

# Fermi surfaces and gauge-gravity duality

Aspen Center for Physics, Feb 1-5, 2011

Lecture notes  
arXiv:1010.0682  
arXiv:1012.0299

[sachdev.physics.harvard.edu](http://sachdev.physics.harvard.edu)



# Compressible quantum matter

- Consider a continuum quantum system with a globally conserved U(1) charge  $Q$  (the “electron density”) in spatial dimension  $d > 1$ .

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There are only a few established examples of such phases in condensed matter physics.

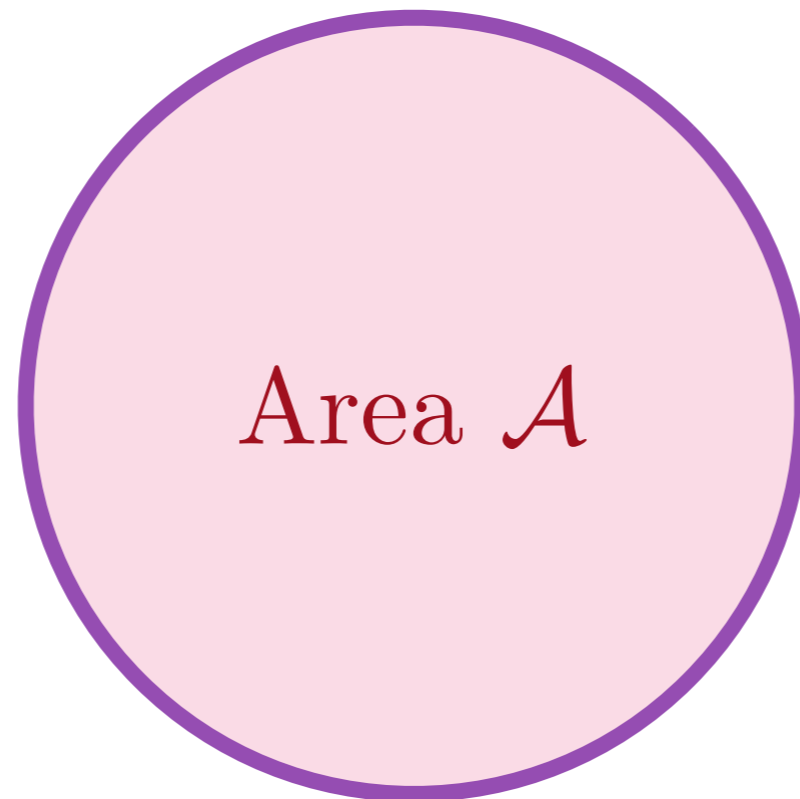
However, they appear naturally as duals of gravitational theories, and we want to interpret them in the gauge theory.

# The Fermi surface

All known examples of such phases have a *Fermi surface*: the locus of zero energy singularities in momentum space in the two-point correlator of fermions carrying charge  $Q$ .

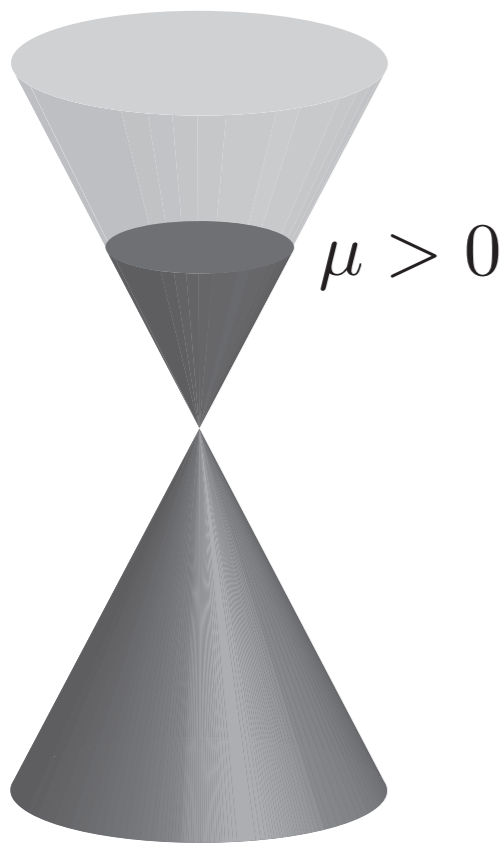
$$G_{\text{fermion}}^{-1}(k = k_F, \omega = 0) = 0.$$

**Luttinger relations:** The “volume (area)”  $\mathcal{A}$  enclosed by the Fermi surface has a simple linear relation to  $\langle Q \rangle$ .



# The Fermi Liquid (FL)

Most common example: electrons with short-range interactions (or screened long-range interactions), which are adiabatically connected to the non-interacting limit. The electron Green's function  $G_c$  has a pole which crosses zero energy at  $k = k_F$ , and the Fermi surface has the same area as the non-interacting case.



$$\mathcal{L} = \bar{c} (\partial_a - \mu \delta_{at}) \gamma^a c + 4 \text{ Fermi terms}$$

$$\mathcal{A} = \langle \bar{c} \gamma^t c \rangle = \langle \mathcal{Q} \rangle$$

$$G_c = \frac{1}{\omega - v_F(k - k_F) + i\omega^2}$$

# Outline

## 1. Fermion-boson mixtures

*Luttinger relations with bosons*

## 2. Gauge theories

*The fractionalized Fermi liquid ( $FL^*$ ) phase*

## 3. Connections to semi-holographic theories

*Low energy theory of  $FL$  and  $FL^*$  phases*

## 4. Solvable models with infinite-range hopping

*Mapping to gravity duals on  $AdS_2 \times R^d$*

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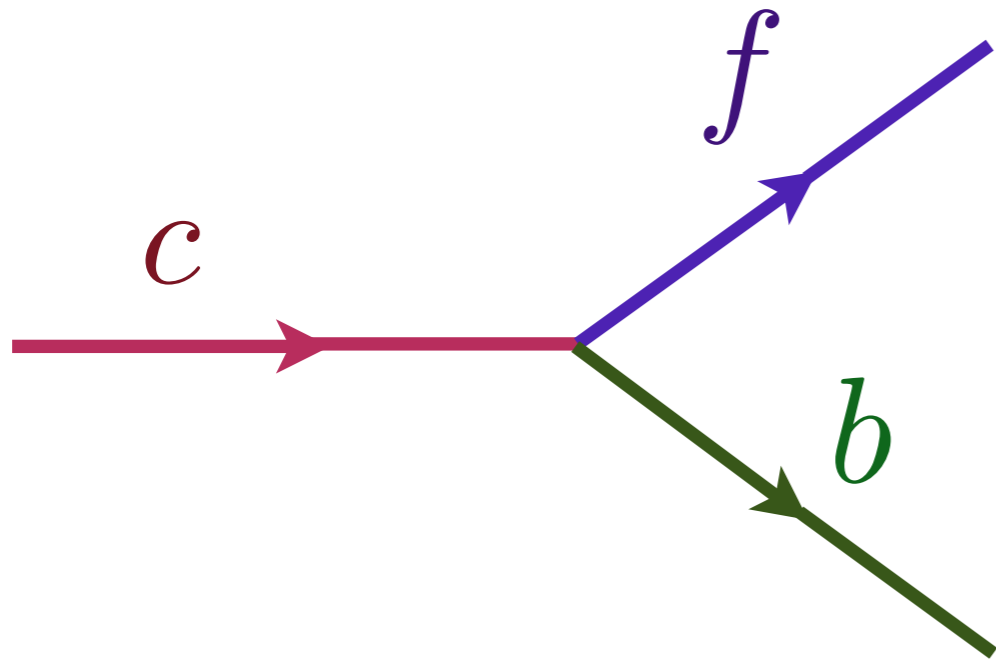
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Introduce a second “flavor” of electrons,  $f$ , and allow  $c$  to decay into  $f$  and a boson  $b$



