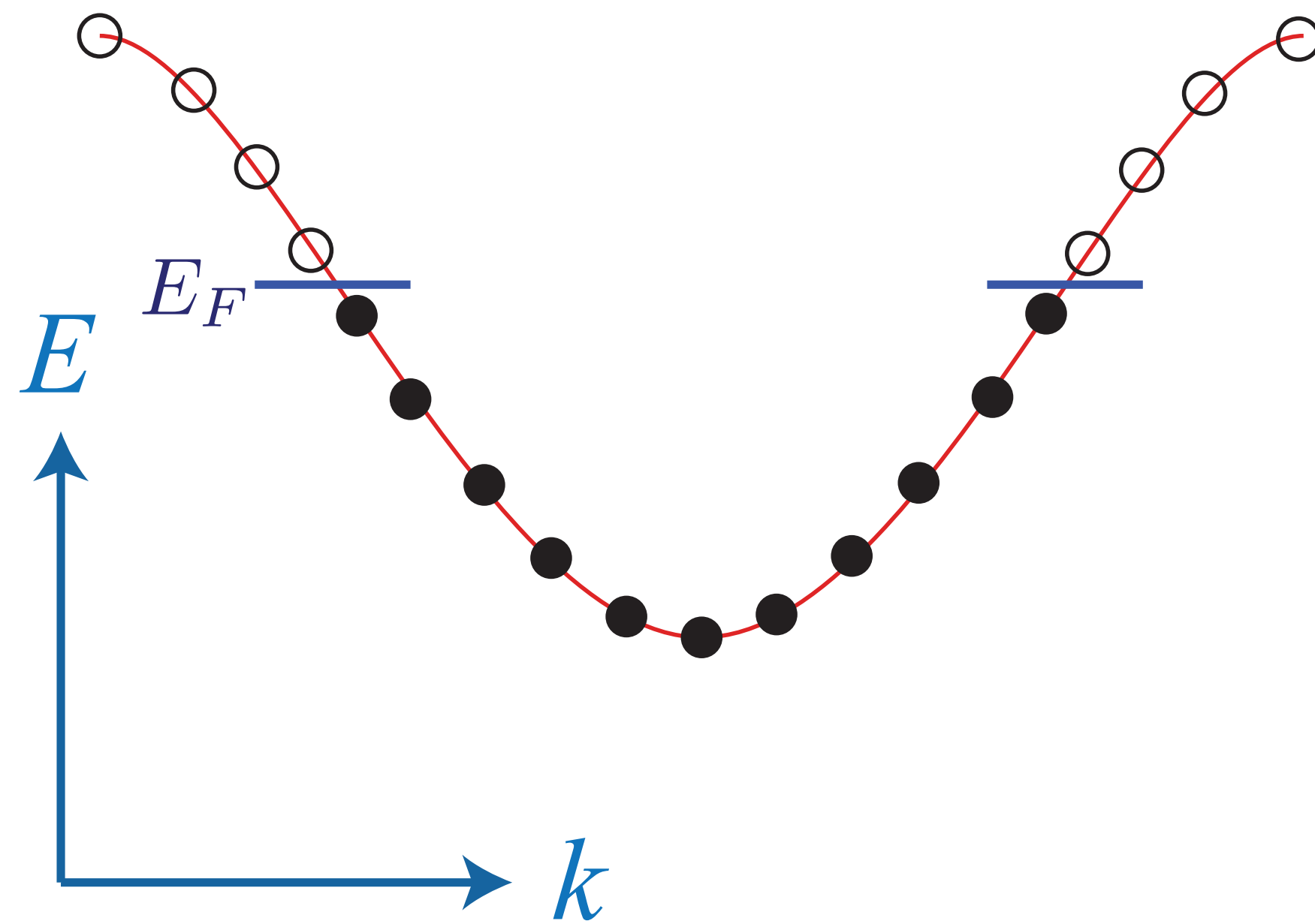
The long scattering time implies that quasiparticles are well-defined.

Band insulators

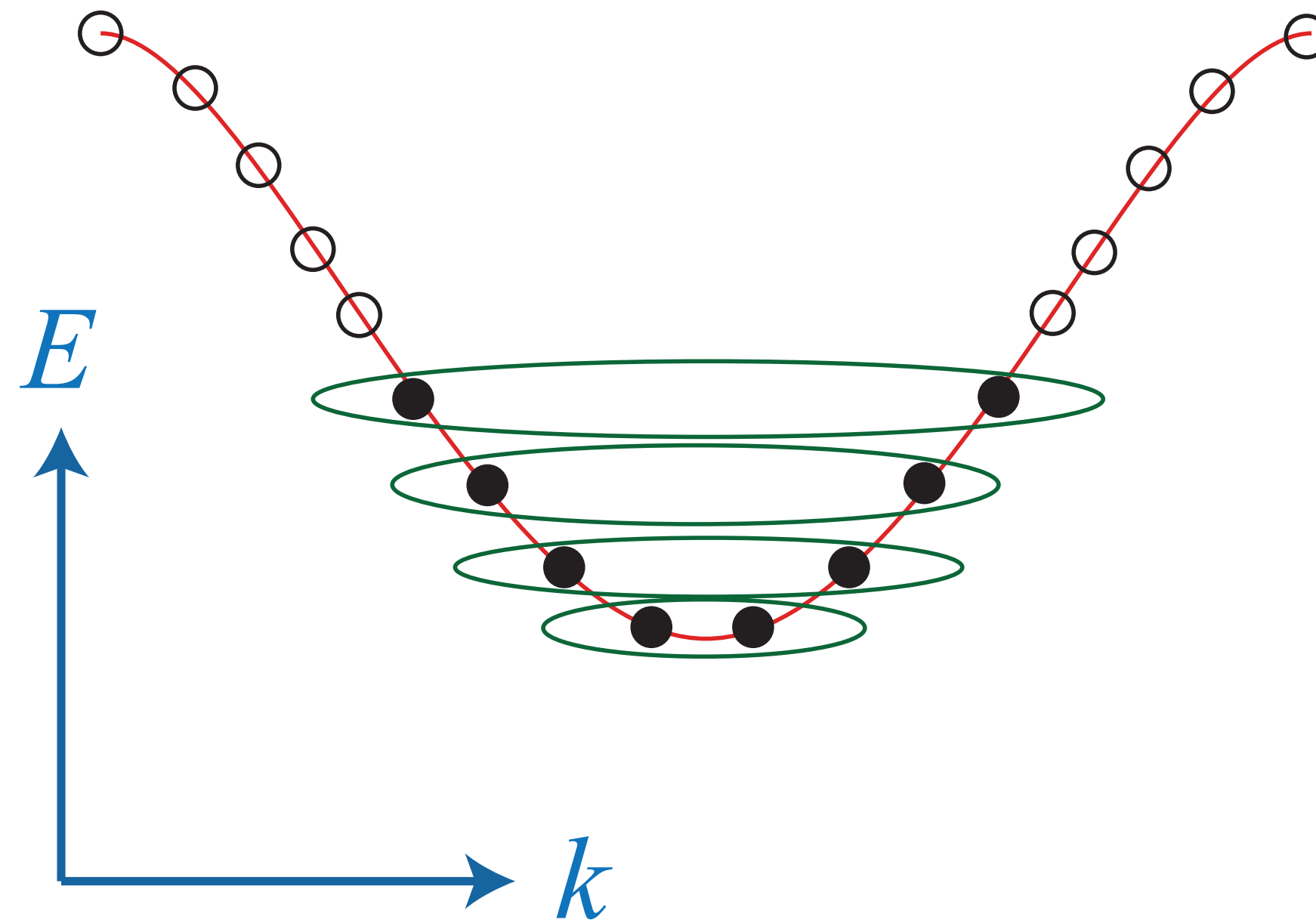


An even number of electrons per unit cell

Metals

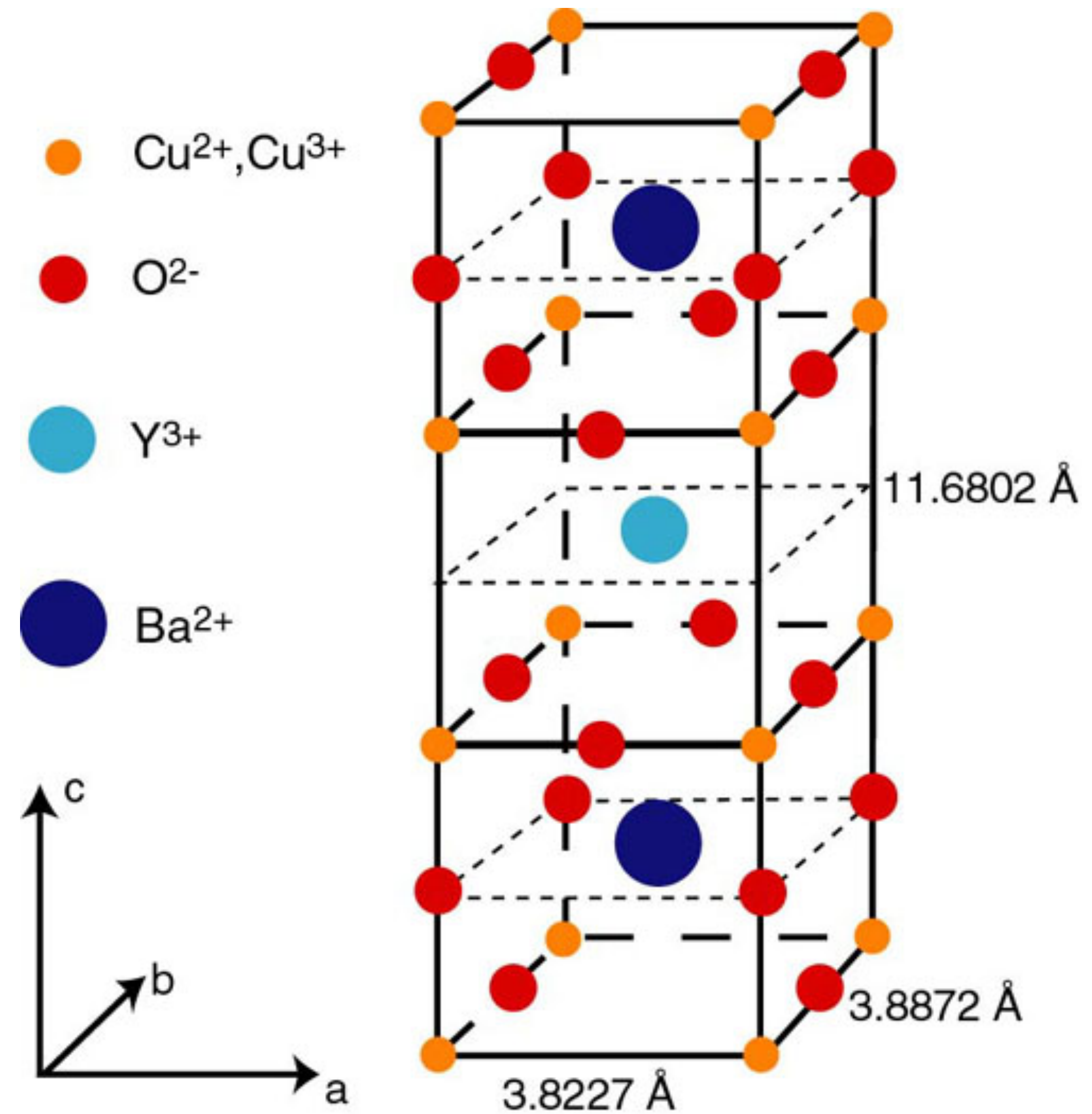


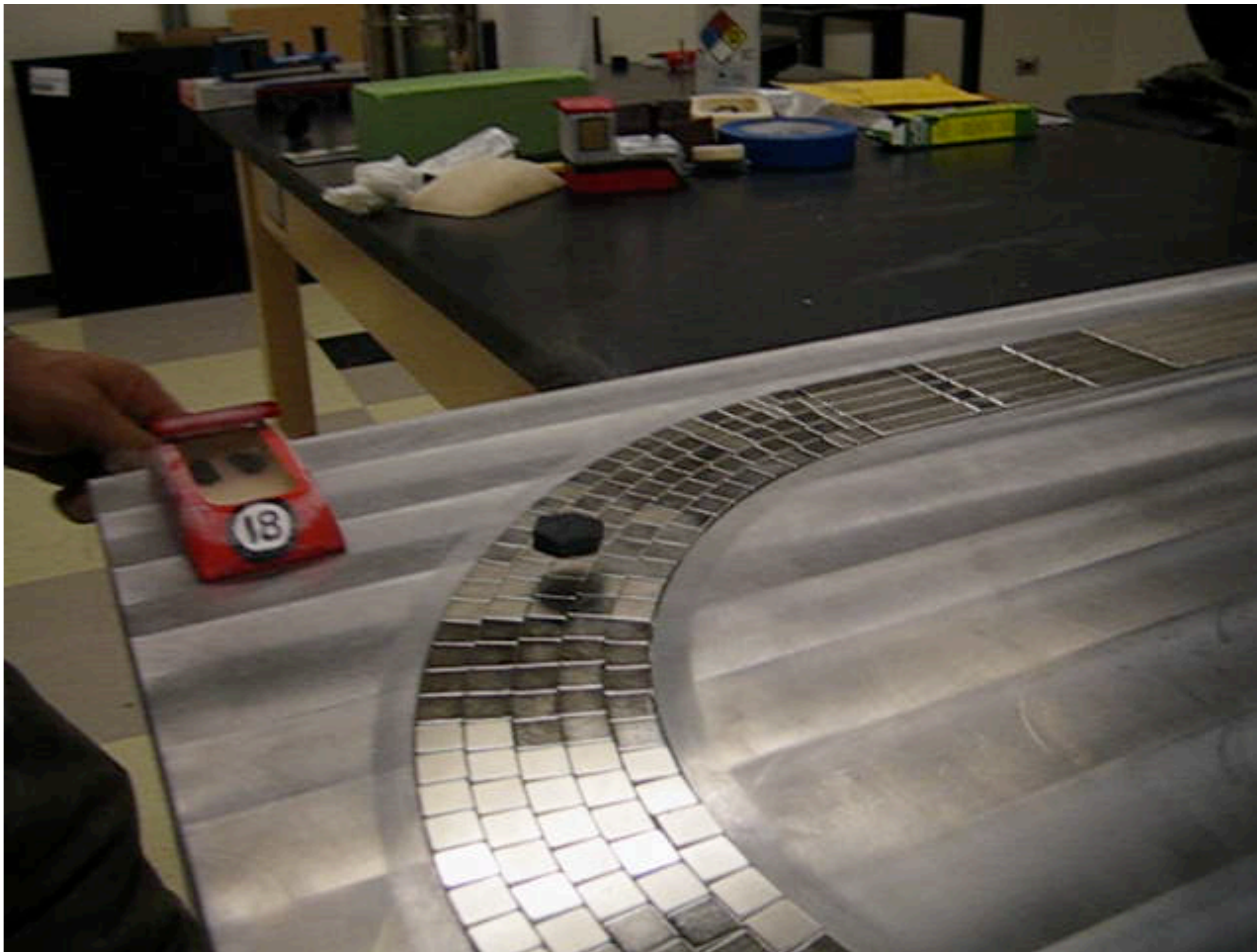
Superconductor



Electrons pair, and the pairs undergo Bose-Einstein condensation

High temperature superconductors





Nd-Fe-B magnets, YBaCuO superconductor

Julian Hetel and Nandini Trivedi, Ohio State University

1. “Conventional” phases of matter

Metals, insulators, superconductors

2. Emergent gauge fields and topology

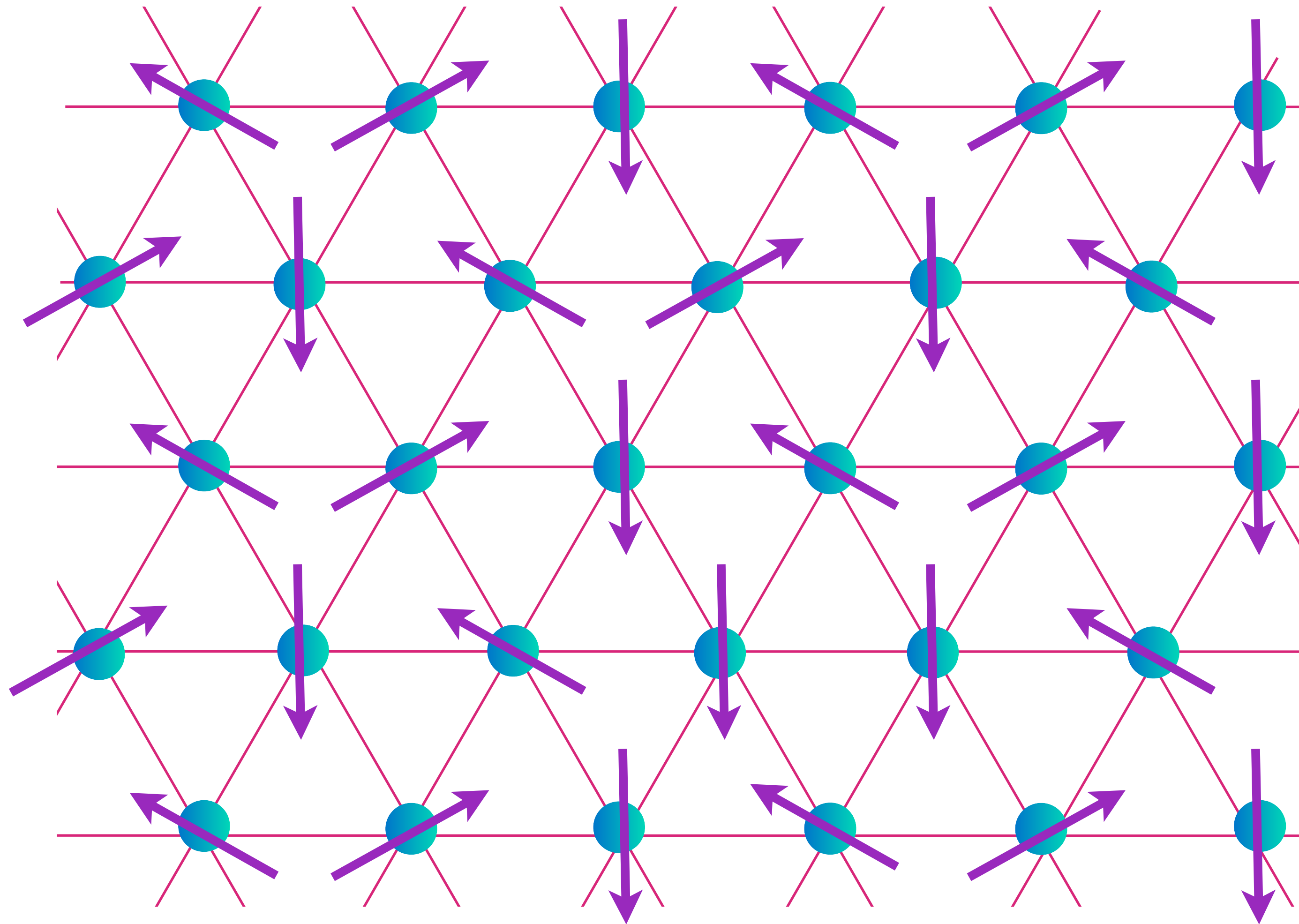
Spin liquids with Rydberg atoms

3. Strange metals

SYK model and emergent gravity

Mott insulator: Triangular lattice antiferromagnet

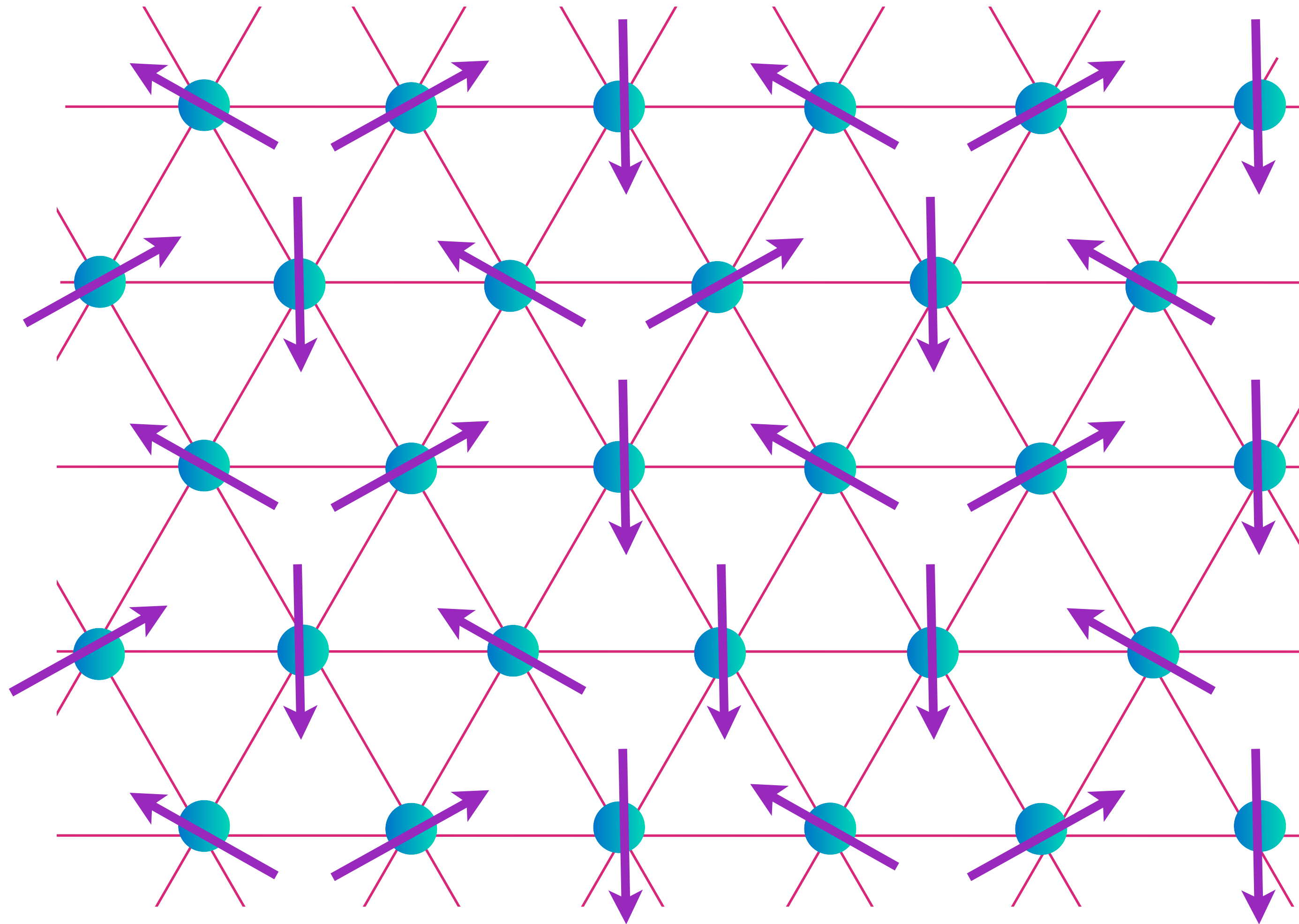
$$H = J \sum_{\langle ij \rangle} \vec{S}_i \cdot \vec{S}_j$$



Nearest-neighbor model has non-collinear Neel order

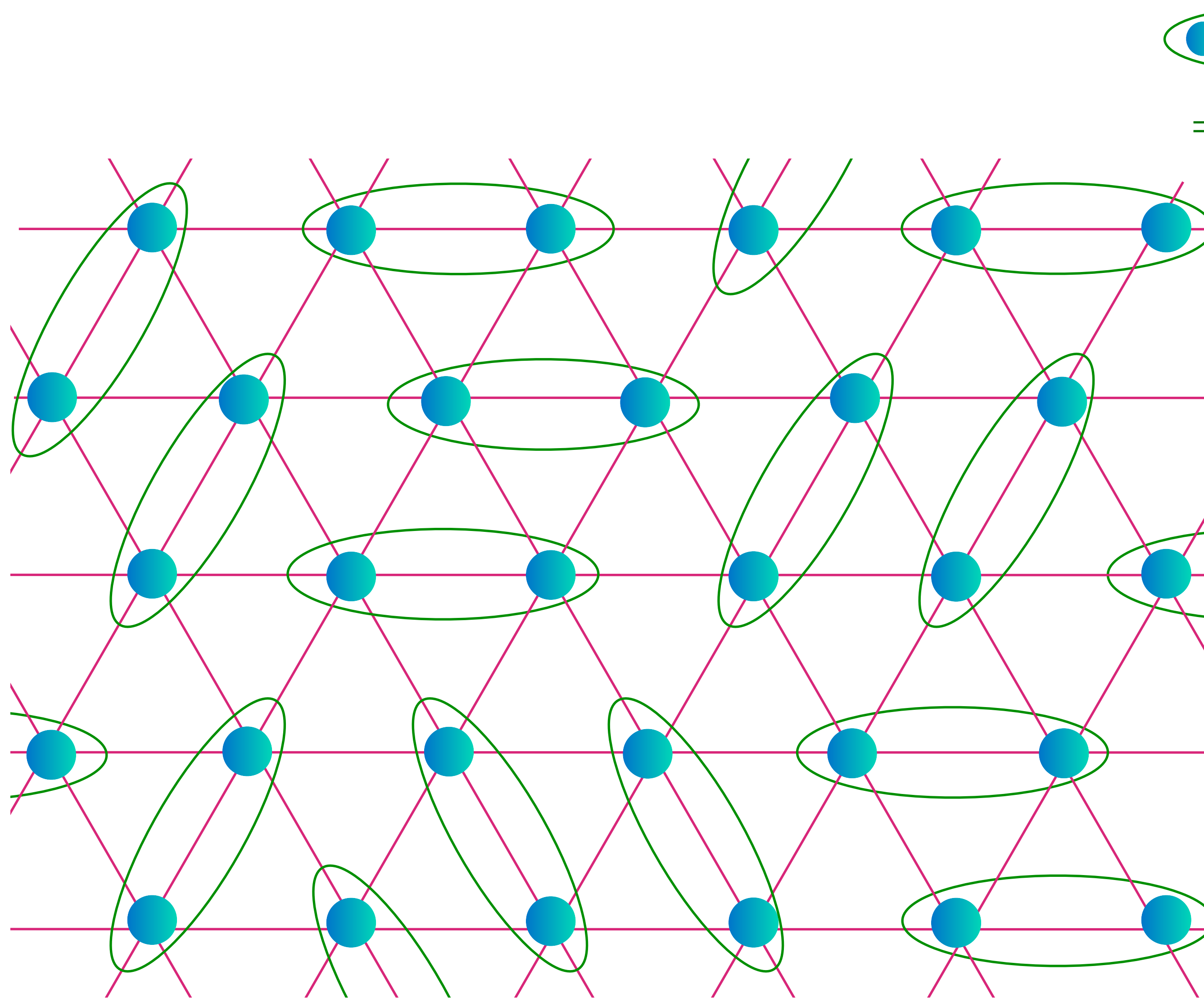
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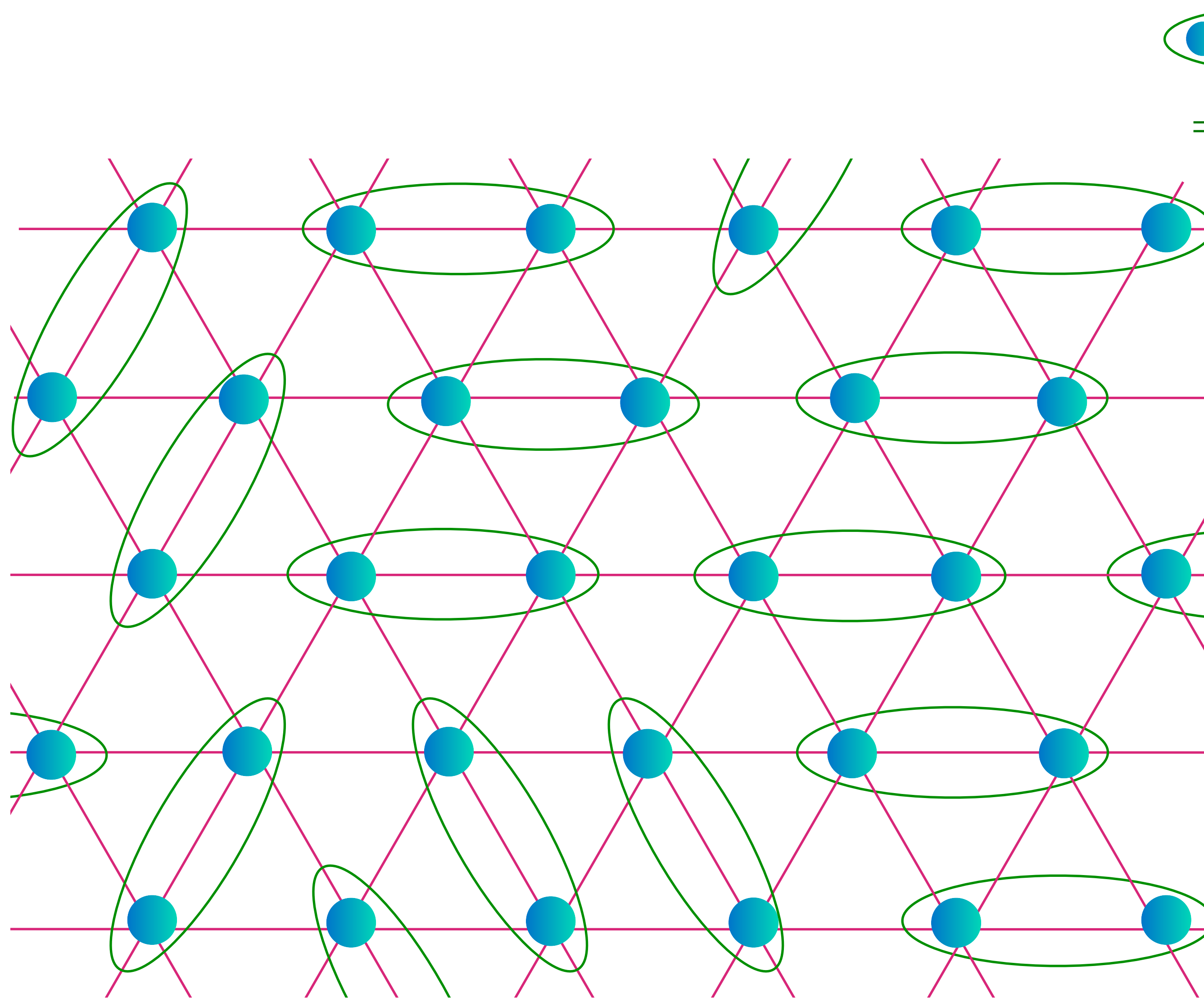


$$\begin{array}{c} \text{○} \quad \text{○} \\ = \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) \end{array}$$

$$|G\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} |\mathcal{D}\rangle$$

$\mathcal{D} \rightarrow$ dimer covering
of lattice

Mott insulator: Triangular lattice antiferromagnet

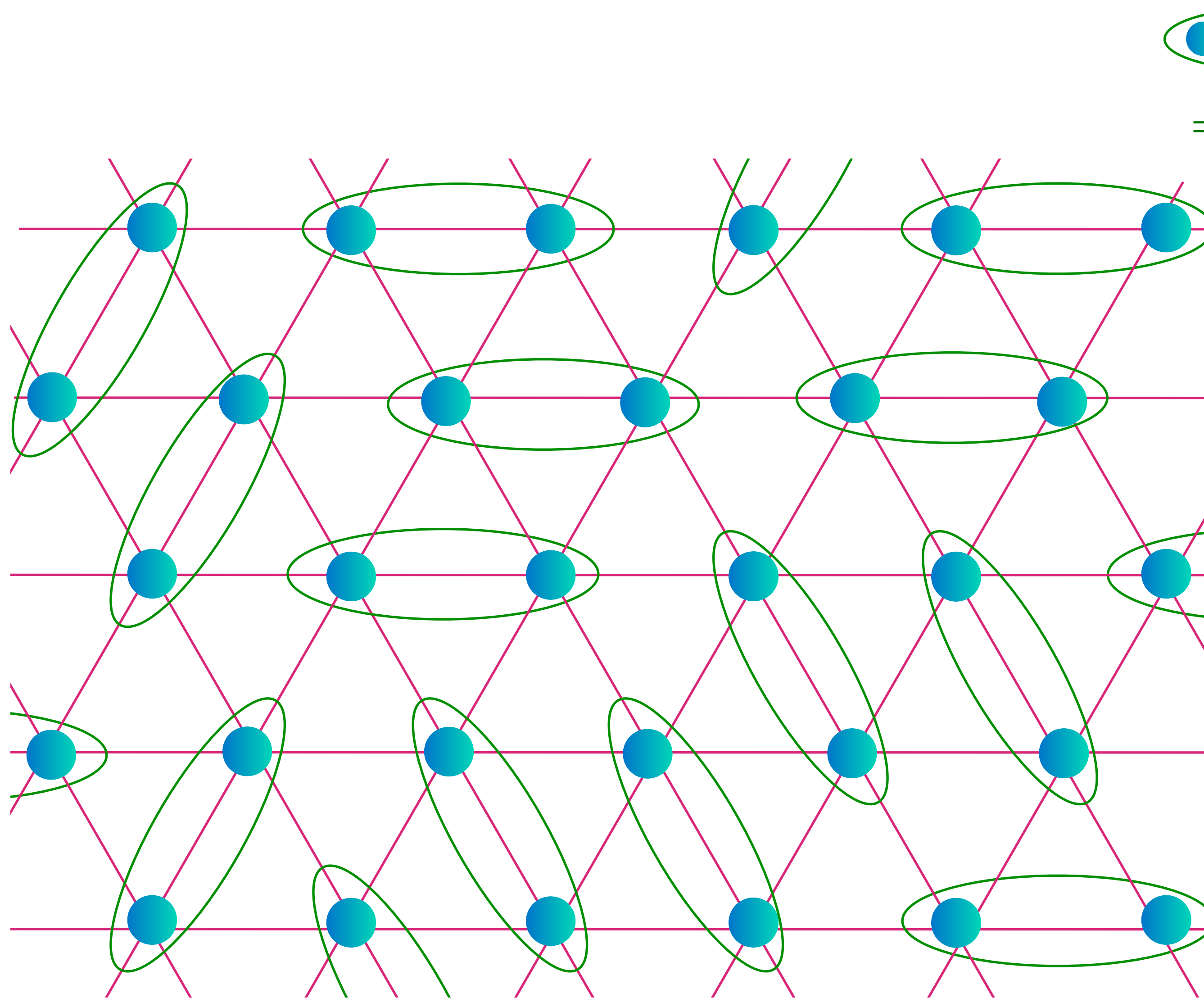


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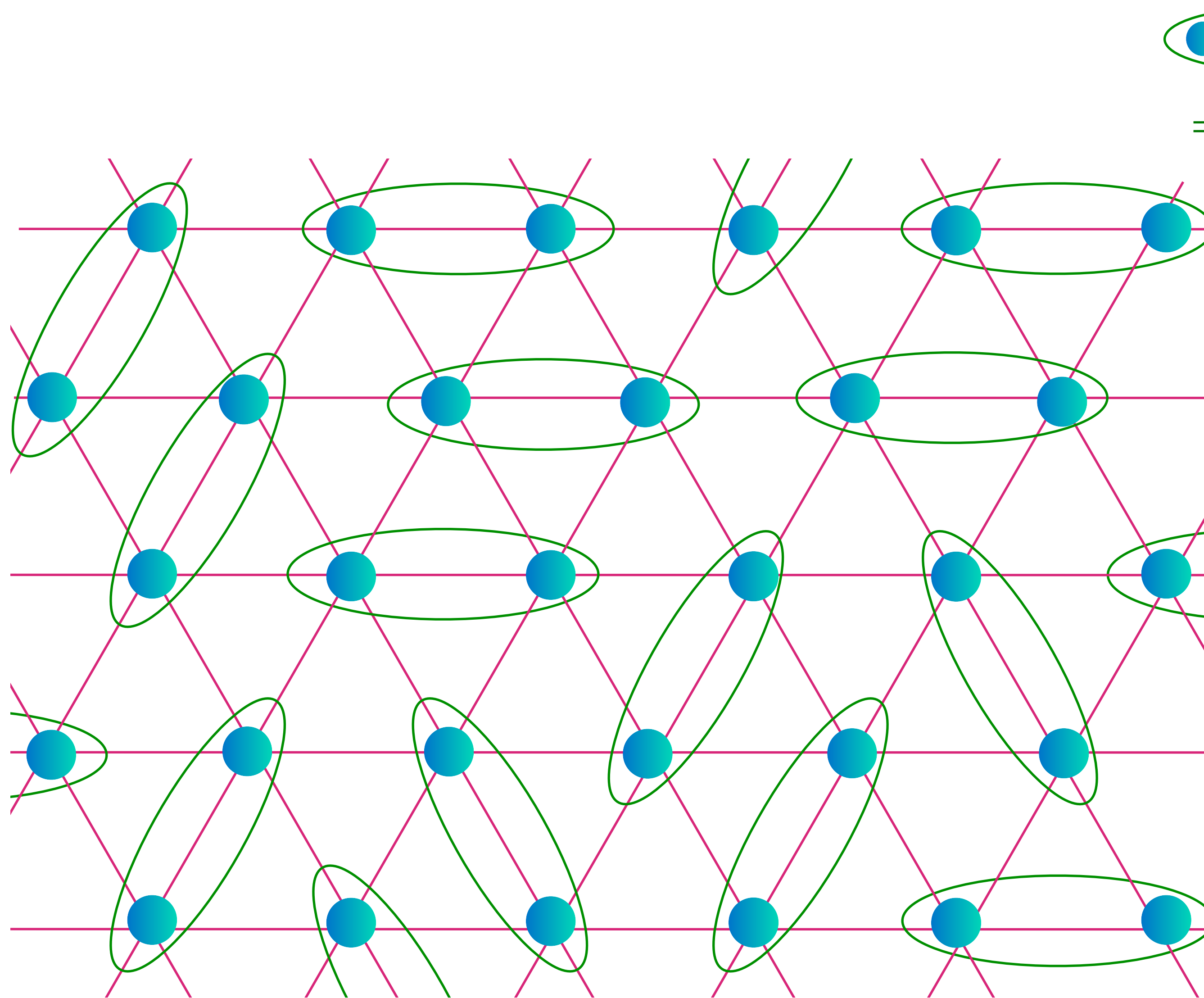


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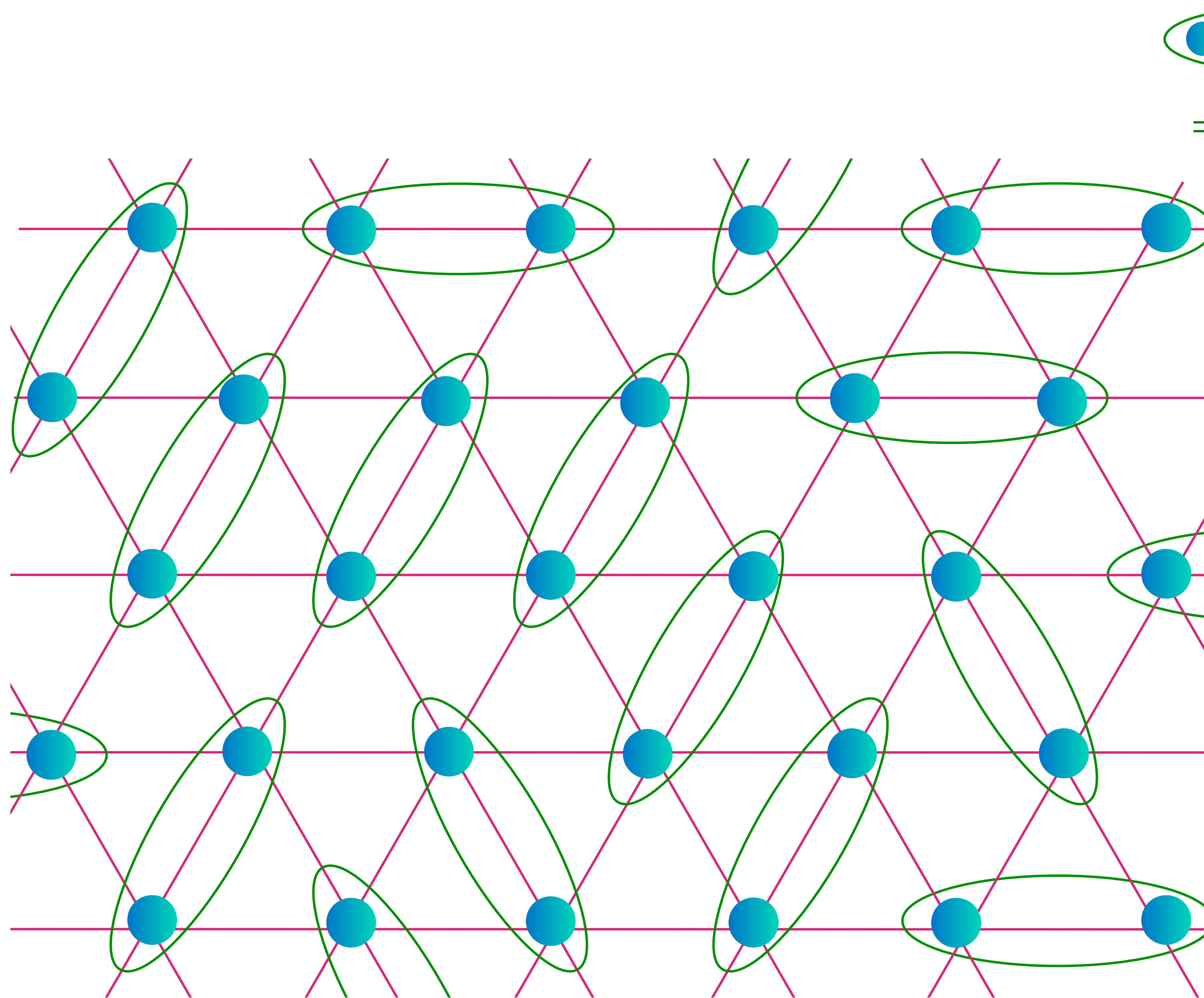


