

For a relativistic CFT in  $d$  spatial dimensions, the metric in the holographic space is uniquely fixed by demanding the following scale transformation ( $i = 1 \dots d$ )

$$x_i \rightarrow \zeta x_i \quad , \quad t \rightarrow \zeta t \quad , \quad ds \rightarrow ds$$

This gives the unique metric

$$ds^2 = \frac{1}{r^2} \left( -dt^2 + dr^2 + dx_i^2 \right)$$

Reparametrization invariance in  $r$  has been used to the prefactor of  $dx_i^2$  equal to  $1/r^2$ . This fixes  $r \rightarrow \zeta r$  under the scale transformation. This is the metric of the space  $\text{AdS}_{d+2}$ .