$$Q = \bar{c} \gamma^t c + \bar{f} \gamma^t f$$

$$Q_g = \bar{f} \gamma^t f - \bar{b} \overset{\leftrightarrow}{\partial}_t b$$

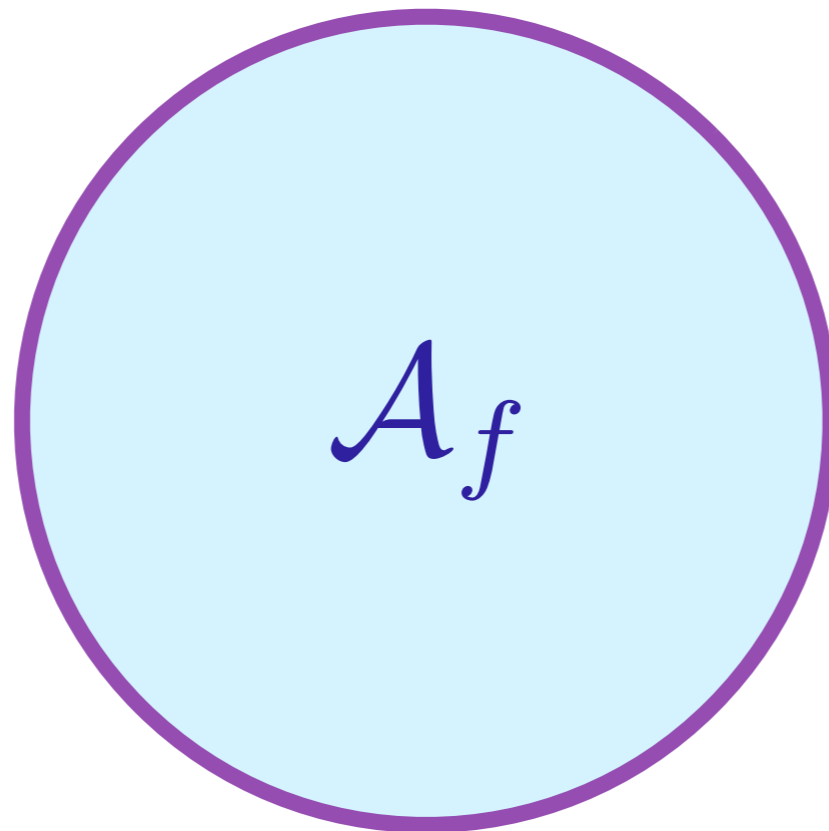
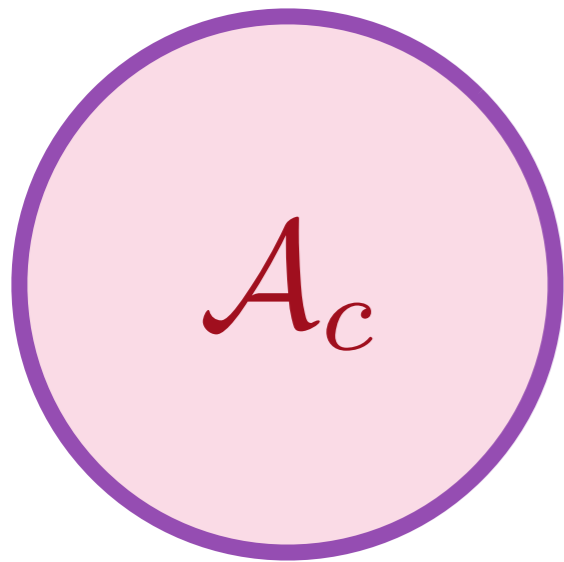
Two conserved charges:  
 $U(1) \times U_g(1)$

$$\mathcal{L} = \bar{c} (\partial_a - \mu \delta_{at}) \gamma^a c + \bar{f} (\partial_a - (\mu + \mu_g) \delta_{at}) \gamma^a f$$

$$+ |(\partial_a + \mu_g \delta_{at}) b|^2 + s |b|^2 + \lambda (\bar{c} f b + \text{c.c.}) + \dots$$

There is a Luttinger relation for each conserved U(1) charge. However, the boson,  $b$  cannot have a Fermi surface in its Green's function, and so there is no area associated with it, although the boson density is *included* in the Luttinger relation

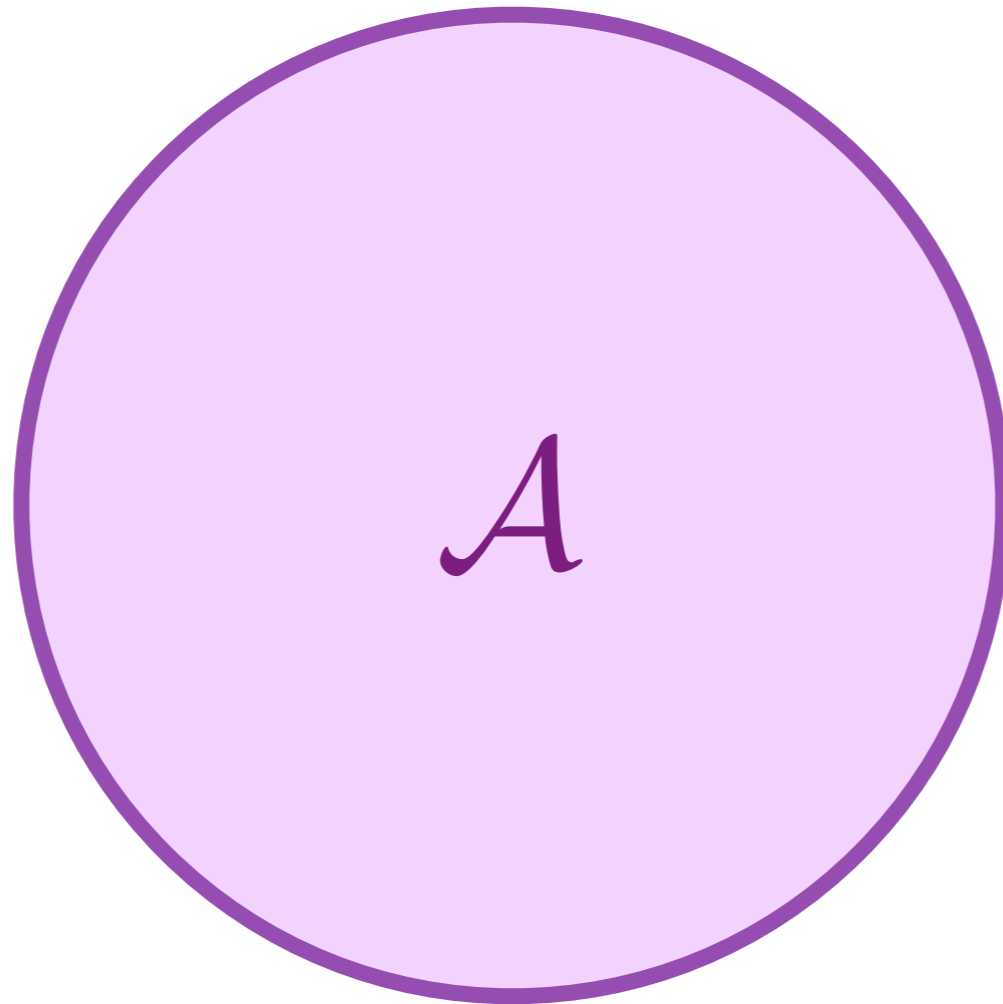
$$\begin{aligned}
 A_c + A_f &= \langle \bar{c} \gamma^t c \rangle + \langle \bar{f} \gamma^t f \rangle = \langle Q \rangle \\
 A_f &= \langle \bar{f} \gamma^t f \rangle - \langle \bar{b} \overset{\leftrightarrow}{\partial}_t b \rangle = \langle Q_g \rangle
 \end{aligned}$$