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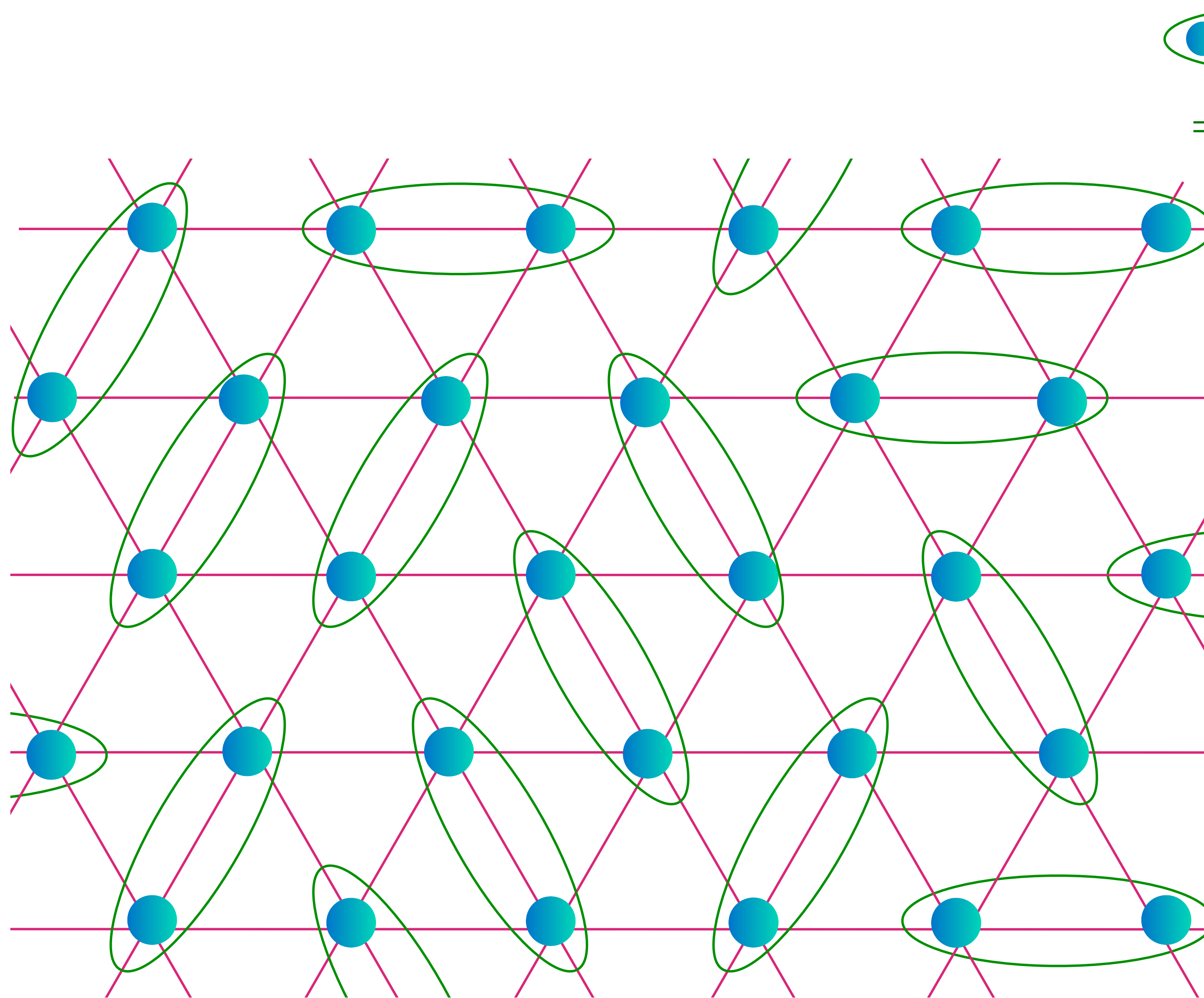


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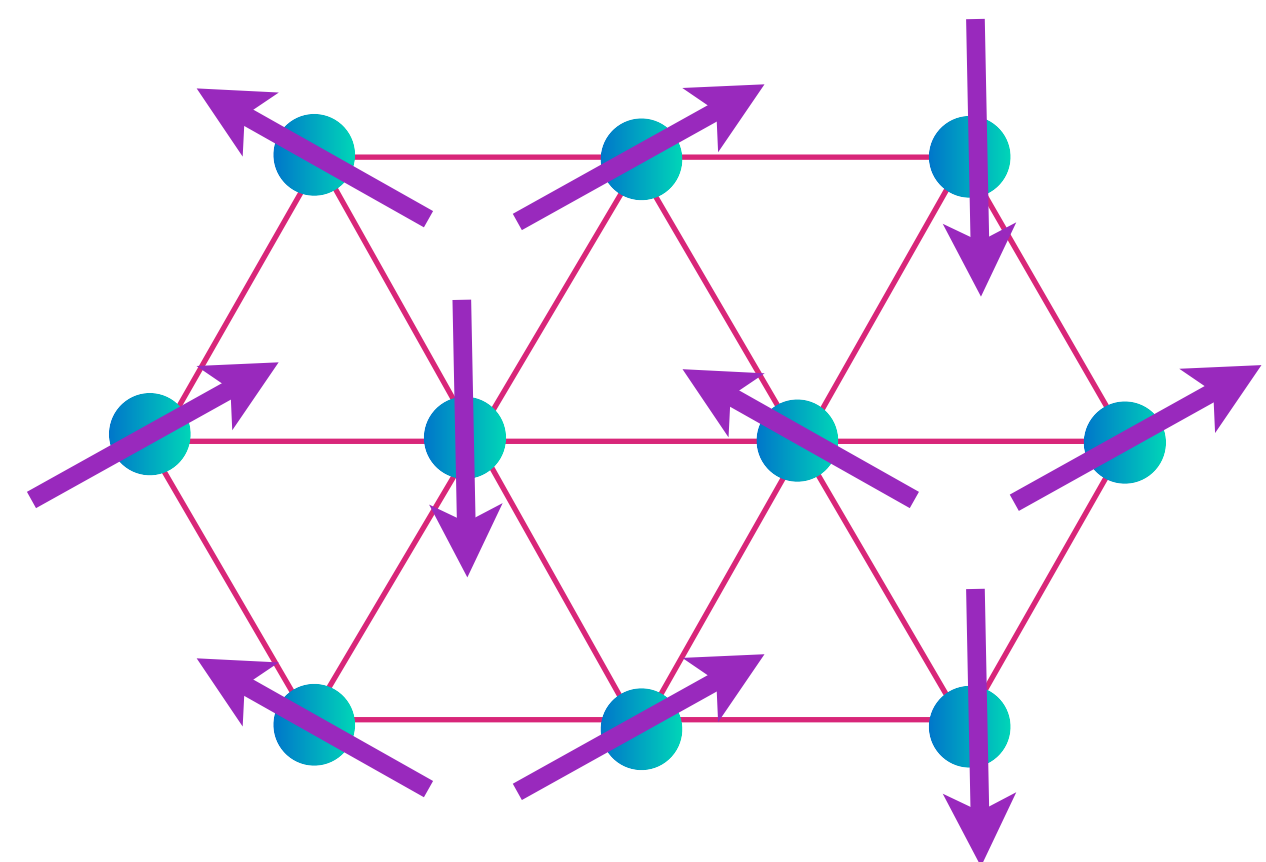


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Mott insulator: Triangular lattice antiferromagnet



non-collinear Néel state

Z_2 spin liquid
with neutral $S = 1/2$ spinons
and **vison** excitations

S_c

S

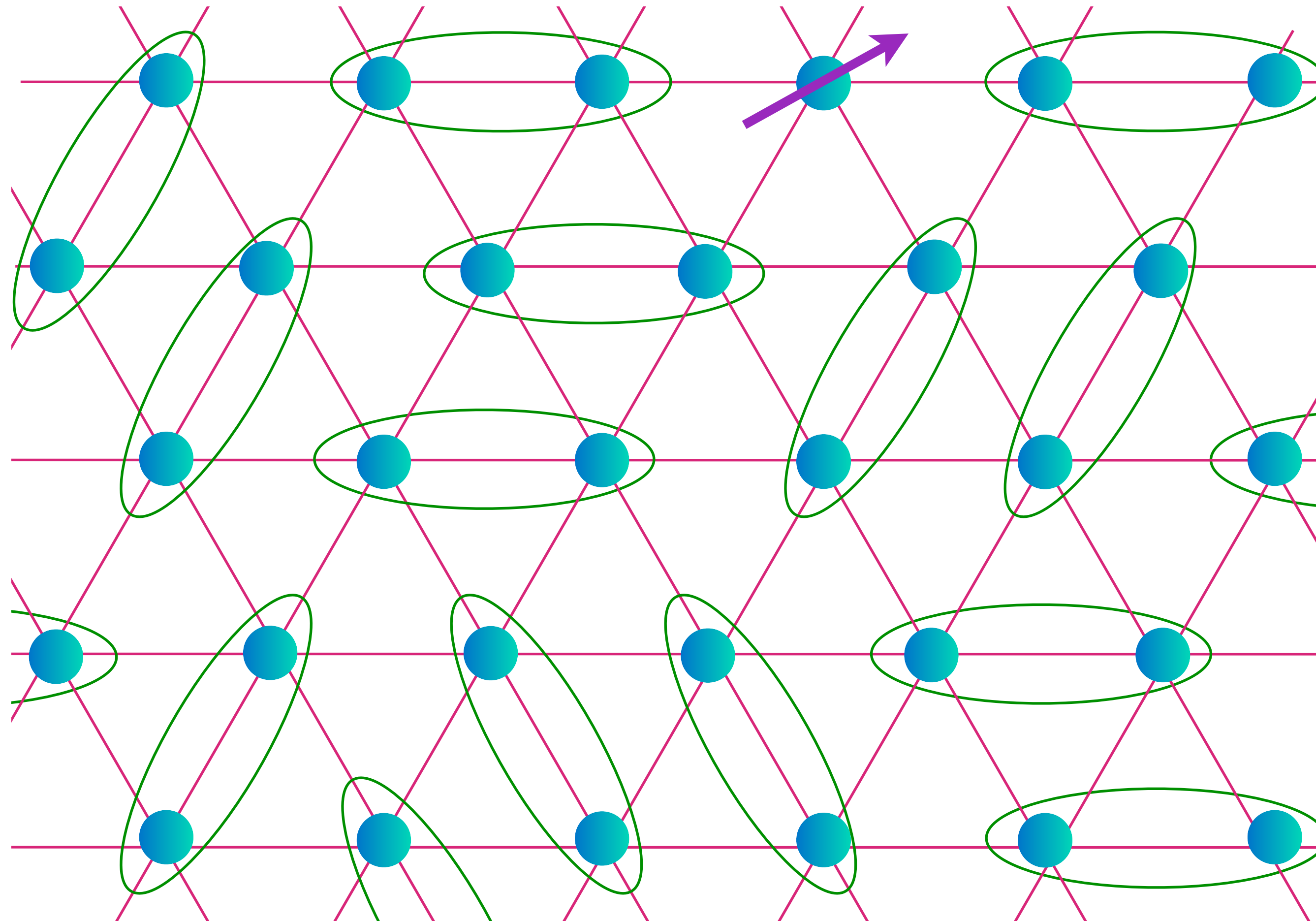
N. Read and S. Sachdev, *Phys. Rev. Lett.* **66**, 1773 (1991)
X.-G. Wen, *Phys. Rev. B* **44**, 2664 (1991)

Excitations of the Z_2 Spin liquid

Spinon: $S_z = 1/2$

e (boson) or ϵ (fermion) particle

$$\begin{array}{c} \text{---} \circ \text{---} \circ \text{---} \\ \text{---} \end{array} = \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$

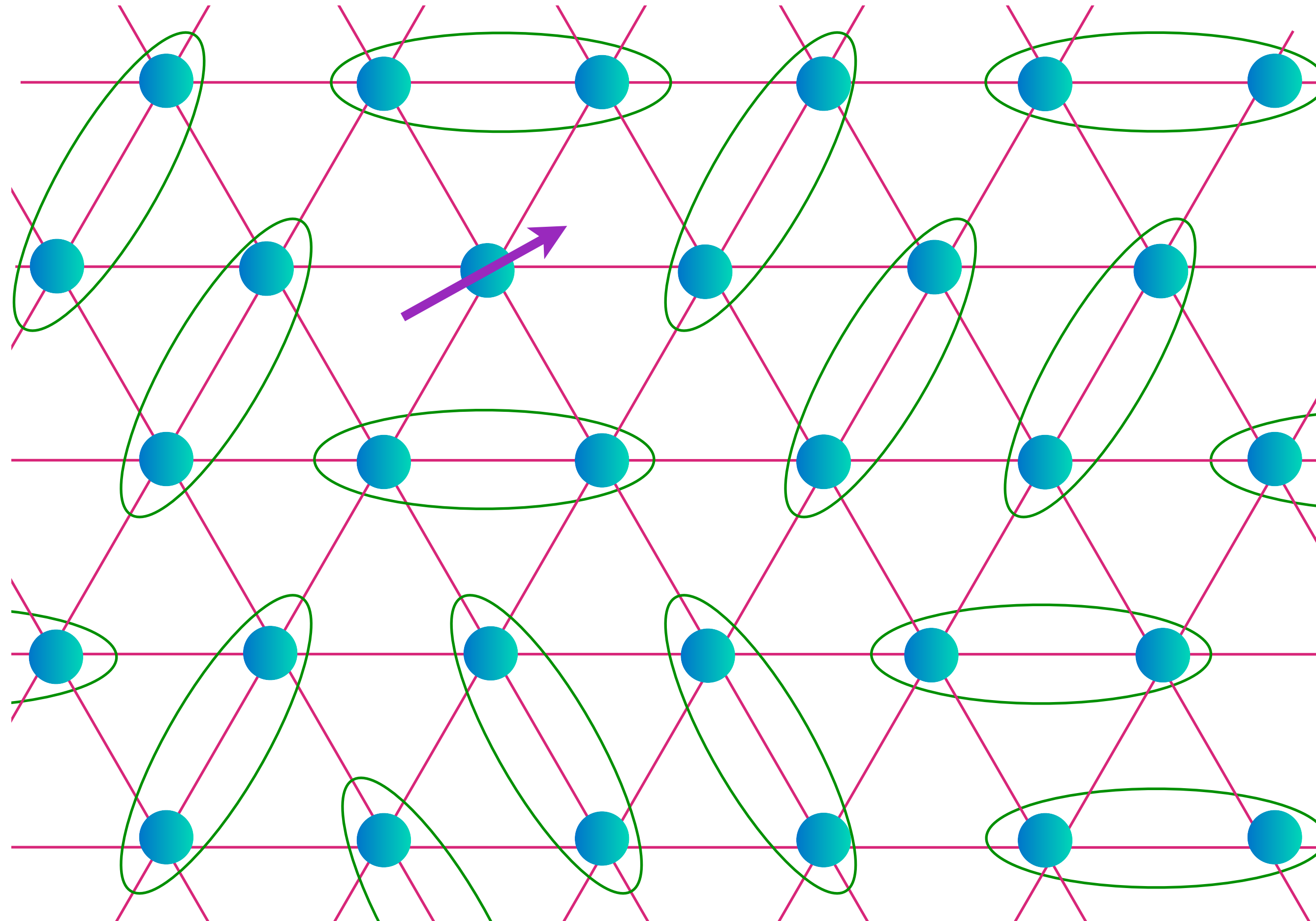


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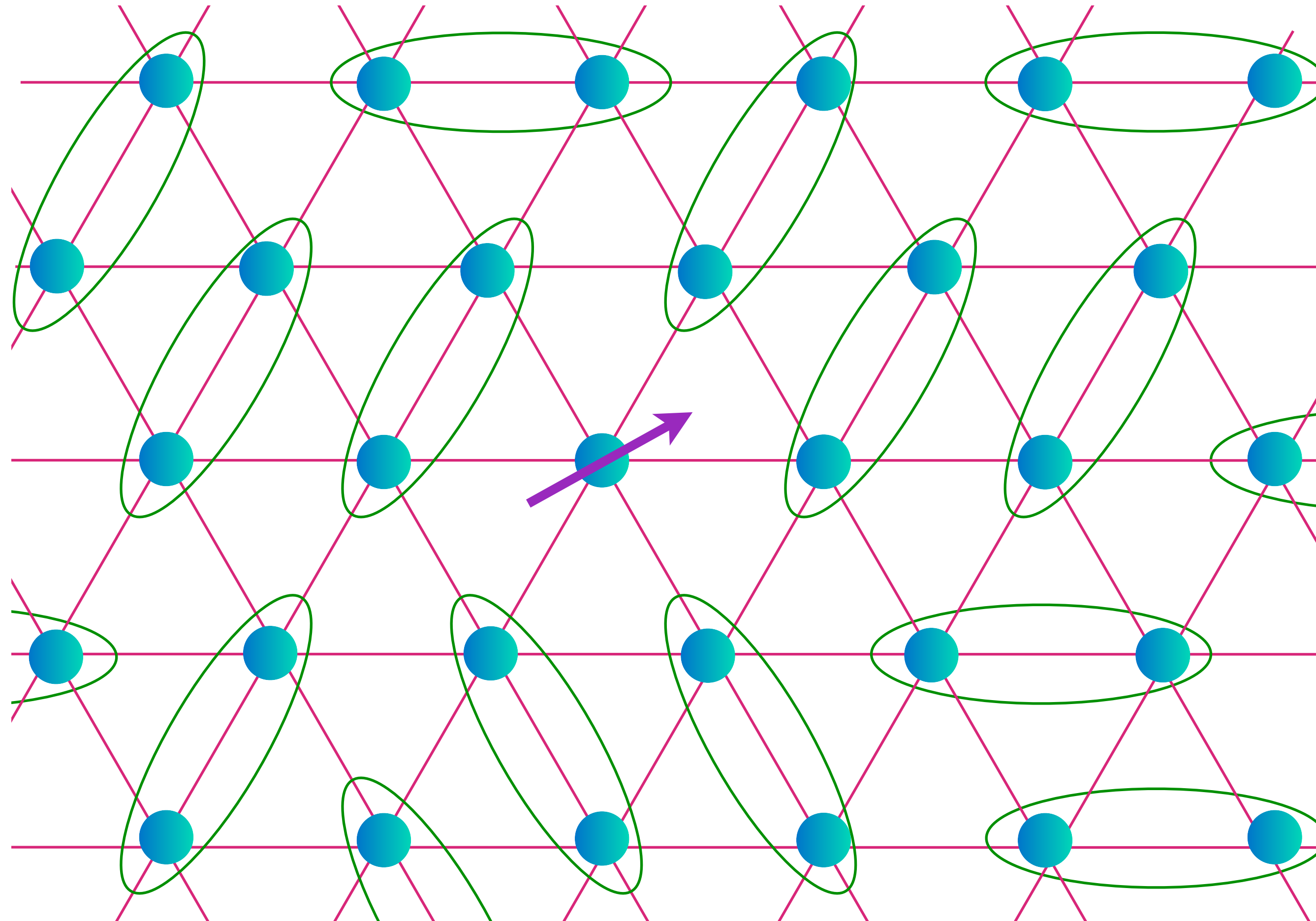


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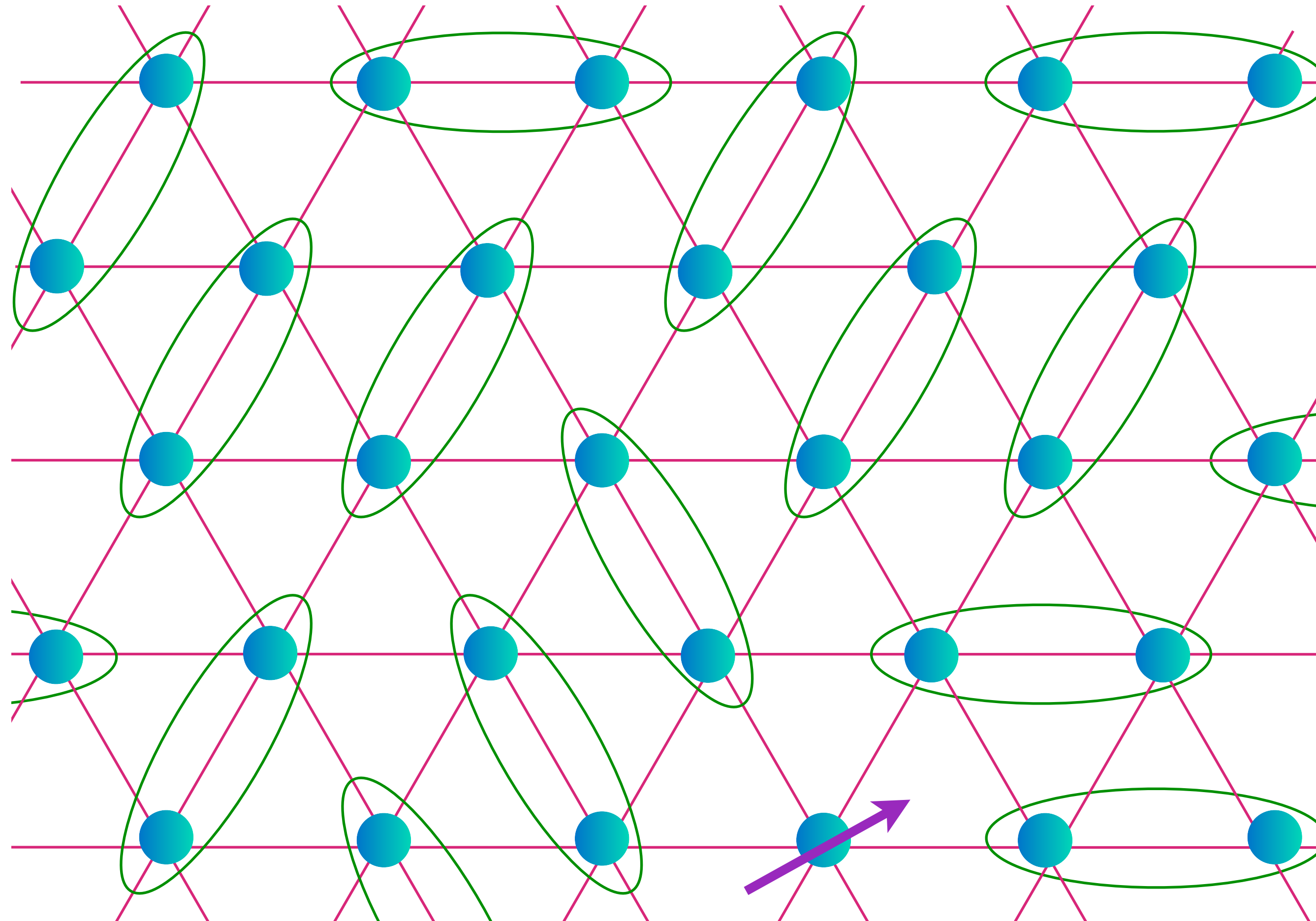


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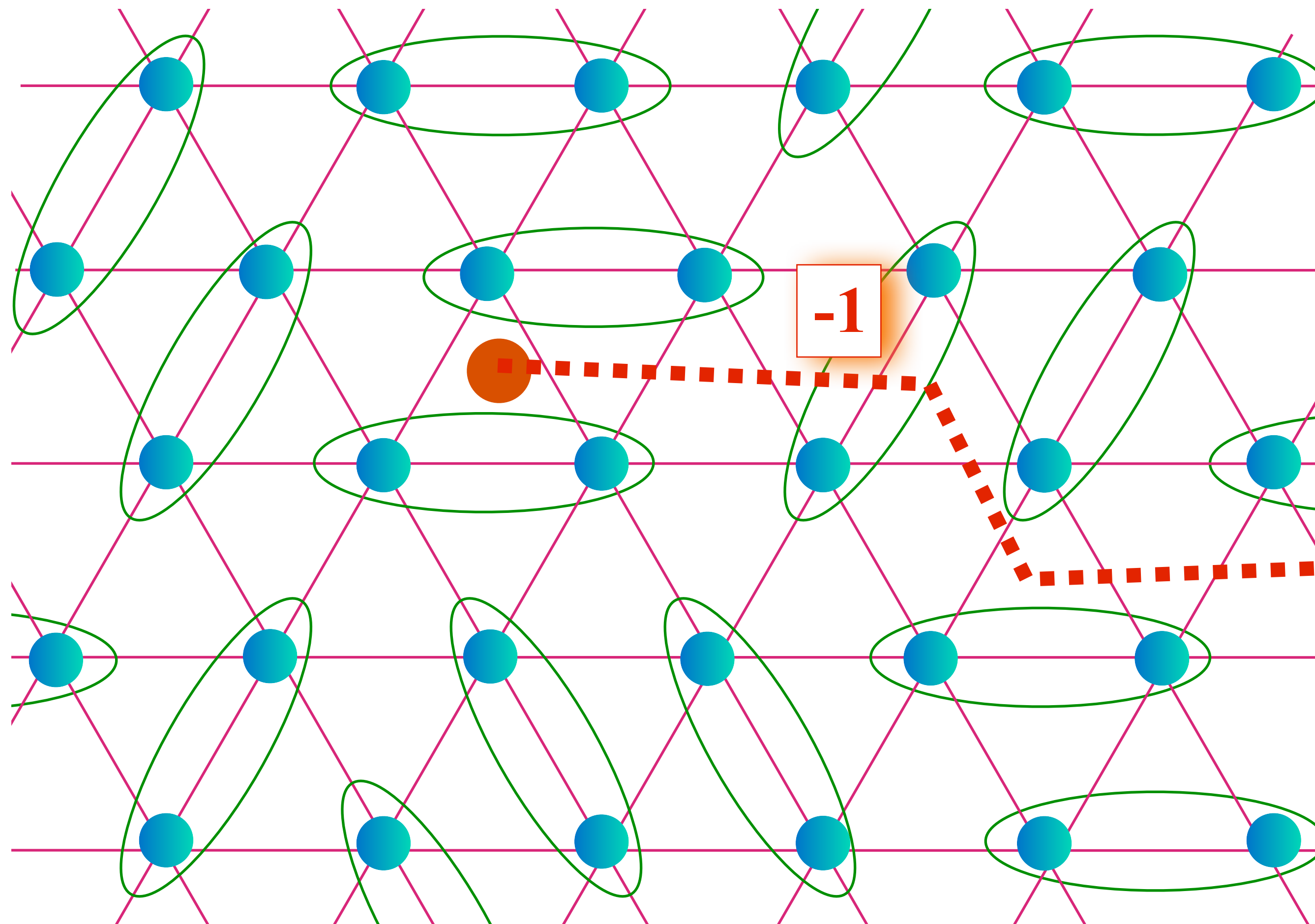


Excitations of the Z_2 Spin liquid

A vison

m (boson) particle

$$= \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$$



$$|v\rangle = \sum_{\mathcal{D}} c_{\mathcal{D}} (-1)^{n_{\mathcal{D}}} |\mathcal{D}\rangle$$

$\mathcal{D} \rightarrow$ dimer covering of lattice

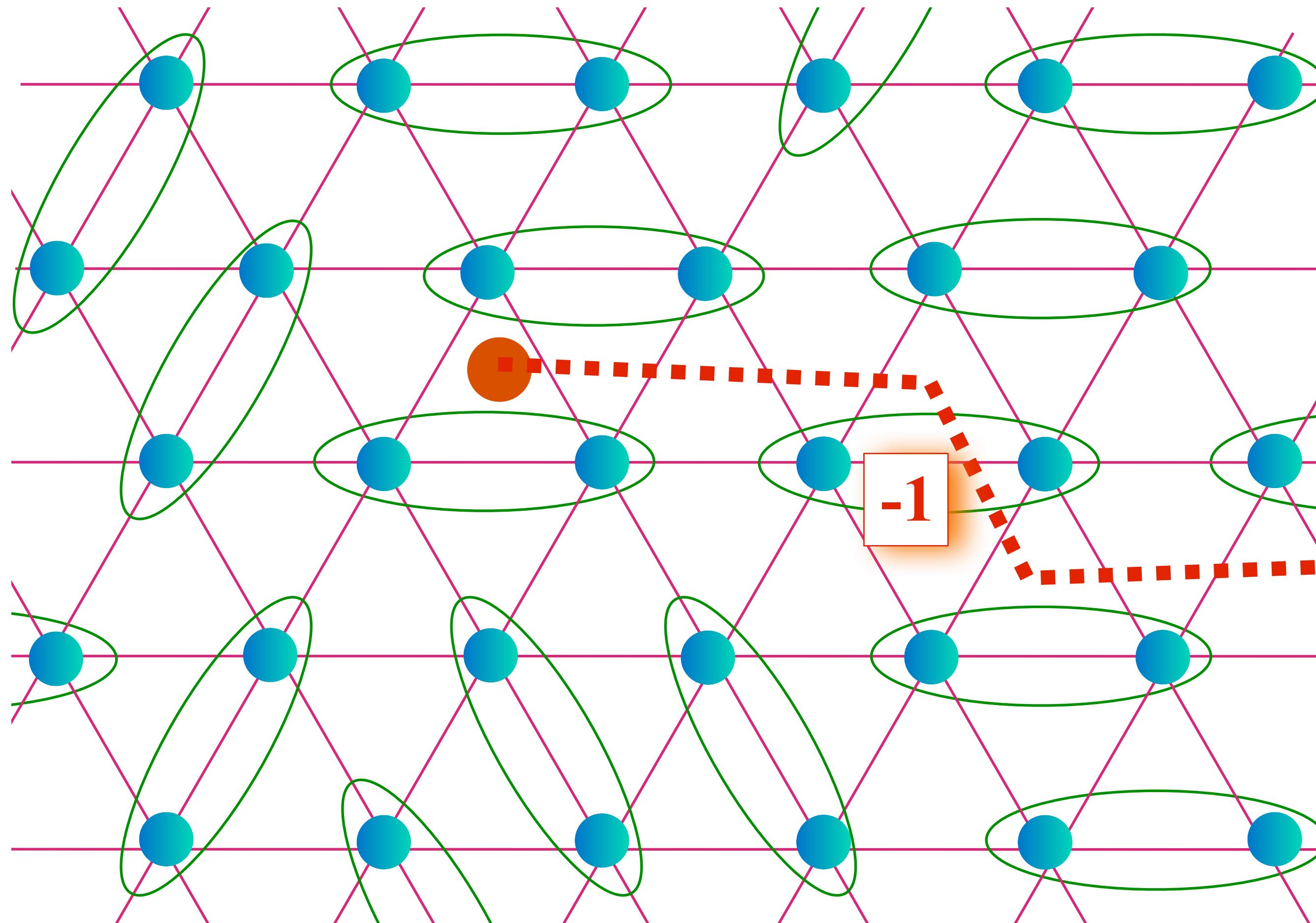
$n_{\mathcal{D}} \rightarrow$ number of dimers crossing red line

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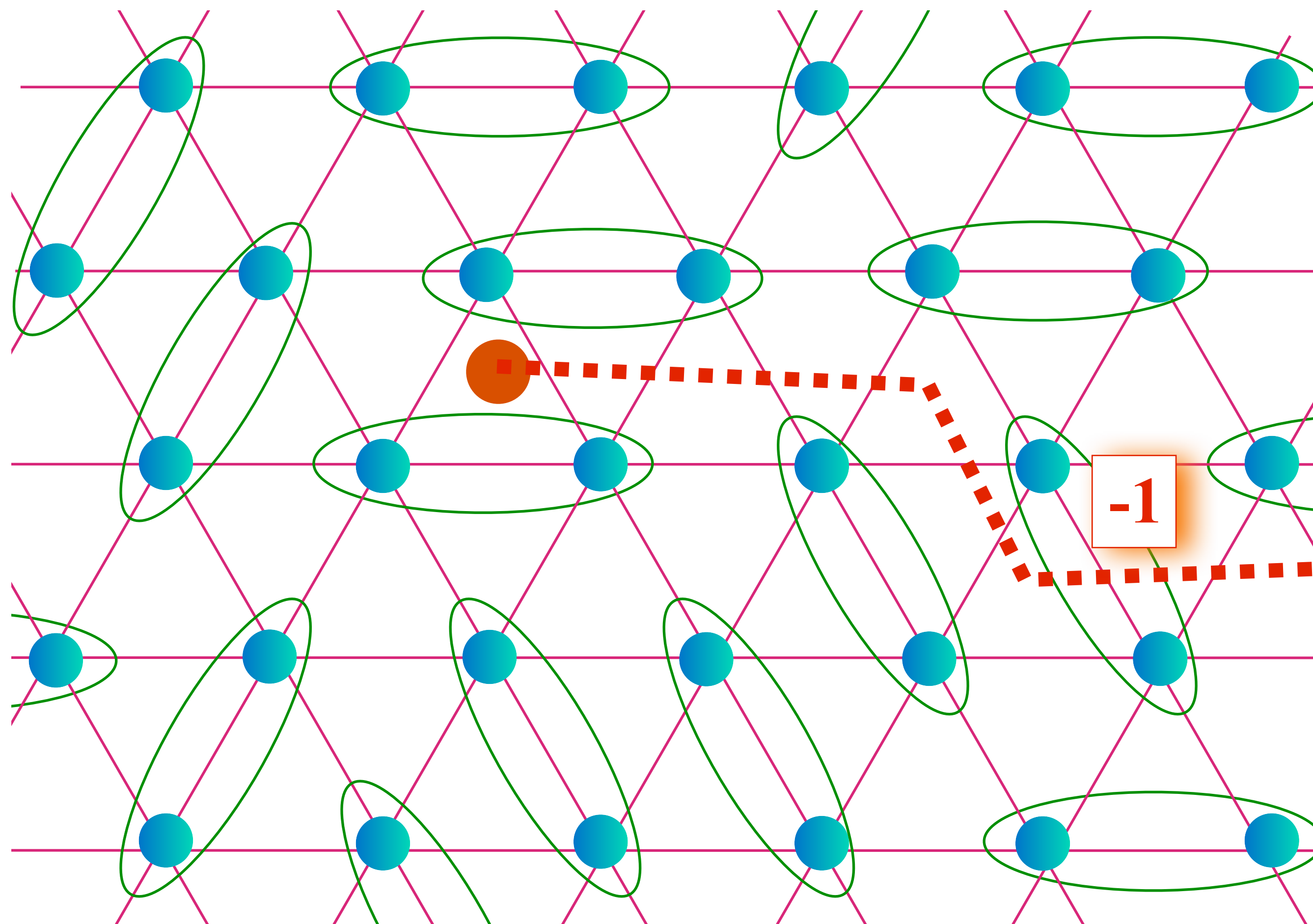
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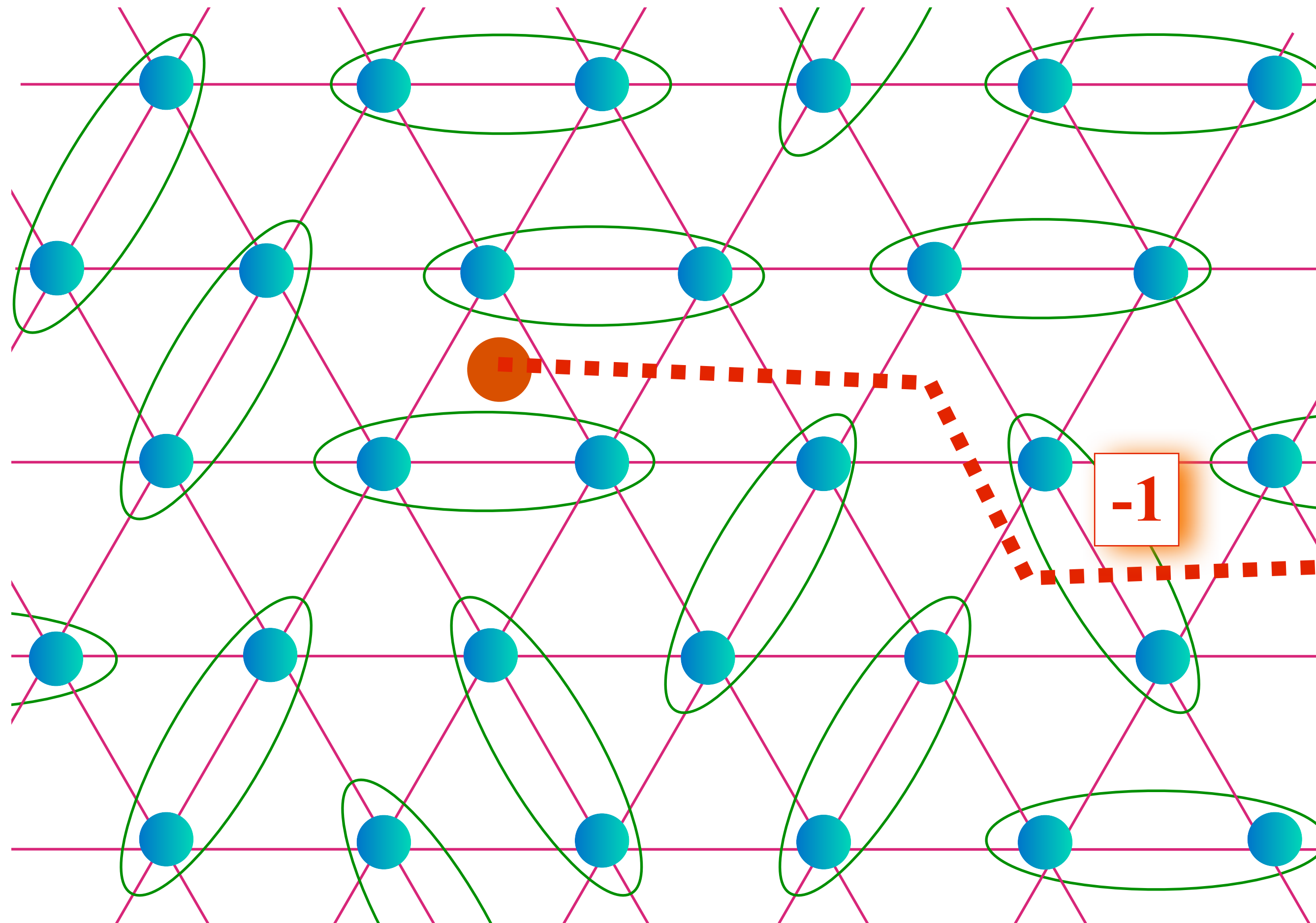
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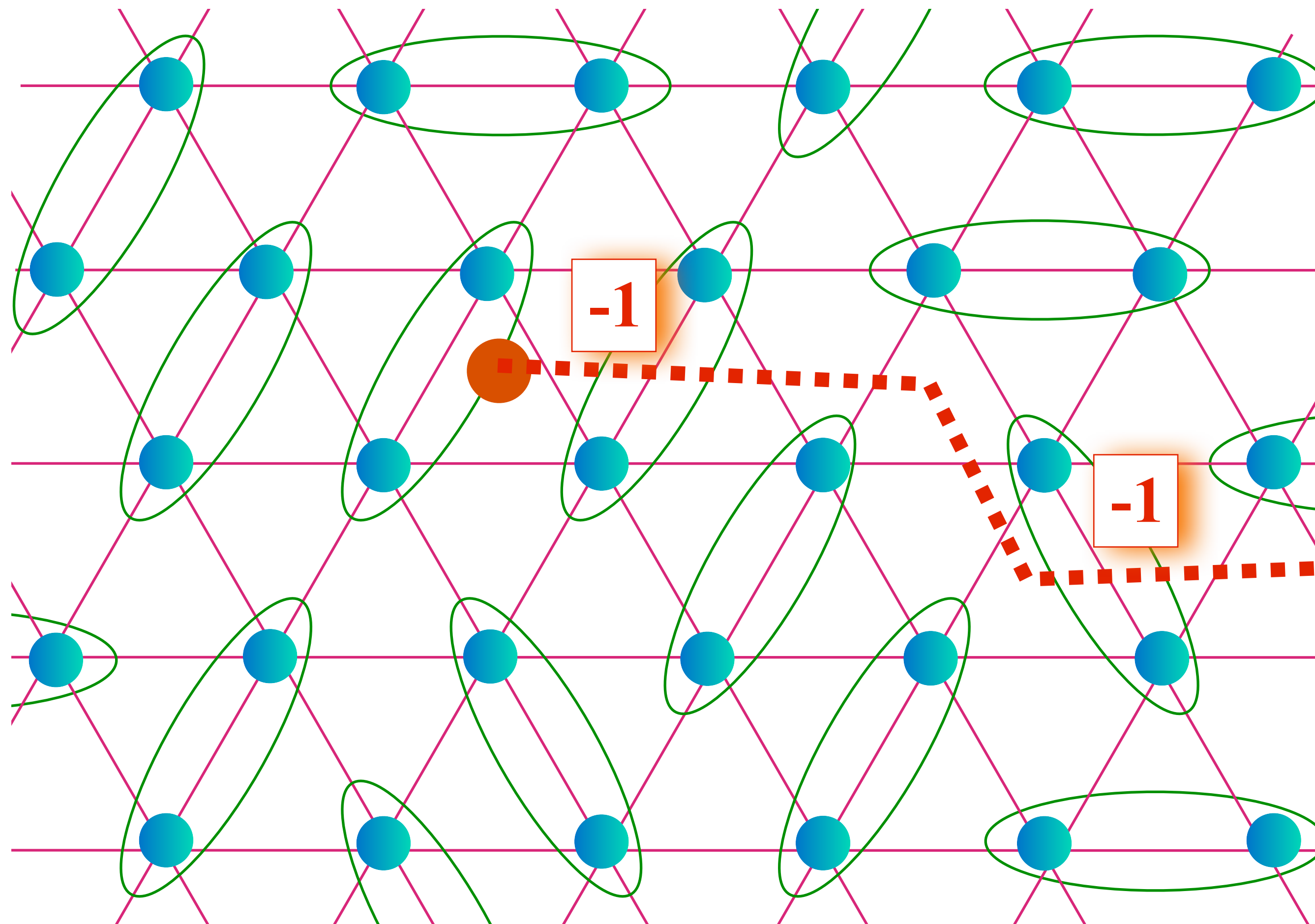
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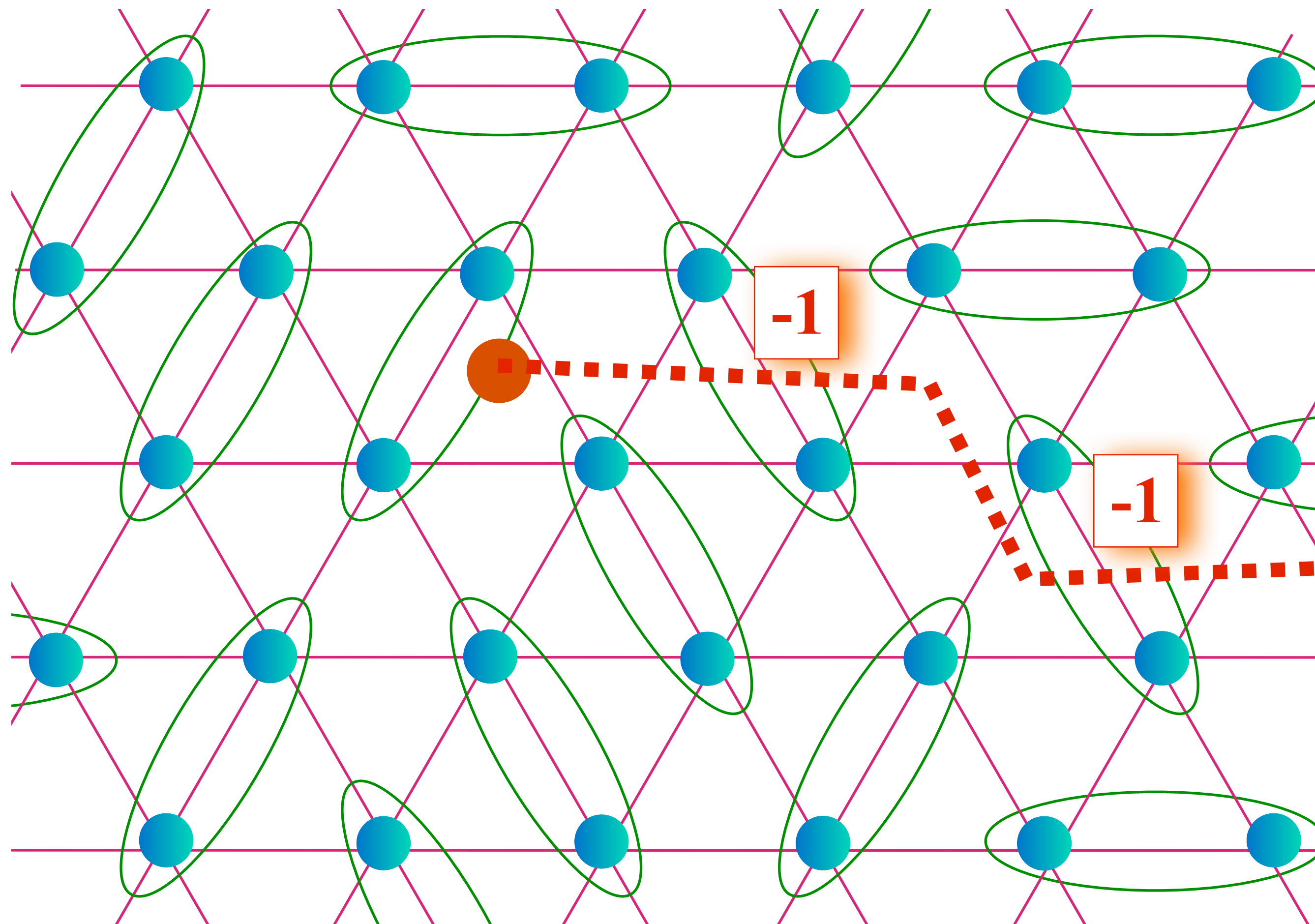
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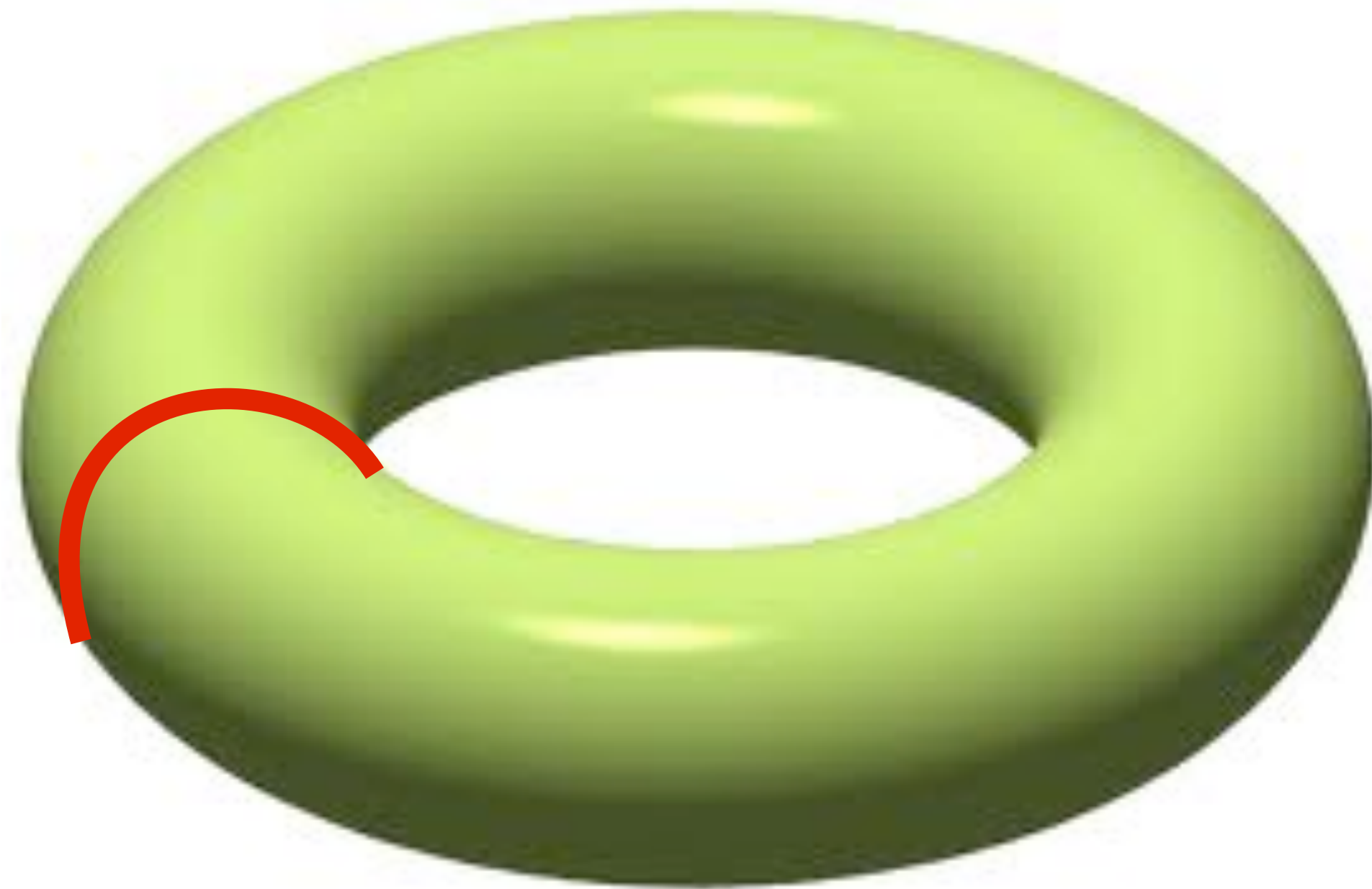
- A spinon adiabatically transported around a vison picks up a phase factor of -1 : spinons and visons are **mutual semions**.
- A bound state of a spinon and a vison picks up a phase factor of -1 when exchanged with another bound state of a spinon and a vison:
 - The ϵ spinon (fermion) is a bound state of the e spinon (boson) and a vison ($\epsilon = e \times m$).
 - The e spinon (boson) is a bound state of the ϵ spinon (fermion) and a vison ($e = \epsilon \times m$).