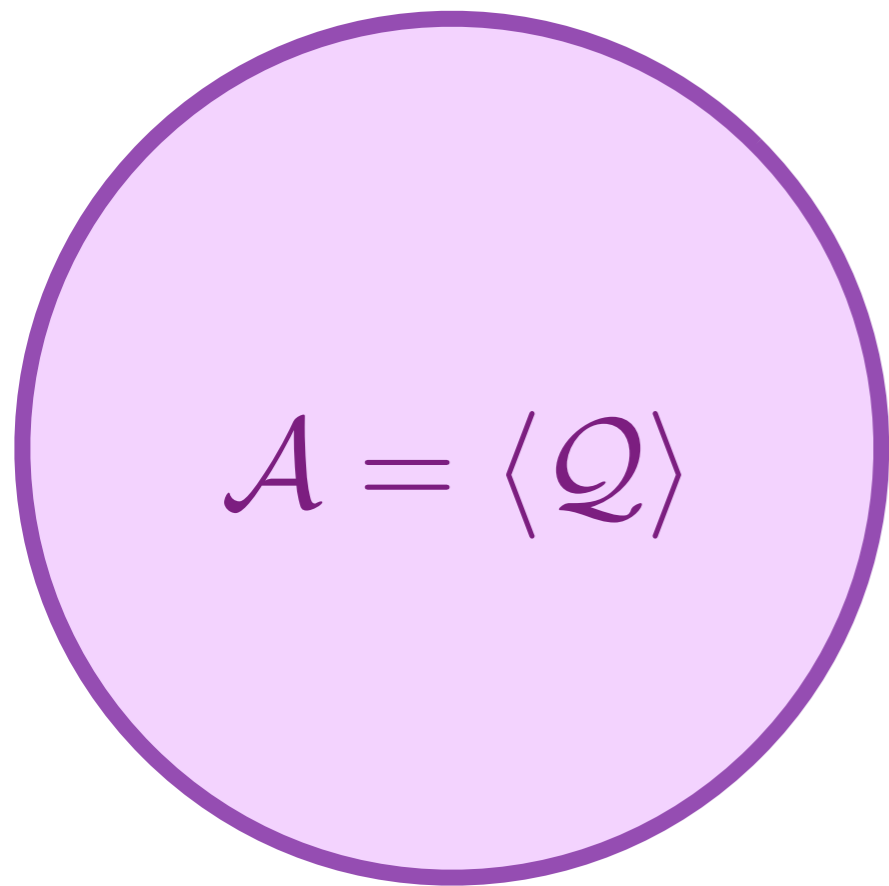
The  $b$  bosons have bound with  $f$  fermions to form  $c$  “molecules”

If  $U_g(1)$  is spontaneously broken by condensation of  $b$ , only the Luttinger relation associated with  $U(1)$  applies. Also the  $c$  and  $f$  flavors can now mix (“hybridize”), and so form only a single Fermi surface when the mixing is large enough.

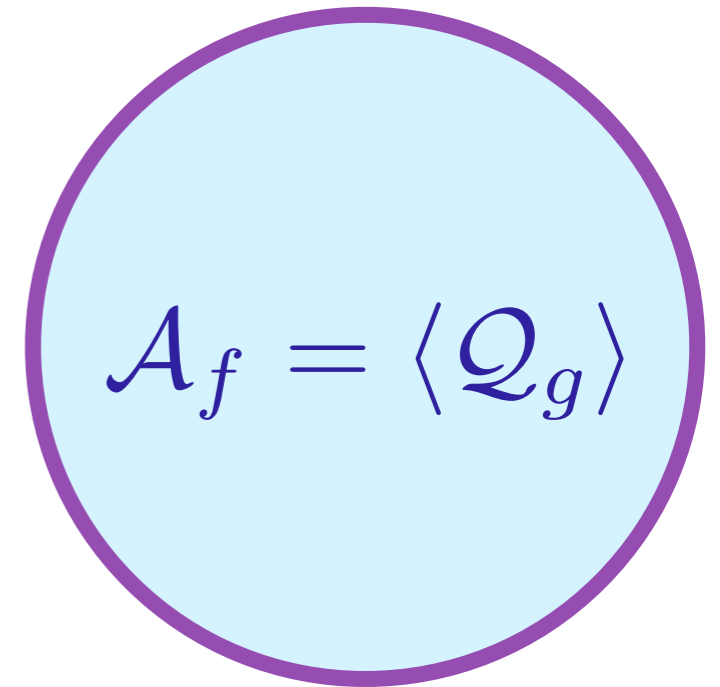
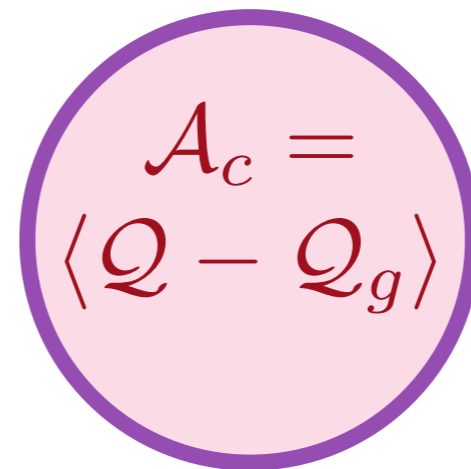
$$A = \langle \bar{c} \gamma^t c \rangle + \langle \bar{f} \gamma^t f \rangle = \langle Q \rangle$$



# Phase diagram of boson-fermion mixture



Superfluid:  $\langle b \rangle \neq 0$   
 $U_g(1)$  broken  
 $U(1)$  unbroken



Normal:  $\langle b \rangle = 0$   
 $U(1) \times U_g(1)$  unbroken

$\rightarrow S$

$$\mathcal{L} = \bar{c} (\partial_a - \mu \delta_{at}) \gamma^a c + \bar{f} (\partial_a - (\mu + \mu_g) \delta_{at}) \gamma^a f$$

$$+ |(\partial_a + \mu_g \delta_{at}) b|^2 + s |b|^2 + \lambda (\bar{c} f b + \text{c.c.}) + \dots$$

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- Now gauge  $U_g(1)$  by a dynamical (“emergent”) gauge field  $A_a$ .

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- Longitudinal gauge fluctuations are screened by the  $f$  fermions. But transverse gauge fluctuations remain unscreened, and are Landau-damped by excitations near the  $f$  Fermi surface. The theory of a Fermi surface coupled to transverse gauge fluctuations is *strongly coupled in two spatial dimensions*.

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- The overdamped transverse gauge modes lead to “non-Fermi liquid” broadening of the fermion pole near the  $f$  Fermi surface.

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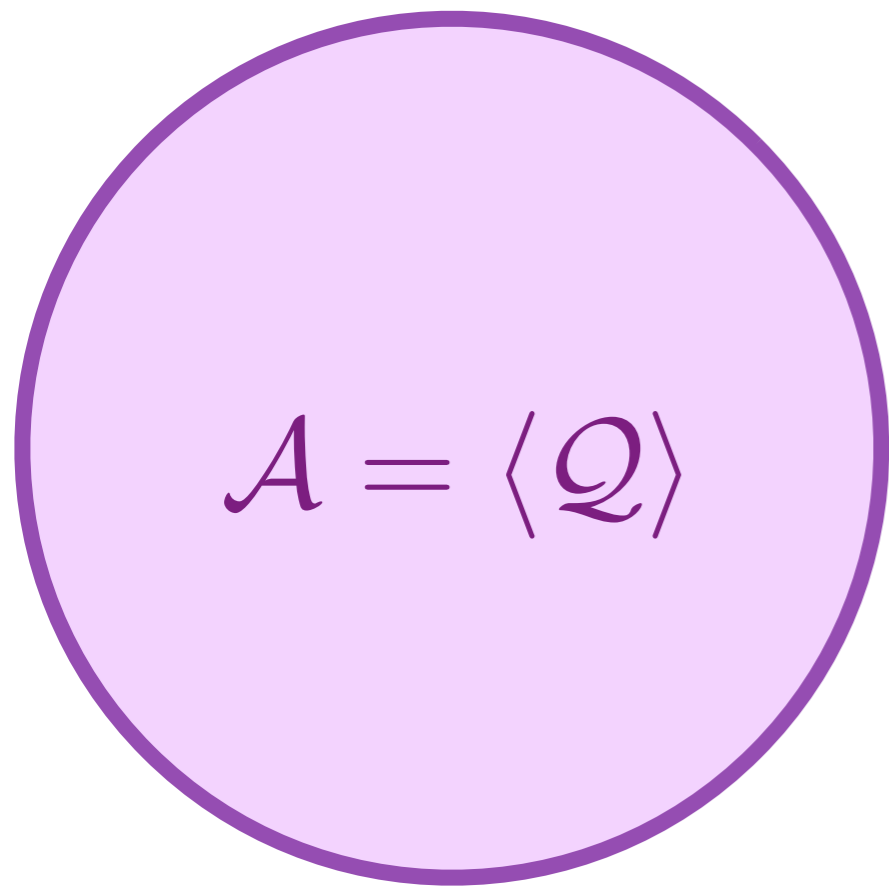
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- The overdamped transverse gauge modes lead to “non-Fermi liquid” broadening of the fermion pole near the  $f$  Fermi surface.
- The gauge-neutral  $c$  fermion also acquires a weaker non-Fermi liquid broadening.