Ground state degeneracy on the torus



Place
insulator
on a torus:

Ground state degeneracy on the torus

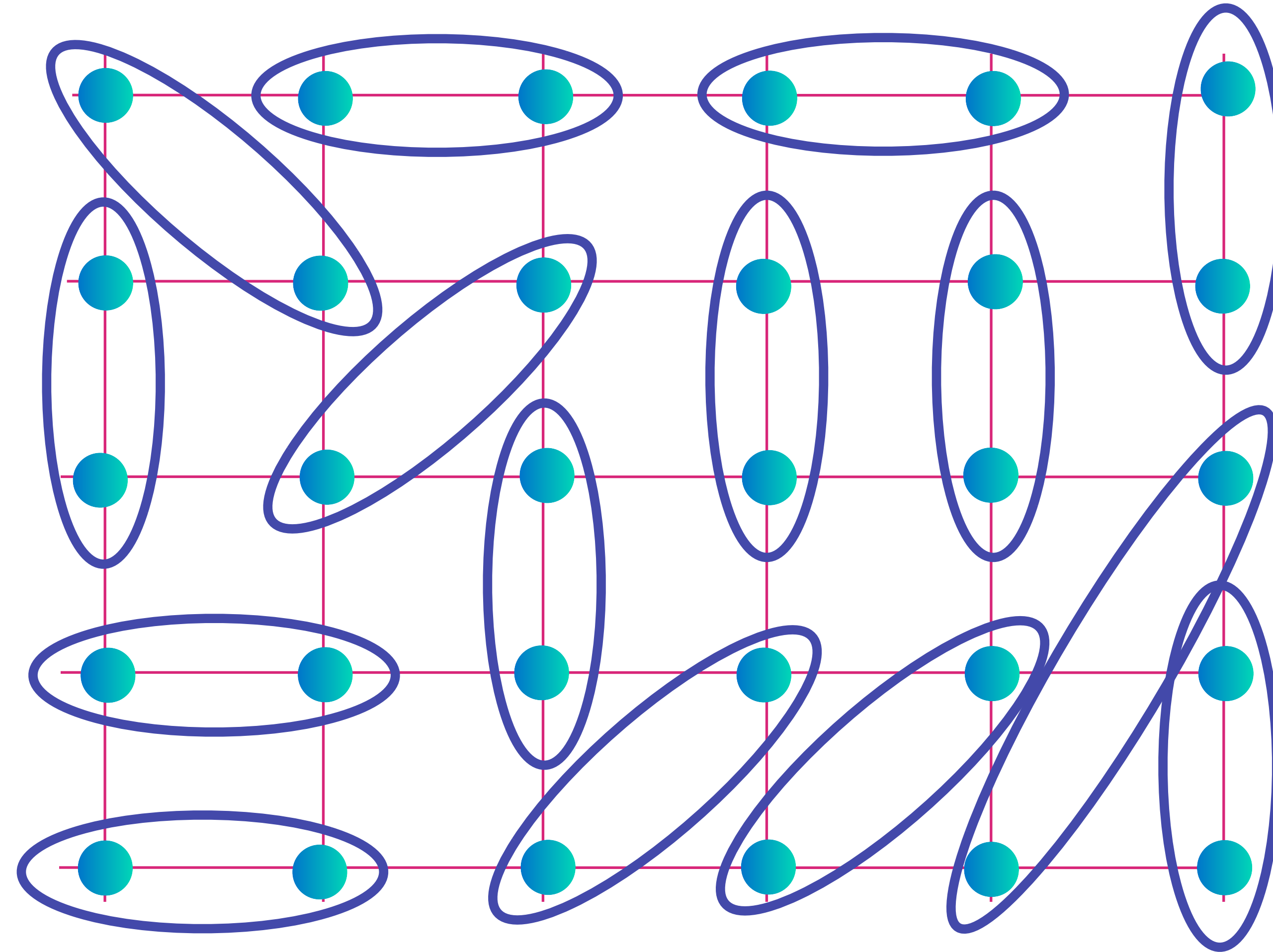


**Place
insulator
on a torus:**

Obtain a
degenerate
orthogonal state
by modifying the
wavefunction on
a “branch-cut”
encircling the
torus.

Ground state degeneracy on the torus

$$\text{[Two teal dots in a blue oval]} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2}$$



**Place
insulator
on a torus:**

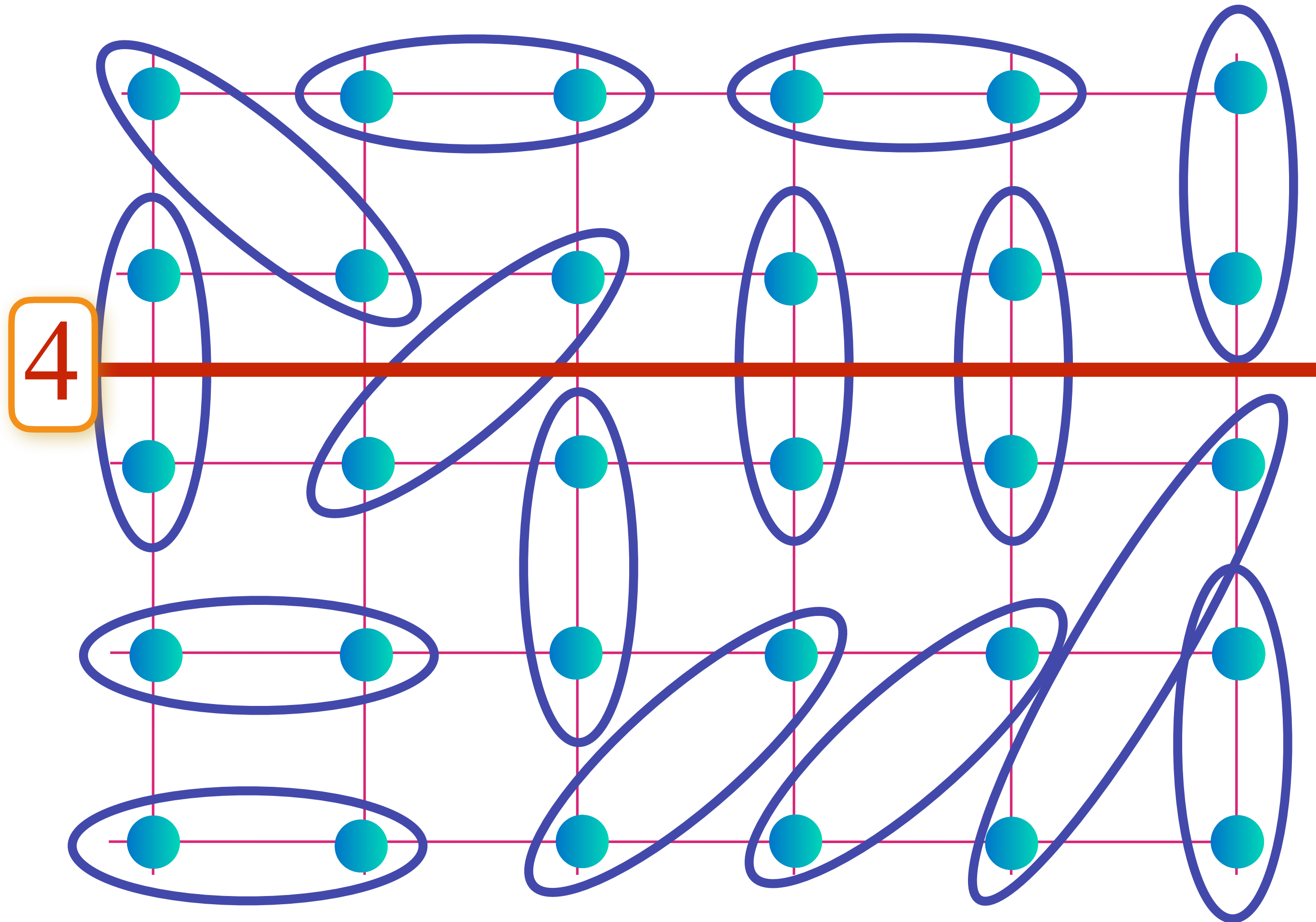
Number of
dimers crossing
“branch-cut” is
conserved
modulo 2:
there are nearly
degenerate
states with odd
and even
dimer-cuts

D.J. Thouless, PRB **36**, 7187 (1987)

S.A. Kivelson, D.S. Rokhsar and J.P. Sethna, Europhys. Lett. **6**, 353 (1988)

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$$\text{[Diagram: two teal dots in a blue oval]} = (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) / \sqrt{2}$$



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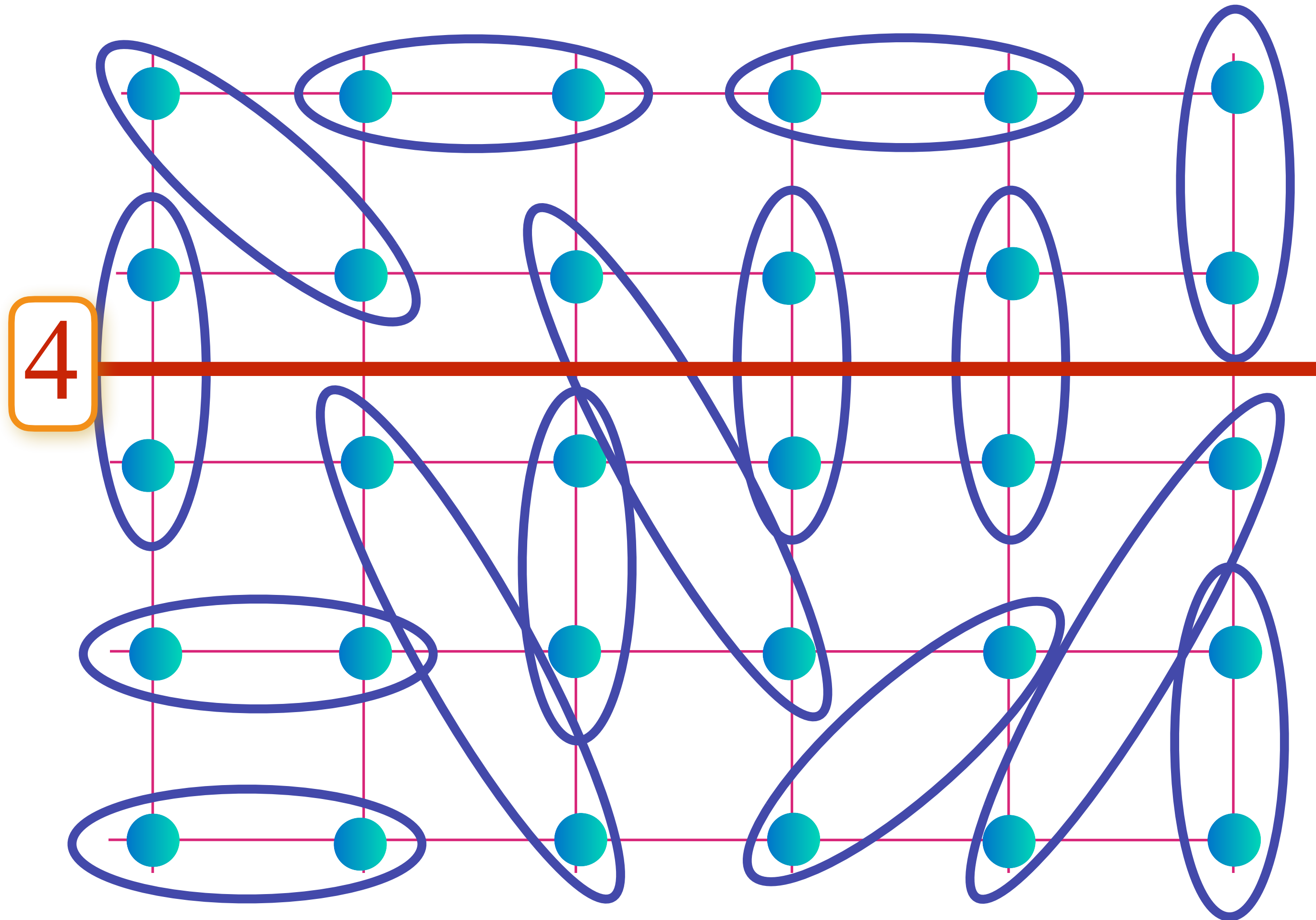
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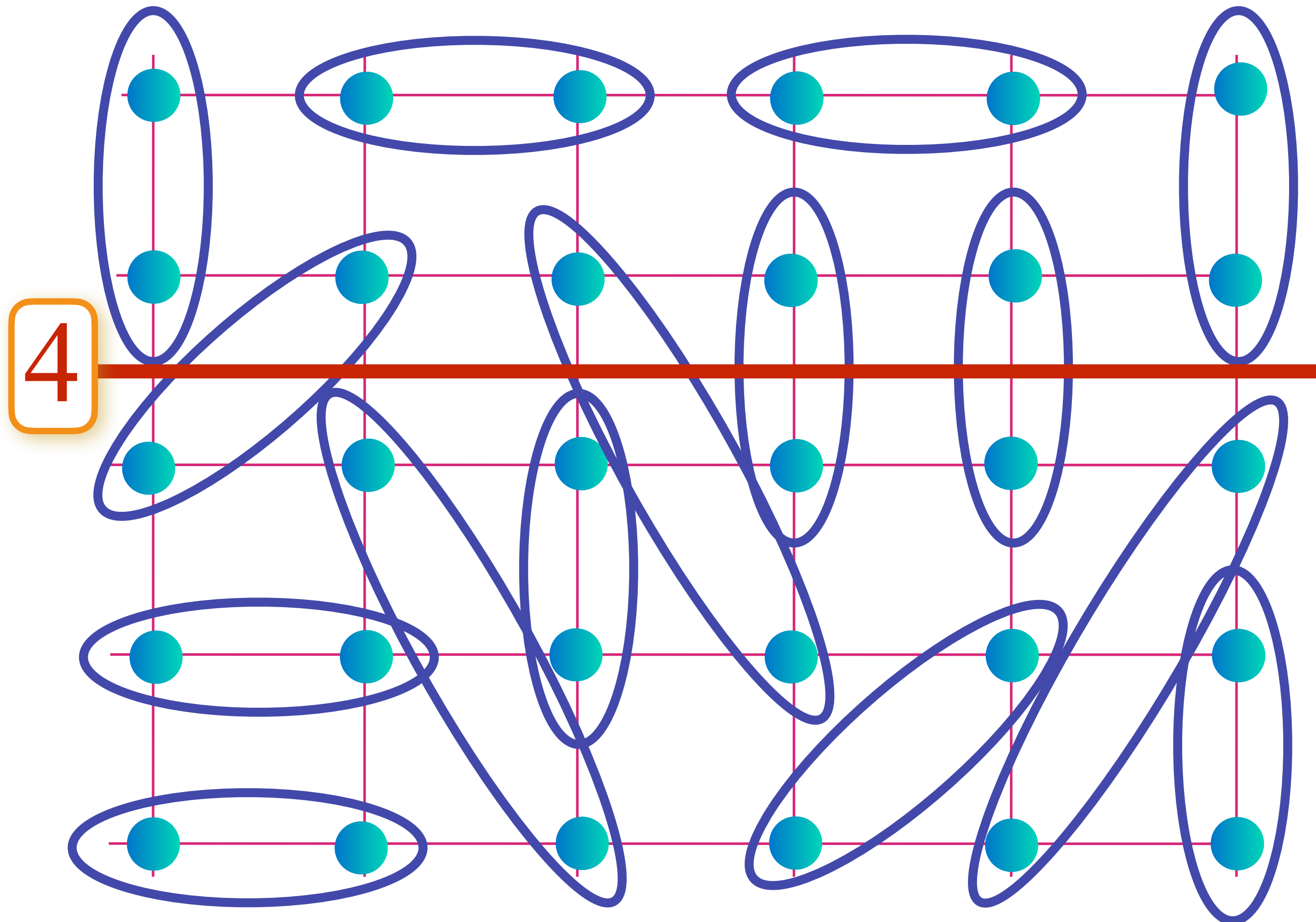
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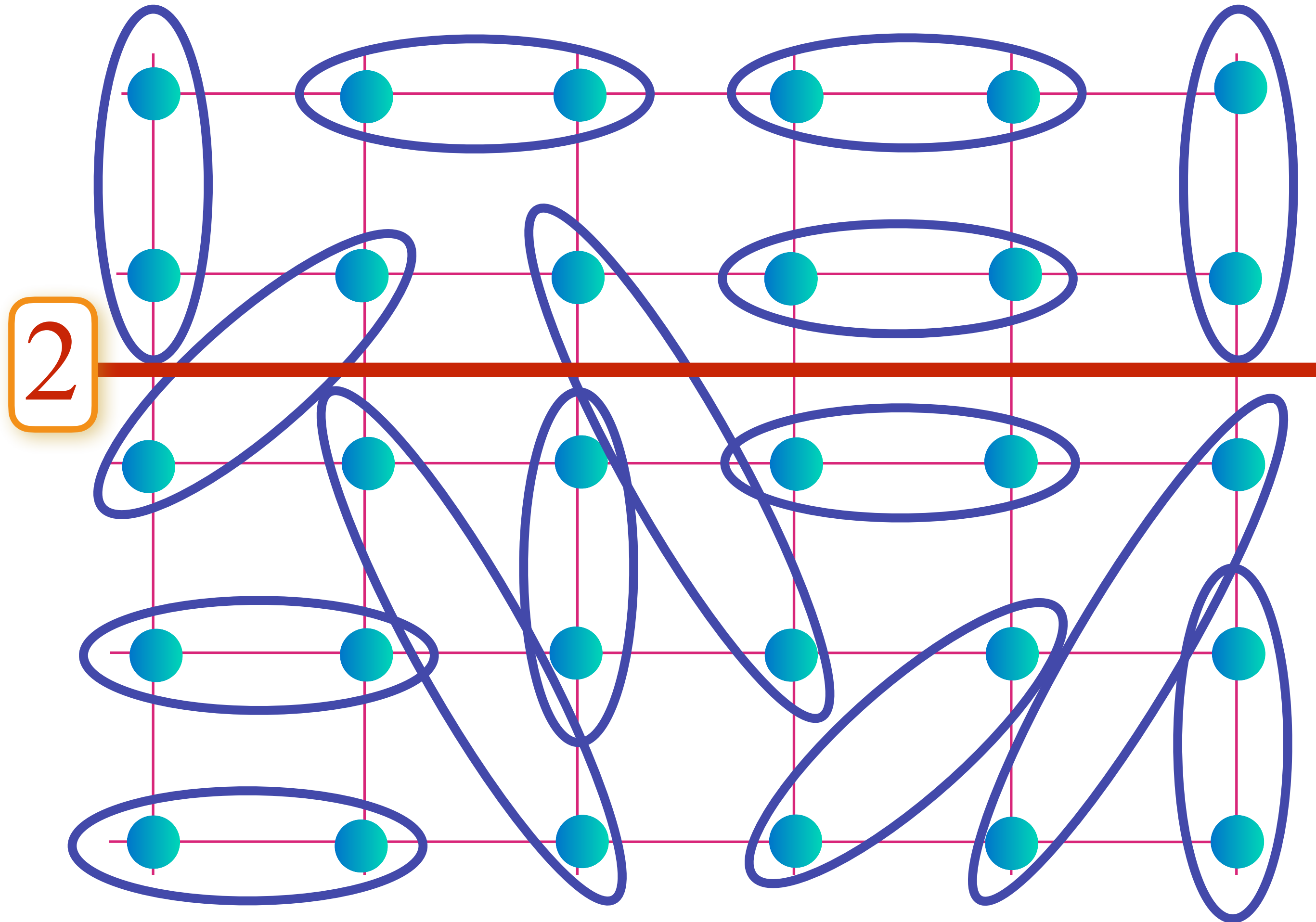
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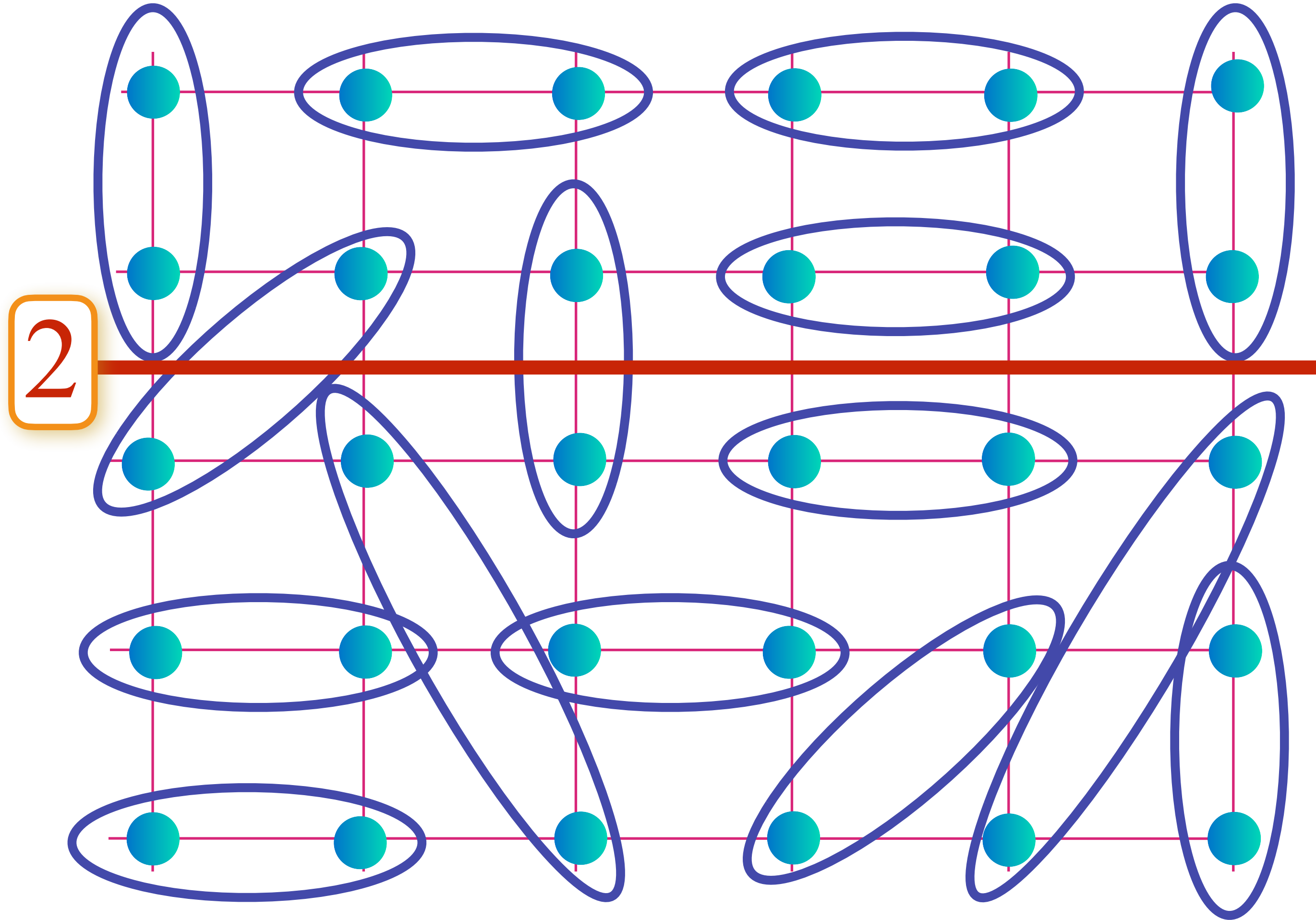
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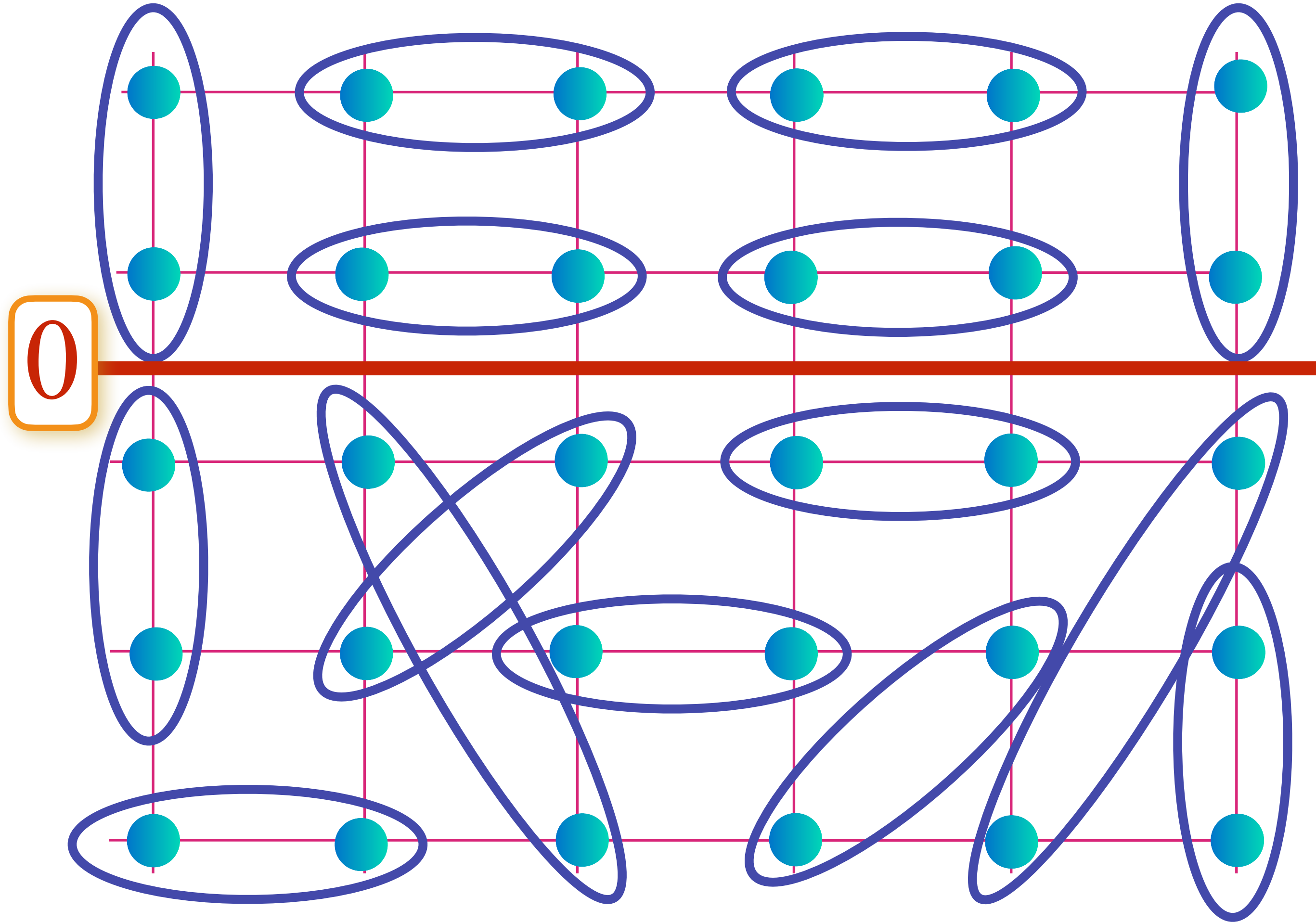
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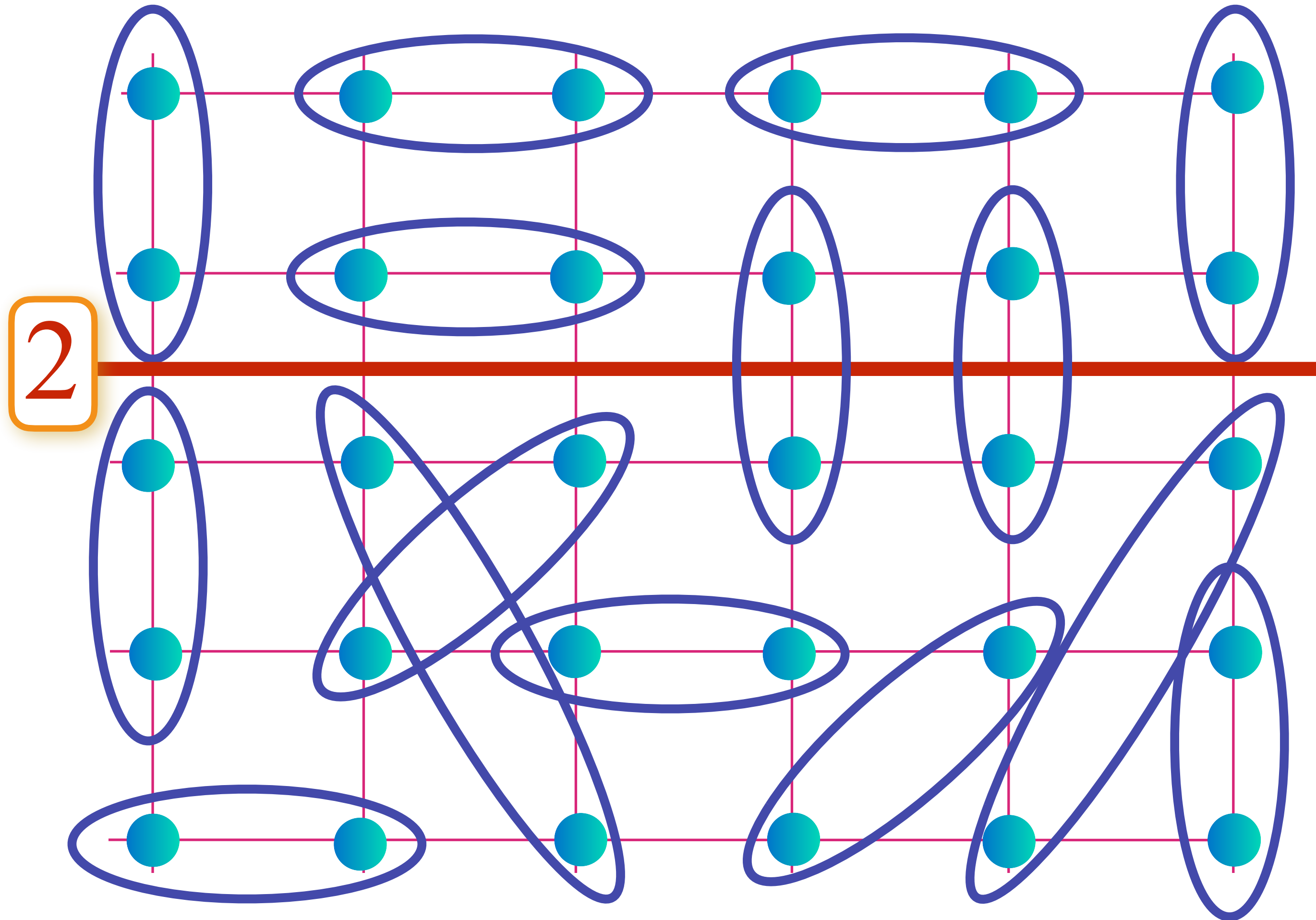
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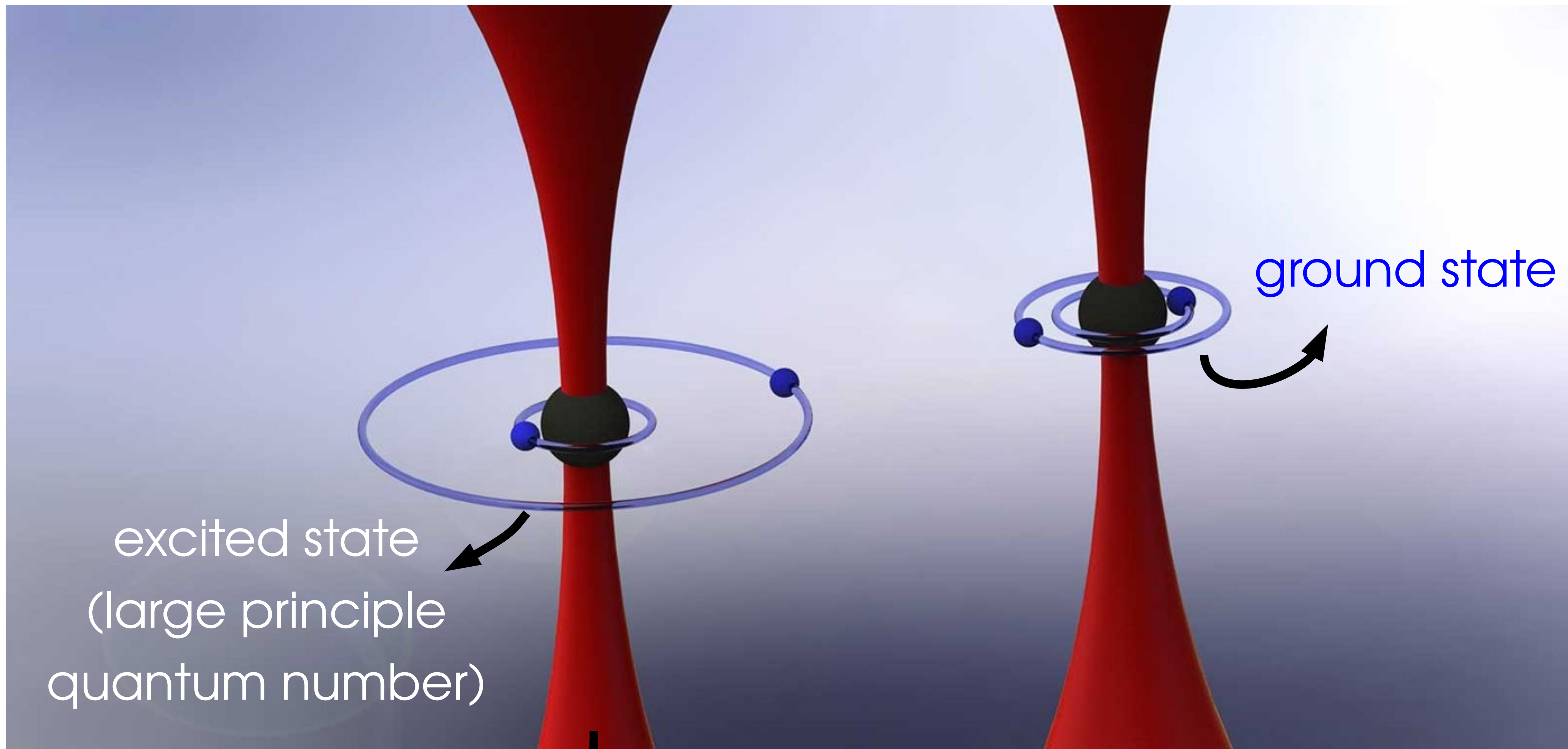


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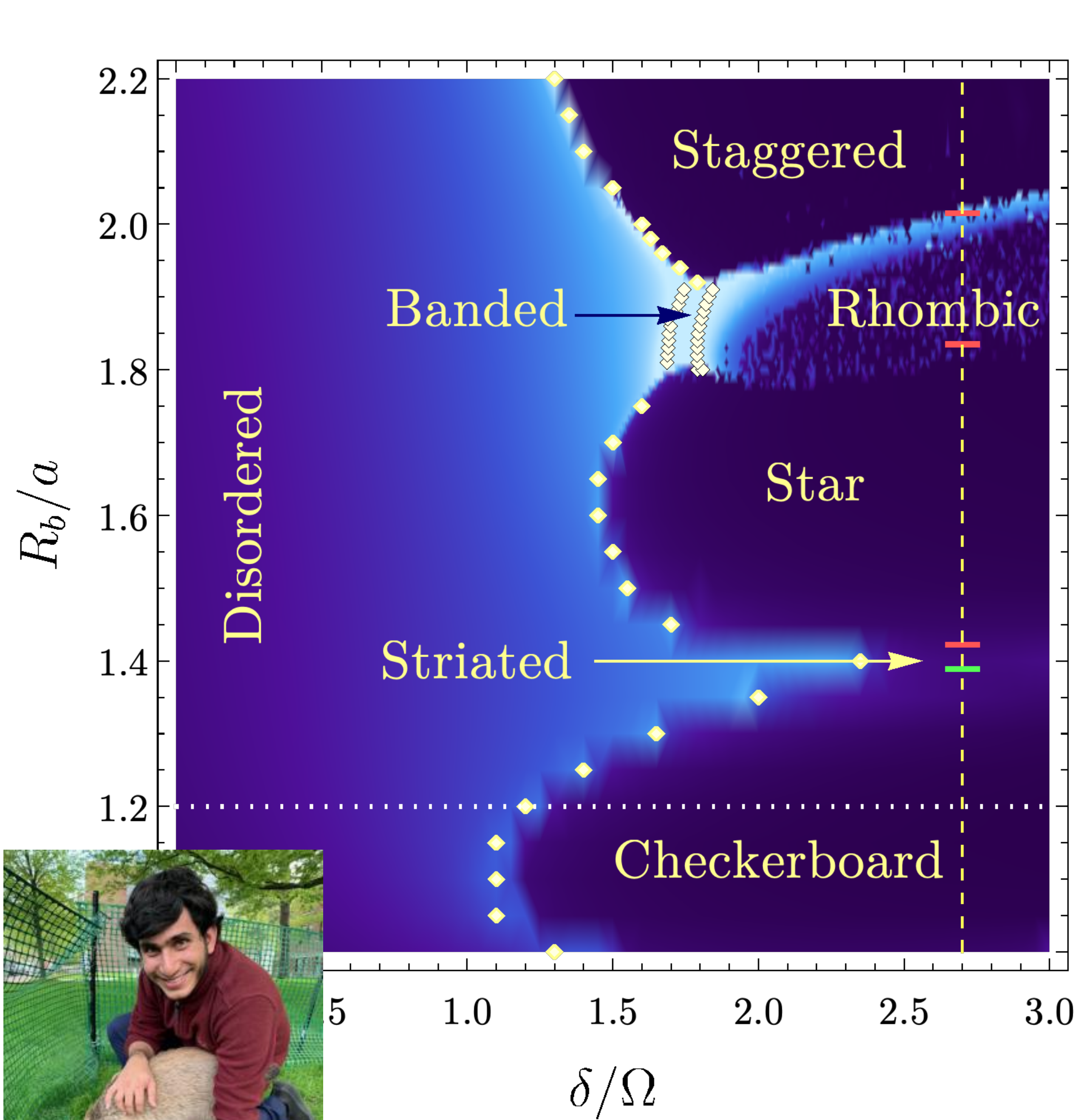
$$V_{|i-j|} \sim |i - j|^{-6}$$

optical tweezer (traps atom)

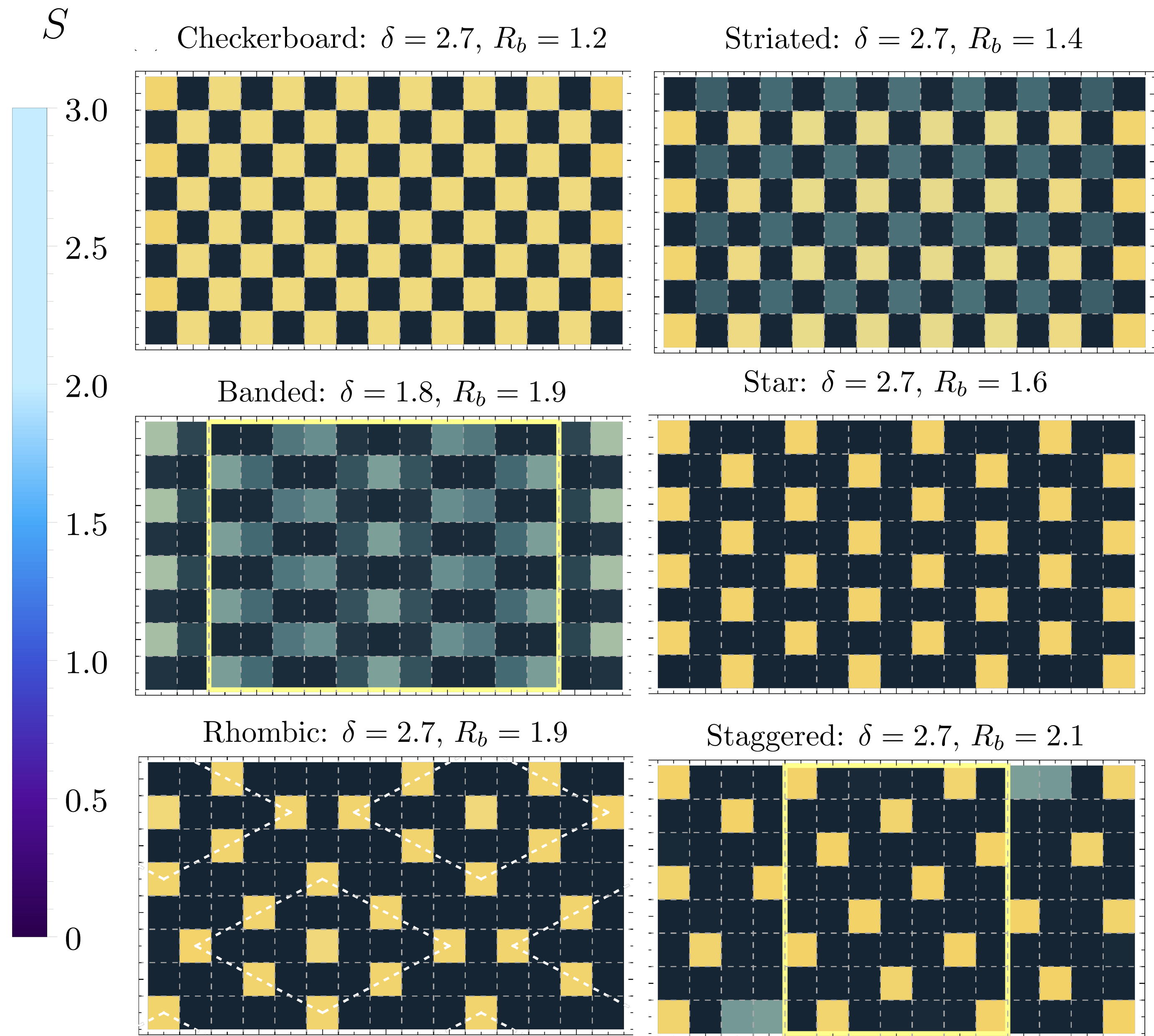
Fig: <https://www.caltech.edu/about/news/quantum-innovations-achieved-using-alkaline-earth-atoms>

$$H_{\text{Ryd}} = \sum_i \left[\frac{\Omega}{2} (|g\rangle\langle r| + |r\rangle\langle g|)_i - \Delta |r\rangle\langle r| \right] + \sum_{(i,j)} V_{|i-j|} (|r\rangle\langle r|_i \otimes |r\rangle\langle r|_j)$$

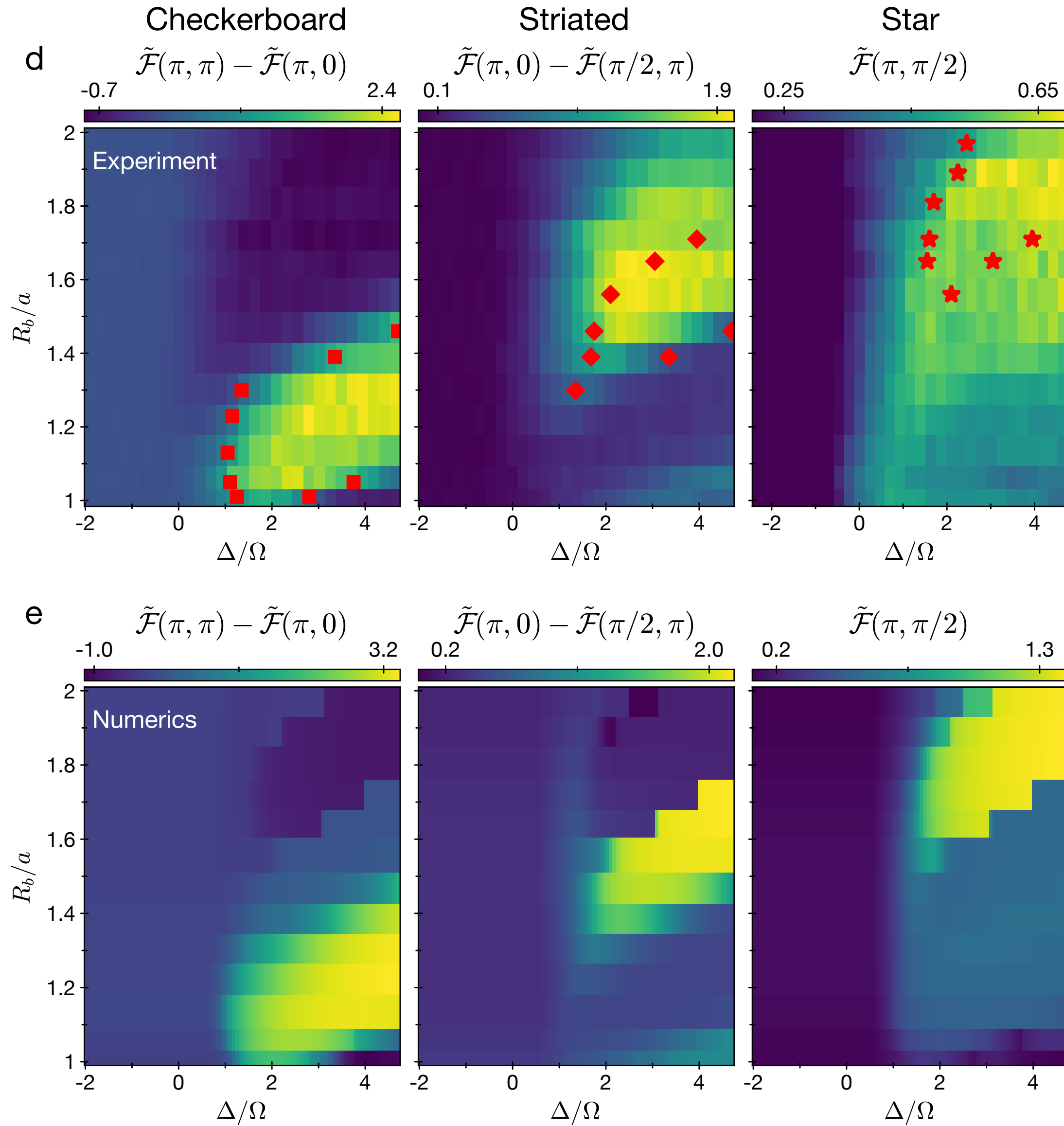
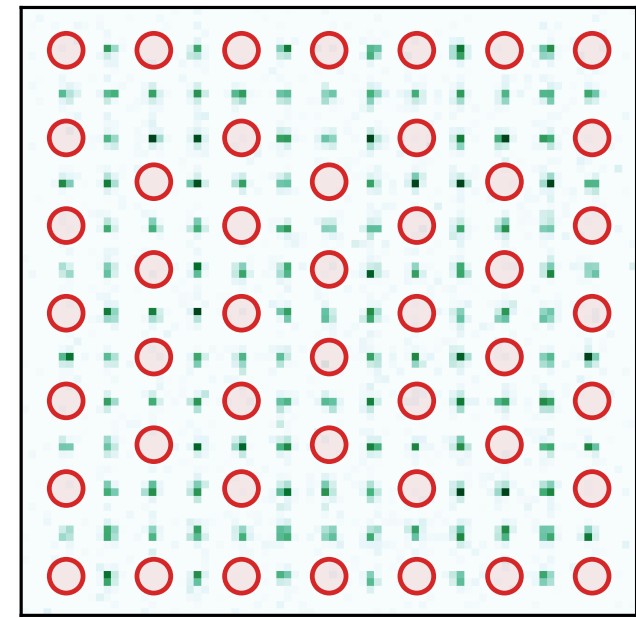
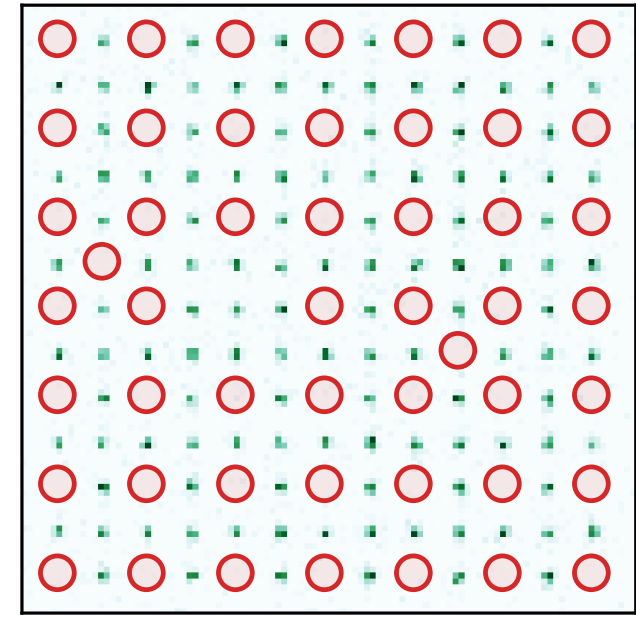
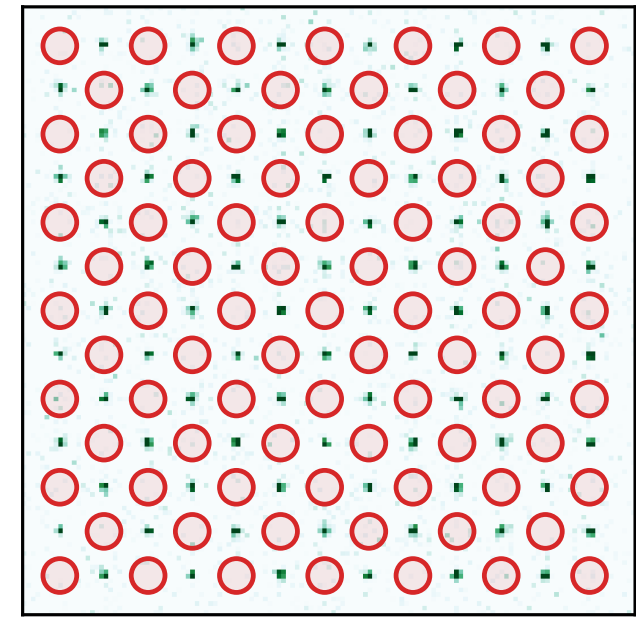
Rydberg atoms on the square lattice: theory



R. Samajdar, Wen Wei Ho, H. Pichler, M. D. Lukin, S. Sachdev, PRL **124**, 103601 (2020)

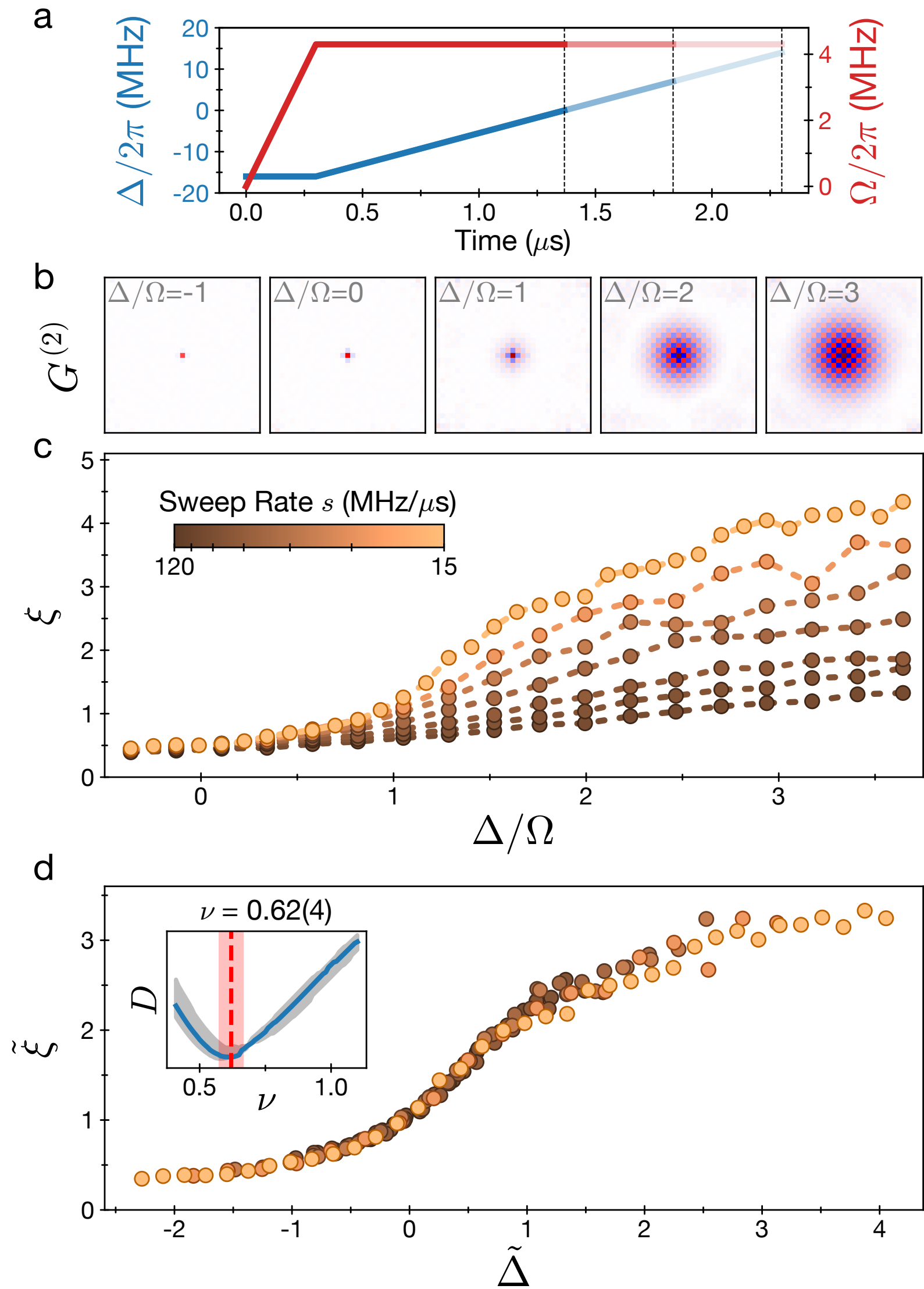


Rydberg atoms on the square lattice: experiment



$$\tilde{\xi} = \xi(s/s_0)^\mu$$

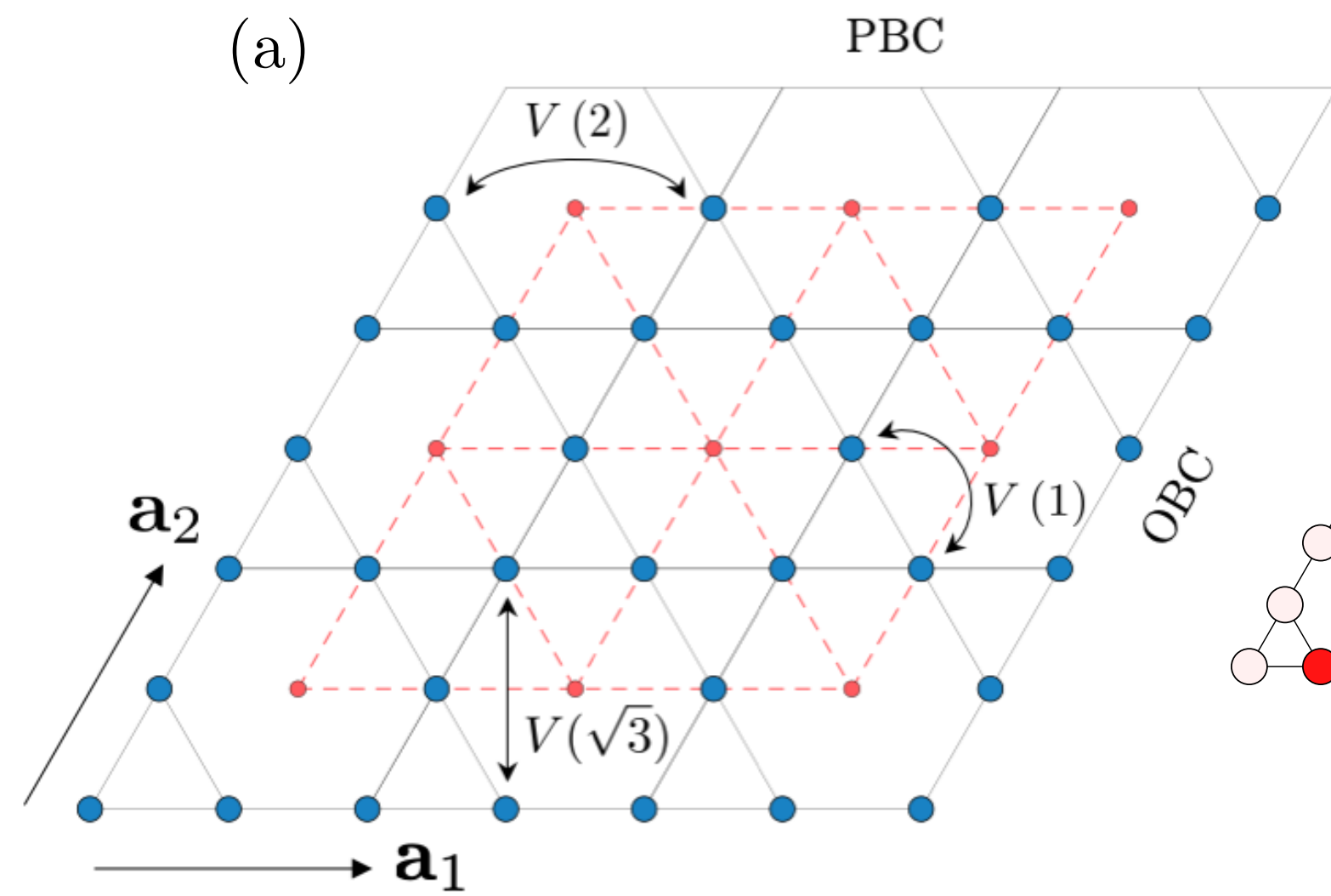
$$\tilde{\Delta} = (\Delta - \Delta_c)(s/s_0)^\kappa$$



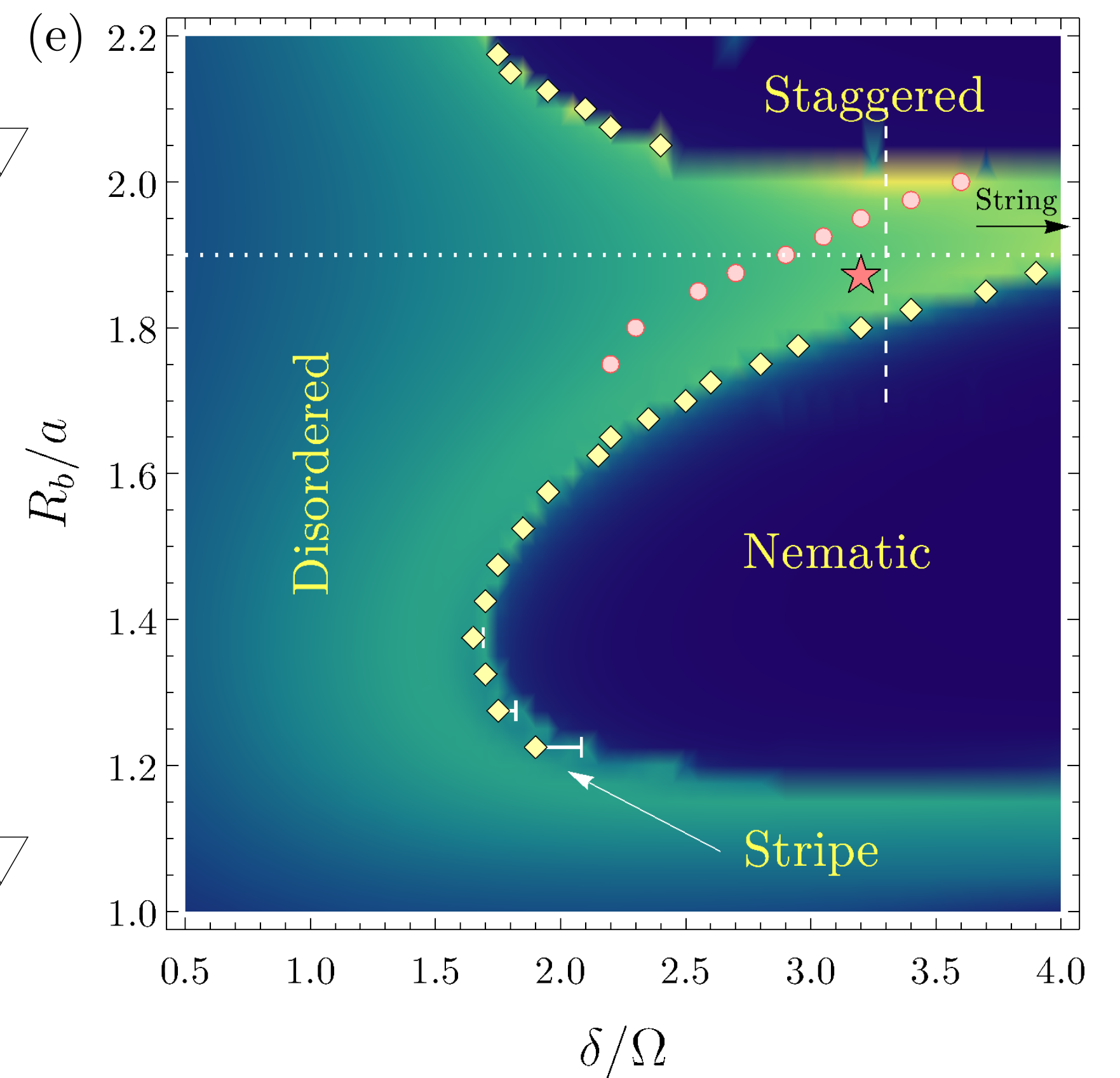
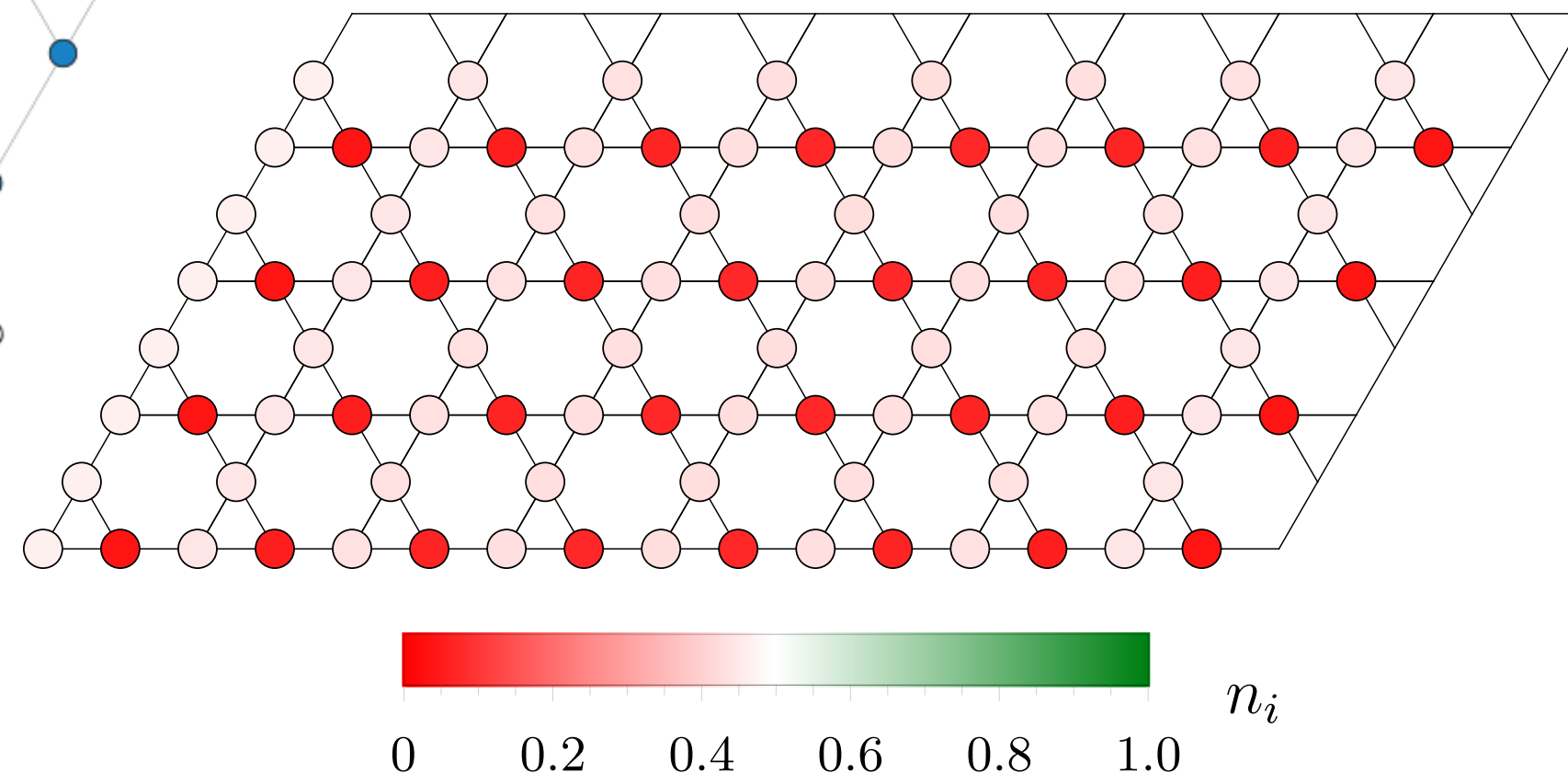
Quantum Phases of Matter on a 256-Atom Programmable Quantum Simulator, Sepehr Ebadi, Tout T. Wang, Harry Levine, Alexander Keesling, Giulia Semeghini, Ahmed Omran, Dolev Bluvstein, Rhine Samajdar, Hannes Pichler, Wen Wei Ho, Soonwon Choi, Subir Sachdev, Markus Greiner, Vladan Vuletic, and Mikhail D. Lukin, Nature **595**, 227 (2021); Pascal Scholl et al. arXiv:2012.12268

First observation of Ising quantum phase transition in 2+1 dimensions

Rydberg atoms on site-kagome lattice: theory

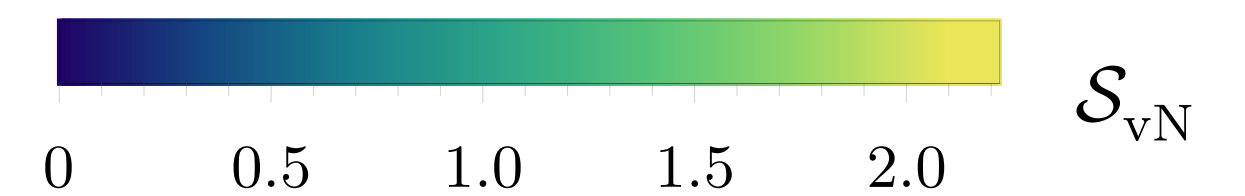
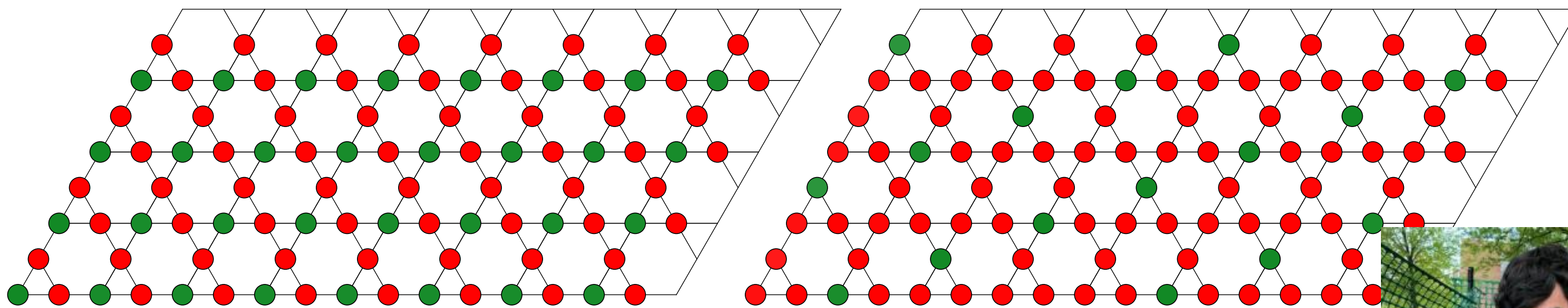


(b) Stripe: $\delta = 2.2, R_b = 1.2$



(c) Nematic: $\delta = 3.3, R_b = 1.7$

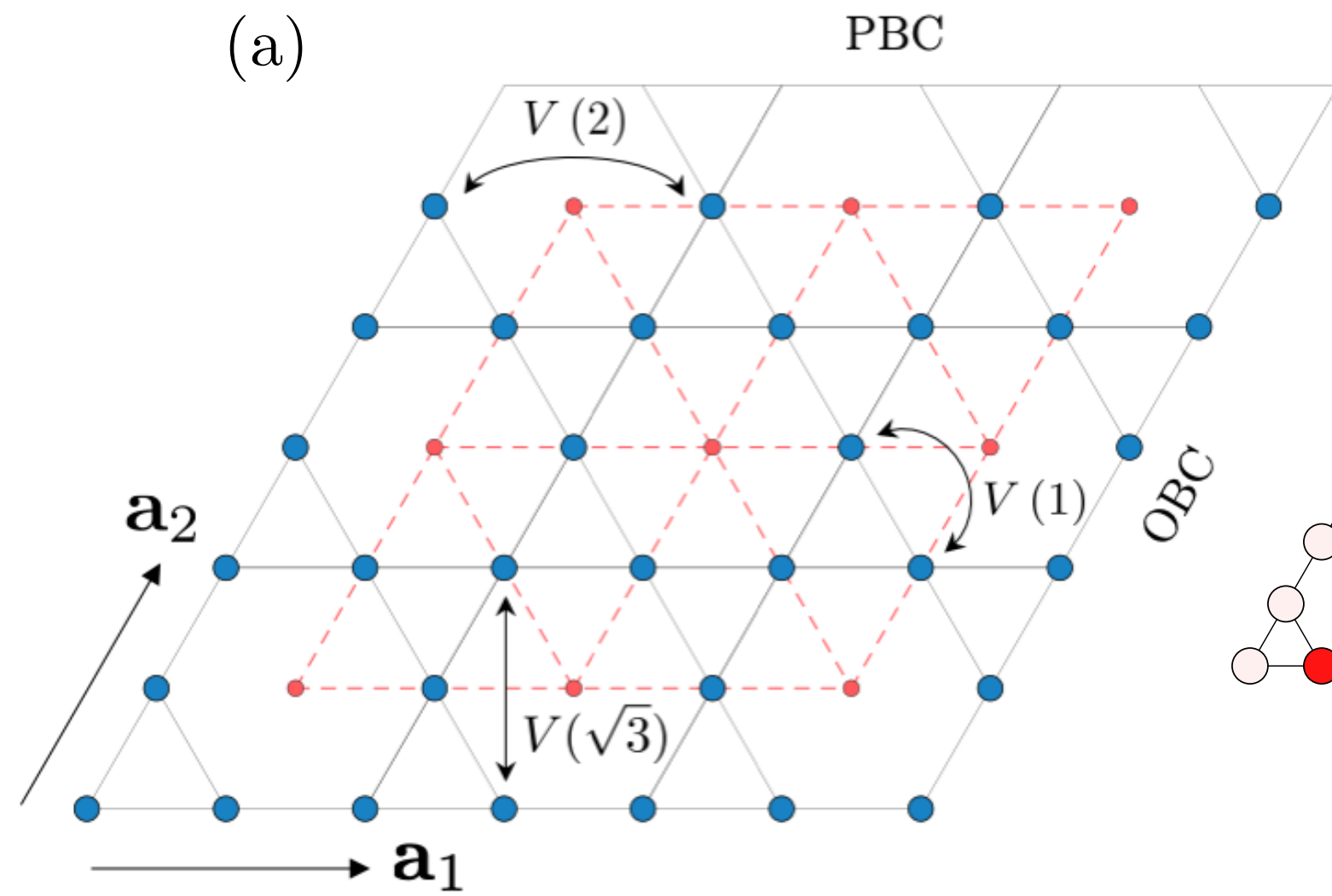
(d) Staggered: $\delta = 3.3, R_b = 2.1$



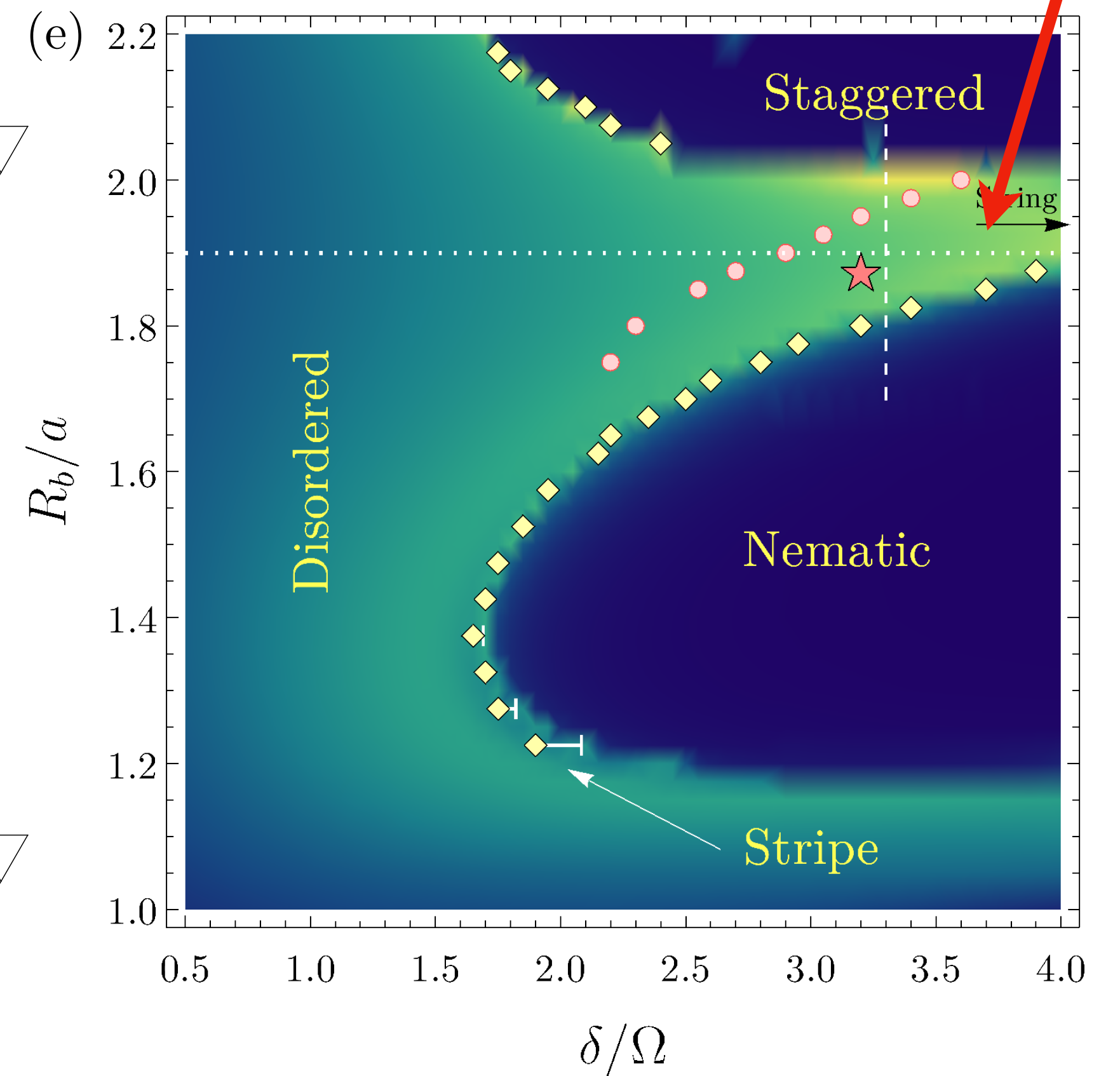
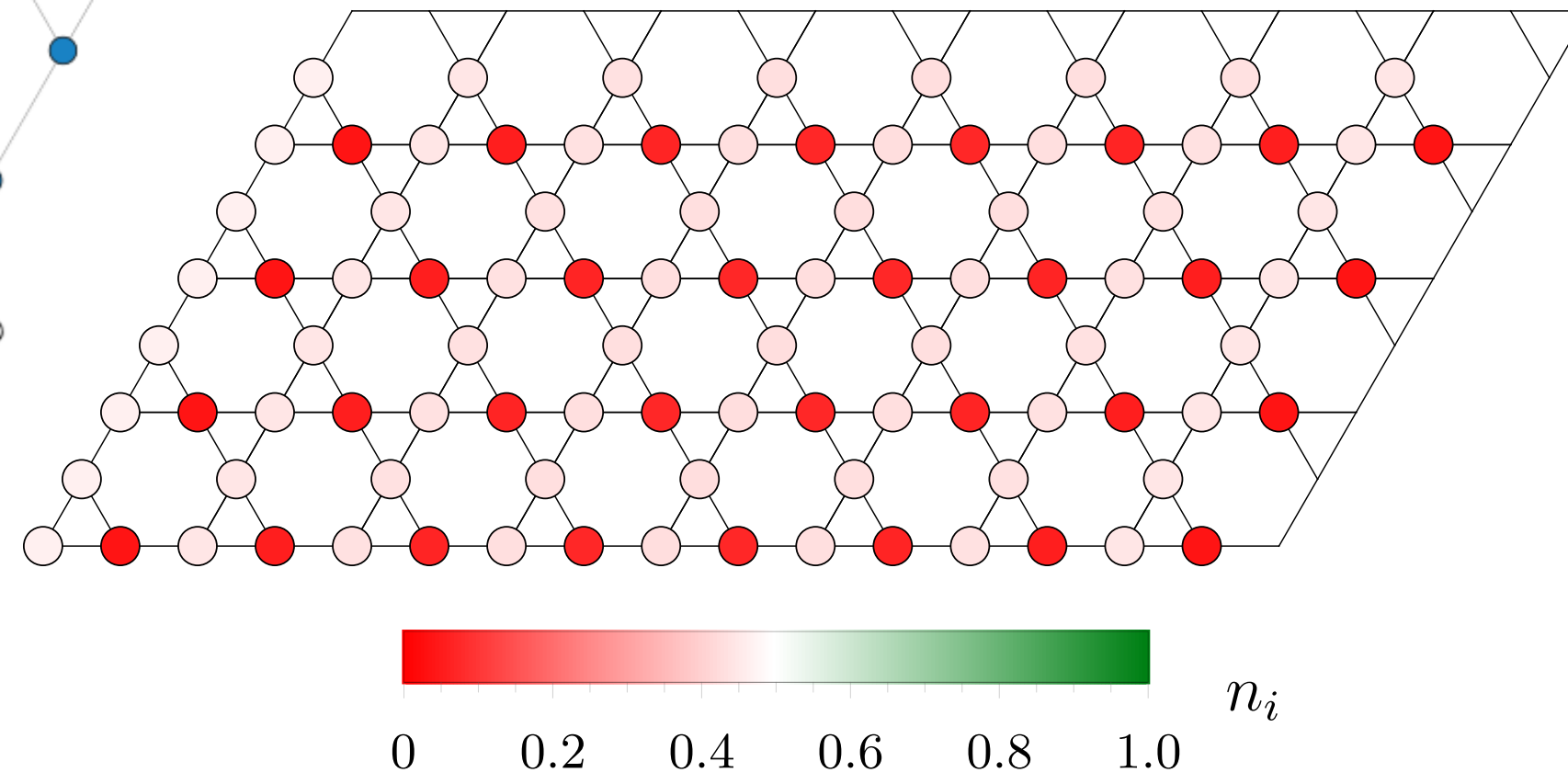
R. Samajdar, Wen Wei Ho, H. Pichler, M. D. Lukin, and S. Sachdev, PNAS **118**, e2015785118 (2021)

Rydberg atoms on site-kagome lattice: theory

?????