$$\mathcal{L} = \bar{c} (\partial_a - \mu \delta_{at}) \gamma^a c + \bar{f} (\partial_a - iA_a + (\mu + \mu_g) \delta_{at}) \gamma^a f + |(\partial_a + iA_a + \mu_g \delta_{at}) b|^2 + s |b|^2 + \lambda (\bar{c} f b + \text{c.c.}) + \dots$$

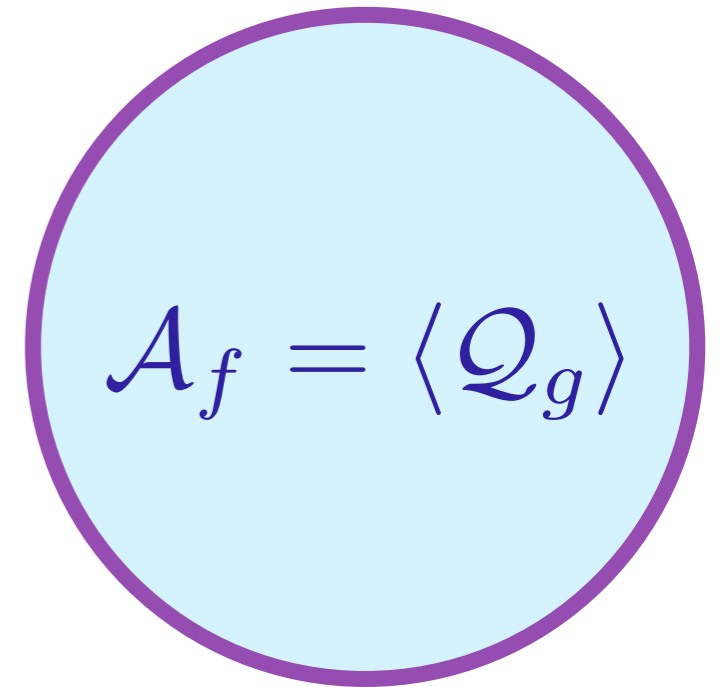
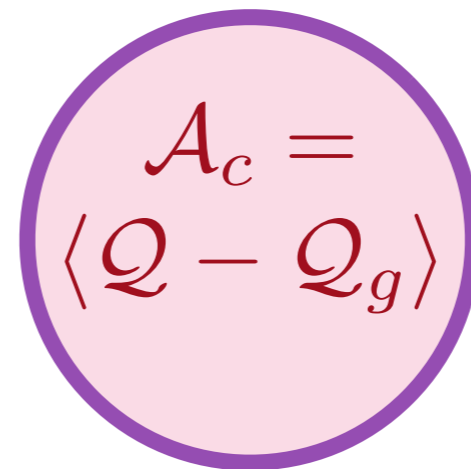
- However, *the locations of the Fermi surfaces are well defined, and the Luttinger relations apply as before.*

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→  $s$

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# Phase diagram of $U_g(I)$ gauge theory

$$A = \langle Q \rangle$$

Higgs/confining phase:  
Fermi liquid (FL)

$$A_c = \langle Q - Q_g \rangle$$

(Only showing Fermi surfaces of the observable gauge-neutral fermions.)

Deconfined phase:  
Fractionalized  
Fermi liquid (FL\*)

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T. Senthil, M. Vojta, and S. Sachdev, *Physical Review B* **69**, 035111 (2004)

# Phase diagram of gauge theories with global U(1) charge density

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$S$

The same phase diagram applies when  $U_g(1)$  is generalized to non-Abelian or discrete gauge groups. It also applies when the  $f$  Fermi surface is gapped by the lattice potential, or by pairing of the  $f$  fermions.

# Phase diagram of gauge theories with global U(1) charge density

Needed: AdS/CFT description of these phases and of the quantum phase transition between them

(Showing Fermi surfaces of the deconfined gauge-fermions.)

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Fermi liquid (FL)

Deconfined phase:  
Fractionalized  
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$\rightarrow S$

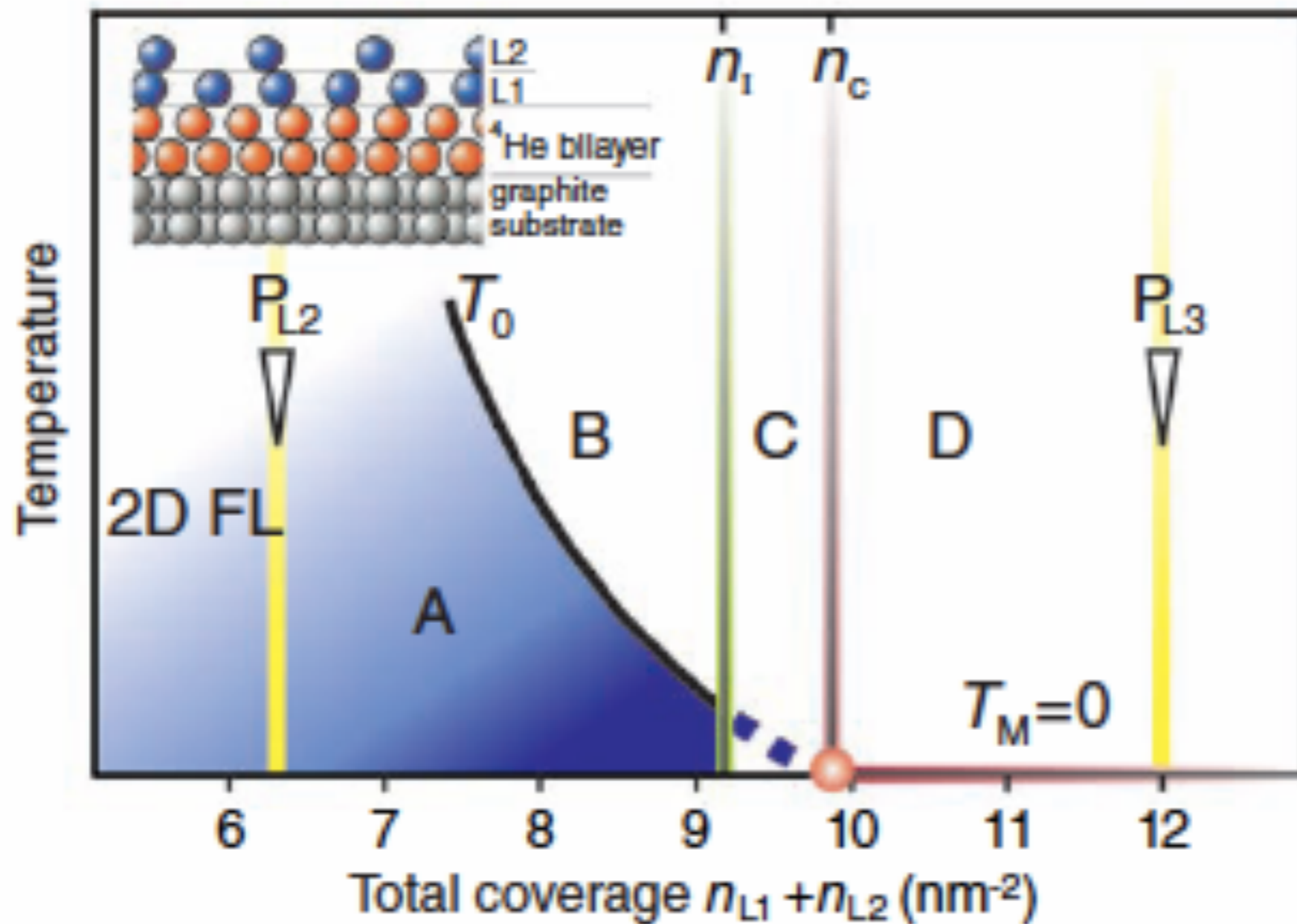
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# Bilayer $^3\text{He}$ : A Simple Two-Dimensional Heavy-Fermion System with Quantum Criticality

*Science* **317**, 1356 (2007)