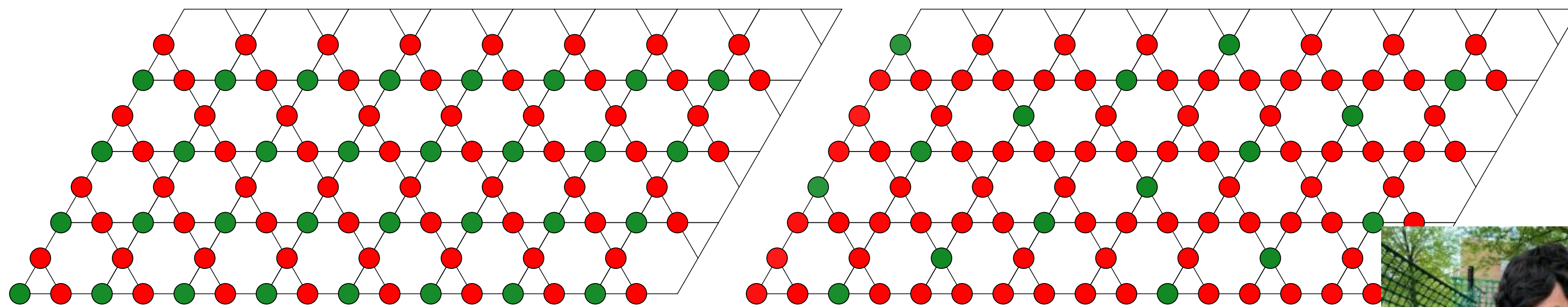


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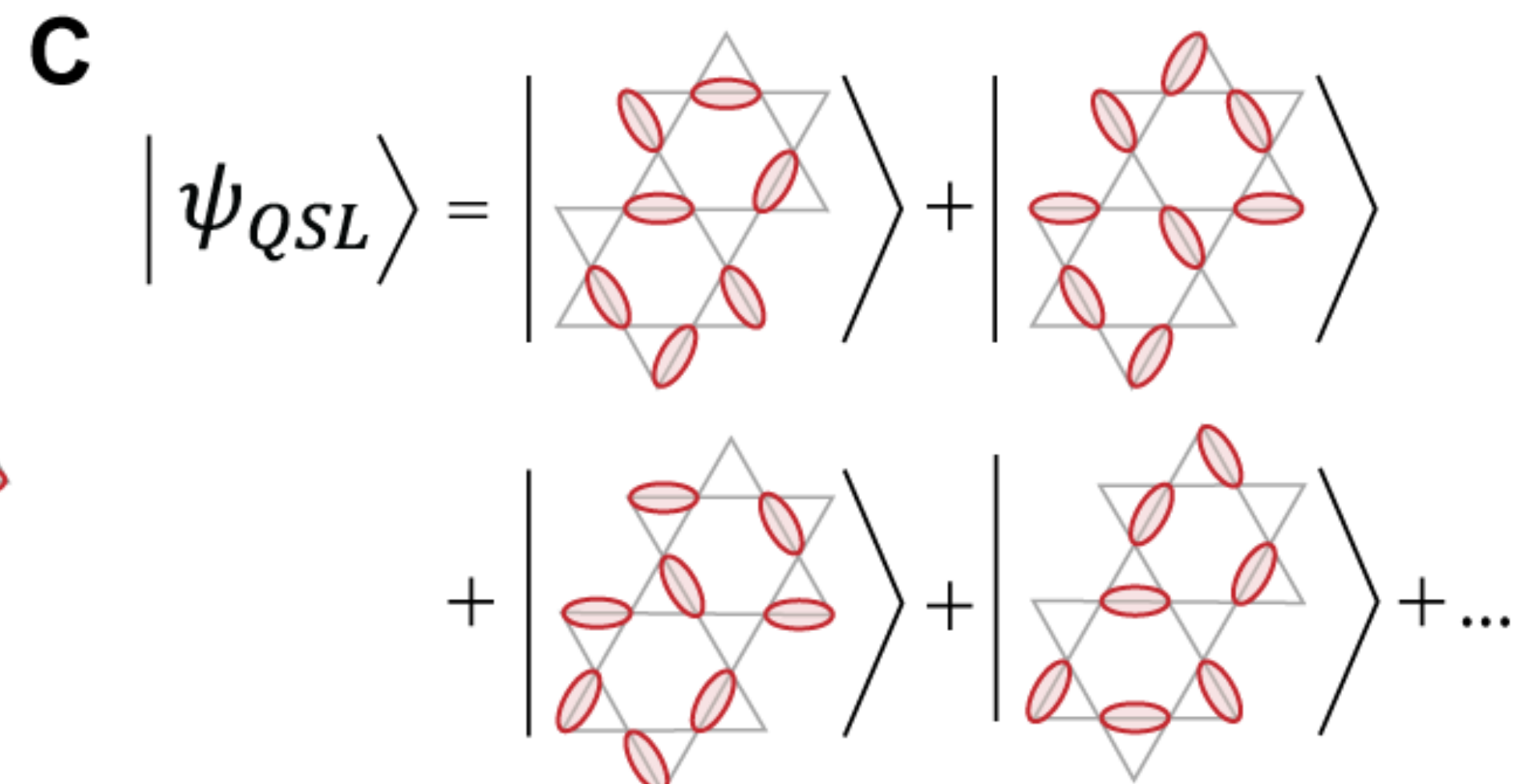
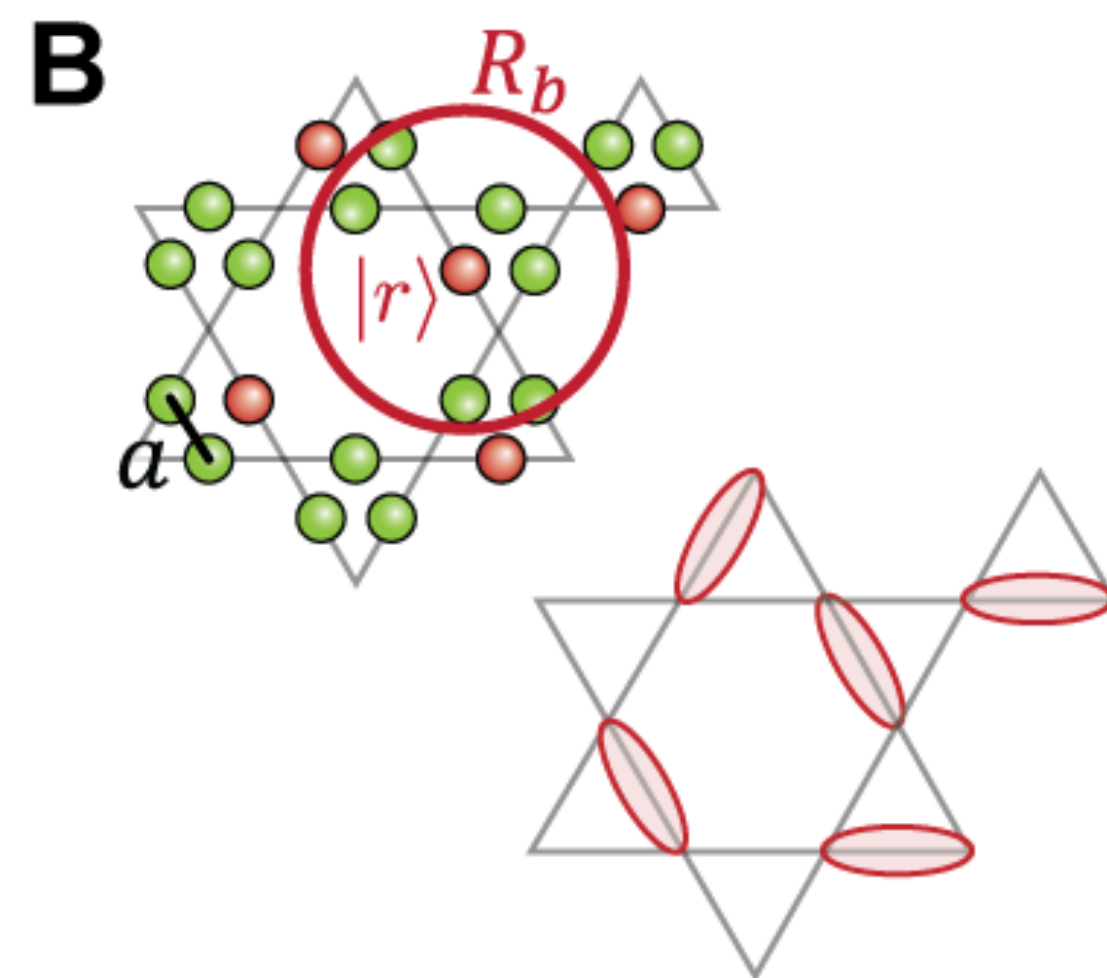
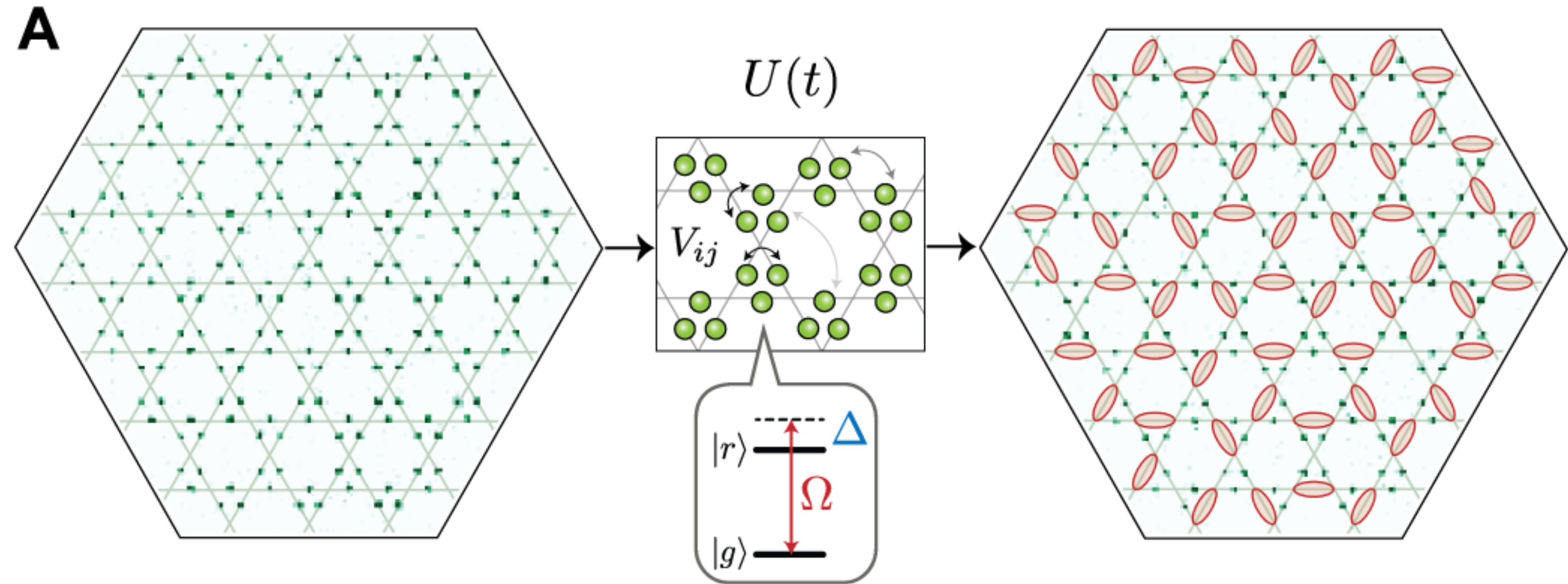


R. Samajdar, Wen Wei Ho, H. Pichler, M. D. Lukin, and S. Sachdev, PNAS **118**, e2015785118 (2021)

Probing Topological Spin Liquids on a Programmable Quantum Simulator

G. Semeghini, H. Levine, A. Keesling, S. Ebadi, T.T. Wang, D. Bluvstein, R. Verresen, H. Pichler, M. Kalinowski, R. Samajdar, A. Omran, S. Sachdev, A. Vishwanath, M. Greiner, V. Vuletic, M. D. Lukin, arXiv:2104.04119

Rydberg atoms
on the
link-kagome lattice:
experiment



1. “Conventional” phases of matter

Metals, insulators, superconductors

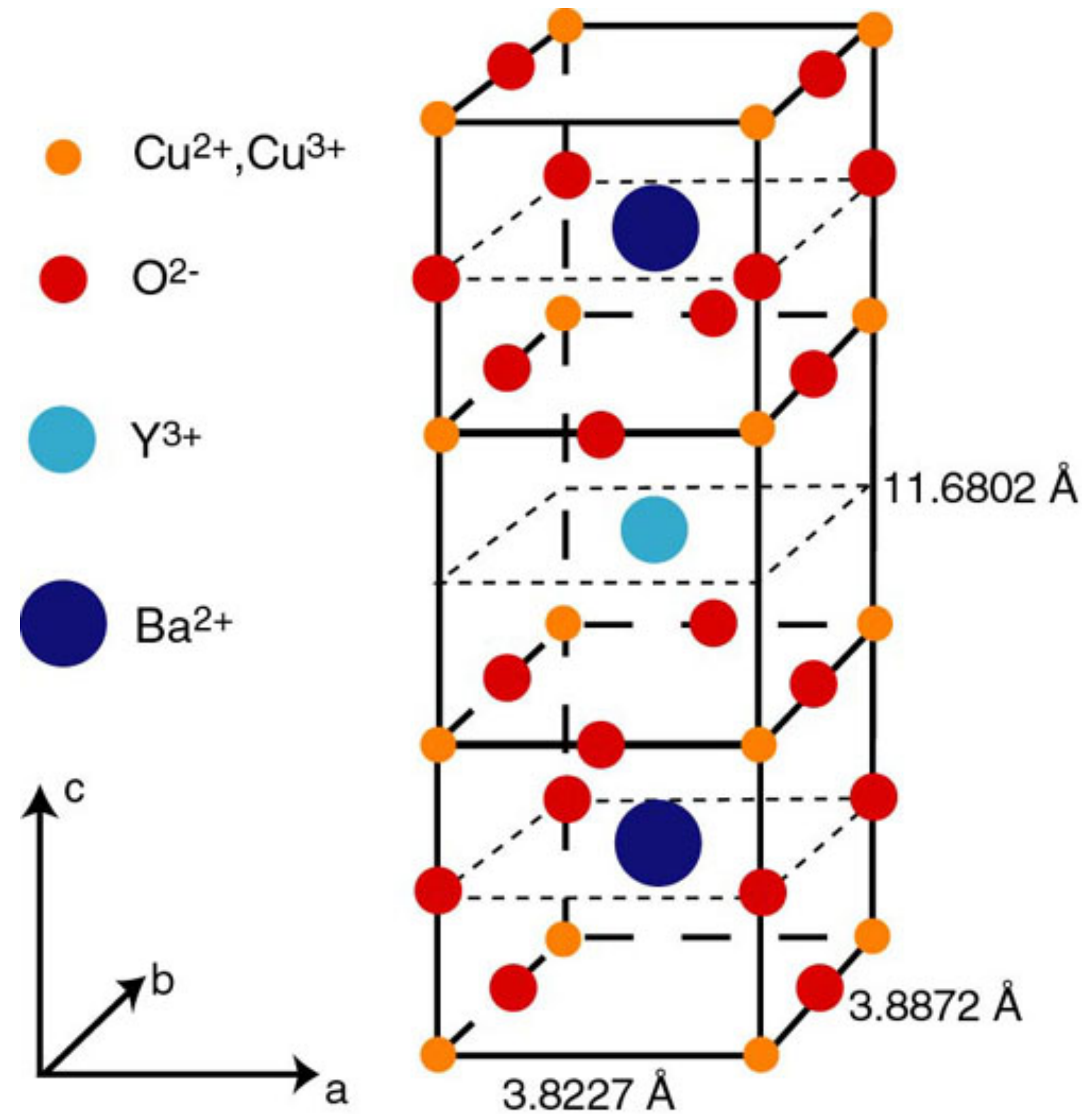
2. Emergent gauge fields and topology

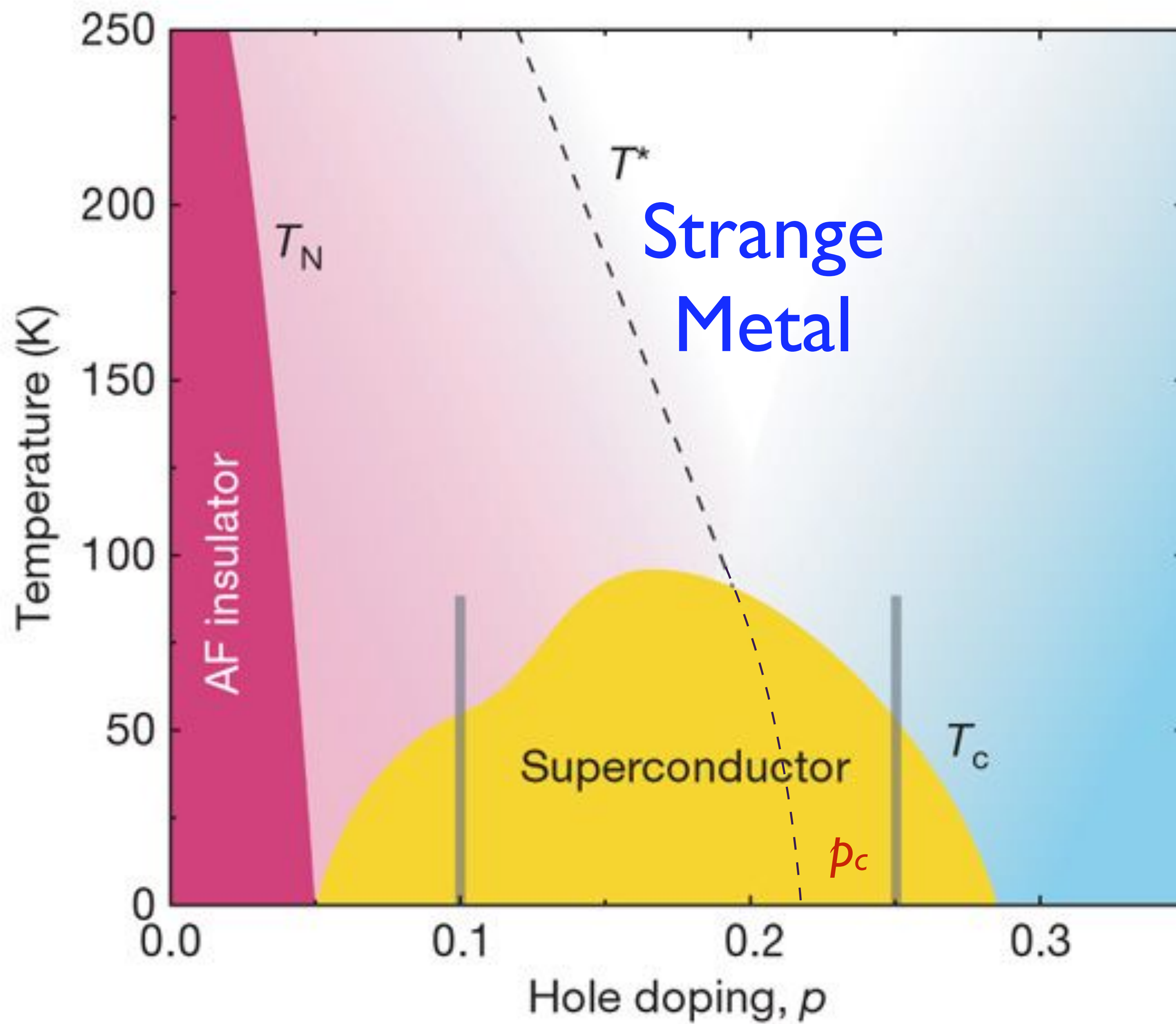
Spin liquids with Rydberg atoms

3. Strange metals

SYK model and emergent gravity

High temperature superconductors



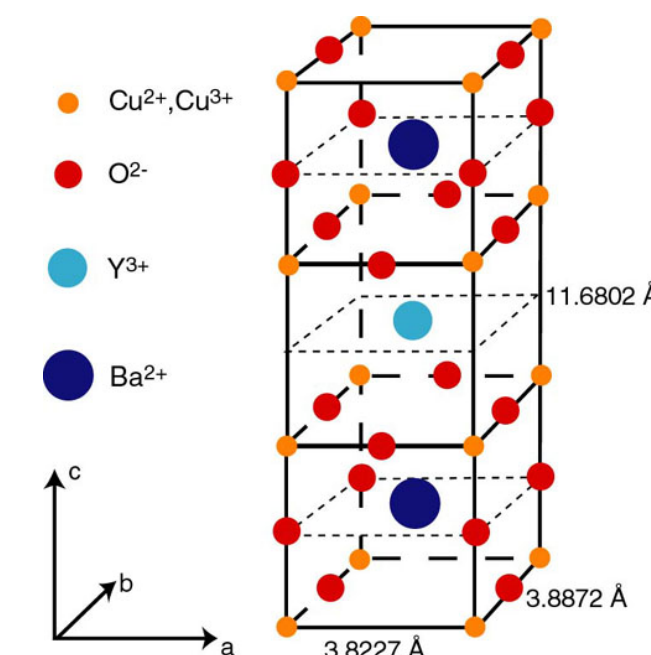


Material		n (10^{27} m^{-3})	m^* (m_0)	A_1 / d (Ω / K)	$h / (2e^2 T_F)$ (Ω / K)	α
Bi2212	$p = 0.23$	6.8	8.4 ± 1.6	8.0 ± 0.9	7.4 ± 1.4	1.1 ± 0.3
Bi2201	$p \sim 0.4$	3.5	7 ± 1.5	8 ± 2	8 ± 2	1.0 ± 0.4
LSCO	$p = 0.26$	7.8	9.8 ± 1.7	8.2 ± 1.0	8.9 ± 1.8	0.9 ± 0.3
Nd-LSCO	$p = 0.24$	7.9	12 ± 4	7.4 ± 0.8	10.6 ± 3.7	0.7 ± 0.4
PCCO	$x = 0.17$	8.8	2.4 ± 0.1	1.7 ± 0.3	2.1 ± 0.1	0.8 ± 0.2
LCCO	$x = 0.15$	9.0	3.0 ± 0.3	3.0 ± 0.45	2.6 ± 0.3	1.2 ± 0.3
TMTSF	$P = 11 \text{ kbar}$	1.4	1.15 ± 0.2	2.8 ± 0.3	2.8 ± 0.4	1.0 ± 0.3

Electron scattering time τ in 7 different strange metals

$$\frac{1}{\tau} = \alpha \frac{k_B T}{\hbar}$$

Current flow without quasiparticles

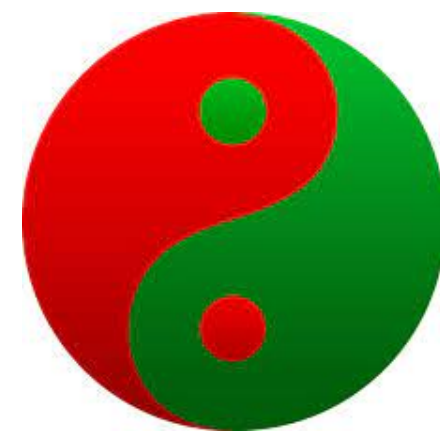


The Sachdev-Ye-Kitaev (SYK) model

The SYK model has a scale-invariant entanglement structure:
i.e. electrons are entangled at all distance and time scales

In one set of variables, it describes certain ***strange metals***

Sachdev, Ye (1993)

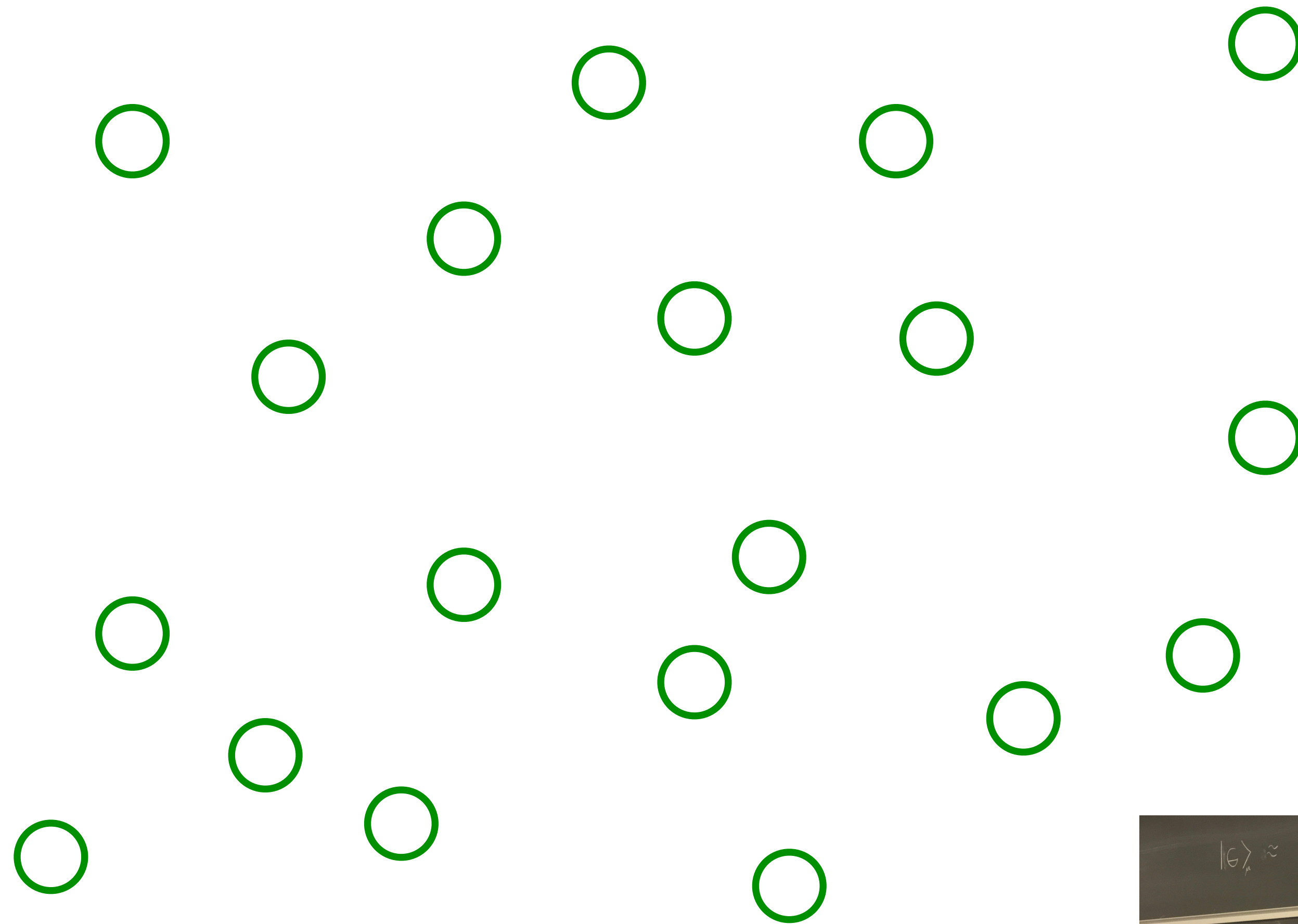


In a ***dual*** set of variables it describes certain ***black holes***

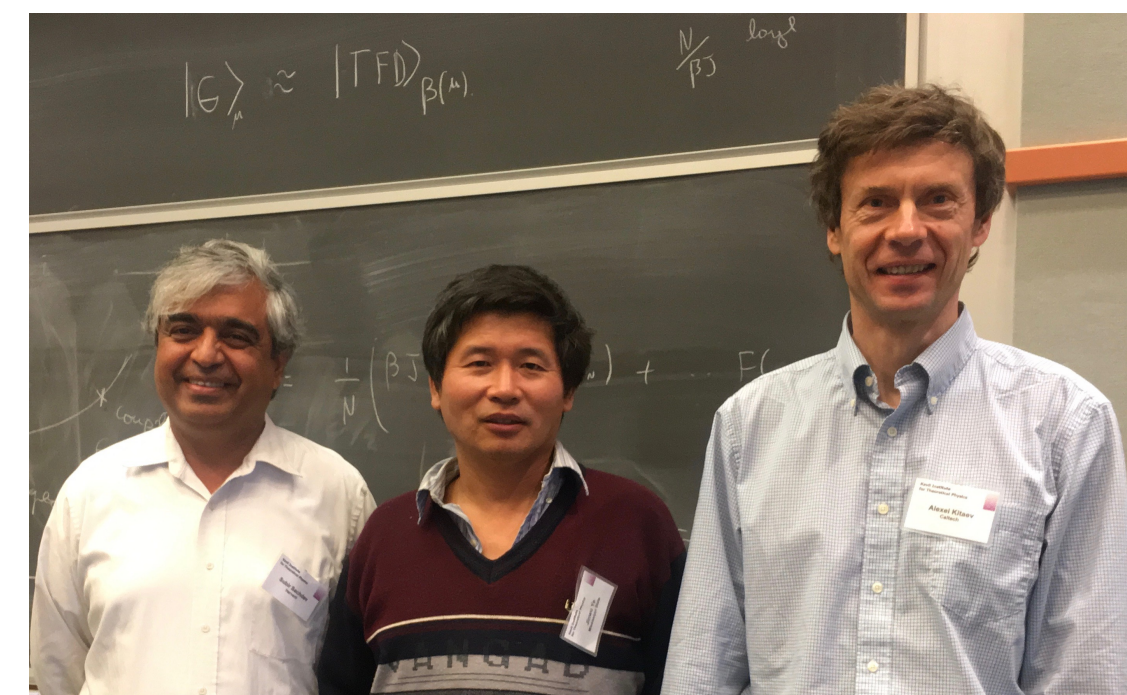
Sachdev (2010), Kitaev (2015), Maldacena Stanford (2015)

The Sachdev-Ye-Kitaev (SYK) model

Sachdev, Ye (1993); Kitaev (2015)

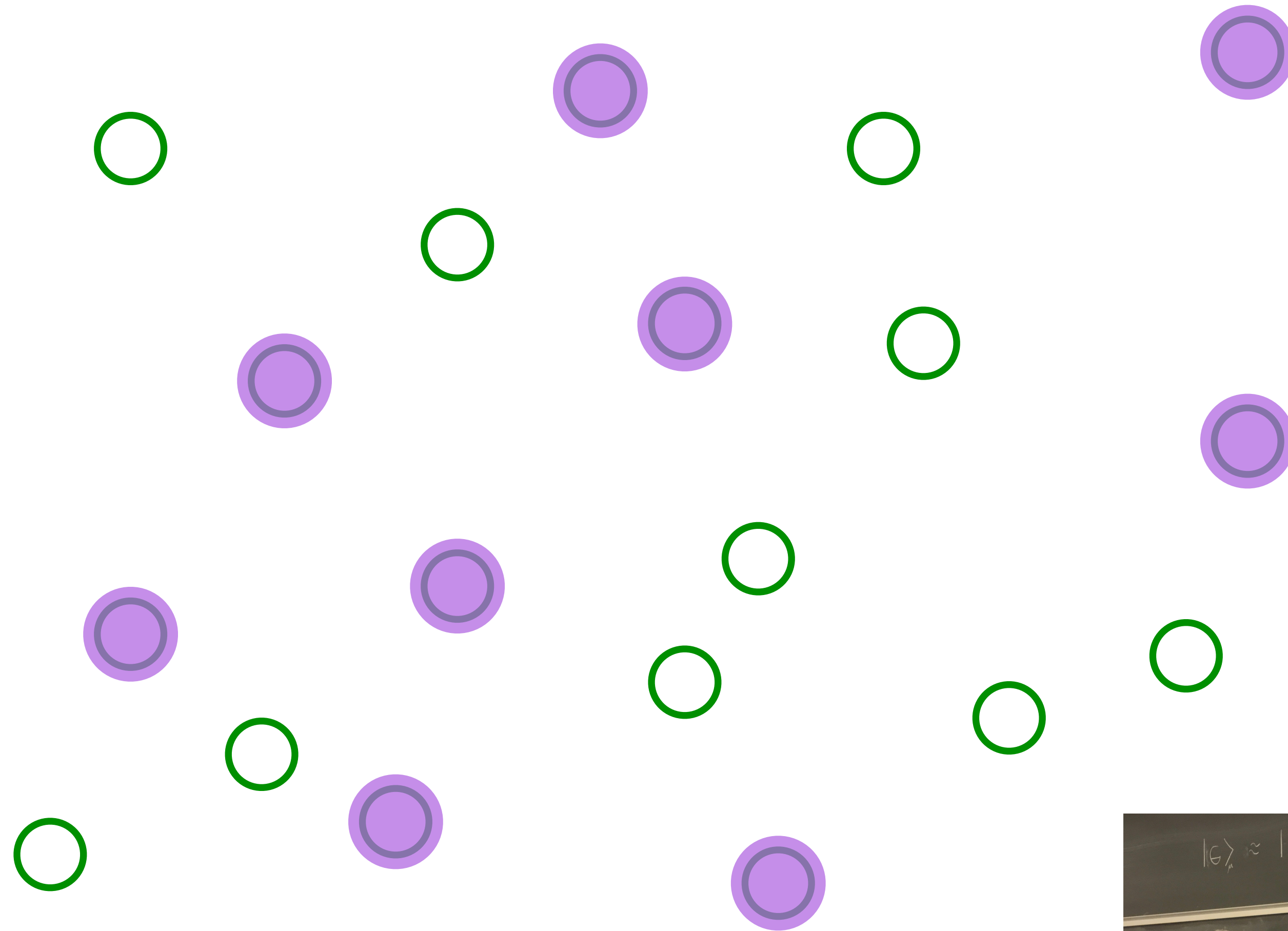


Pick a set of random positions

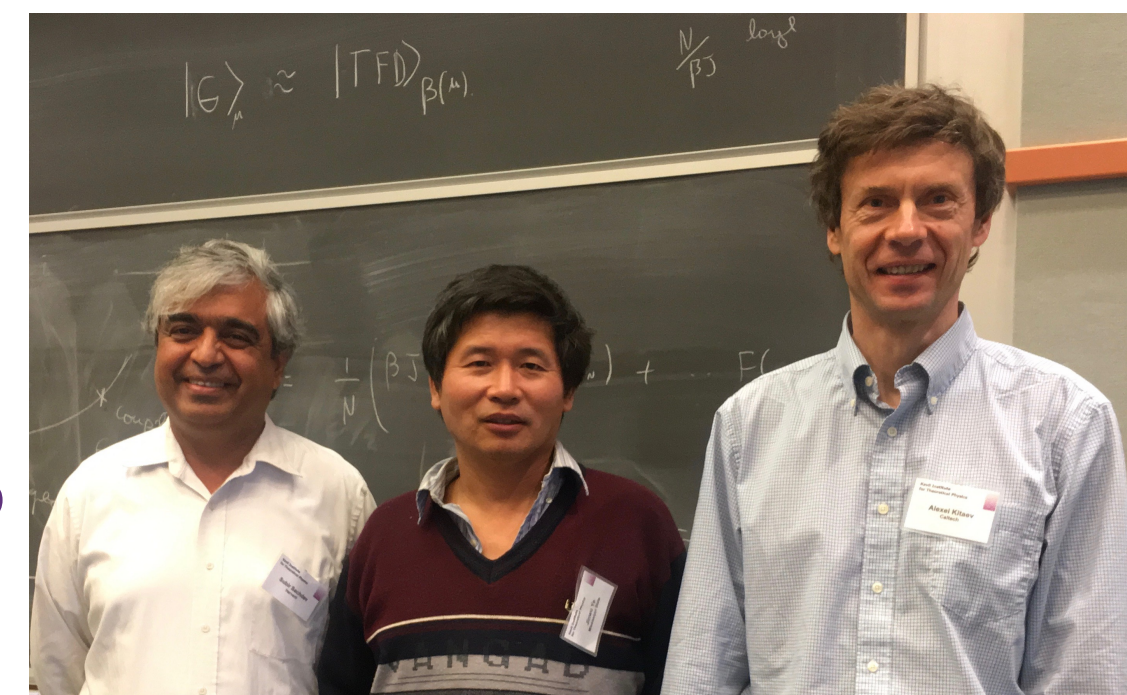


The SYK model

Sachdev, Ye (1993); Kitaev (2015)

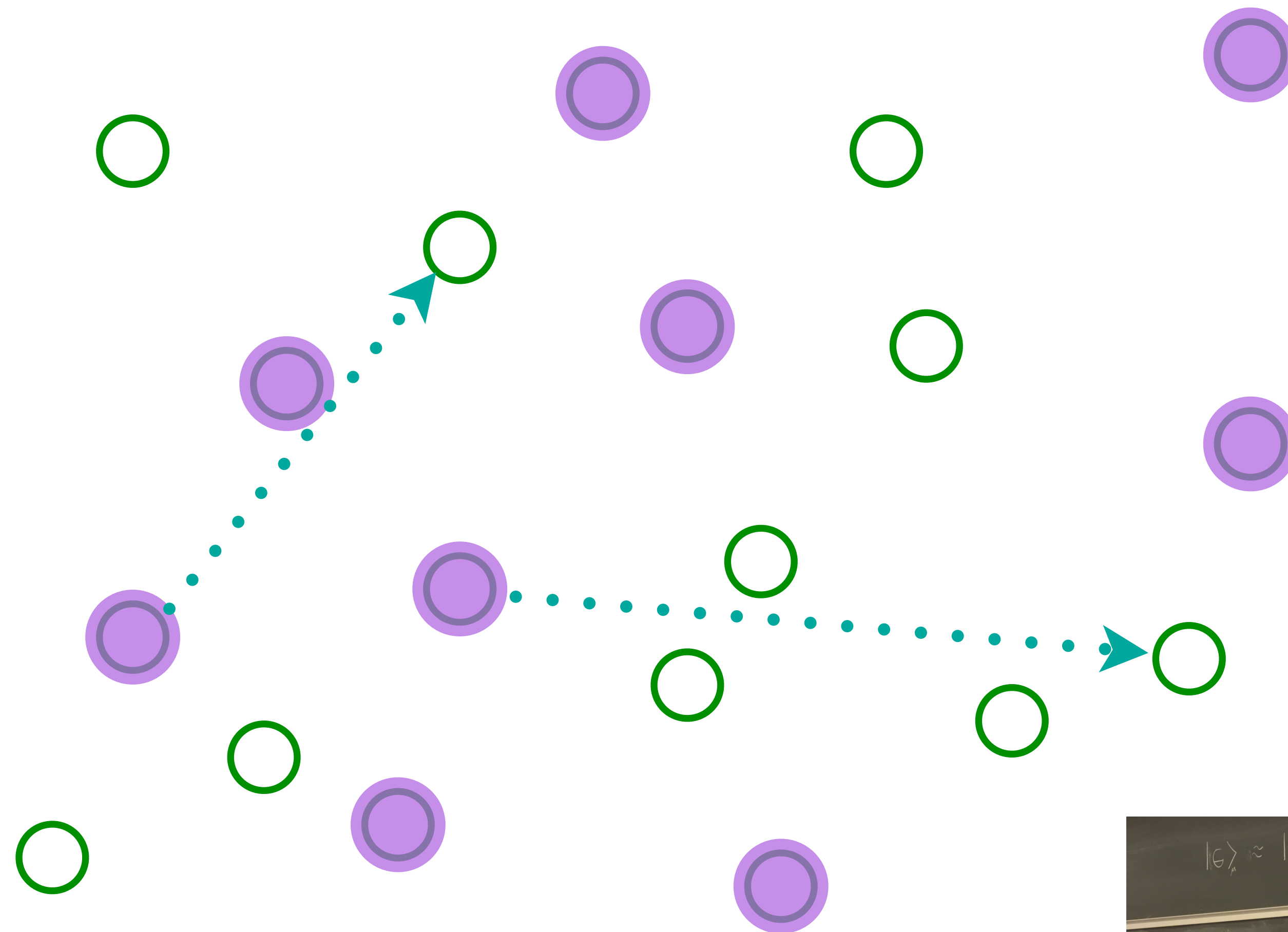


Place electrons randomly on some sites

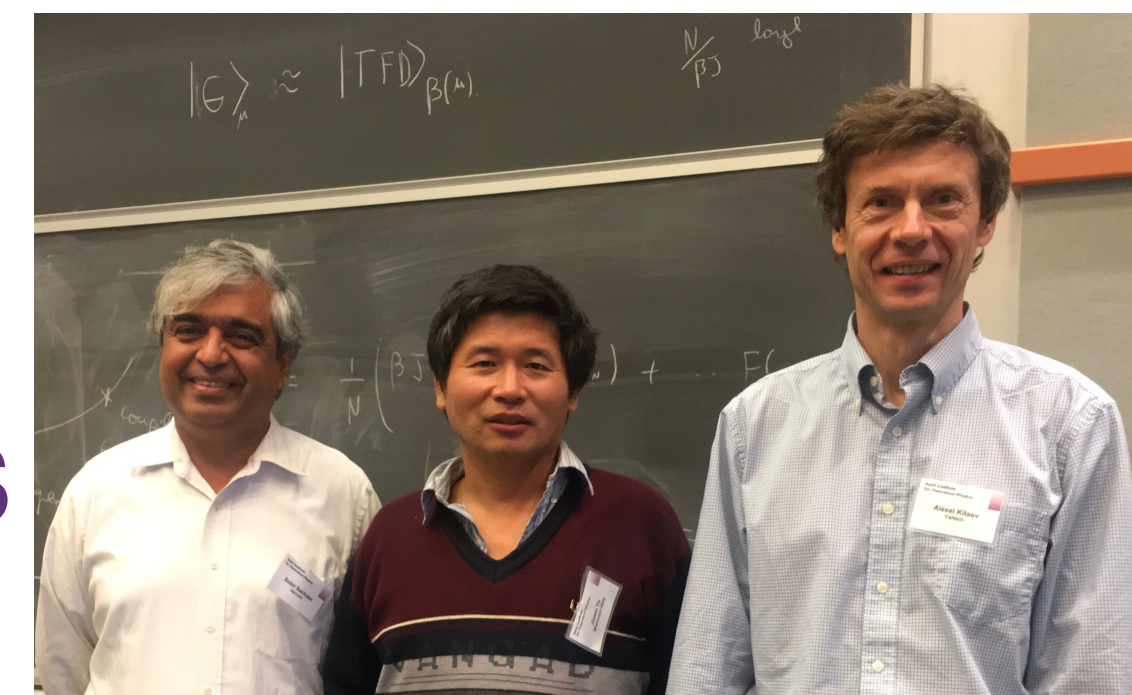


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Sachdev, Ye (1993); Kitaev (2015)

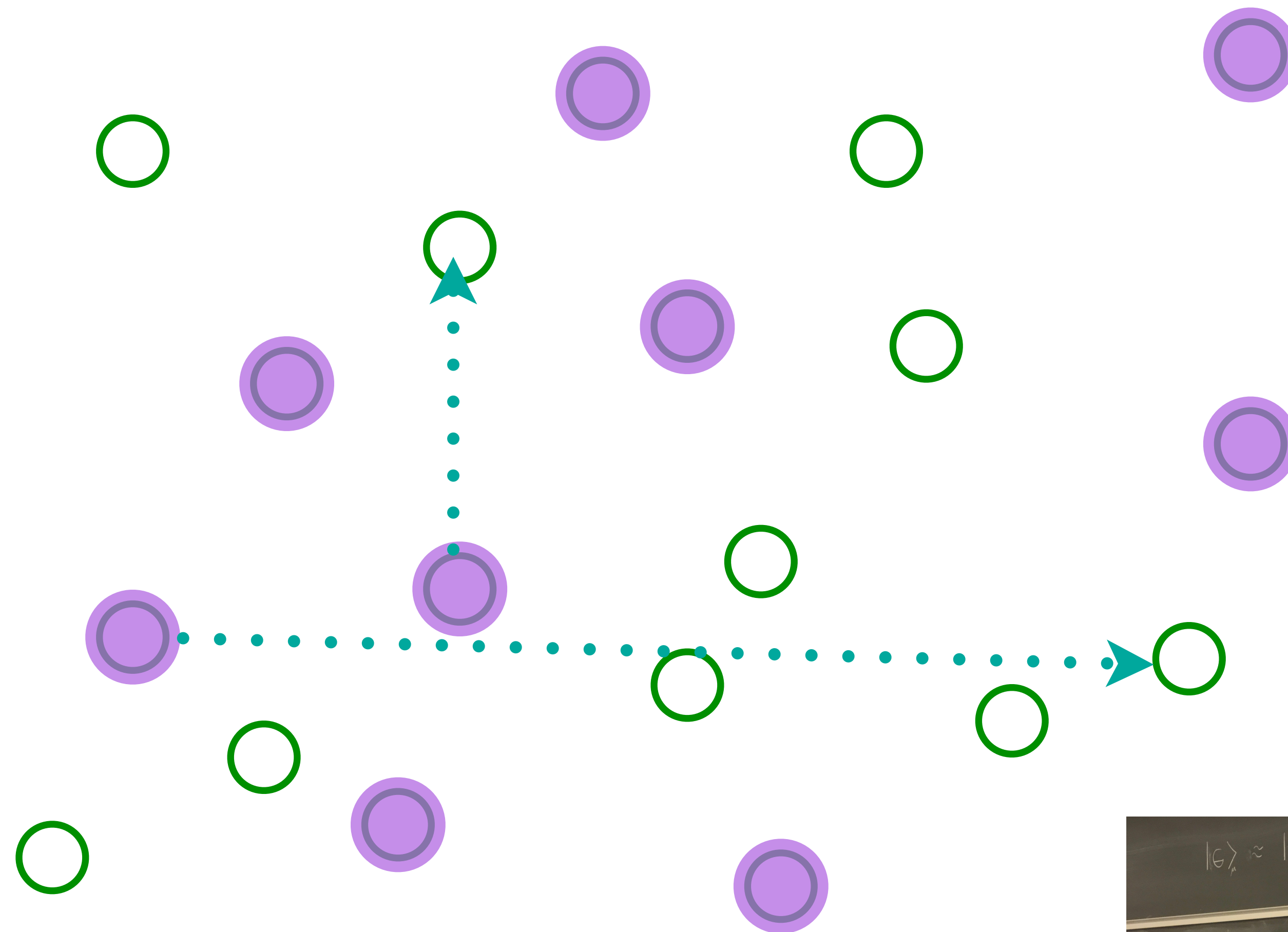


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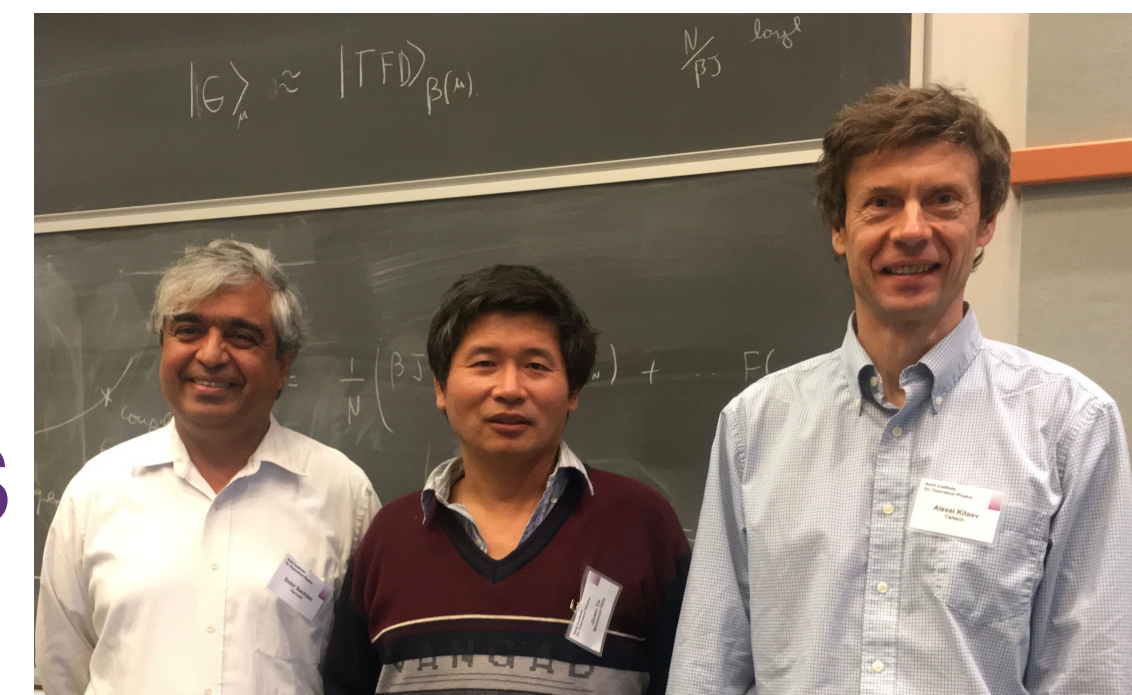


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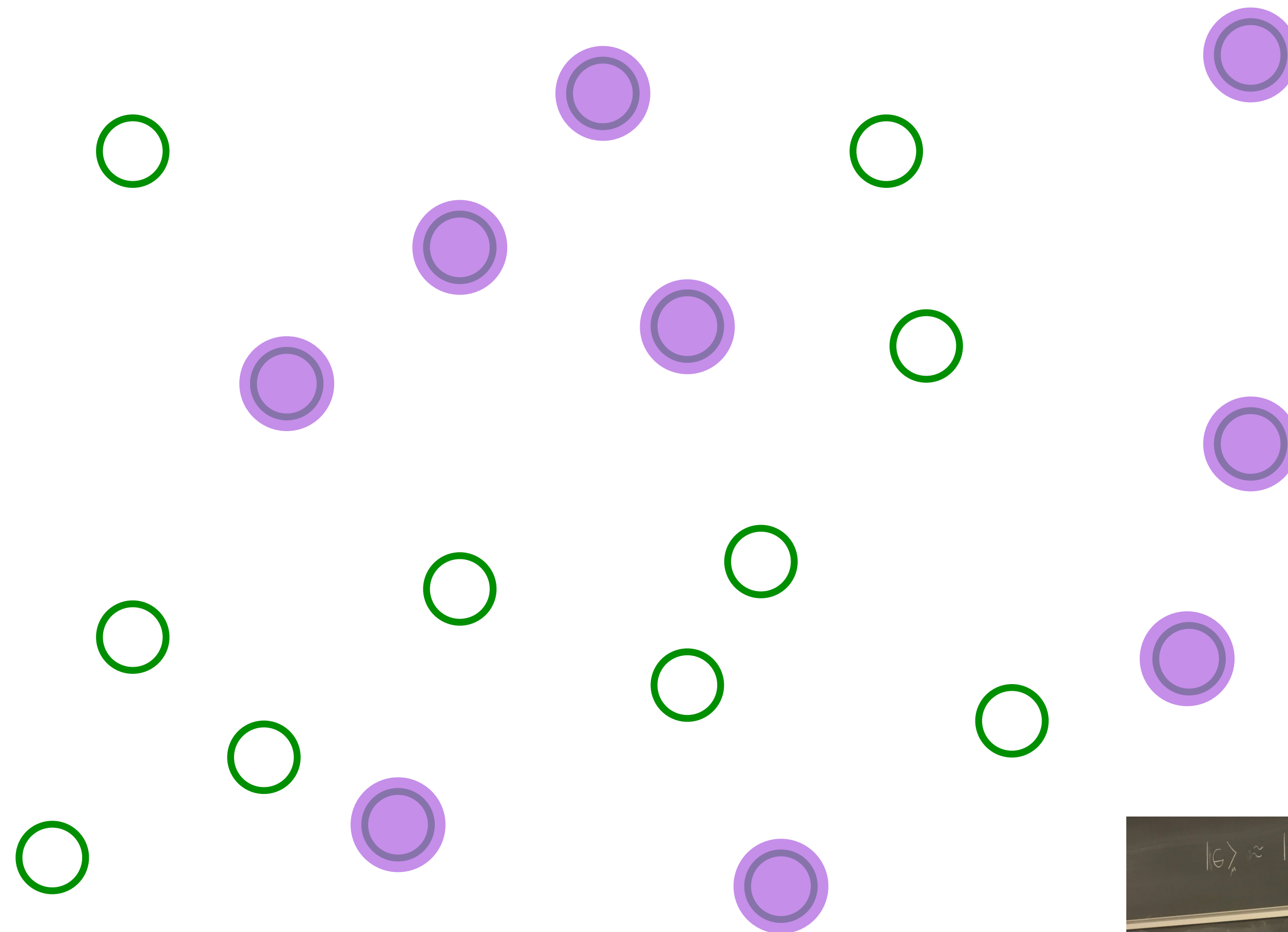


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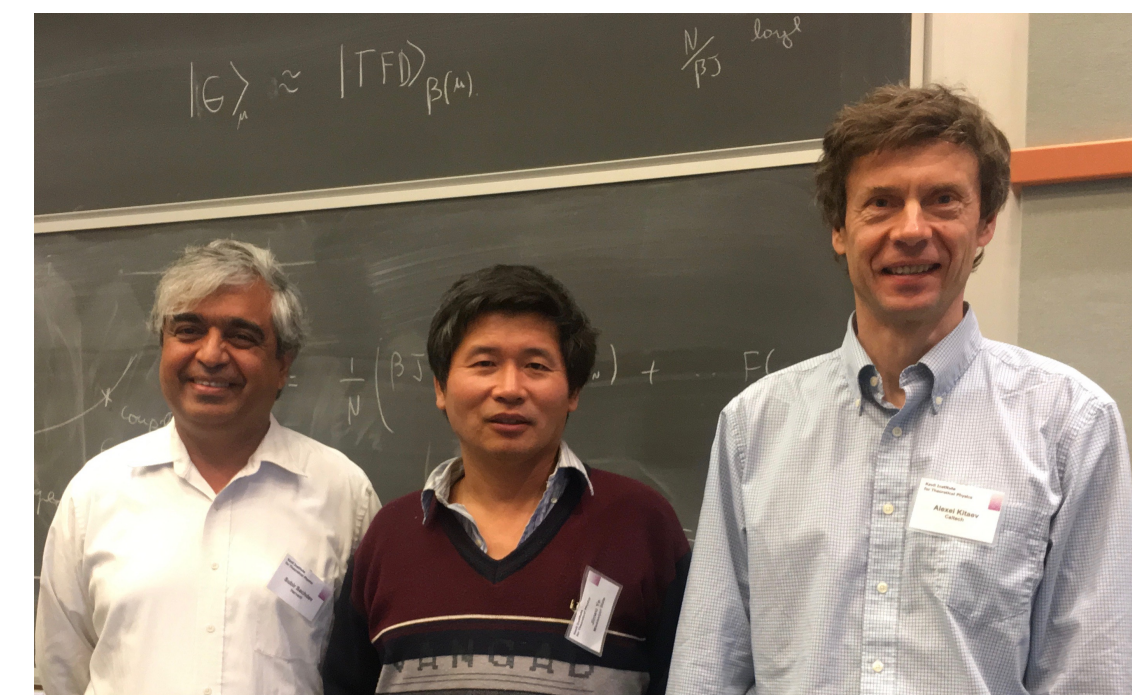


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Sachdev, Ye (1993); Kitaev (2015)

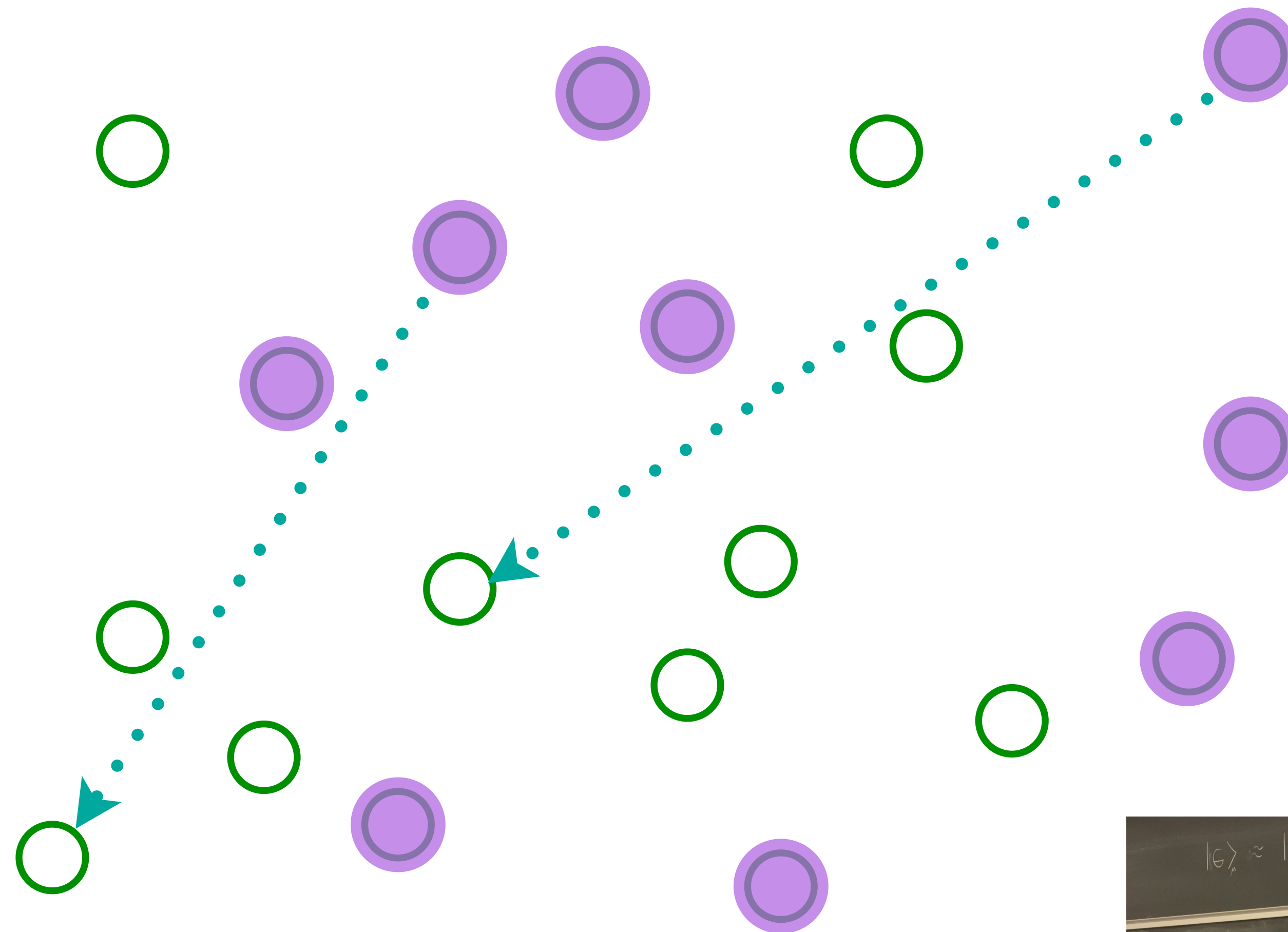


Entangle electrons pairwise randomly

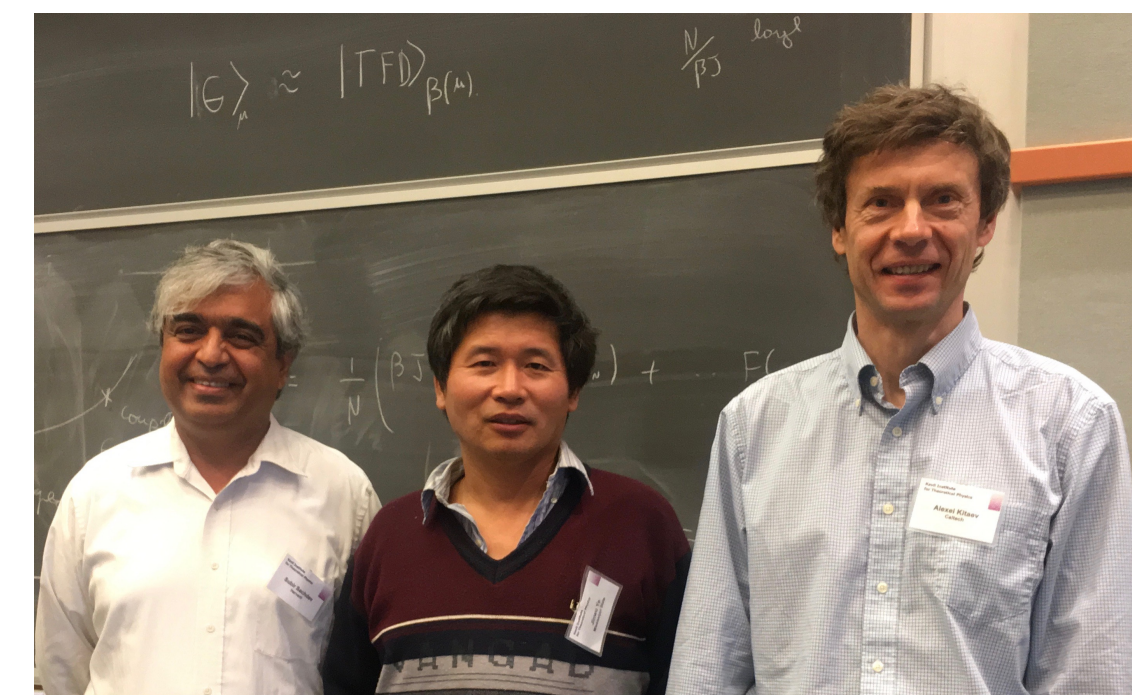


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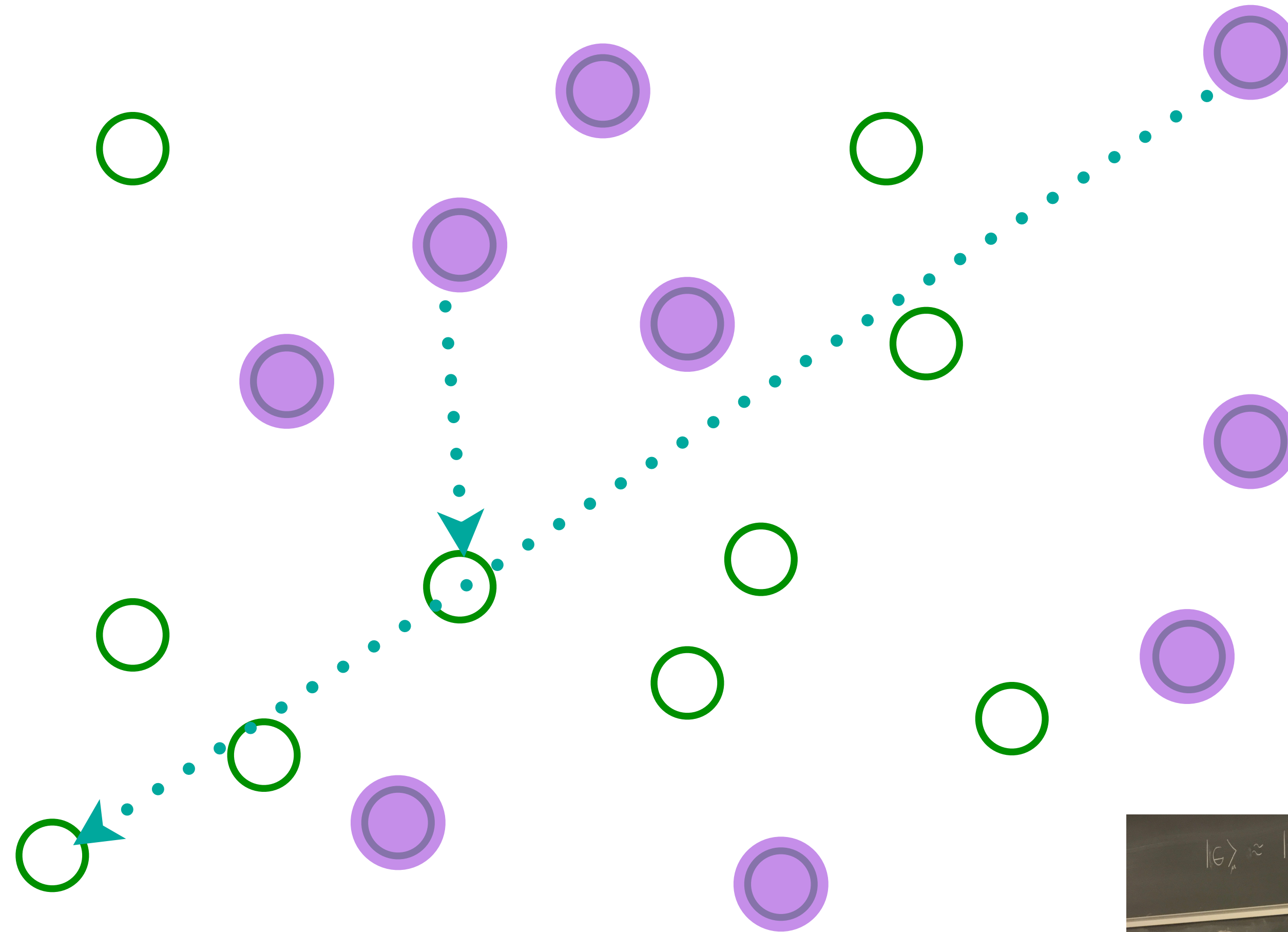


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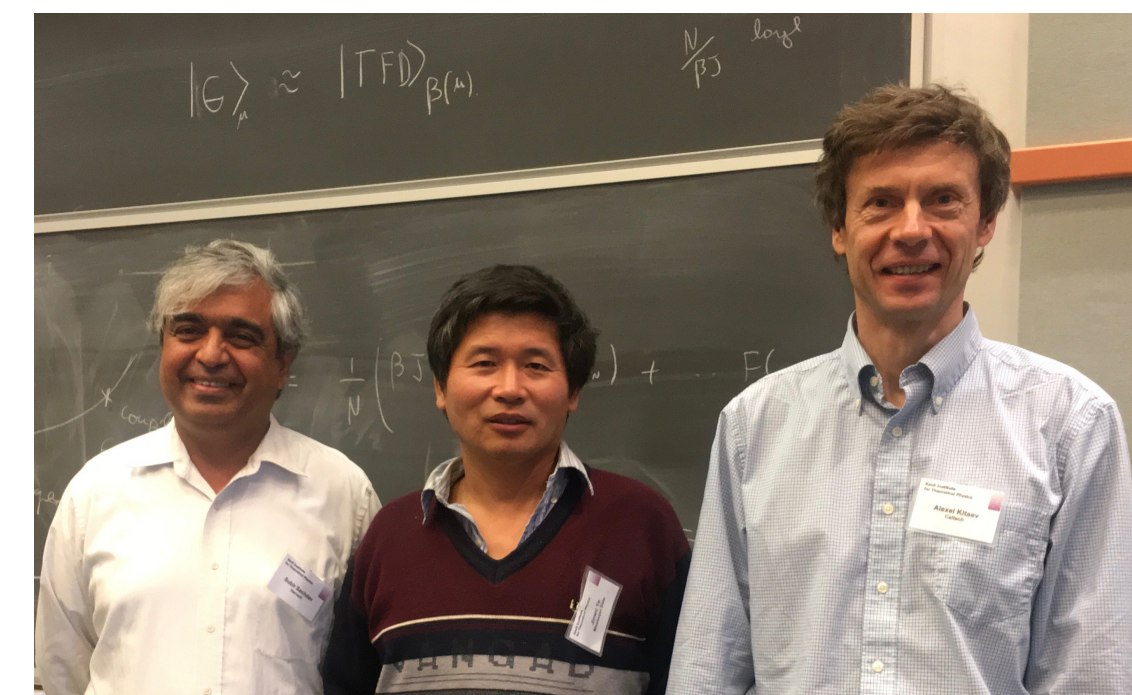


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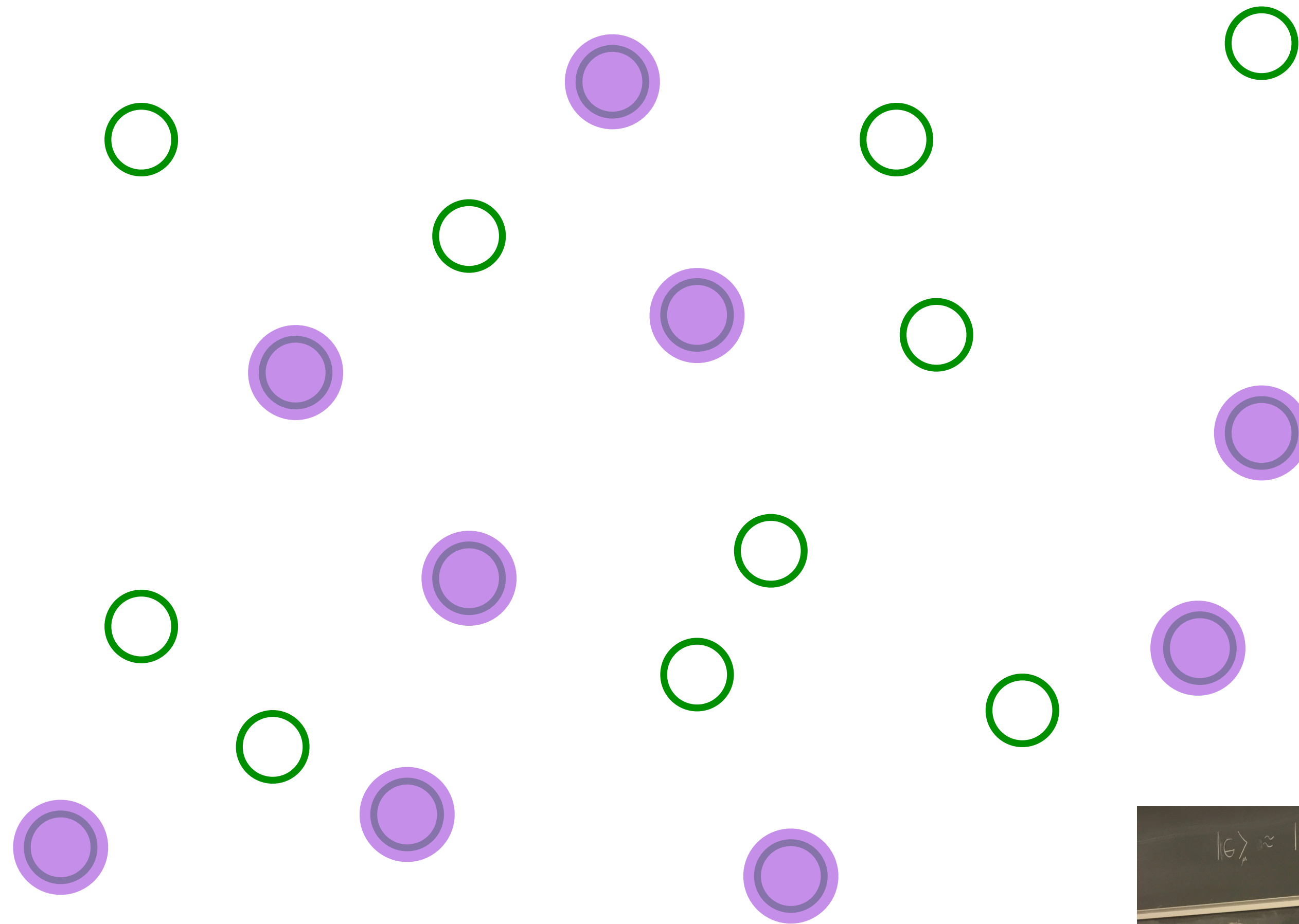


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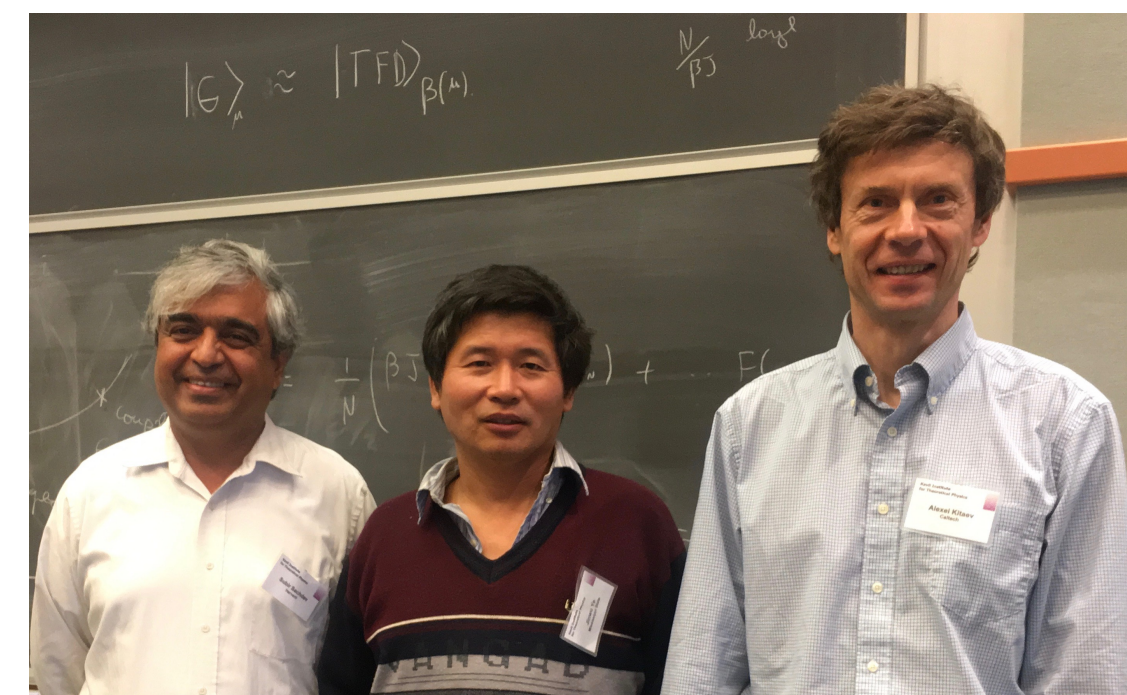


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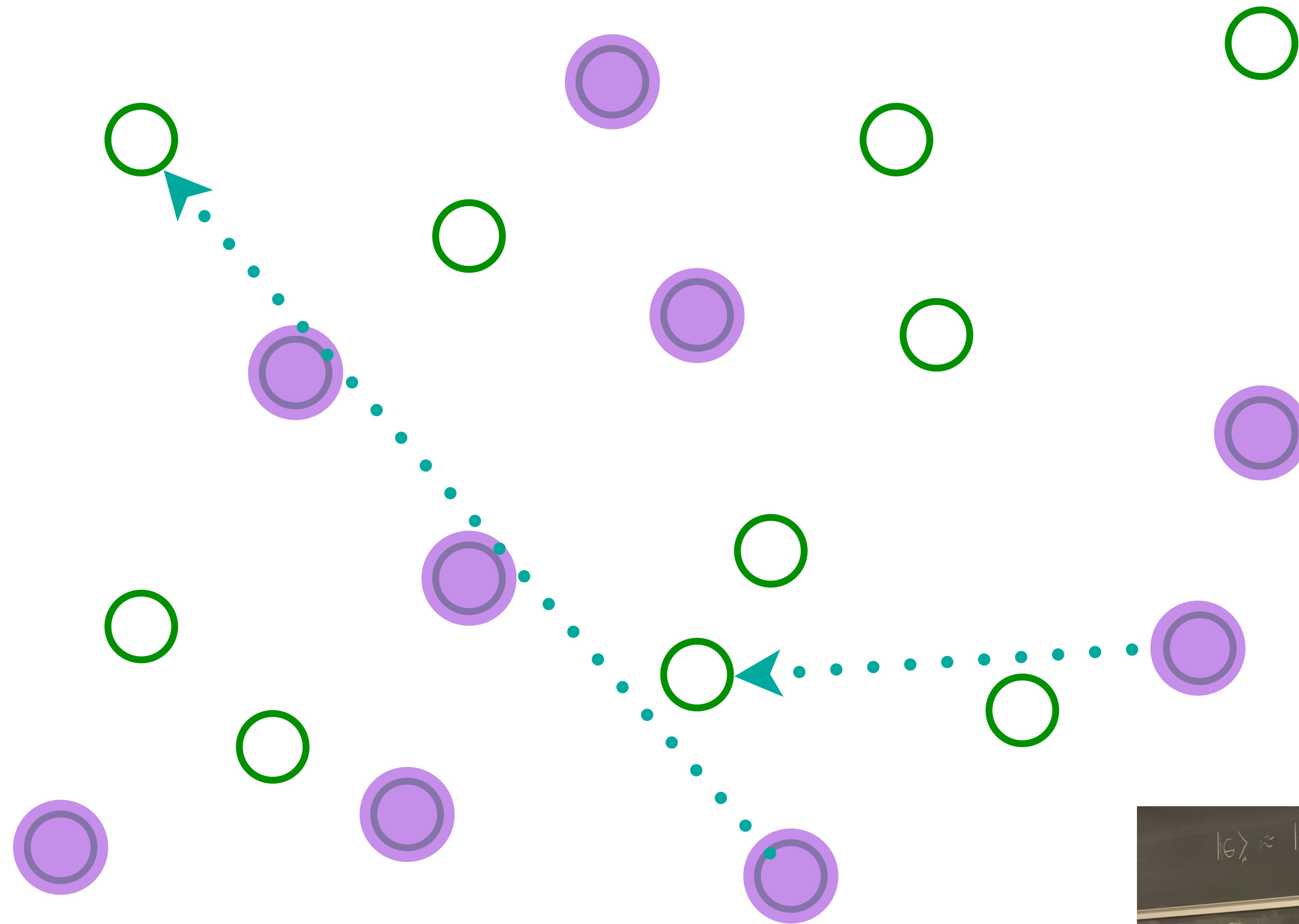


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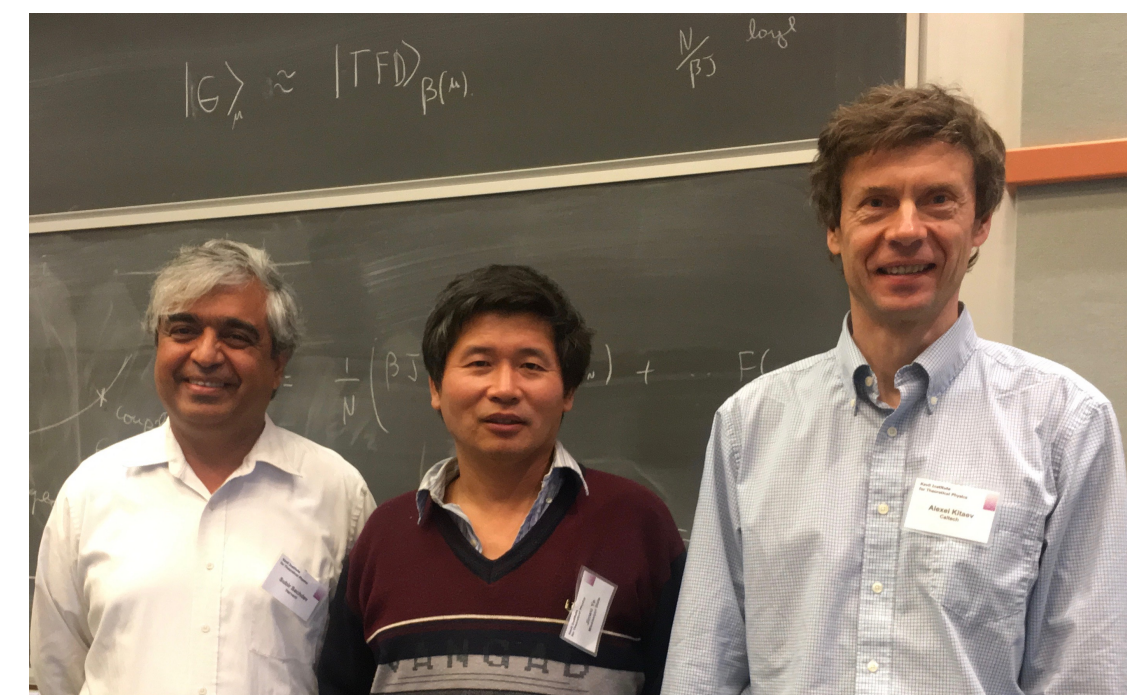


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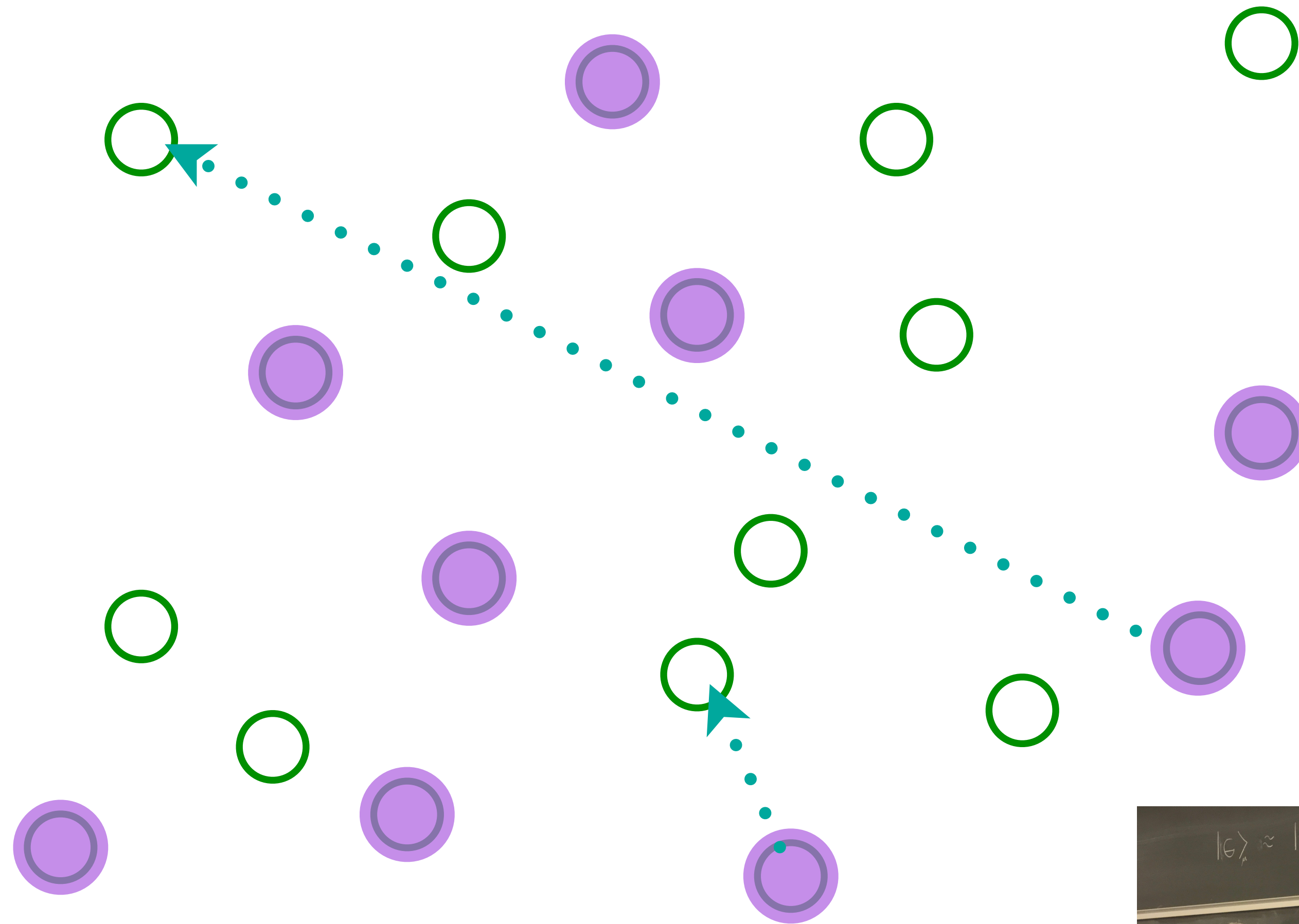


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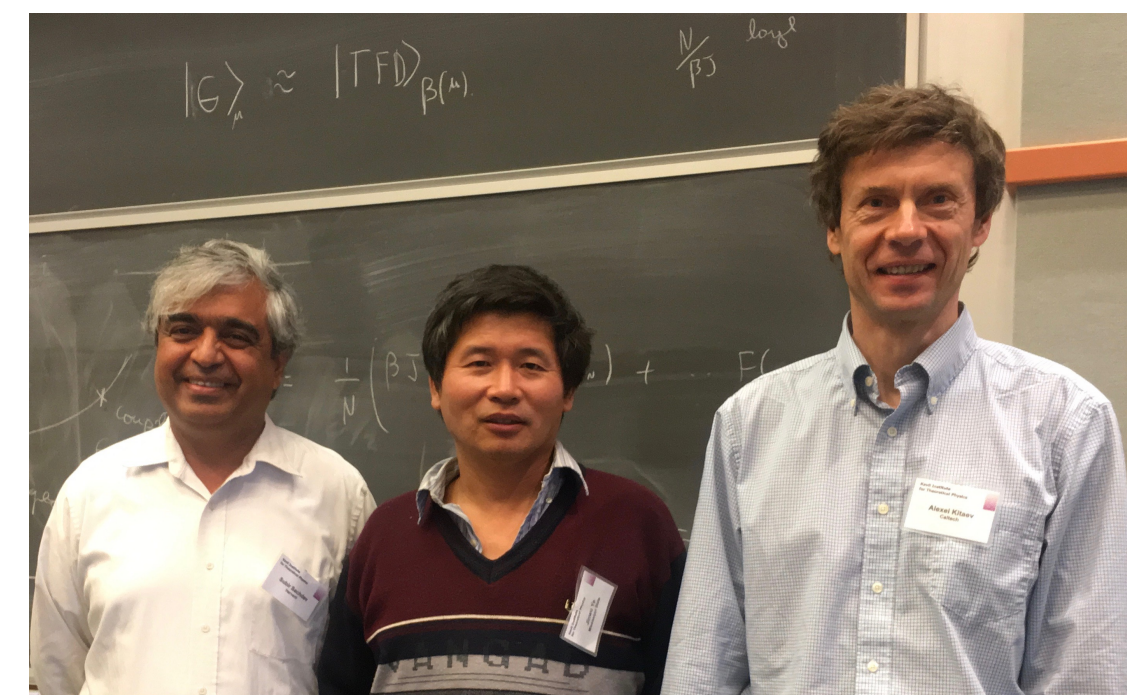


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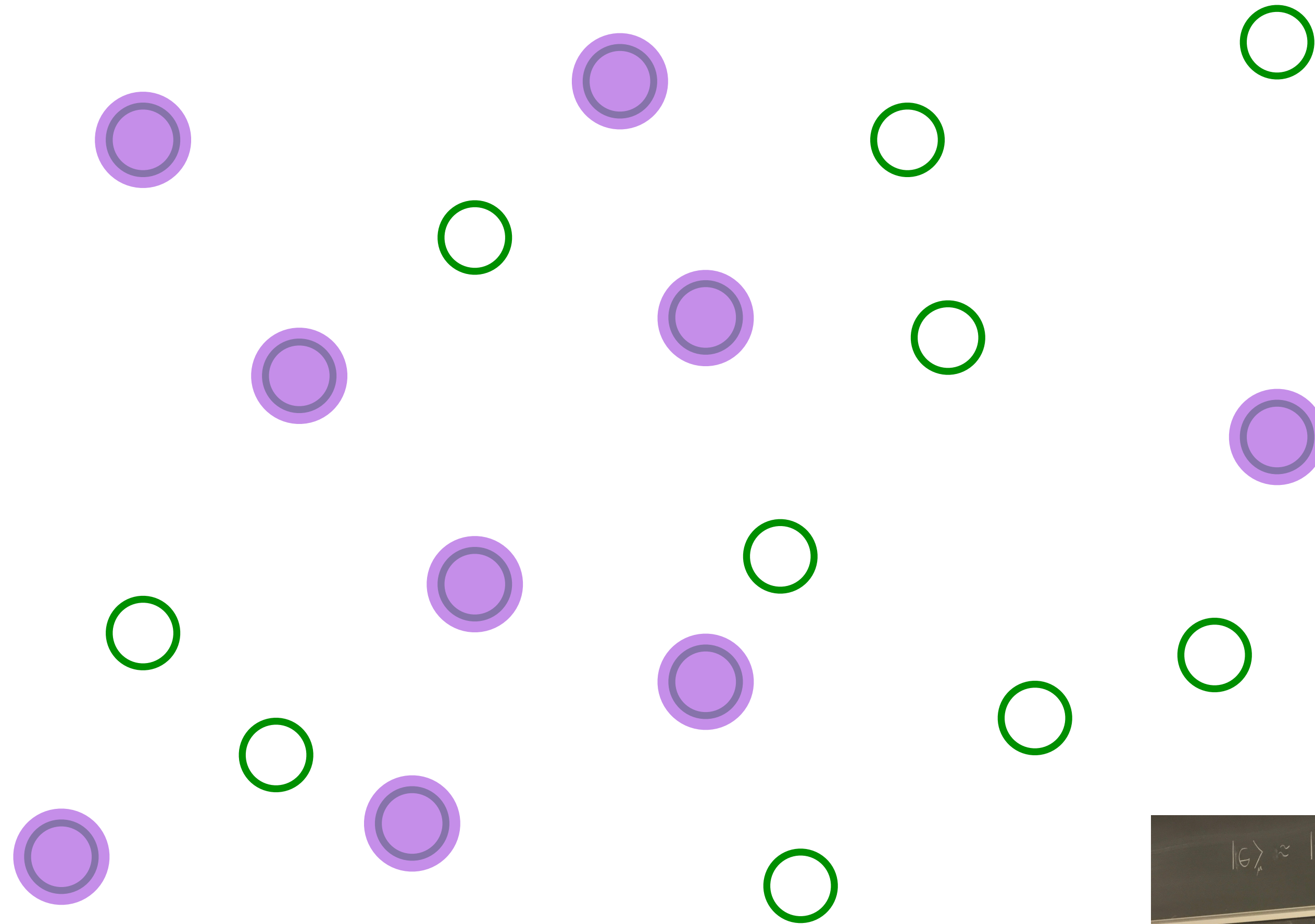