Michael Neumann, Ján Nyéki, Brian Cowan, John Saunders\*



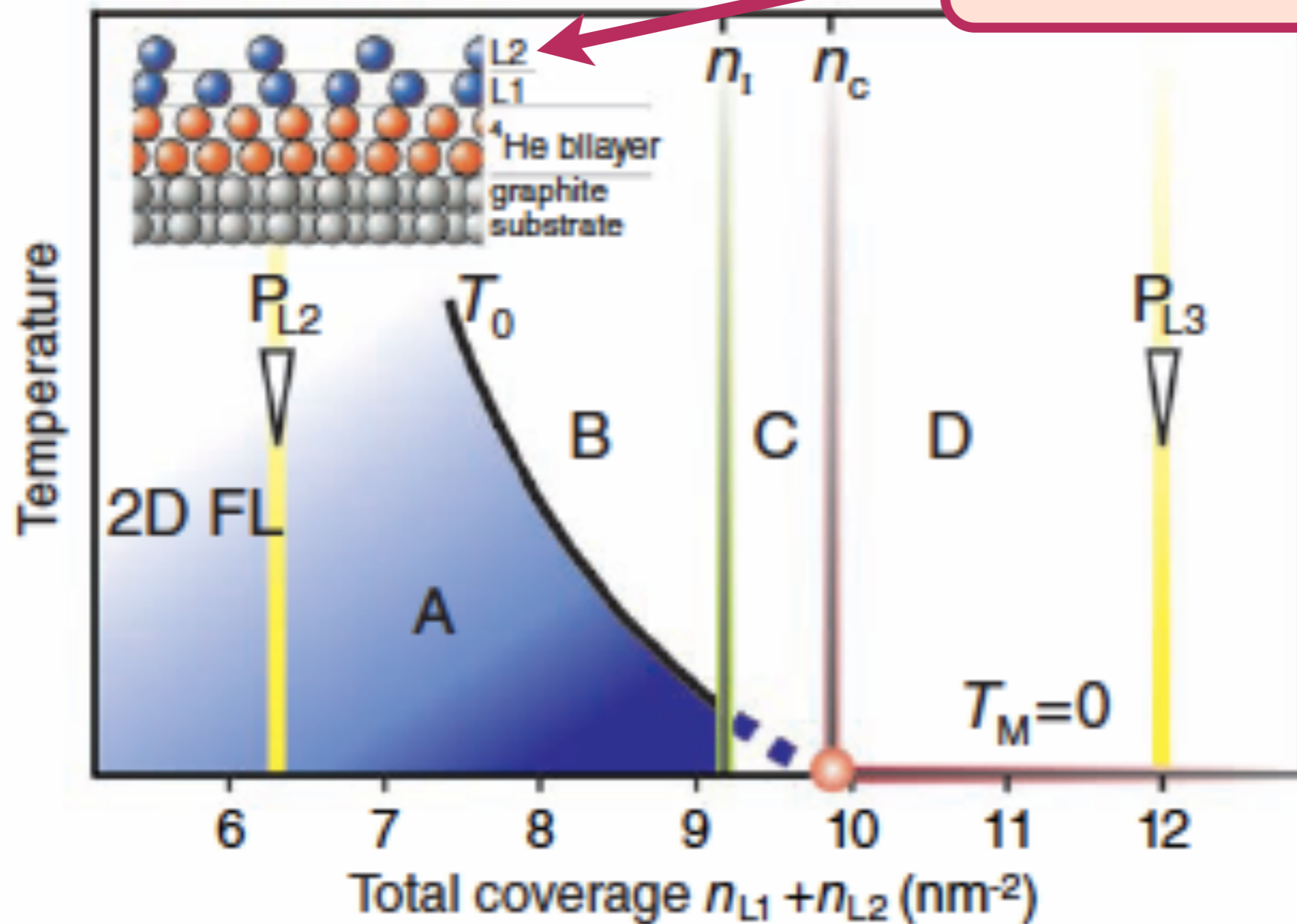
A bilayer Hubbard model or a "Kondo lattice"