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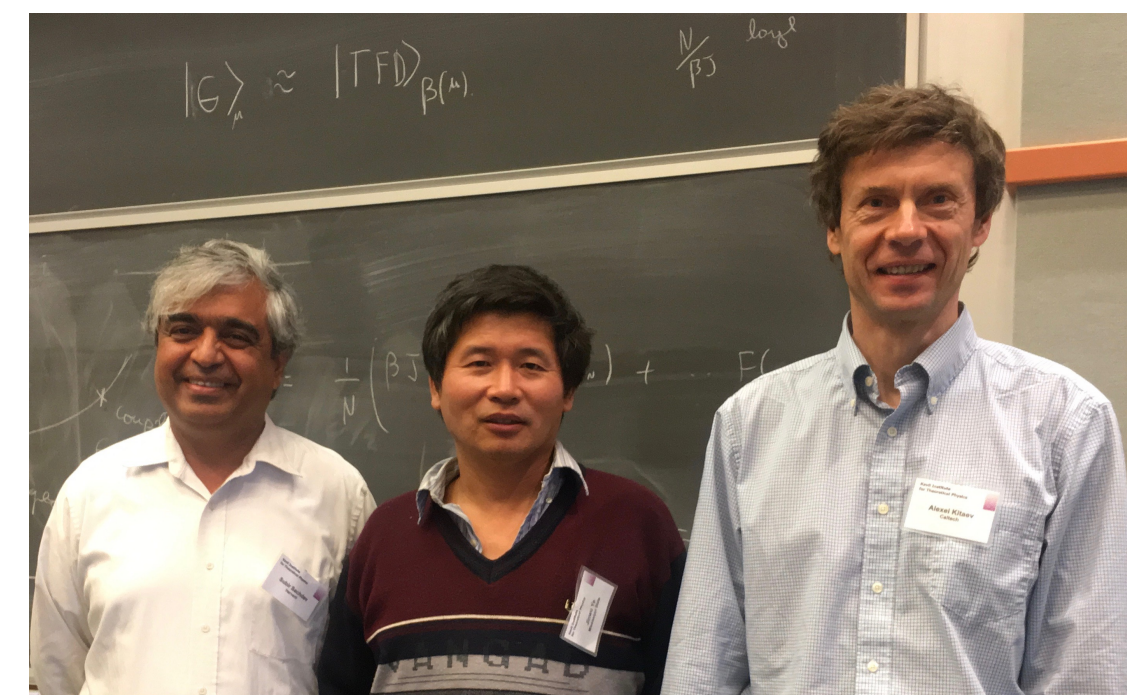


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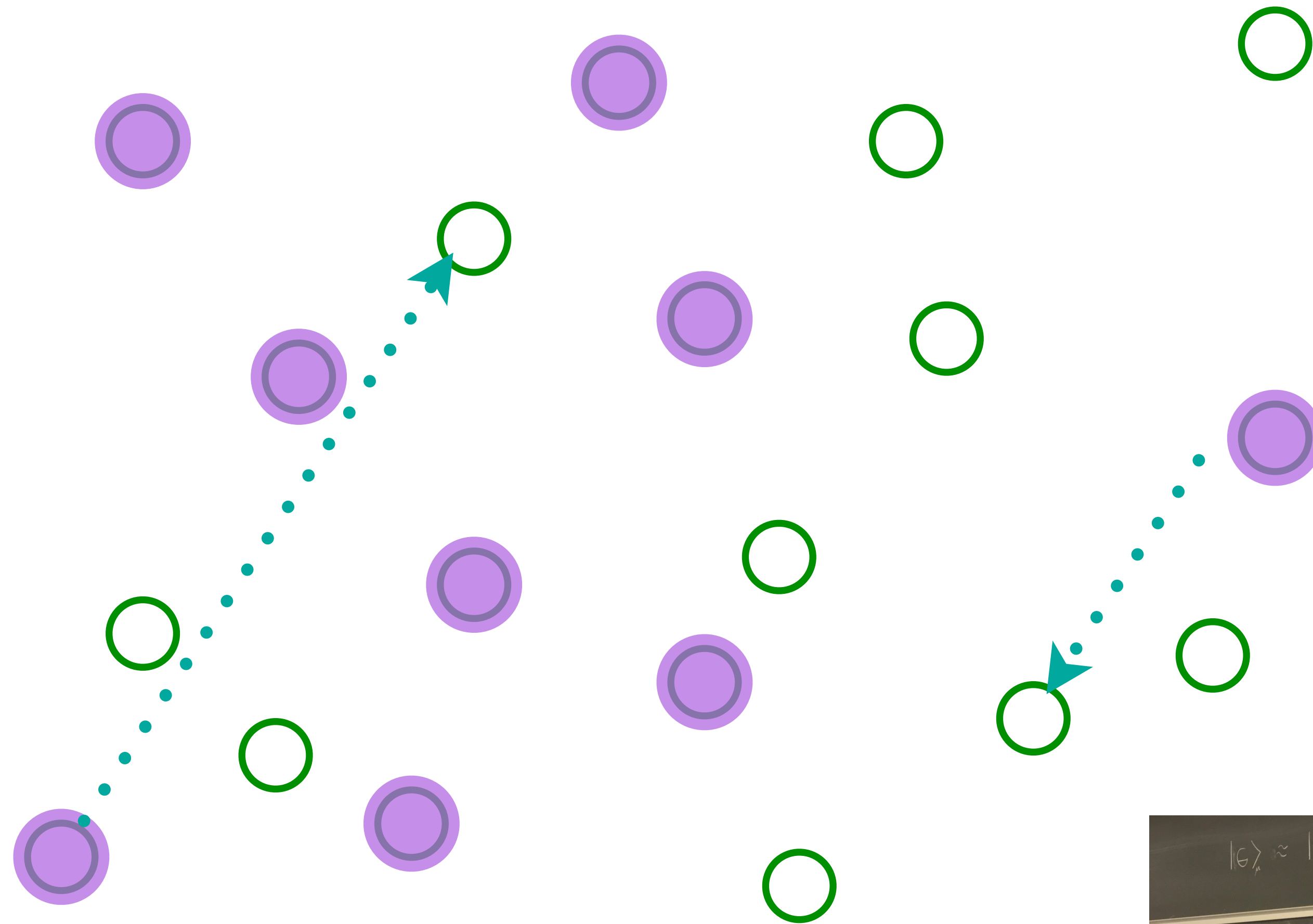


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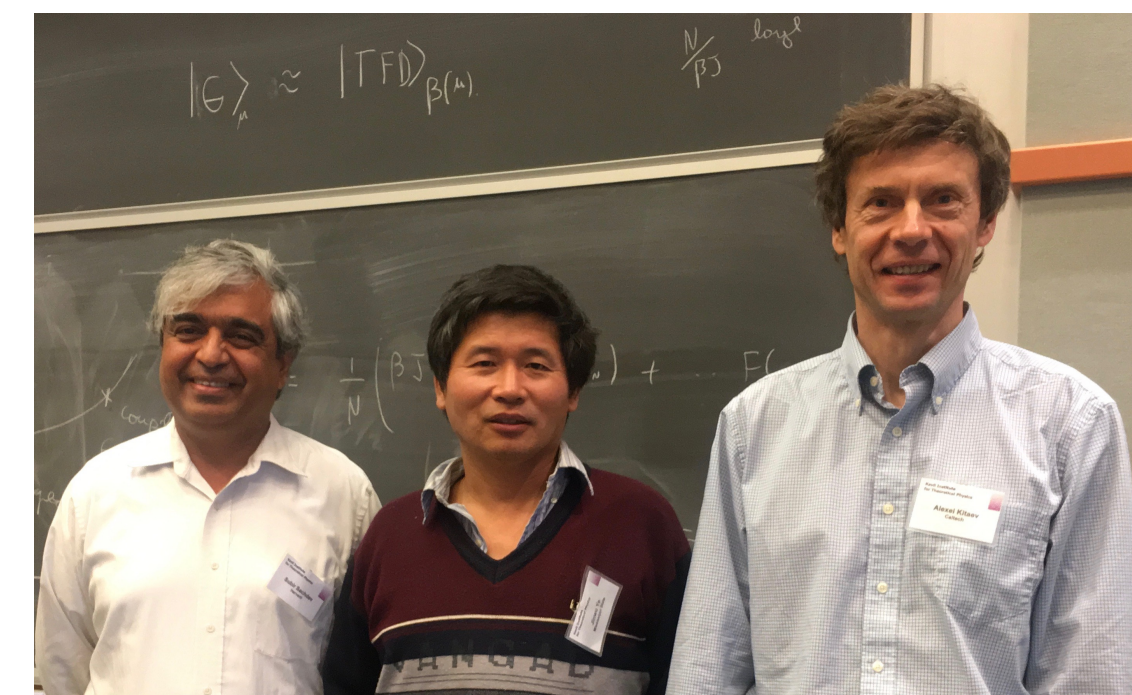


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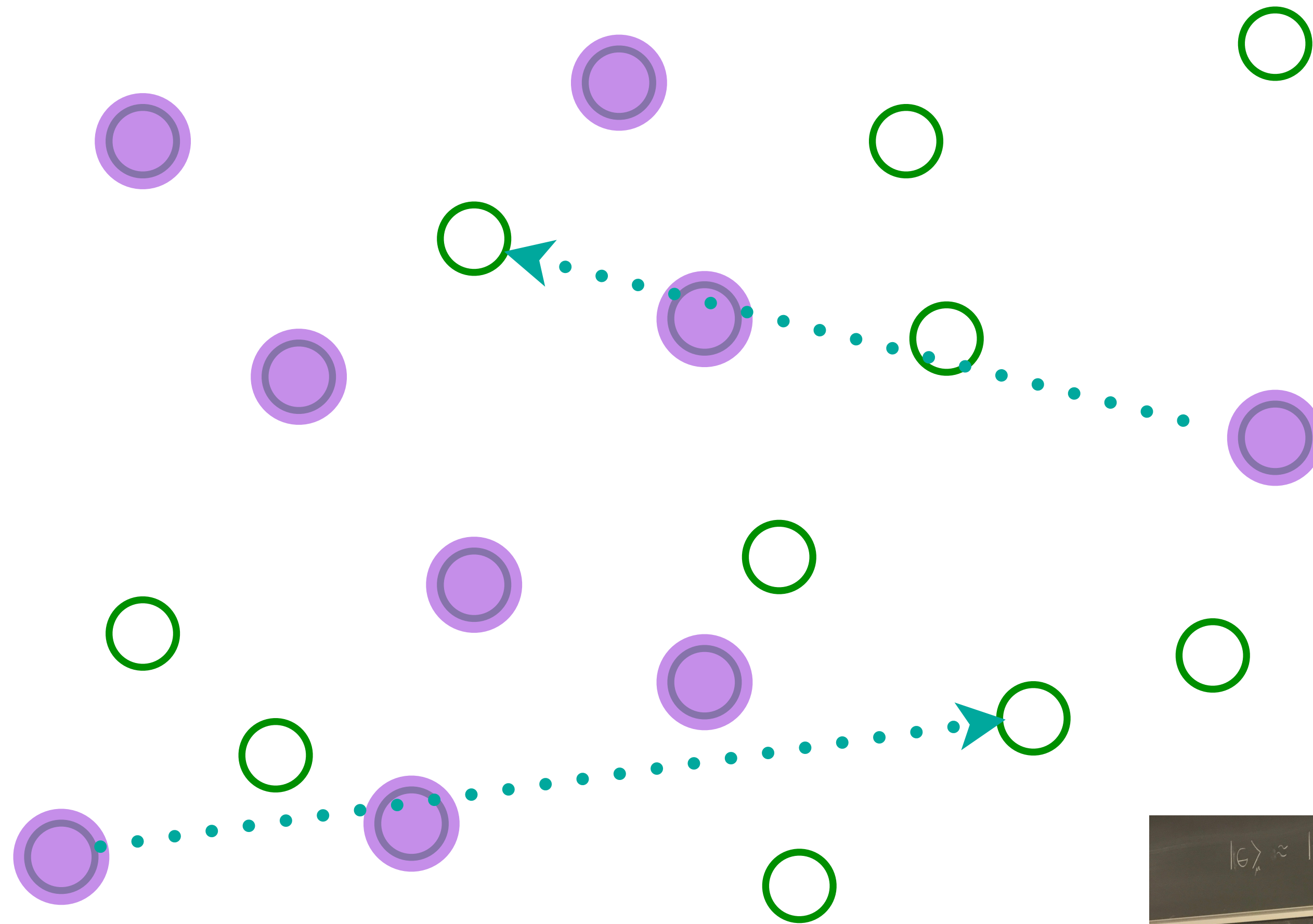


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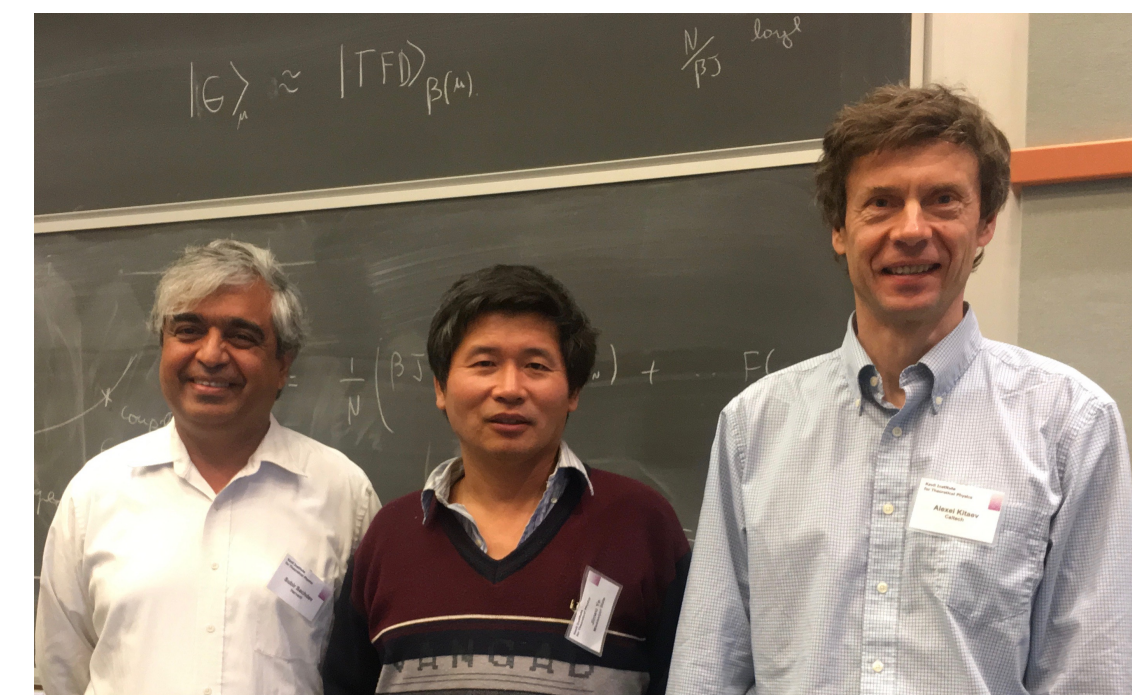


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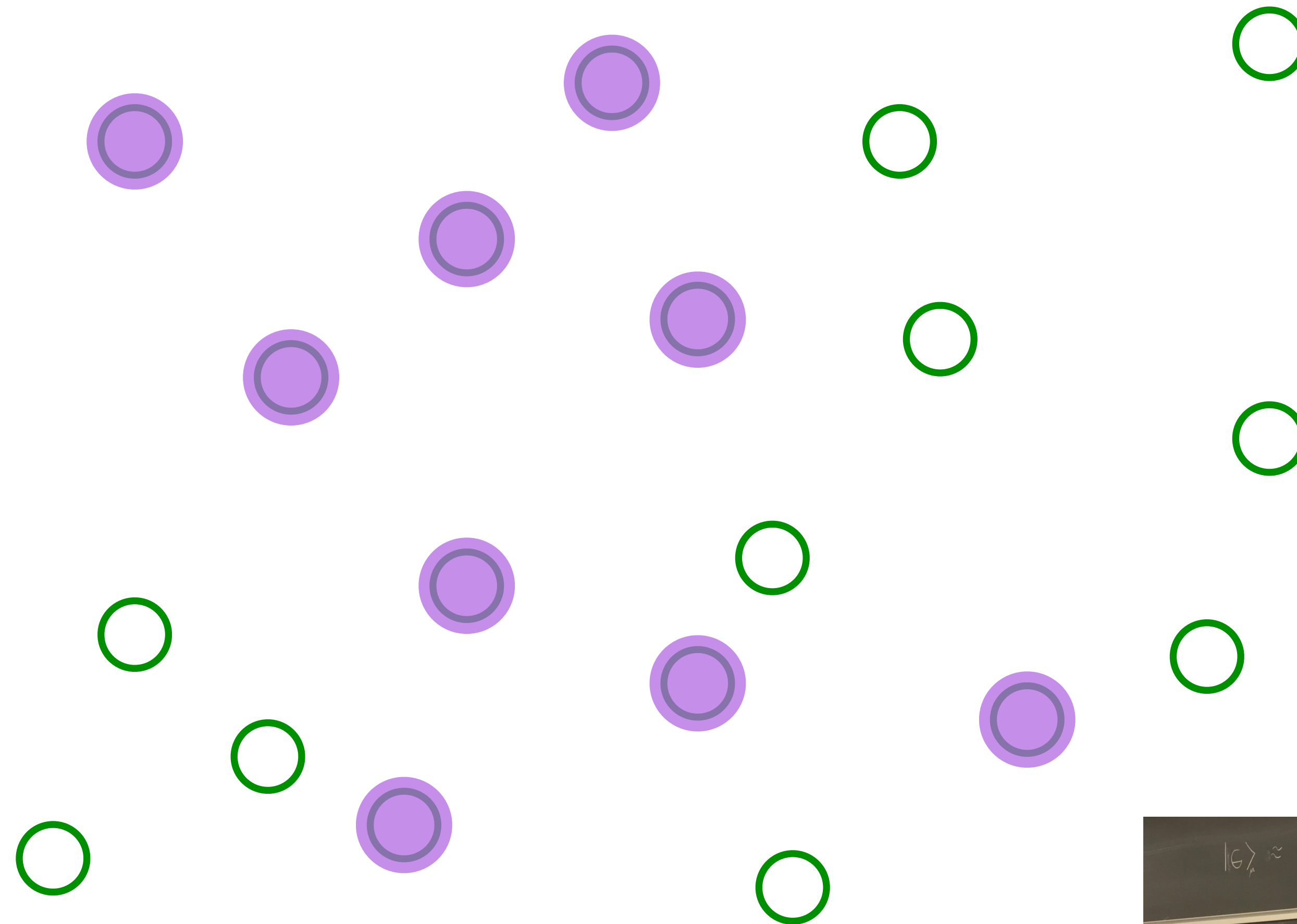


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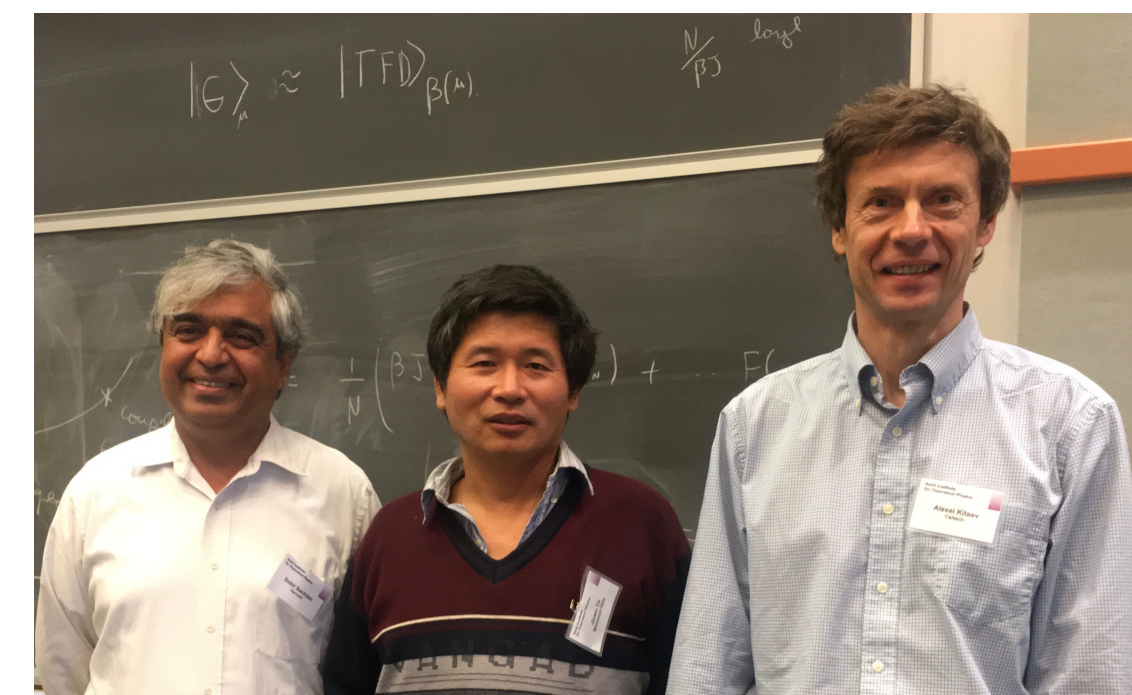


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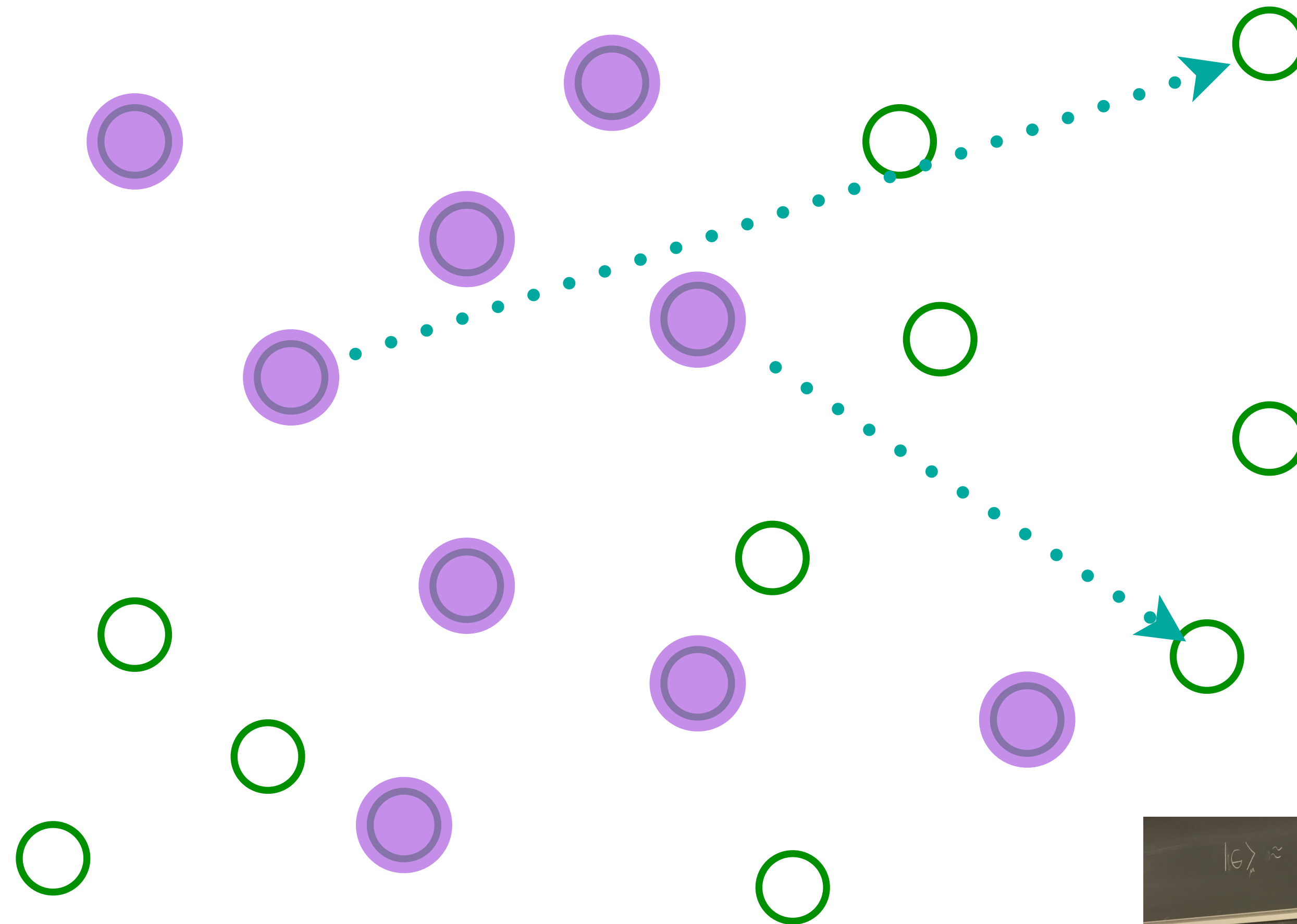


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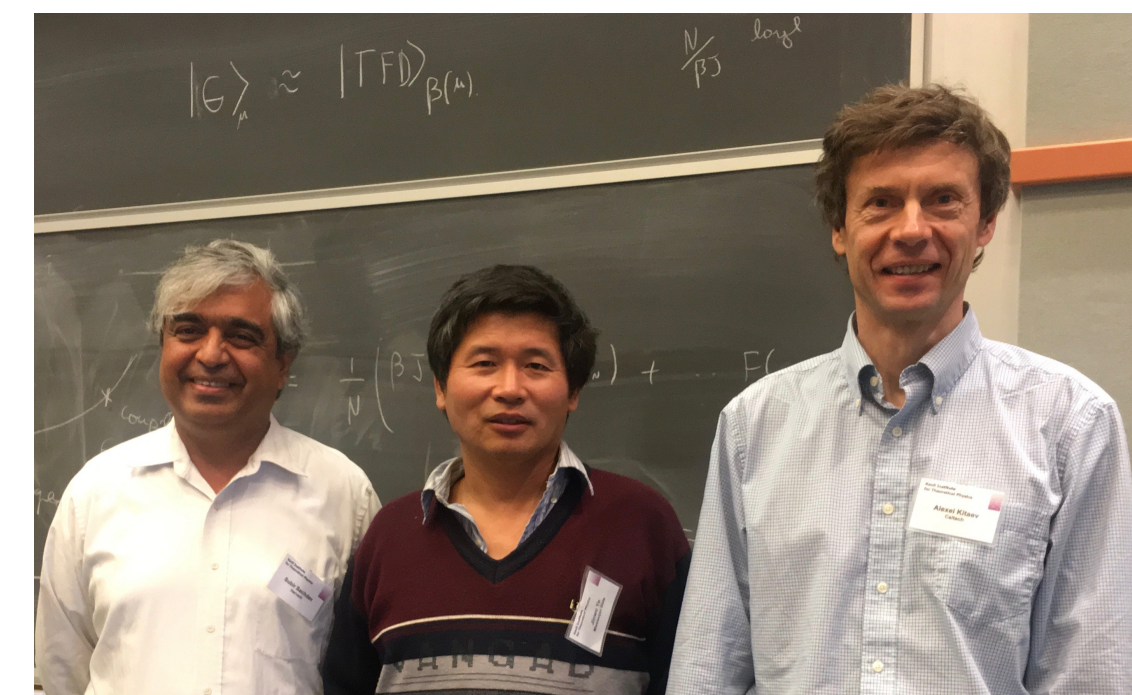


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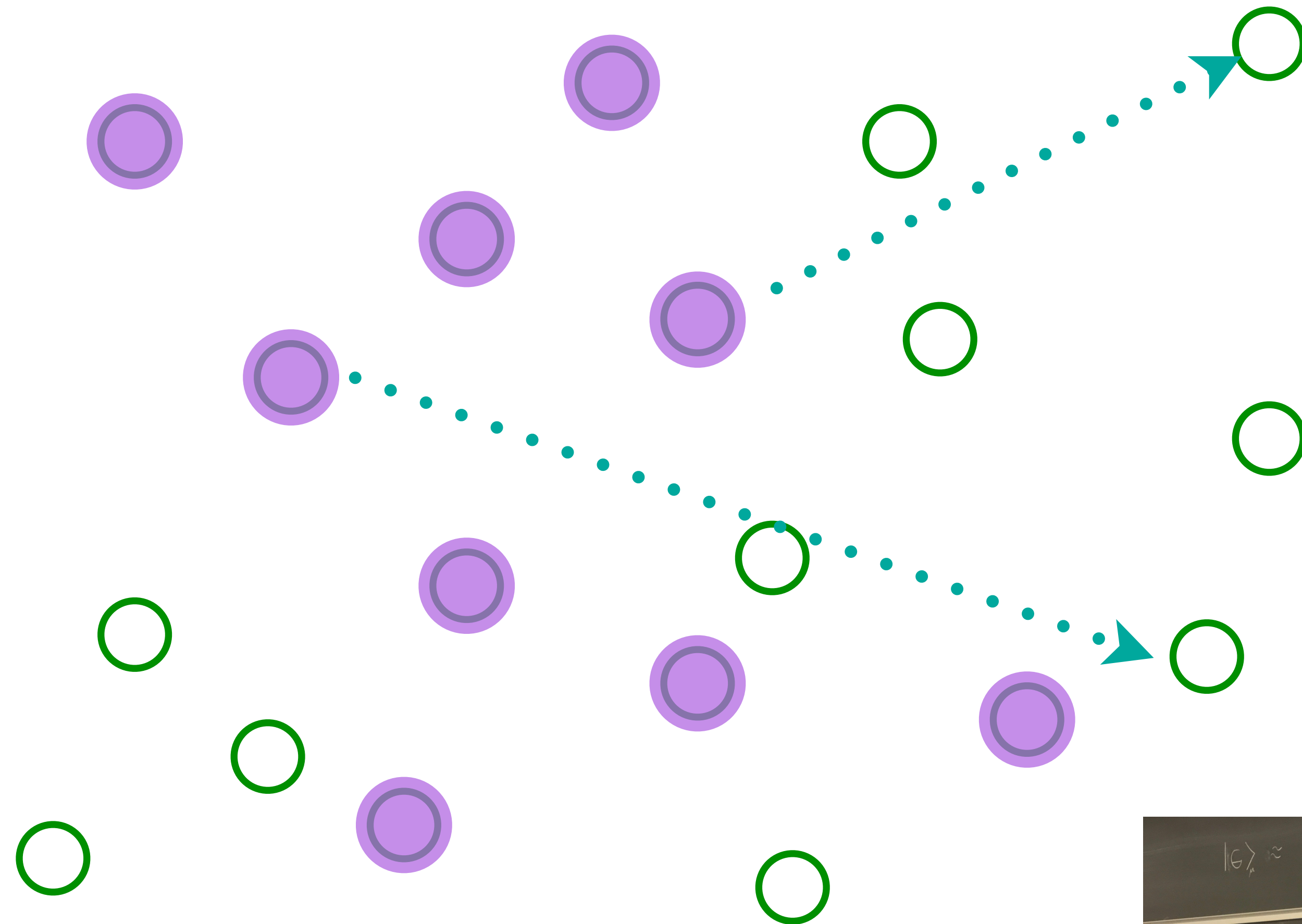


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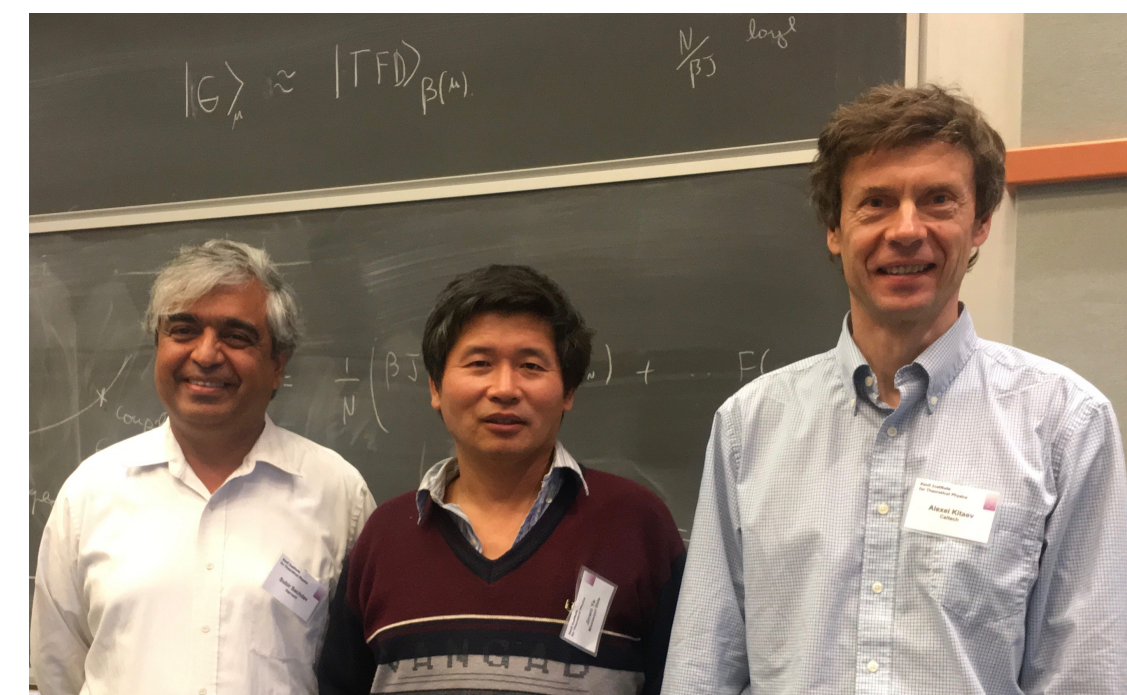


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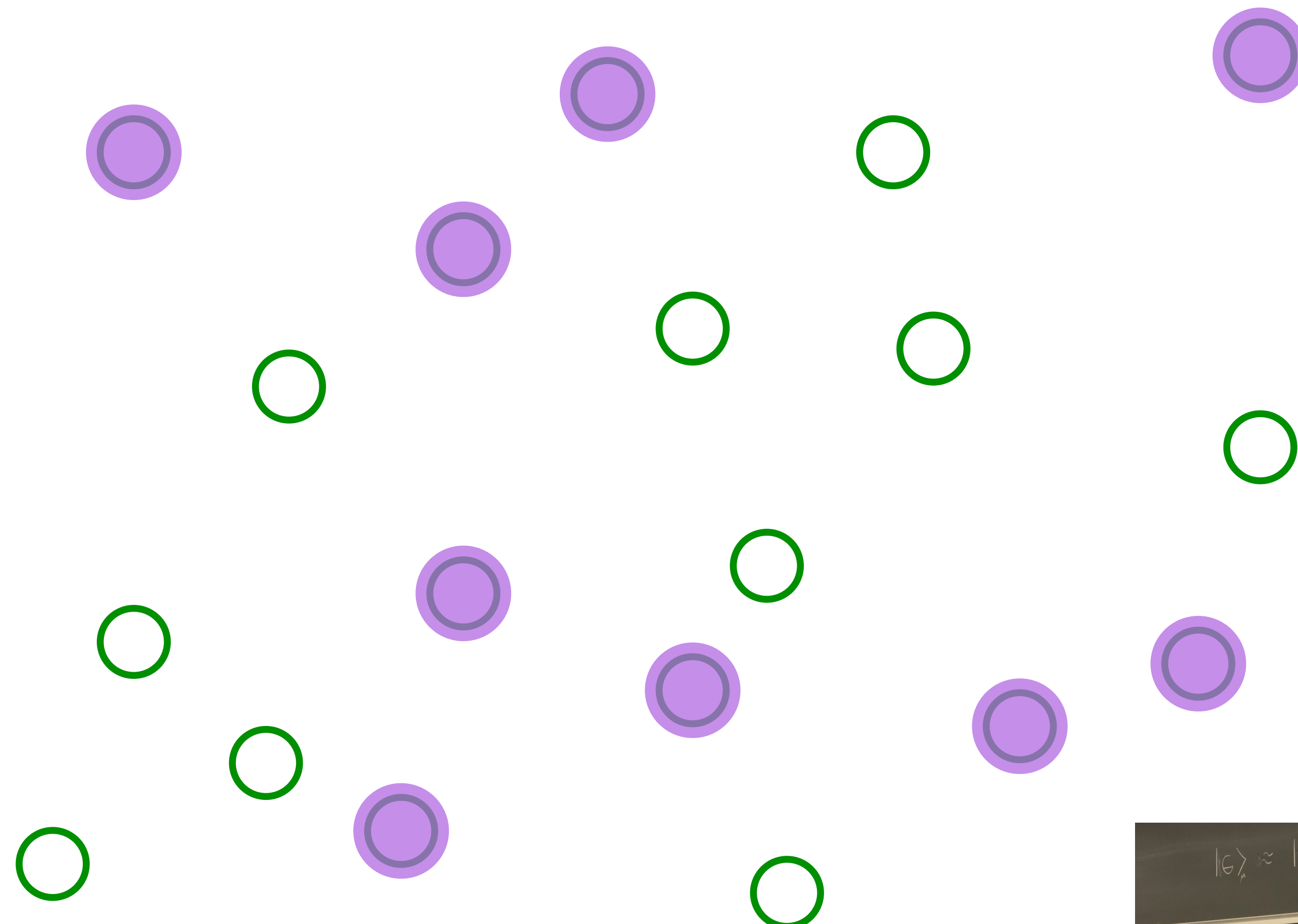


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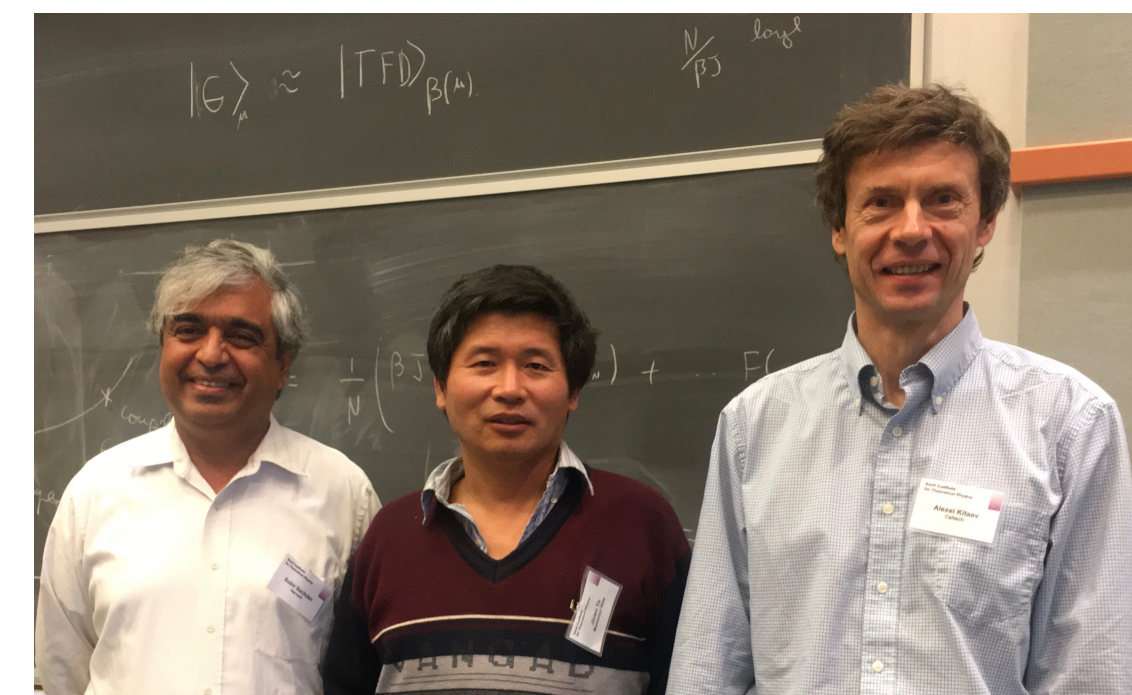


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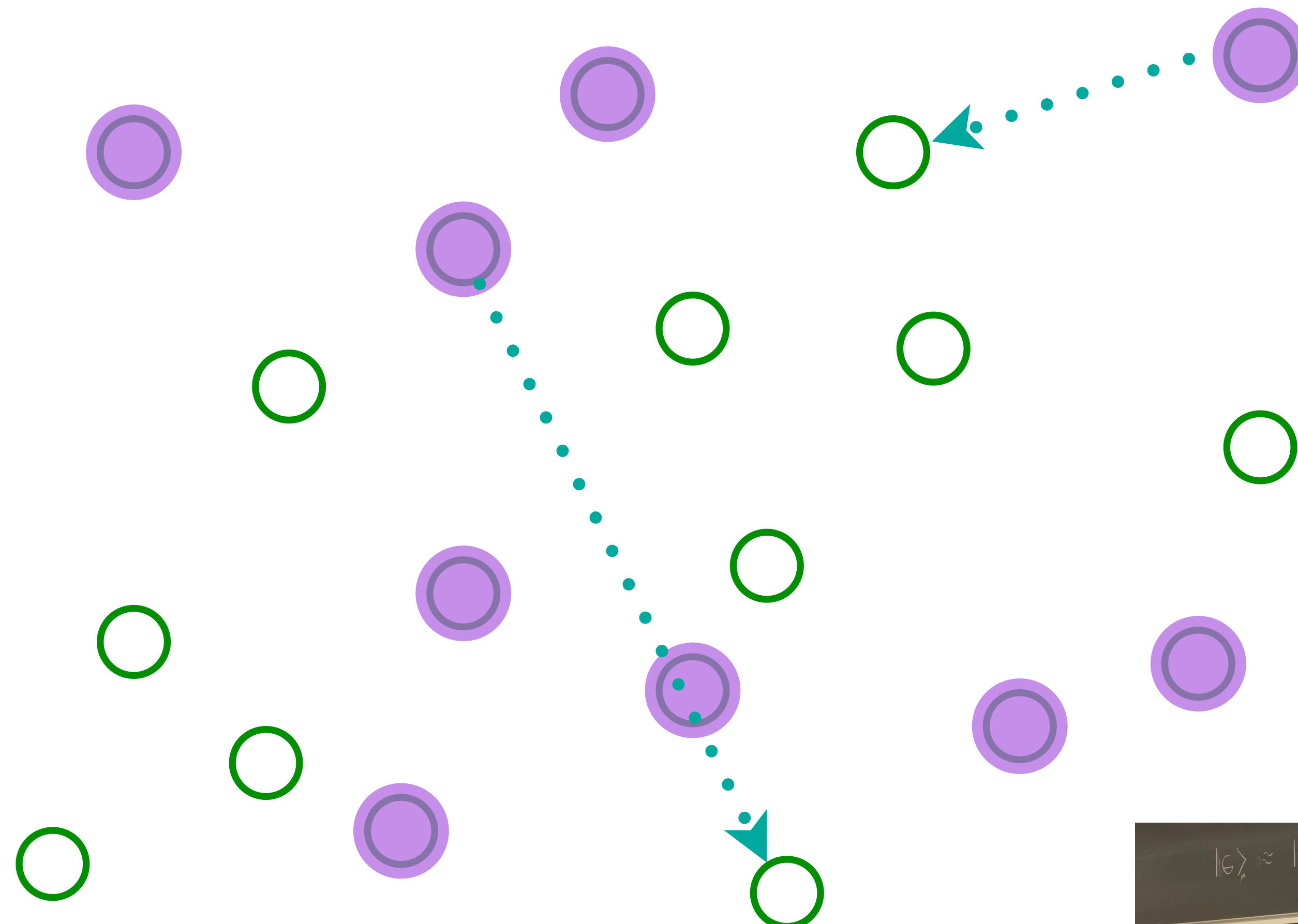


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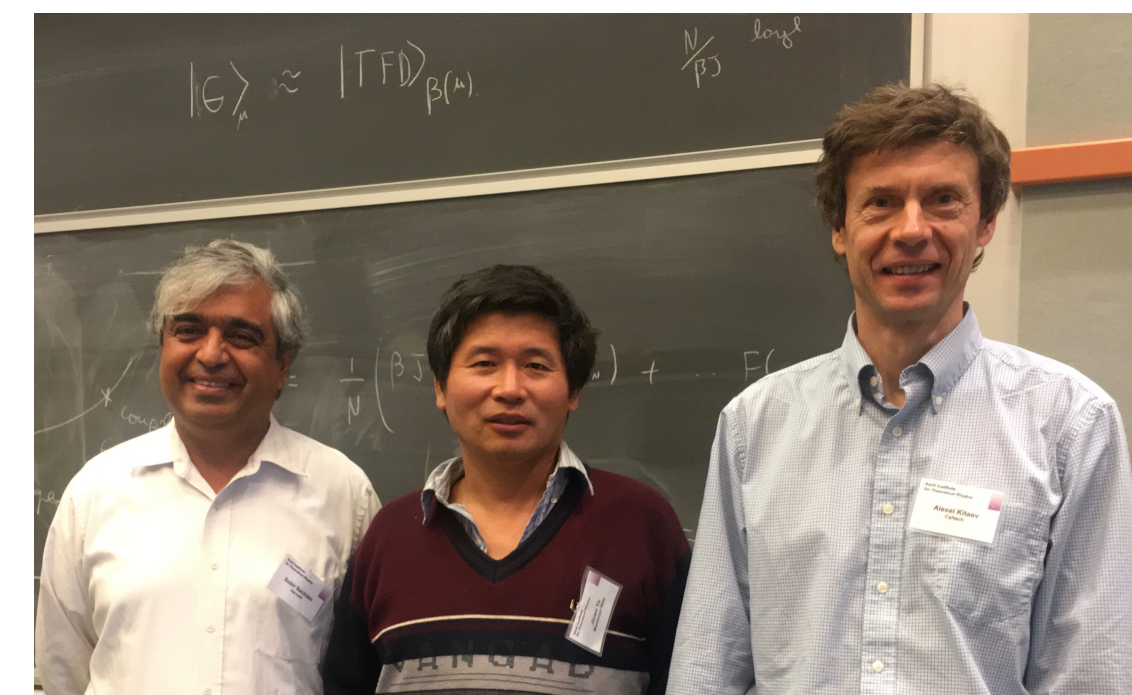


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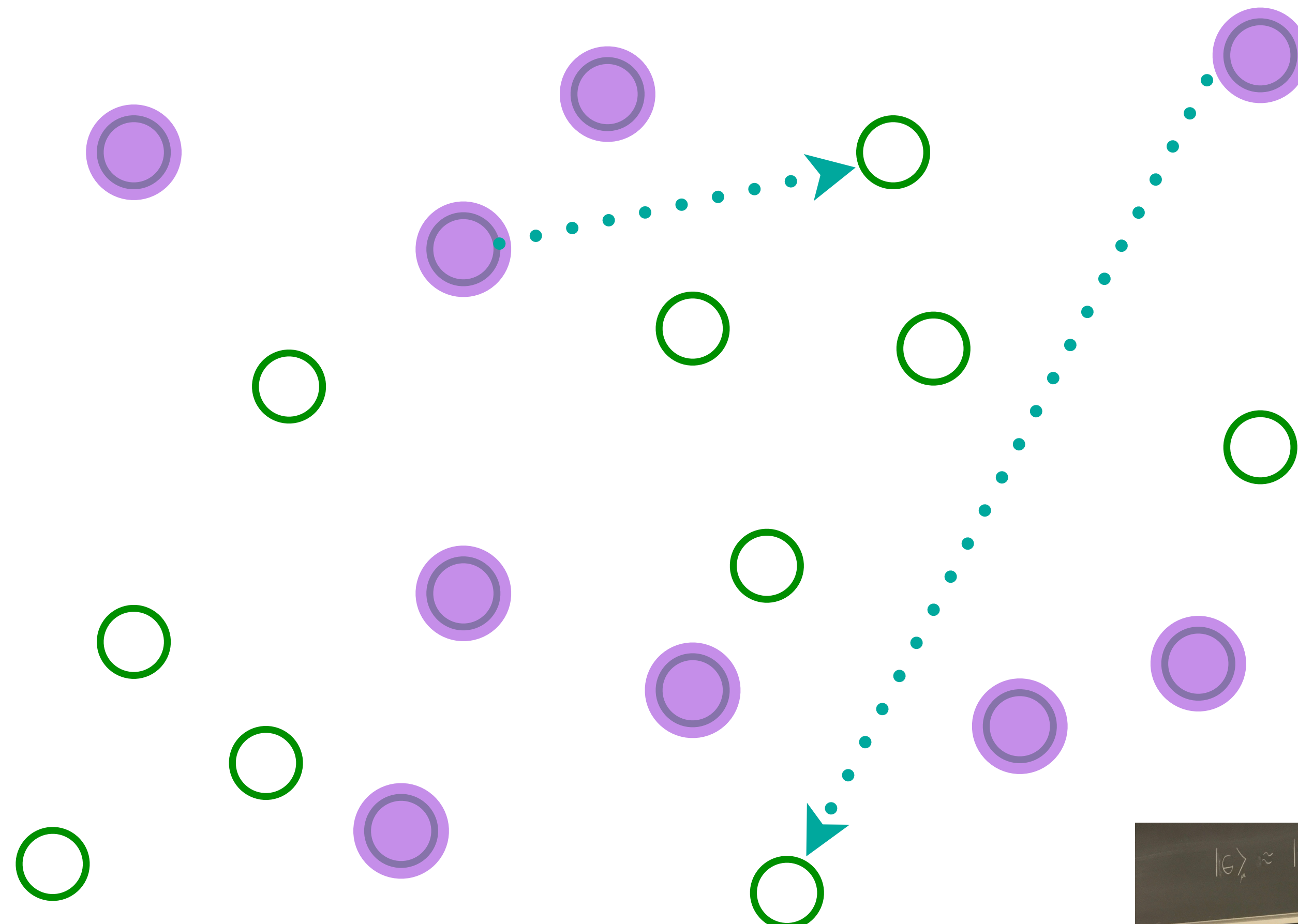


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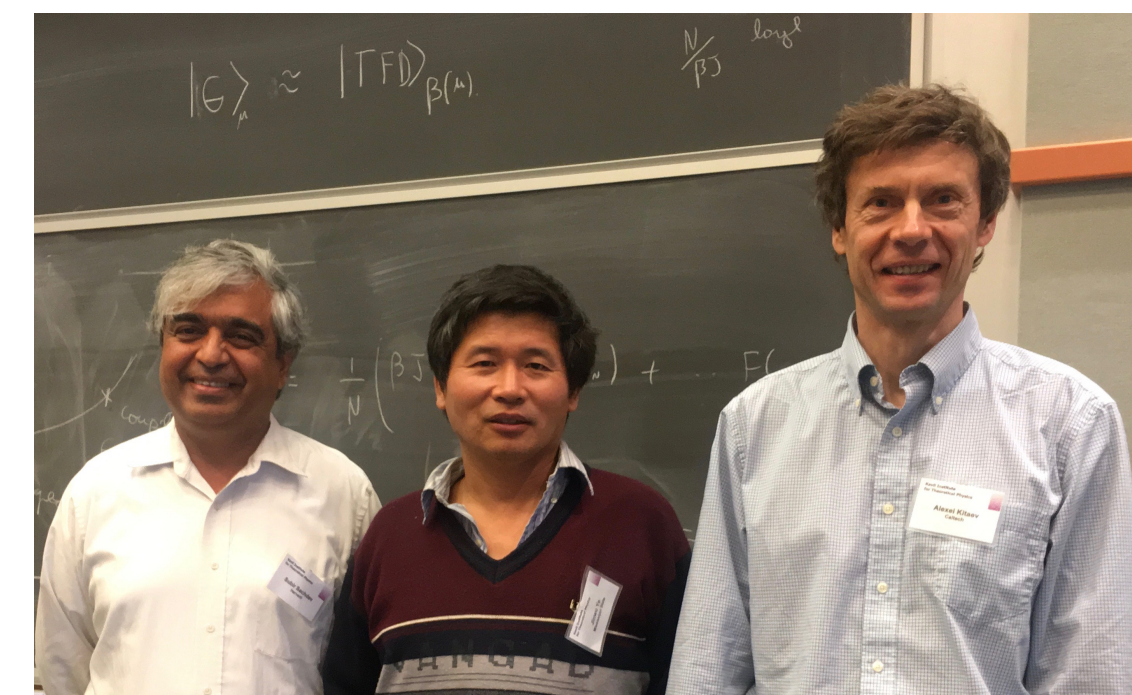


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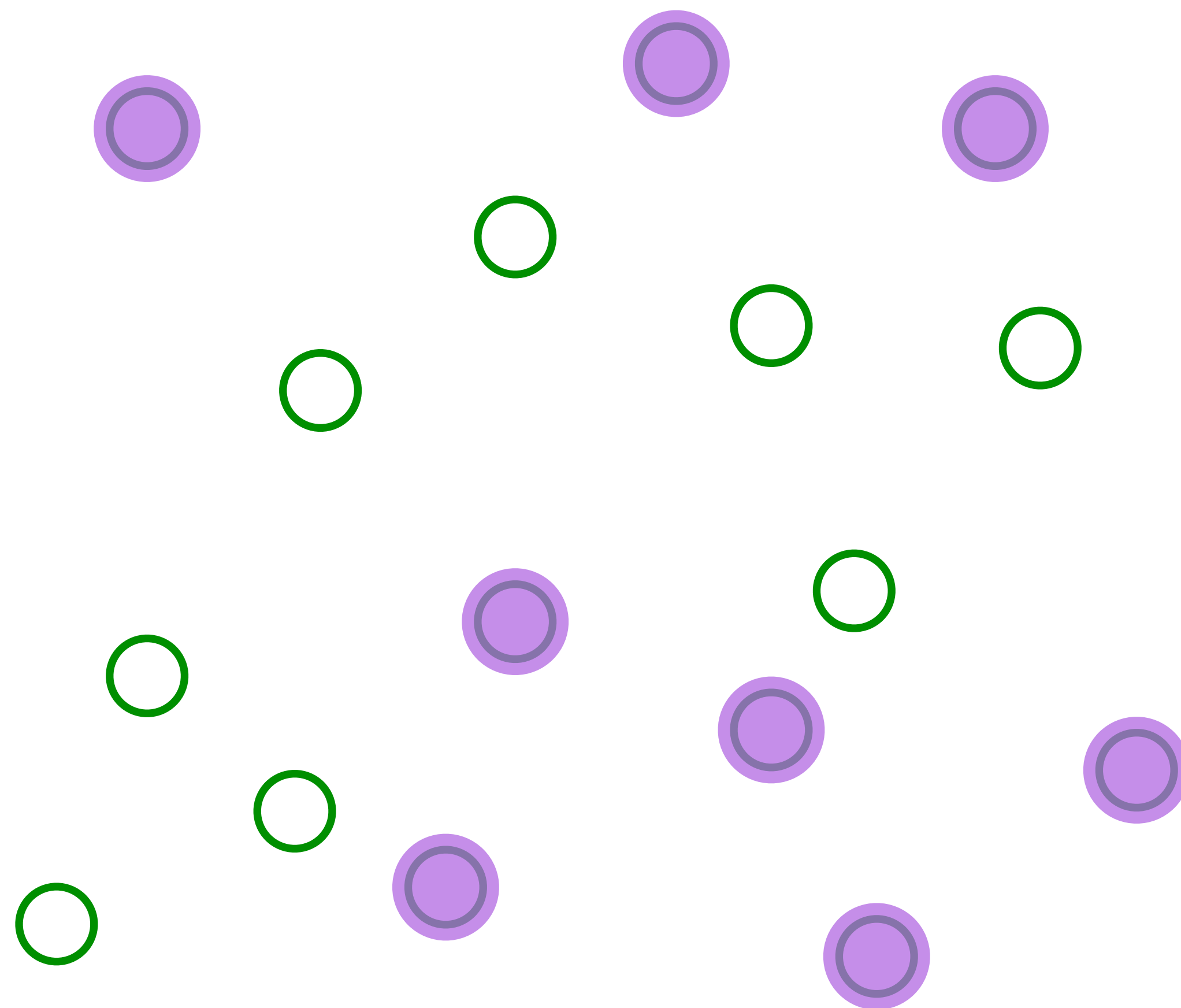


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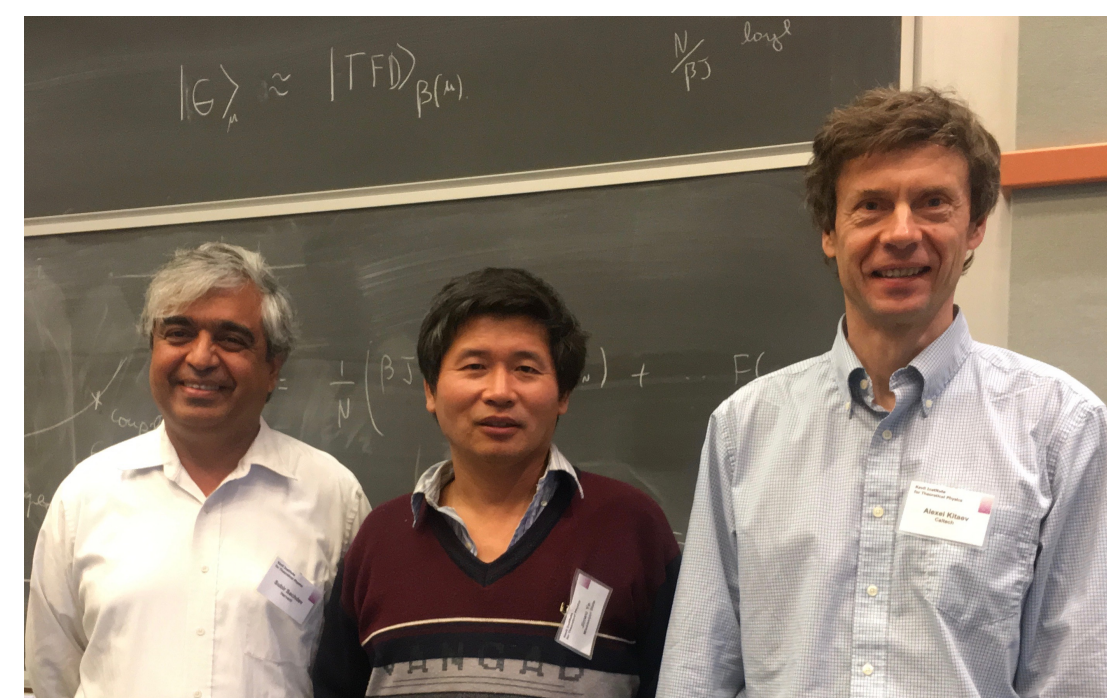
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○ Electron scattering
time τ in
the SYK model

$$\frac{1}{\tau} = \alpha \frac{k_B T}{\hbar}$$

Entangle electrons pairwise randomly

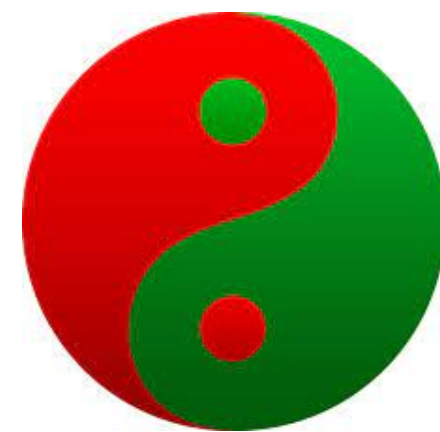


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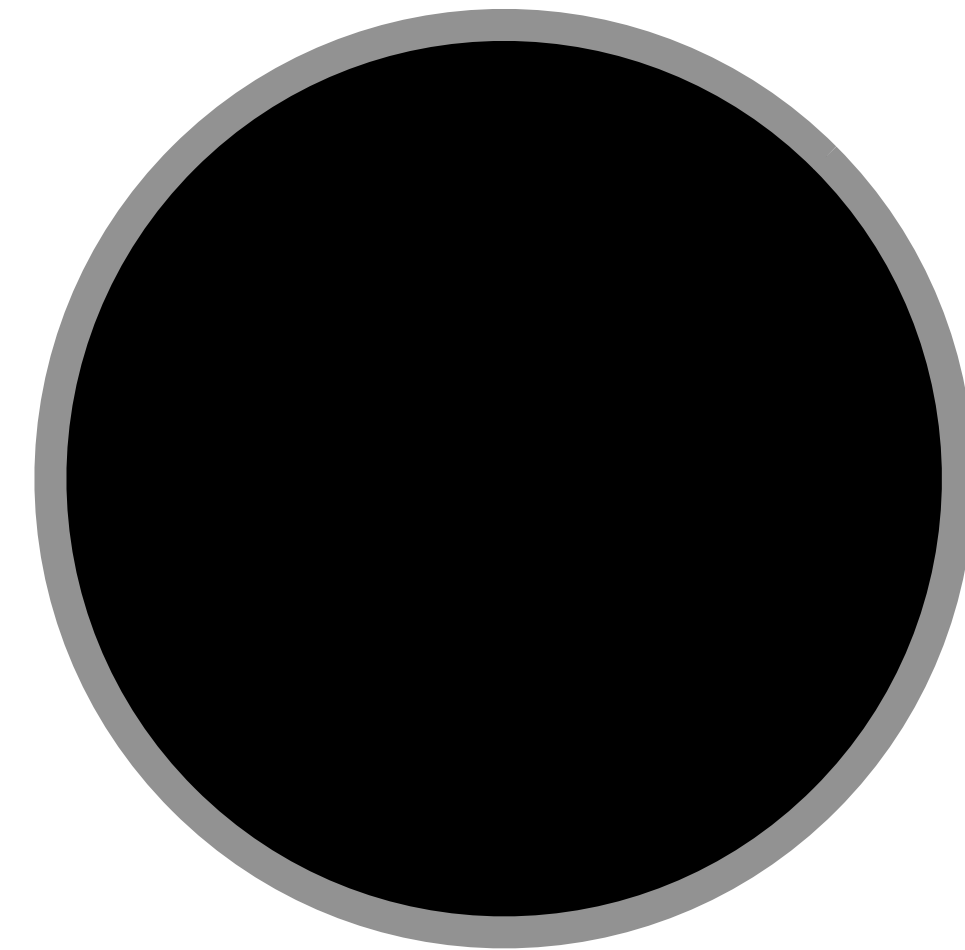
In a ***dual*** set of variables it describes certain ***black holes***

Sachdev (2010), Kitaev (2015), Maldacena Stanford (2015)

Black Holes

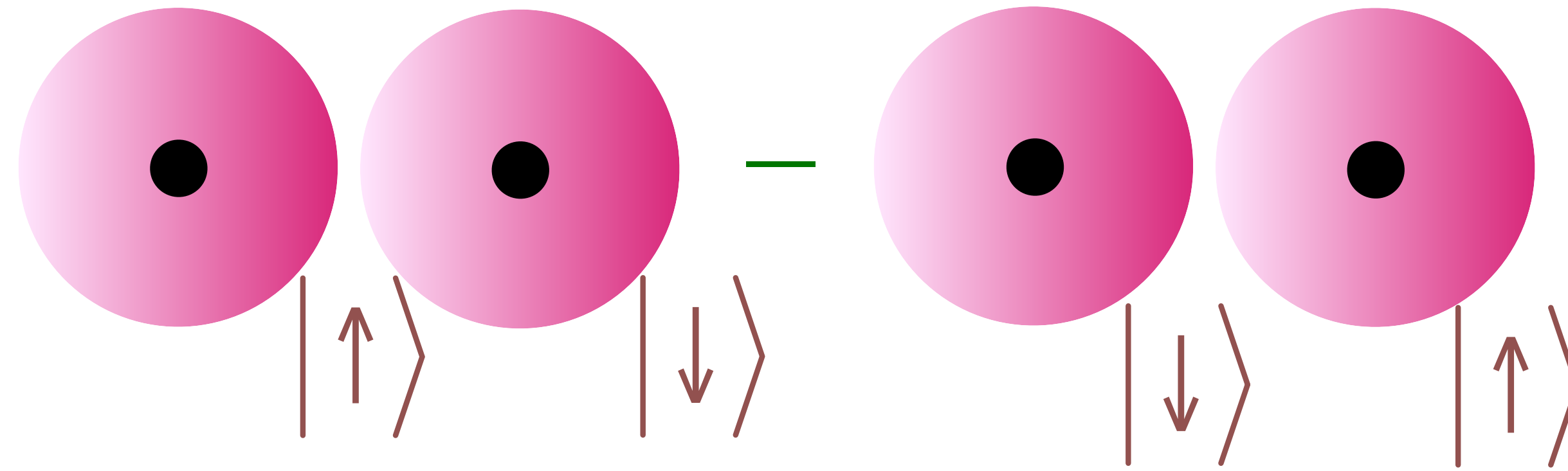
Objects so dense that light is gravitationally bound to them.

Horizon radius $R = \frac{2GM}{c^2}$

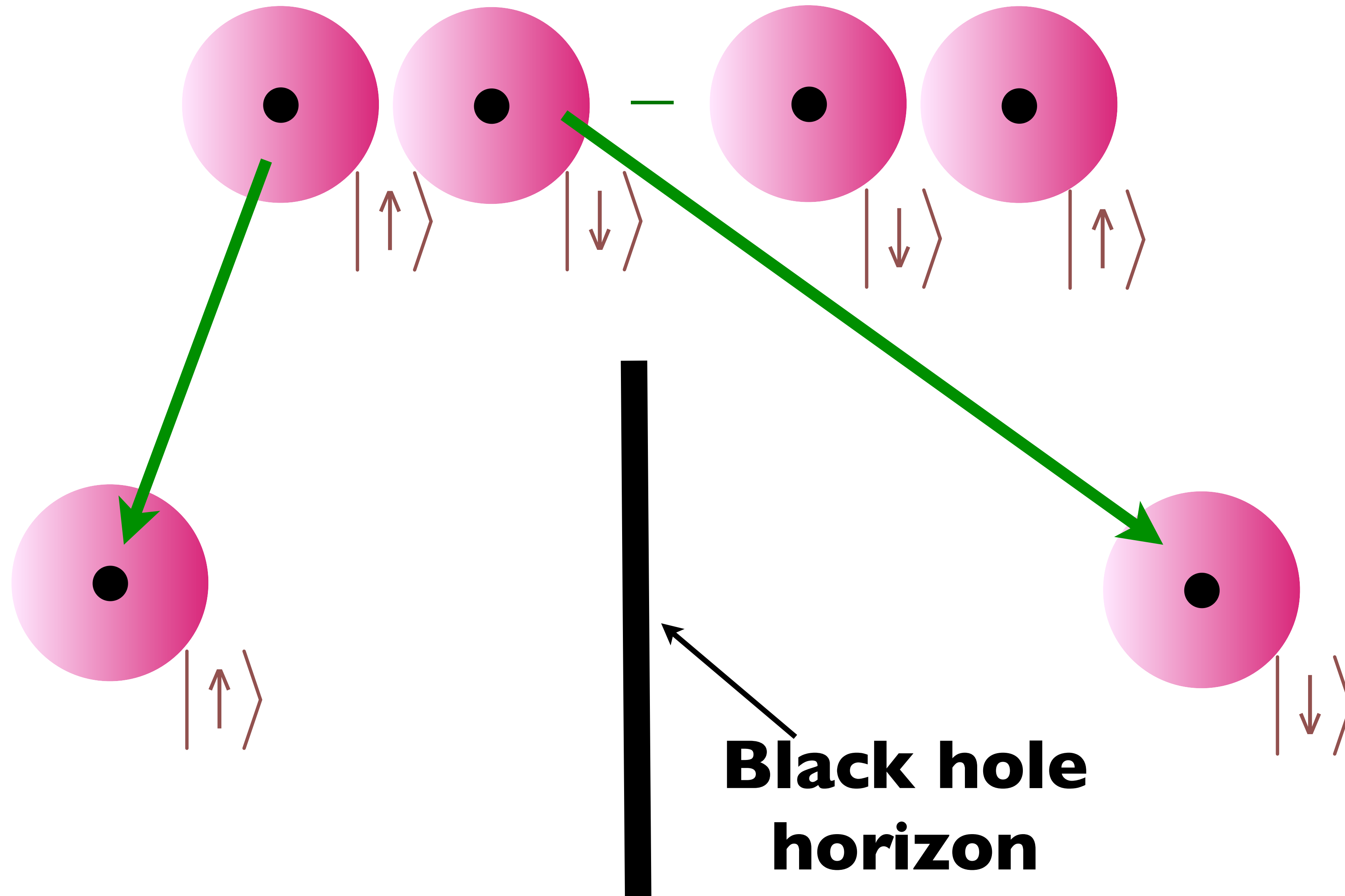


G Newton's constant, c velocity of light, M mass of black hole
For $M = \text{earth's mass}$, $R \approx 9 \text{ mm}$!

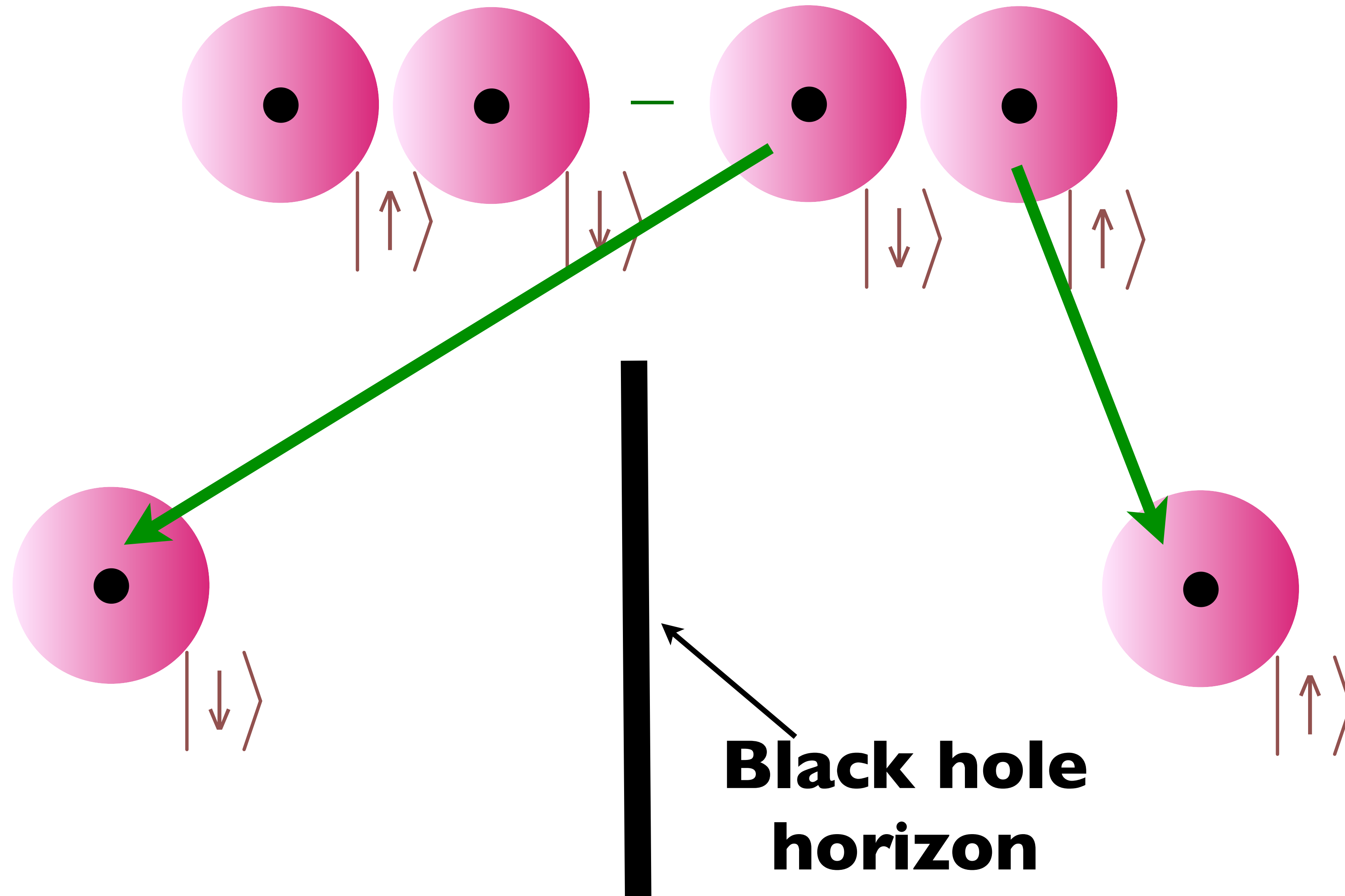
Quantum Entanglement across a black hole horizon



Quantum Entanglement across a black hole horizon

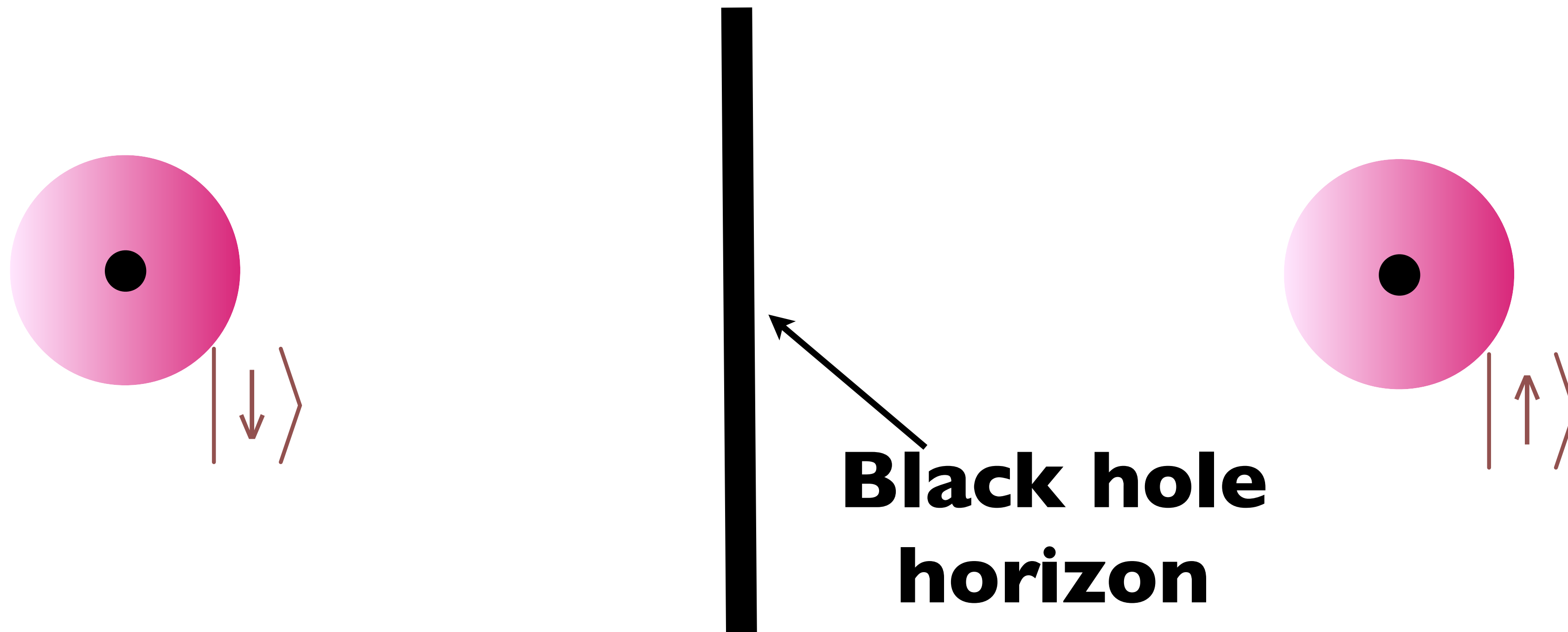


Quantum Entanglement across a black hole horizon



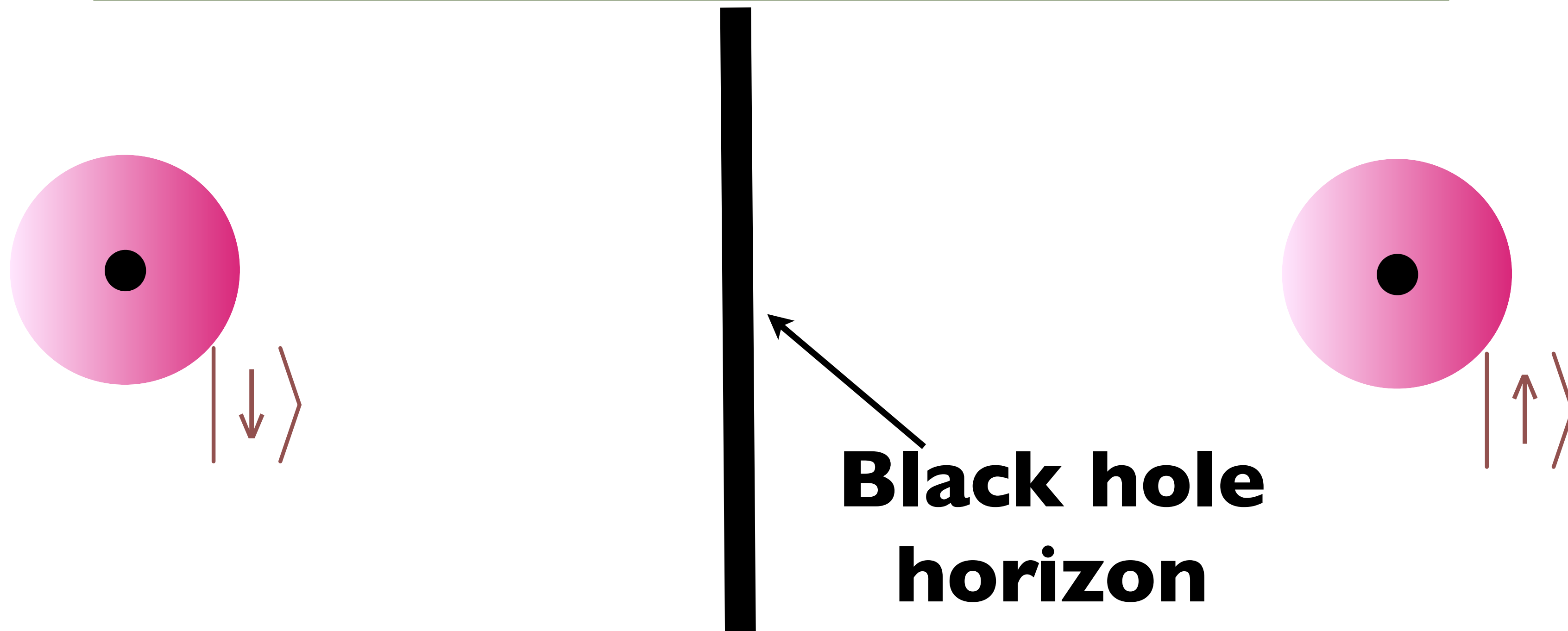
Quantum Entanglement across a black hole horizon

There is quantum entanglement between the inside and outside of a black hole



Quantum Entanglement across a black hole horizon

Hawking (1975) used other arguments to show that black hole horizons have a temperature
(The entanglement reasoning: to an outside observer, the state of the electron inside the black hole cannot be known, and so the outside electron is in a random state.)



Quantum Black holes

- Black holes have an entropy and a temperature, T_H
- The entropy is proportional to their surface area.
- They relax to thermal equilibrium in a Planckian time $\sim \hbar/(k_B T_H)$.

Black holes are represented as a '*hologram*' by a quantum many-body system in one lower dimension.

Duality: a '*change of variables*' between the many-particle configurations and the metric of spacetime

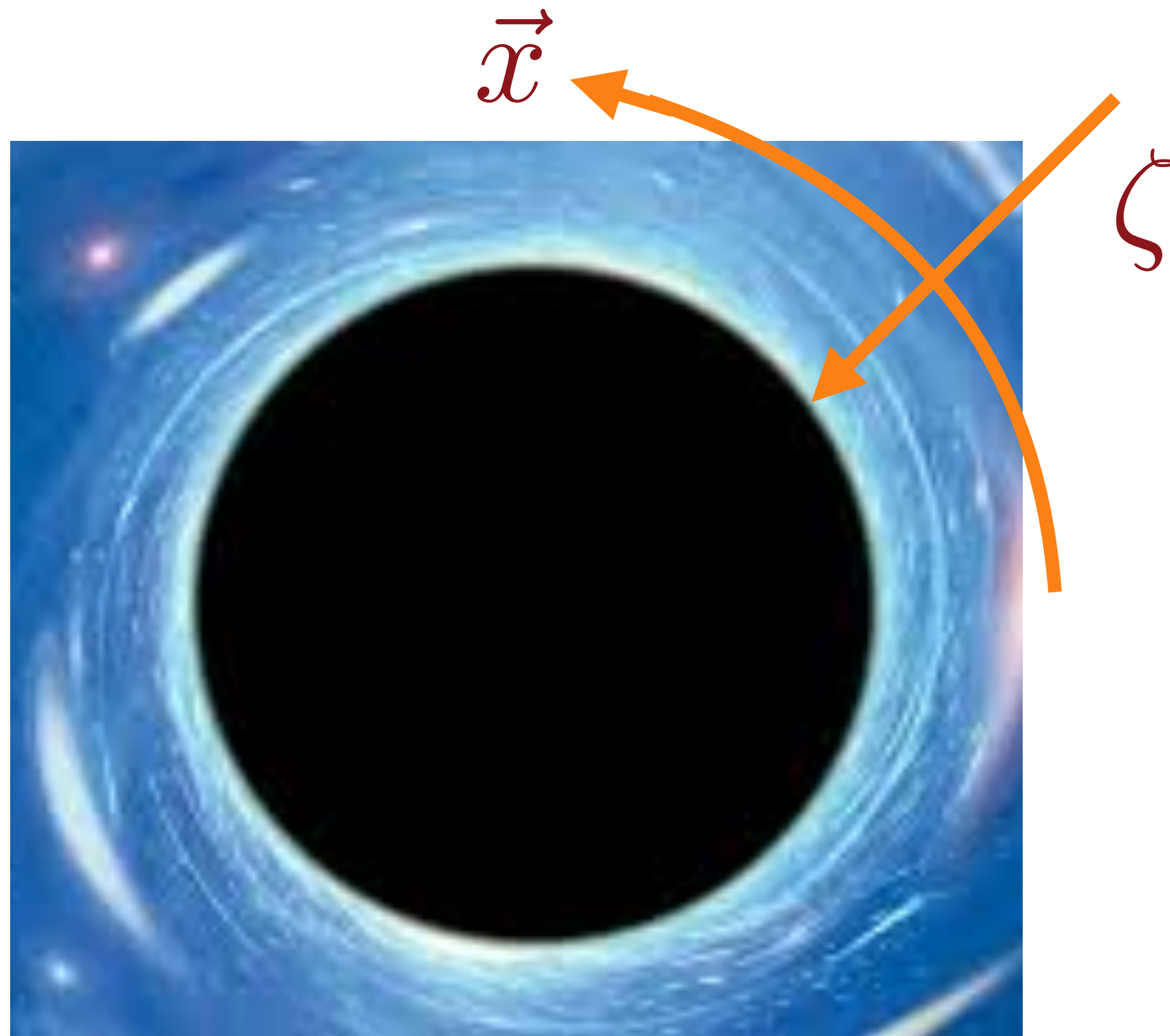
Quantum Black holes

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The hologram of a black hole
in d dimensions
is a quantum many-particle system
in $(d - 1)$ dimensions
which relaxes to thermal equilibrium
in a Planckian time $\sim \hbar/(k_B T)$



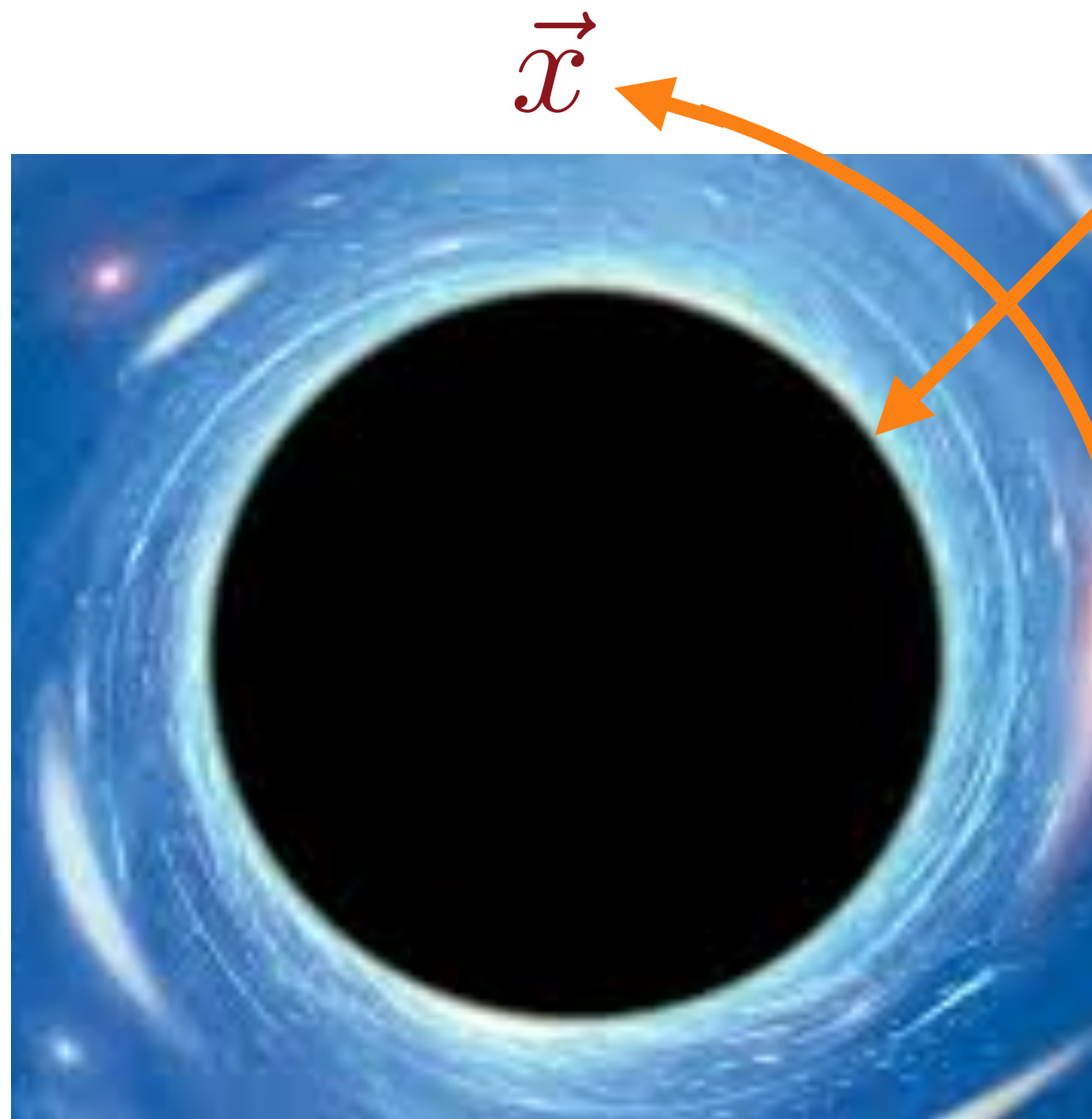
Maxwell's electromagnetism
and Einstein's general relativity
allow black hole solutions with a net charge



The near-horizon
geometry of a
charged black hole is
one-dimensional (ζ)



Maxwell's electromagnetism
and Einstein's general relativity
allow black hole solutions with a net charge



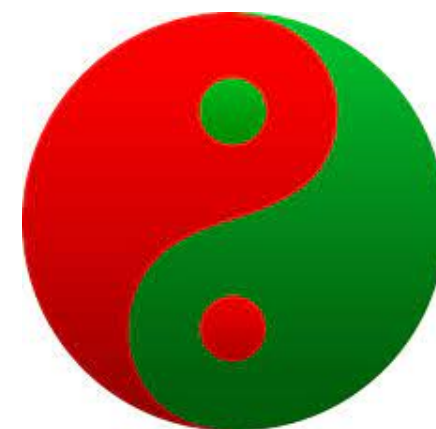
The hologram of the
 $1+1$ dimensional
gravity near the
horizon of a charged
black hole is the $0+1$
dimensional SYK
model

The Sachdev-Ye-Kitaev (SYK) model

The SYK model has a scale-invariant entanglement structure:
i.e. electrons are entangled at all distance and time scales

In one set of variables, it describes certain ***strange metals***

Sachdev, Ye (1993)



In a ***dual*** set of variables it describes certain ***black holes***

Sachdev (2010), Kitaev (2015), Maldacena Stanford (2015)

1. “Conventional” phases of matter

Metals, insulators, superconductors

2. Emergent gauge fields and topology

Spin liquids with Rydberg atoms

3. Strange metals

SYK model and emergent gravity