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$c$  fermions

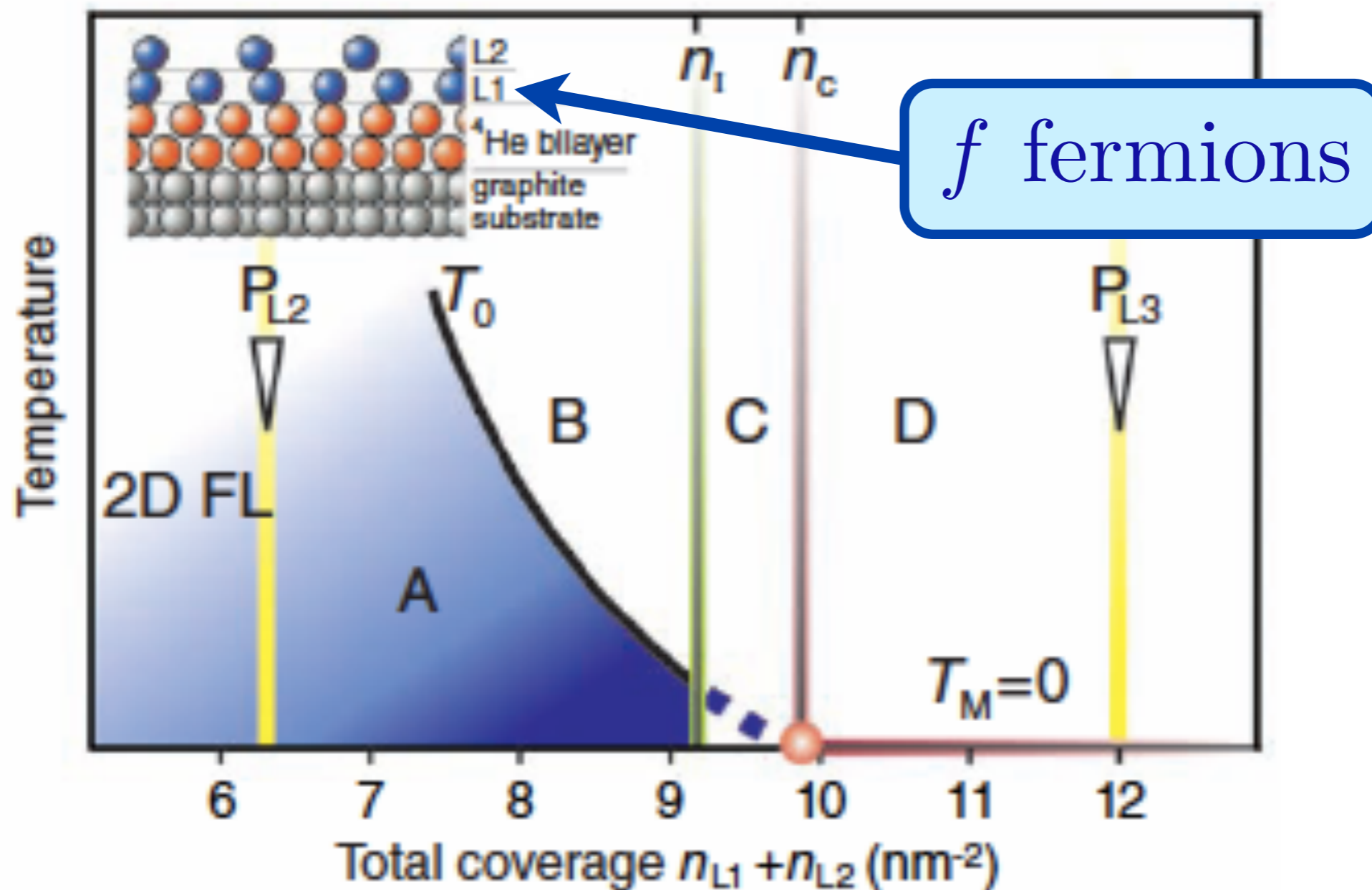


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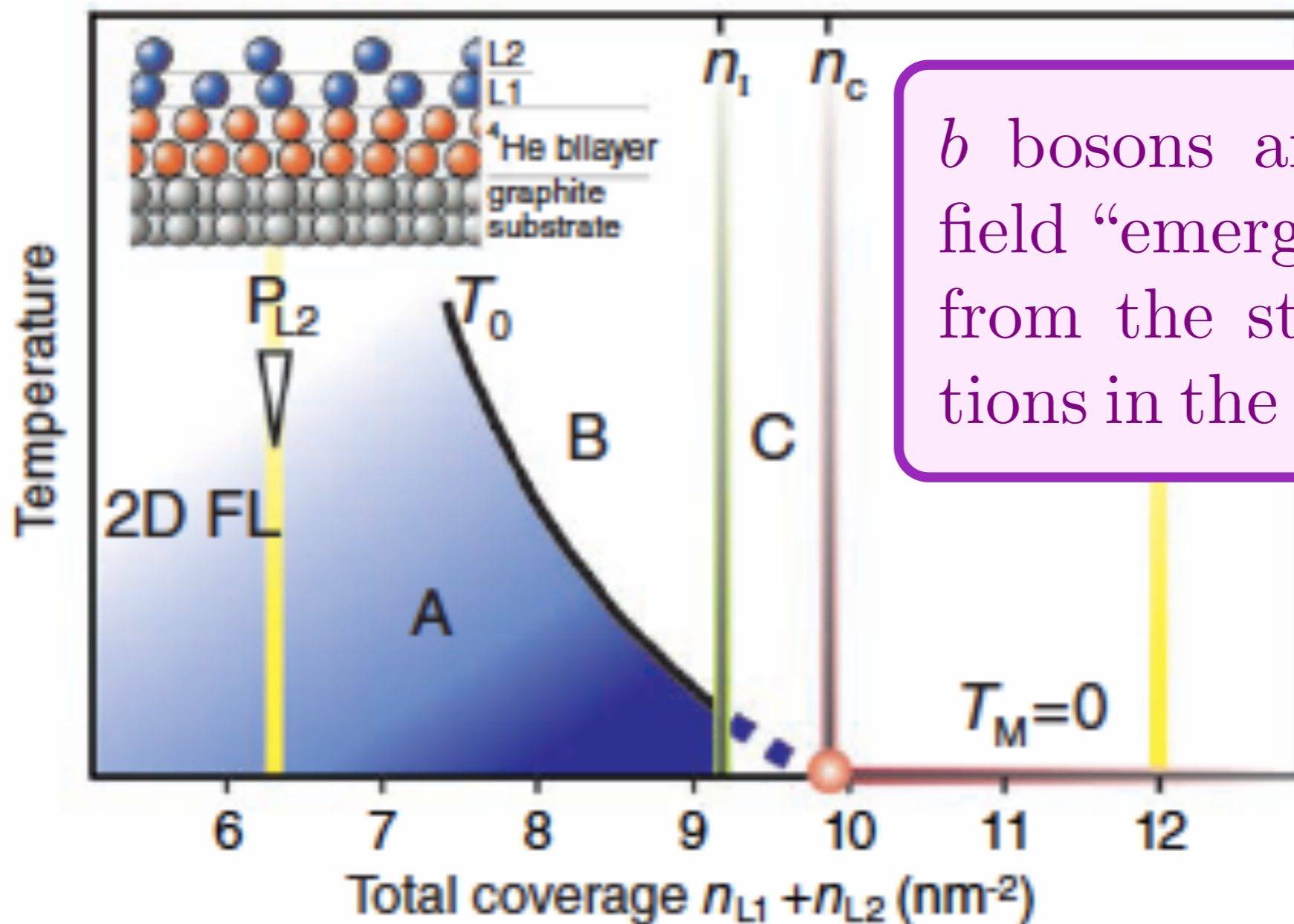


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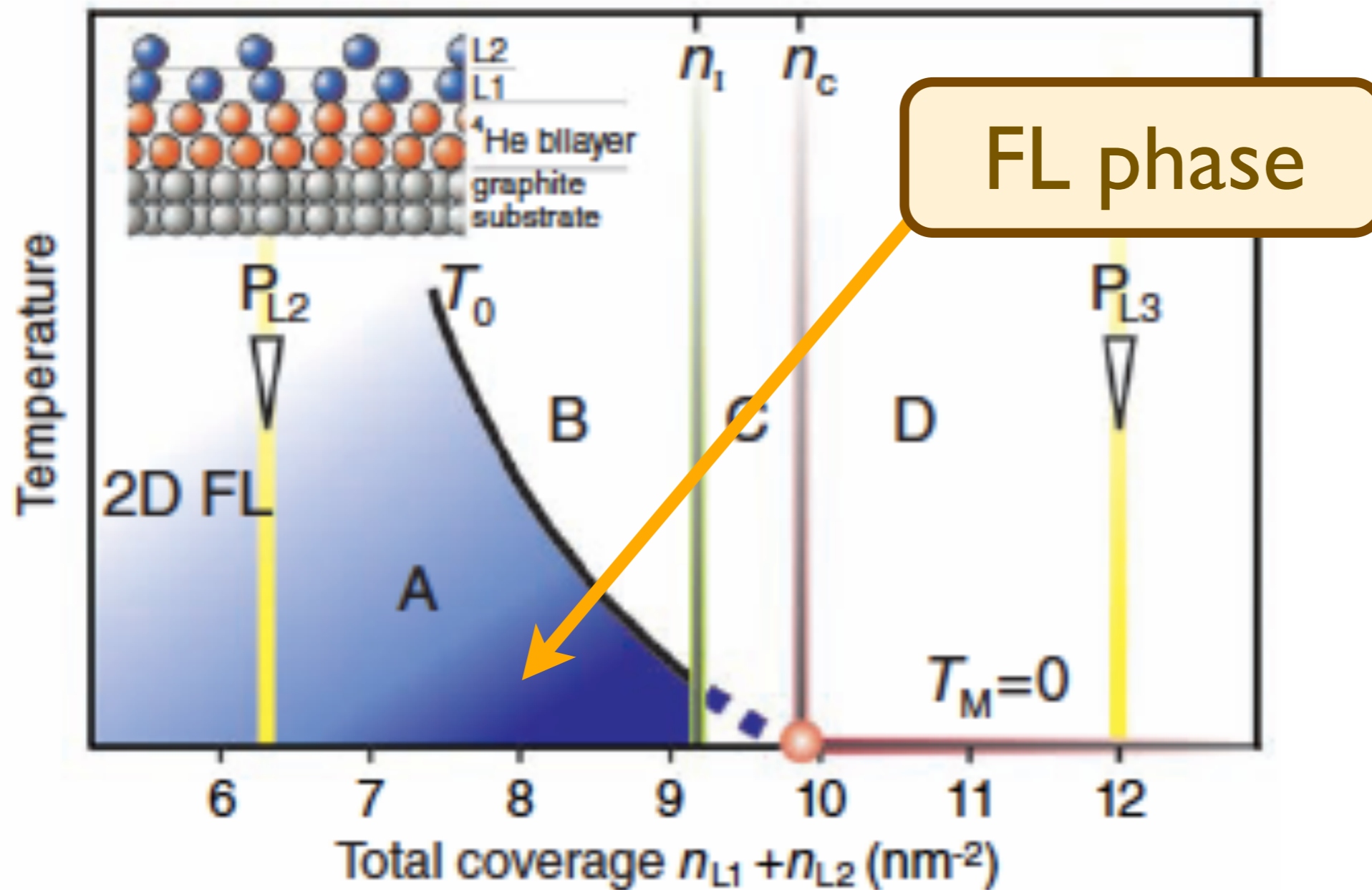
$b$  bosons and  $A_a$  gauge field “emerge” dynamically from the strong interactions in the Hubbard model.

A bilayer Hubbard model or a “Kondo lattice”

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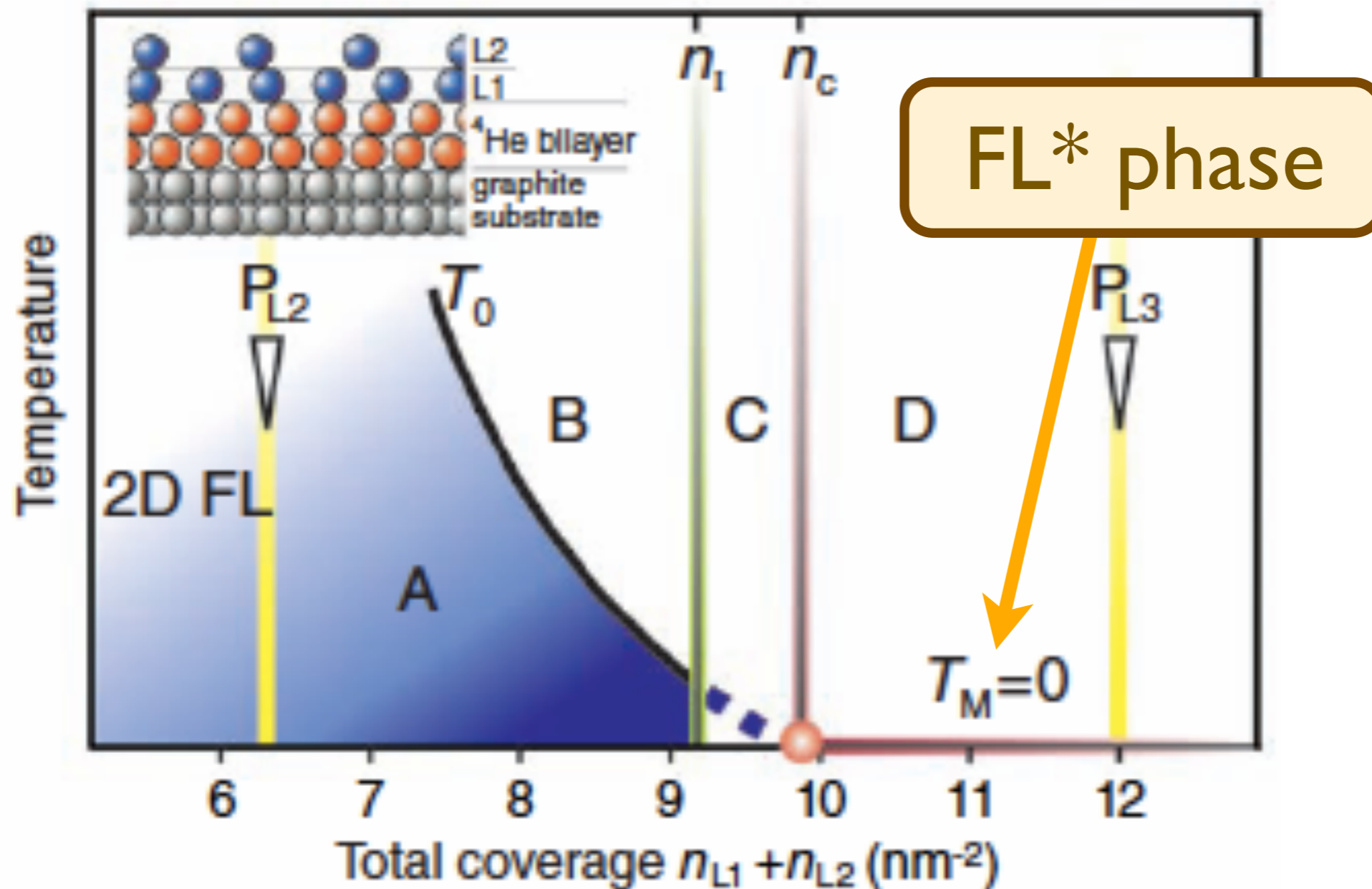


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# Low energy theory of FL\* phase

Integrate out gapped  $b$  bosons, and write theory of  $c$  electrons as

$$\mathcal{L}_c = \bar{c}(\partial_a - \mu\delta_{at})c + \lambda(\bar{c}F + \bar{F}c)$$

- The  $c$  are the observable gauge-invariant fermions (“probe UV fermions”).
- The  $F$  are composite gauge-invariant operators (“IR fermions”), carrying global U(1) charge, which probe the strongly-coupled physics of the  $f$  Fermi surface coupled to a fluctuating gauge field

$$F \sim (\bar{f}f)c$$

Note this also involves a contribution from the “probe sector” (the factor of  $c$ ), so the UV and IR are not completely decoupled.

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*If we ignore UV-IR mixing, this structure is formally the same as that in the semi-holographic theories of metals (T. Faulkner, H. Liu, J. McGreevy and D. Vegh, arXiv:0907.2694; T. Faulkner and J. Polchinski, arXiv:1001.5049.)*

# Low energy theory of FL phase

Now  $b$  is condensed; so write  $b = e^{-i\vartheta}$  and integrate out the  $f$  fermions. Then the  $c$  electrons (“UV fermions”) obey

$$\mathcal{L}_c = \bar{c}(\partial_a - \mu\delta_{at} - \Sigma_f - iA_a^{\text{ext}})c + \Pi_f(\tilde{A}_a) + (\partial_a\vartheta - \tilde{A}_a + A_a^{\text{ext}})^2$$

Here  $A_a^{\text{ext}}$  is an external source coupling to the global U(1) charge,  $\tilde{A}_a = A_a + A_a^{\text{ext}}$ , and  $\Sigma_f$  and  $\Pi_f$  are the self-energy and effective action generated by integrating out the  $f$ .

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This structure is similar to the semi-holographic theory of Nickel and Son (arXiv:1009.3094).

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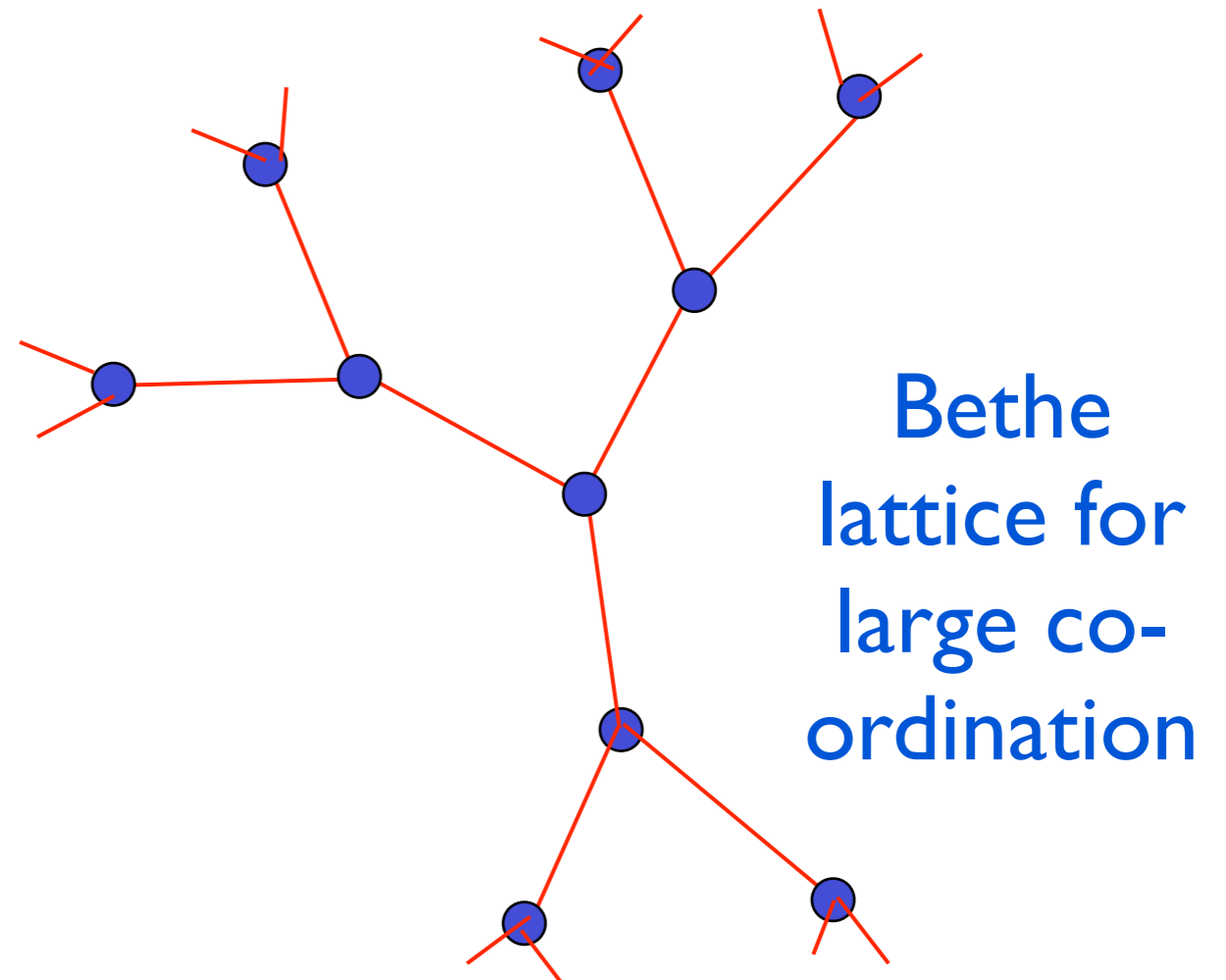
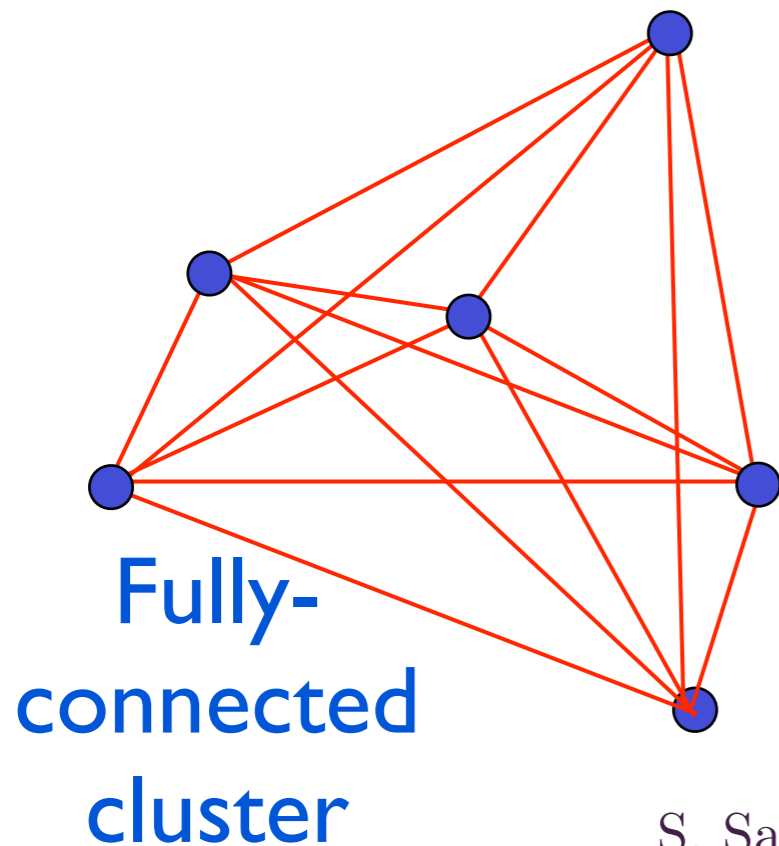
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# Solution of lattice models

Place theory on lattice, integrate out  $b$  and  $A_a$ , to obtain Kondo lattice Hamiltonian

$$H = - \sum_{i < j} t_{ij} c_{i\alpha}^\dagger c_{j\alpha} + \sum_{i < j} J_H(i, j) \vec{S}_i \cdot \vec{S}_j + J_K \sum_i \vec{S}_i \cdot c_{i\alpha}^\dagger \vec{\sigma}_{\alpha\beta} c_{i\beta}$$

where  $\vec{S}_i = f_{i\alpha}^\dagger \vec{\sigma}_{\alpha\beta} f_\beta$

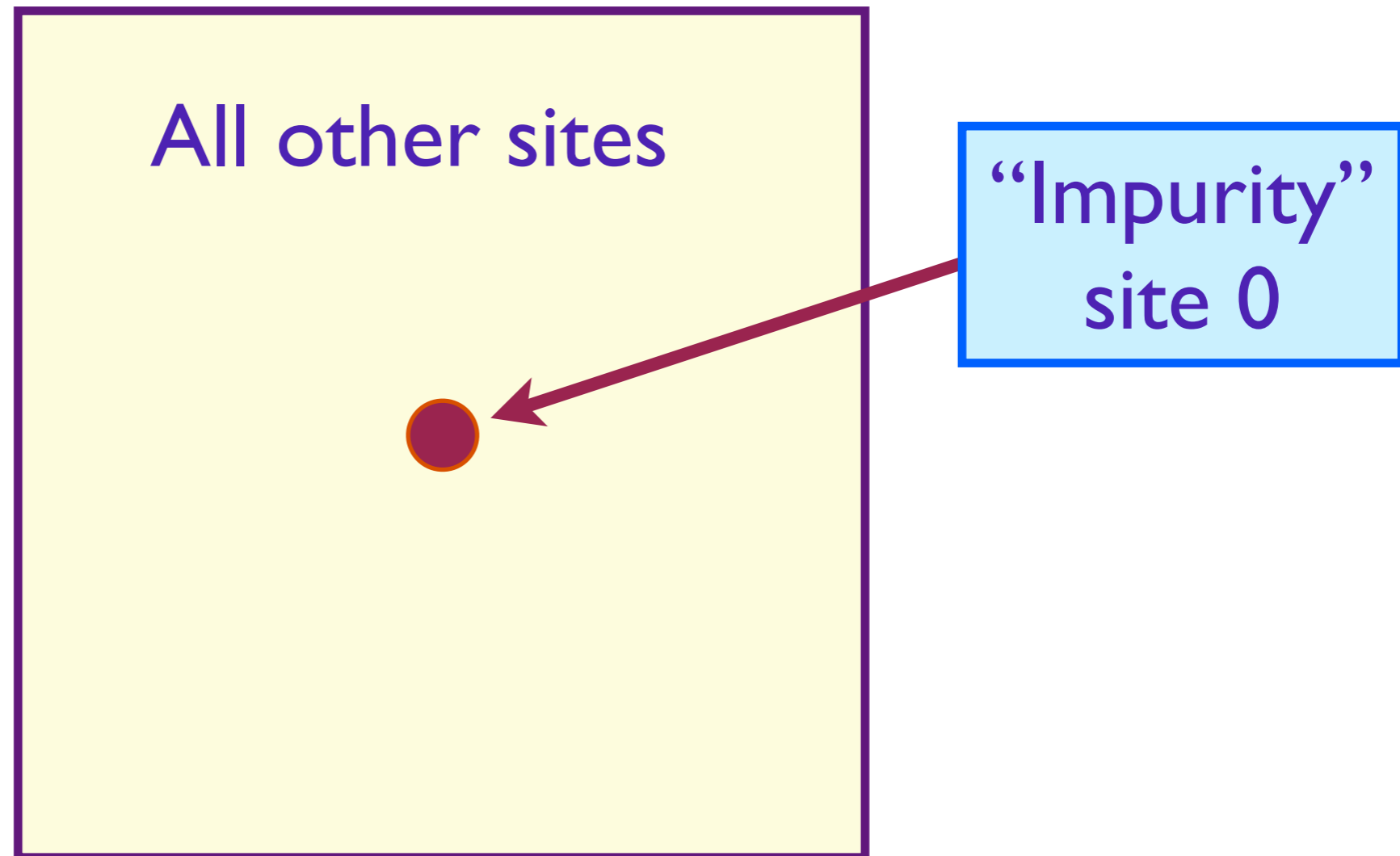


S. Sachdev and J. Ye, Phys. Rev. Lett. **70**, 3339 (1993).

A. Georges, O. Parcollet, and S. Sachdev, Phys. Rev. B **63**, 134406 (2001).

S. Burdin, D. R. Grempel, and A. Georges, Phys. Rev. B **66**, 045111 (2002)

# Solution of lattice models



$$\mathcal{L} = \mathcal{L}_{\text{imp}}[c_0, f_0] + c_0^\dagger F_{\text{bulk}} + F_{\text{bulk}}^\dagger c_0 + \mathcal{L}_{\text{bulk}}$$

Has to be combined with a *self-consistency condition* between correlators on the impurity and the bulk.

S. Sachdev and J. Ye, Phys. Rev. Lett. **70**, 3339 (1993).

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Obtain both FL and FL\* phases;  
properties of the FL\* phase:

- The ground state has a non-zero entropy density

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- Imposition of the self-consistency condition between impurity and boundary yields the scaling dimension  $\Delta = 1$ , the ‘marginal Fermi liquid’ value.

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These features, and the resulting fermion correlator and transport properties, co-incide with those obtained (for general  $\Delta$ ) using the holographic  $\text{AdS}_2 \times \mathbb{R}^d$  theory defined on the extremal horizon of the Reissner-Nordstrom black hole (T. Faulkner, H. Liu, J. McGreevy and D. Vegh, arXiv:0907.2694)

S. Sachdev, Phys. Rev. Lett. **105**, 151602 (2010).

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## Conclusions

- Compressible quantum matter is characterized by Fermi surfaces.
- Fermi surfaces can be removed from the Luttinger count if the fermions acquire gauge charges
- Phases of a strongly-coupled gauge theory contains Fermi liquid (FL) and fractionalized Fermi liquid (FL\*) phases: attractive candidate for a dual gravity theory

# Conclusions

- Mean field Kondo lattice models capture the physics of holographic metals with a  $AdS_2 \times R^d$  geometry
- Needed: Holographic theory without a factorized geometry, in which the probe fermions and the strongly-coupled IR refer to the same degrees of freedom.